Assignment -5 Part-2 Report

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STATES

We consider the tuple (Agent Position, Target Position, Call) as a state and we have 3x3 matrix so we gave 9 possible positions for the and for each there are 9 possible positions of target and it can be calling or not calling which further makes 2 more positions. So total 9x9x2 possible states i.e 162 states.

Possible positions of agent (0,0) -> 0, (1,0) -> 1, (2,0) -> 2, (0,1) -> 3, (1.1) -> 4, (2,1) -> 5, (0,2) -> 6, (1,2) -> 7, (2,2) -> 8

Possible positions for Target
$$(0,0)$$
 - > 0, $(1,0)$ - > 1, $(2,0)$ - > 2, $(0,1)$ -> 3, (1.1) -> 4, $(2,1)$ -> 5, $(0,2)$ -> 6, $(1,2)$ -> 7, $(2,2)$ -> 8

Cell no.(Encoding)

For call two possibilities 0 and 1.

A state is presented in following format:

• abc

a -> represents position of agent

b -> represents position of target

c -> call on or off

I assumed the Grid This way.

(0,2)	(1,2)	(2,2)
(0,1)	(1,1)	(2,1)
(0,0)	(1,0)	(2,0)

All possible states(in order):

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 \begin{array}{l} \text{States}: \left[ \; (0,0,0) \; , \; (0,0,1) \; , \; (0,1,0) \; , \; (0,1,1) \; , \; (0,2,0) \; , \; (0,2,1) \; , \; (0,3,0) \; , \; (0,3,1) \; , \; (0,4,0) \; , \; (0,4,1) \; , \; (0,5,0) \; , \\ (0,5,1) \; , \; (0,6,0) \; , \; (0,6,1) \; , \; (0,7,0) \; , \; (0,7,1) \; , \; (0,8,0) \; , \; (0,8,1) \; , \; (1,0,0) \; , \; (1,0,1) \; , \; (1,1,0) \; , \; (1,1,1) \; , \; (1,2,0) \; , \\ (1,2,1) \; , \; (1,3,0) \; , \; (1,3,1) \; , \; (1,4,0) \; , \; (1,4,1) \; , \; (1,5,0) \; , \; (1,5,1) \; , \; (1,6,0) \; , \; (1,6,1) \; , \; (1,7,0) \; , \; (1,7,1) \; , \; (1,8,0) \; , \\ (1,8,1) \; , \; (2,0,0) \; , \; (2,0,1) \; , \; (2,1,0) \; , \; (2,1,1) \; , \; (2,2,0) \; , \; (2,2,1) \; , \; (2,3,0) \; , \; (2,3,1) \; , \; (2,4,0) \; , \; (2,4,1) \; , \; (2,5,0) \; , \\ \end{array}
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 (2,5,1) \ , (2,6,0) \ , (2,6,1) \ , (2,7,0) \ , (2,7,1) \ , (2,8,0) \ , (2,8,1) \ , (3,0,0) \ , (3,0,1) \ , (3,1,0) \ , (3,1,1) \ , (3,2,0) \ , (3,2,1) \ , (3,3,0) \ , (3,3,1) \ , (3,4,0) \ , (3,4,1) \ , (3,5,0) \ , (3,5,1) \ , (3,6,0) \ , (3,6,1) \ , (3,7,0) \ , (3,7,1) \ , (3,8,0) \ , (3,8,1) \ , (4,0,0) \ , (4,0,1) \ , (4,1,0) \ , (4,1,1) \ , (4,2,0) \ , (4,2,1) \ , (4,3,0) \ , (4,3,1) \ , (4,4,0) \ , (4,4,1) \ , (4,5,0) \ , (4,5,1) \ , (4,6,0) \ , (4,6,1) \ , (4,7,0) \ , (4,7,1) \ , (4,8,0) \ , (4,8,1) \ , (5,0,0) \ , (5,0,1) \ , (5,1,0) \ , (5,1,1) \ , (5,2,0) \ , (5,2,1) \ , (5,3,0) \ , (5,3,1) \ , (5,4,0) \ , (5,4,1) \ , (5,5,0) \ , (5,5,1) \ , (5,6,0) \ , (5,6,1) \ , (5,7,0) \ , (5,7,1) \ , (5,8,0) \ , (5,8,1) \ , (6,0,0) \ , (6,0,1) \ , (6,1,0) \ , (6,1,1) \ , (6,2,0) \ , (6,2,1) \ , (6,3,0) \ , (6,3,1) \ , (6,4,0) \ , (6,4,1) \ , (6,5,0) \ , (7,2,1) \ , (7,3,0) \ , (7,3,1) \ , (7,4,0) \ , (7,4,1) \ , (7,5,0) \ , (7,5,1) \ , (7,6,0) \ , (7,6,1) \ , (7,7,0) \ , (7,7,1) \ , (7,8,0) \ , (7,8,1) \ , (8,0,0) \ , (8,0,1) \ , (8,1,0) \ , (8,1,1) \ , (8,2,0) \ , (8,2,1) \ , (8,3,0) \ , (8,3,1) \ , (8,4,0) \ , (8,4,1) \ , (8,5,0) \ , (8,5,1) \ , (8,6,0) \ , (8,6,1) \ , (8,7,0) \ , (8,7,1) \ , (8,8,0) \ , (8,8,1) \ ]
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A1. Target is in (1,1) cell and observation is o6

o6 is observed when the target is not in the 1 cell neighbourhood of the agent. Hence the agent cannot be in (0,1),(1,0),(1,2),(2,1) so the agent can be in (0,0),(0,2),(2,0),(2,2) with equal probability. Also call can be on or off . So eight states with equal probabilities.

Agent		Agent
	Target	
Agent		Agent

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Initial belief state b: ( agent , target , call )
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States: [(0,4,0), (0,4,1), (6,4,0), (6,4,1), (2,4,0), (2,4,1), (8,4,0), (8,4,1)]

These states have equal Probability = $\frac{1}{8}$ = 0.125 and all other zero.

A2. Agent in (0,1) and Target is in one neighborhood and is not making a call.

Target		
Agent \ Target	Target	
Target		

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Target can be in (0,0) , (0,1) , (0,2) , (1,1) c is 0 States : [ (3,0,0) , (3,3,0) , (3,6,0) , (3,4,0) ] These states have equal Probability = \frac{1}{4} = 0.25 and all other zero.
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A3. Expected utility for initial belief states in 1 and 2

1.

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#Simulations | Exp Total Reward | 95% Confidence Interval
1000 3.70183 (3.51431, 3.88935)
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2.

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#Simulations | Exp Total Reward | 95% Confidence Interval
1000 8.54886 (8.35421, 8.74351)
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A4. Agent is in (0,1) with probability 0.6 and in (2,1) with probability 0.4 and the target is in the 4 corner cells with equal probability.

Target	Target
Agent(0.6)	Agent(0.4)
Target	Target

This gives the observations o3 and o5 with probability with probability $\frac{1}{4}$ and o6 with probability $\frac{1}{2}$ when the agent is in (0, 1).

This gives the observations o3 and o5 with probability with probability $\frac{1}{4}$ and o6 with probability $\frac{1}{2}$ when the agent is in (2, 1).

P(o1)= 0 P(o2)=0 P(o3)=0.6*0.25+0.4*25=0.25 P(o4)=0 P(o5)=0.6*0.25+0.4*25=0.25 P(o6)=0.6*0.5+0.4*0.5=0.5

Hence O6 is most likely to be observed

A5. Total no. of Policy trees:

The formula for calculating the number of trees in POMDP is $|A|^N$ where N = Number of nodes in the tree and A = All possible actions Formula to calculate N:

$$N = \frac{|O|^{T-1} - 1}{|O| - 1}$$

where T = Levels in the tree and O = Number of observations

Number of trees obtained is dependent on the horizon T . The value of N increases as the value of T increases. In the SARSOP Solver, the horizon is not a fixed value, but depends on the precision value obtained. The program terminates when a target precision is obtained for a certain converging calculated value. Hence, the number of policy trees obtained is not a fixed value and can not be calculated without running the program.