

Tutorial-7

Construct CFGs for the following language.

① $L = \{a, b\}^+$

Solve

$$L = \{a, b, aa, bb, aab, abb, \dots\}$$

$$S \rightarrow aS \mid bS \mid a, b$$

② $L = \{a^n b^m a^n \mid n \geq 1, m \geq 0\}$

Solve

$$\begin{aligned} S &\rightarrow aS a \mid aa \\ A &\rightarrow bA \mid \epsilon \end{aligned}$$

$$S \rightarrow aAa \mid aa$$

③ $L = \{(ab)^n \mid n \geq 0\}$

Solve

CFG =

$$S \rightarrow aSb \mid \epsilon$$

④ $L = \{w \mid n_a(w) = n_b(w)\}$

Solve

$$\begin{aligned} S &\rightarrow aSb \mid A \\ A &\rightarrow bSa \mid B \\ B &\rightarrow SS \mid \epsilon \end{aligned}$$

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Ans $L = \{ a^n b^m c^{n+m} \mid n, m \geq 0 \}$

Solve

C.F.G

$$\begin{aligned} S &\rightarrow aSc \mid \epsilon \\ B &\rightarrow bBc \mid \epsilon \end{aligned}$$

Ans $L = \{ a^n b^m \mid n \neq m \}$

Solve

C.F.G

$$\begin{aligned} S &\rightarrow aSb \mid \epsilon \\ A &\rightarrow aA \mid bA \mid \epsilon \end{aligned}$$

~~$$S \rightarrow aAb$$~~

$$S \rightarrow aSb \mid A$$