## 1

## **GATE 2023**

## EE22BTECH11060 - TEJAVATH KUSHAL\*

**Q 20 :** The solution x(t),  $t \ge 0$ , to the differential equation  $\ddot{x} = -k\dot{x}$ , k > 0 with initial conditions x(0) = 1 and  $\dot{x}(0) = 0$  is:  $(GATE\ 2023, IN)$ 

Ans:

Differential equation	$\ddot{x} = -k\dot{x}$
Initial conditions	$x()) = 1$ and $\dot{x}(0) = 0$
x(t)	?
TABLE 0	
Parameter Table	

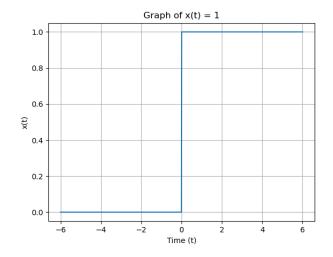


Fig. 0. Stem Plot of x(t) v/s t

$$\implies \frac{d^2x(t)}{dt^2} = -k\frac{dx(t)}{dt} \tag{1}$$

Taking Laplace transform on both sides,

$$\frac{d^2x(t)}{dx^2}Ls^2X(s) - sx(0) - \dot{x}(0)$$
 (2)

$$\frac{dx(t)}{dx}LsX(s) - x(0) \tag{3}$$

$$s^{2}X(s) - sx(0) - \dot{x}(0) = -k(sX(s) - x(0))$$
 (4)

$$s^{2}X(s) - s = -k(sX(s) - 1)$$
 (5)

$$sX(s)(s+k) = (s+k)$$
(6)

$$s \neq -k \tag{7}$$

$$X(s) = \frac{1}{s} \tag{8}$$

$$x(t) = u(t) \tag{9}$$

$$t \ge 0 \implies x(t) = 1$$
 (10)