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GATE 2021

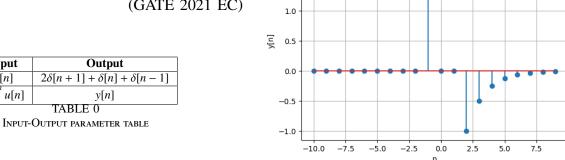
EE22BTECH11060 - TEJAVATH KUSHAL*

Q.40: For a unit step input u[n], a discrete-time LTI system produces an output signal $(2\delta[n+1] +$ $\delta[n] + \delta[n-1]$). Let y[n] be the output of the system for an input $\left(\left(\frac{1}{2}^n\right)u[n]\right)$. The value of y[0] is:

(GATE 2021 EC)

Ans.

Input	Output
u[n]	$2\delta[n+1] + \delta[n] + \delta[n-1]$
$\left(\frac{1}{2}\right)^n u[n]$	y[n]
TABLE 0	



2.0

1.5

For impulse response

$$h(n) = s(n) - s(n-1)$$
 (1)

$$h(n) = 2\delta(n+1) + \delta(n) + \delta(n-1) - 2\delta(n) - \delta(n-1) - \delta(n-1-1)$$

$$\implies h(n) = 2\delta(n+1) - \delta(n) - \delta(n-2) \tag{3}$$

For input $x(n) = \left(\frac{1}{2}\right)^n u(n)$

$$y(n) = x(n)h(n)$$
 (4)

$$y(n) = x(n) [2\delta(n+1) - \delta(n) - \delta(n-2)]$$
 (5)

$$y(n) = 2x(n+1) - x(n) - x(n-2)$$
 (6)

$$y(n) = 2\left(\frac{1}{2}\right)^{n+1} u(n+1) - \left(\frac{1}{2}\right)^n u(n)$$

$$-\left(\frac{1}{2}\right)^{n-2}u(n-2) \quad (7)$$

$$y(0) = 2\left(\frac{1}{2}\right)^{0+1} u(0+1) - \left(\frac{1}{2}\right)^{0} u(0)$$

$$-\left(\frac{1}{2}\right)^{0-2}u(0-2) \quad (8)$$

$$\implies y(0) = 0 \tag{9}$$

Fig. 0. Plot of
$$y(n)$$
 v/s n

Graph of y[n] vs n