

Time Complexity :

1. Topological Sort (Kahn's Algorithm)

Time Complexity: $O(V + E)$

Steps:

- Initialize indegree[] of all vertices $\rightarrow O(V)$
- Add all vertices with indegree 0 to queue $\rightarrow O(V)$
- While queue not empty:
 - Pop front node, add to result $\rightarrow O(V)$
 - Reduce indegree of neighbors, if any hits 0 \rightarrow add to queue $\rightarrow O(E)$
- Total: $O(V + E)$

2. Dijkstra's Algorithm (Min Heap / Priority Queue)

Time Complexity: $O((V + E) \log V)$

Steps:

- Initialize distance[] with ∞ , set source = 0 $\rightarrow O(V)$
- Use PriorityQueue (min-heap) for selecting min dist $\rightarrow O(\log V)$ per op
- For each node, relax its neighbors $\rightarrow O(E \log V)$
- Total: $O((V + E) \log V)$

3. Prim's Algorithm (Min Heap)

Time Complexity: $O((V + E) \log V)$

Steps:

- Initialize visited[] and minHeap $\rightarrow O(V)$
- Start from any node, add all edges to heap
- Pick min edge, if dest not visited, mark it and push its neighbors $\rightarrow O(E \log V)$
- Repeat until all nodes visited
- Total: $O((V + E) \log V)$

4. QuickSort

Time Complexity:

- Best/Average: $O(n \log n)$
- Worst (unlucky pivot): $O(n^2)$

Steps:

- Choose pivot
- Partition array (place pivot in correct position) $\rightarrow O(n)$
- Recursively quicksort left + right of pivot
- Total: $O(n \log n)$ average

5. Gale-Shapley (Stable Marriage Problem)

Time Complexity: $O(n^2)$

Steps:

- Each unengaged guy proposes to the next girl on his list $\rightarrow O(n^2)$ max
- Each girl picks preferred among current + new proposal
- Repeat until all guys are engaged
- Total: $O(n^2)$

6. Inversion Count (Using Merge Sort)

Time Complexity: $O(n \log n)$

Steps:

- Modify merge sort
- In merge step: if $\text{arr}[i] > \text{arr}[j]$, $\text{count} += \text{mid} - i$
- Recursive divide + merge
- Total: $O(n \log n)$

7. Kruskal's Algorithm (MST using DSU)

Time Complexity: $O(E \log E)$

Steps:

- Sort all edges by weight $\rightarrow O(E \log E)$
- Initialize DSU (Disjoint Set Union) $\rightarrow O(E)$
- For each edge, if endpoints in diff sets \rightarrow add to MST, union sets
- Stop when MST has $(V - 1)$ edges
- Total: $O(E \log E)$

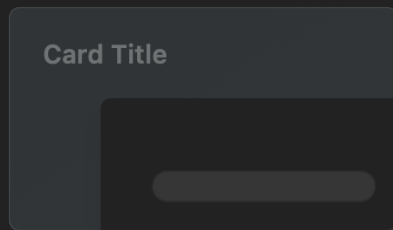
8. Merge Sort

Time Complexity: $O(n \log n)$

Steps:



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- Divide array in halves $\rightarrow O(\log n)$
- Recursively sort left + right
- Merge the two sorted halves $\rightarrow O(n)$
- Total: $O(n \log n)$