

**Time Complexity :**

**1. Topological Sort (Kahn's Algorithm)**

**Time Complexity:**  $O(V + E)$

**Steps:**

- Initialize indegree[] of all vertices  $\rightarrow O(V)$
- Add all vertices with indegree 0 to queue  $\rightarrow O(V)$
- While queue not empty:
  - Pop front node, add to result  $\rightarrow O(V)$
  - Reduce indegree of neighbors, if any hits 0  $\rightarrow$  add to queue  $\rightarrow O(E)$
- Total:  $O(V + E)$

**2. Dijkstra's Algorithm (Min Heap / Priority Queue)**

**Time Complexity:**  $O((V + E) \log V)$

**Steps:**

- Initialize distance[] with  $\infty$ , set source = 0  $\rightarrow O(V)$
- Use PriorityQueue (min-heap) for selecting min dist  $\rightarrow O(\log V)$  per op
- For each node, relax its neighbors  $\rightarrow O(E \log V)$
- Total:  $O((V + E) \log V)$

**3. Prim's Algorithm (Min Heap)**

**Time Complexity:**  $O((V + E) \log V)$

**Steps:**

- Initialize visited[] and minHeap  $\rightarrow O(V)$
- Start from any node, add all edges to heap
- Pick min edge, if dest not visited, mark it and push its neighbors  $\rightarrow O(E \log V)$
- Repeat until all nodes visited
- Total:  $O((V + E) \log V)$

## 4. QuickSort

**Time Complexity:**

- Best/Average:  $O(n \log n)$
- Worst (unlucky pivot):  $O(n^2)$

**Steps:**

- Choose pivot
- Partition array (place pivot in correct position)  $\rightarrow O(n)$
- Recursively quicksort left + right of pivot
- Total:  $O(n \log n)$  average

## 5. Gale-Shapley (Stable Marriage Problem)

**Time Complexity:**  $O(n^2)$

**Steps:**

- Each unengaged guy proposes to the next girl on his list  $\rightarrow O(n^2)$  max
- Each girl picks preferred among current + new proposal
- Repeat until all guys are engaged
- Total:  $O(n^2)$

## 6. Inversion Count (Using Merge Sort)

**Time Complexity:**  $O(n \log n)$

**Steps:**

- Modify merge sort
- In merge step: if  $\text{arr}[i] > \text{arr}[j]$ ,  $\text{count} += \text{mid} - i$
- Recursive divide + merge
- Total:  $O(n \log n)$

## 7. Kruskal's Algorithm (MST using DSU)

**Time Complexity:**  $O(E \log E)$

**Steps:**

- Sort all edges by weight  $\rightarrow O(E \log E)$
- Initialize DSU (Disjoint Set Union)  $\rightarrow O(E)$
- For each edge, if endpoints in diff sets  $\rightarrow$  add to MST, union sets
- Stop when MST has  $(V - 1)$  edges
- Total:  $O(E \log E)$

## 8. Merge Sort

**Time Complexity:**  $O(n \log n)$

**Steps:**



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### Card Title

- Divide array in halves  $\rightarrow O(\log n)$
- Recursively sort left + right
- Merge the two sorted halves  $\rightarrow O(n)$
- Total:  $O(n \log n)$