

DSC 423: Data Analysis & Regression

Assignment 5: Variable Screening

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Honor Statement: I, Kushal Navghare, assure that I have completed this work independently. The solutions given are entirely my own work.

1. The purpose of k-fold cross validation is often misunderstood.

a. How do you use cross validation to select a final (or production) model? **Note: it is not the “best” of the k models you have built using cross validation.** Ans: K-Fold cross validation technique splits the data into k equal parts and considers the k-1 folds as part of training set, the remaining fold is kept aside for testing. The process builds k versions of different model and the overall accuracy metric is aggregated at the end. For each iteration, a new model is trained completely independent of the previous iteration. This way, we get to see more generalized version of the model.

However, to use this technique efficiently, we perform multiple iteration of k-fold cross validation and test multiple assumptions in such way. For example, we can try different set of features for each iteration of k-fold validation. This way, we get different performance metric for each iteration and these metrics can be compared to decide the best version of model and set of features which yields more generalized and accurate predictions on future dataset.

2. The `pgatour2006.csv` dataset contains data for 196 players. The variables in the dataset are:

- Player's name
- PrizeMoney = average prize money per tournament
- DrivingAccuracy = percent of times a player is able to hit the fairway with his tee shot
- GIR = percent of time a player was able to hit the green within two or less than par (Greens in Regulation)
- BirdieConversion = percentage of times a player makes a birdie or better after hitting the green in regulation
- PuttingAverage = putting performance on those holes where the green was hit in regulation.
- PuttsPerRound = average number of putts per round (shots played on the green)

```
# read file
raw_df <- read.csv(paste0(dir.path, 'data/pgatour2006.csv'))

# summary
dim(raw_df)
```

```
## [1] 196 11
```

```
summary(raw_df)
```

```
##      Name      PrizeMoney      AveDrivingDistance      DrivingAccuracy
## Length:196      Min.   : 2240      Min.   :265.9      Min.   :49.75
## Class :character 1st Qu.: 17369      1st Qu.:283.6      1st Qu.:59.76
## Mode  :character Median : 36644      Median :288.2      Median :63.24
```

```
##           Mean    : 50891    Mean    :289.5    Mean    :63.38
##           3rd Qu.: 57915    3rd Qu.:295.5    3rd Qu.:66.97
##           Max.    :662771    Max.    :319.6    Max.    :78.43
##           GIR      PuttingAverage BirdieConversion SandSaves
## Min.      :56.87    Min.      :1.712    Min.      :23.17    Min.      :33.91
## 1st Qu.   :63.52    1st Qu.   :1.763    1st Qu.   :27.51    1st Qu.   :45.13
## Median    :65.36    Median    :1.778    Median    :29.01    Median    :48.66
## Mean      :65.19    Mean      :1.780    Mean      :28.98    Mean      :48.97
## 3rd Qu.   :66.77    3rd Qu.   :1.796    3rd Qu.   :30.55    3rd Qu.   :52.87
## Max.      :74.15    Max.      :1.851    Max.      :35.66    Max.      :63.64
##           Scrambling BounceBack PuttsPerRound
## Min.      :49.02    Min.      :12.29    Min.      :27.96
## 1st Qu.   :55.26    1st Qu.   :17.56    1st Qu.   :28.91
## Median    :57.65    Median    :19.62    Median    :29.19
## Mean      :57.49    Mean      :19.60    Mean      :29.20
## 3rd Qu.   :59.46    3rd Qu.   :21.31    3rd Qu.   :29.48
## Max.      :66.45    Max.      :25.93    Max.      :30.19
```

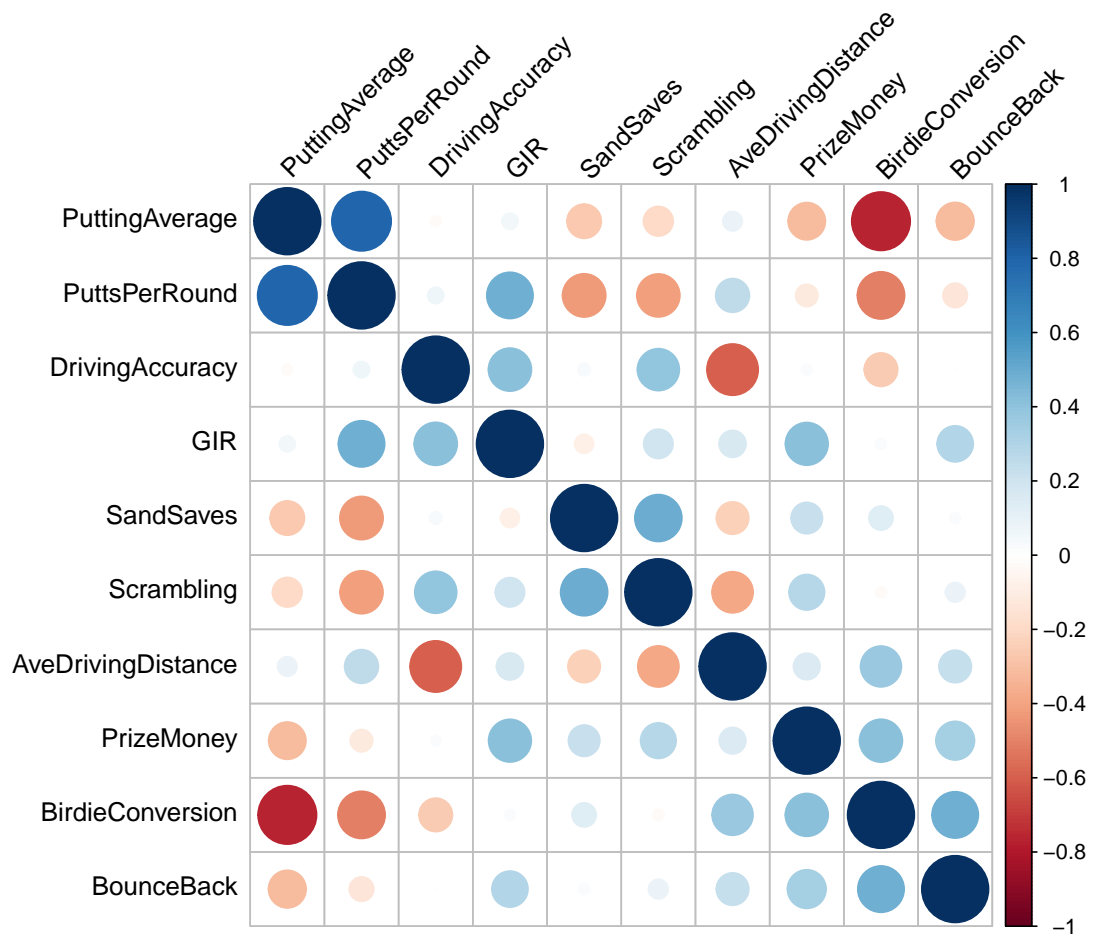
```
str(raw_df)
```

```
## 'data.frame':    196 obs. of  11 variables:
## $ Name          : chr  "Aaron Baddeley" "Adam Scott" "Alex Aragon" "Alex Cejka" ...
## $ PrizeMoney     : int   60661 262045 3635 17516 16683 107294 50620 57273 86782 23396 ...
## $ AveDrivingDistance: num   288 301 303 289 288 ...
## $ DrivingAccuracy  : num   60.7 62 51.1 66.4 63.2 ...
## $ GIR             : num   58.3 69.1 59.1 67.7 64 ...
## $ PuttingAverage   : num    1.75 1.77 1.79 1.78 1.76 ...
## $ BirdieConversion : num    31.4 30.4 29.9 29.3 29.3 ...
## $ SandSaves        : num    54.8 53.6 37.9 45.1 52.4 ...
## $ Scrambling       : num    59.4 57.9 50.8 54.8 57.1 ...
## $ BounceBack       : num    19.3 19.4 16.8 17.1 18.2 ...
## $ PuttsPerRound    : num     28 29.3 29.2 29.5 28.9 ...
```

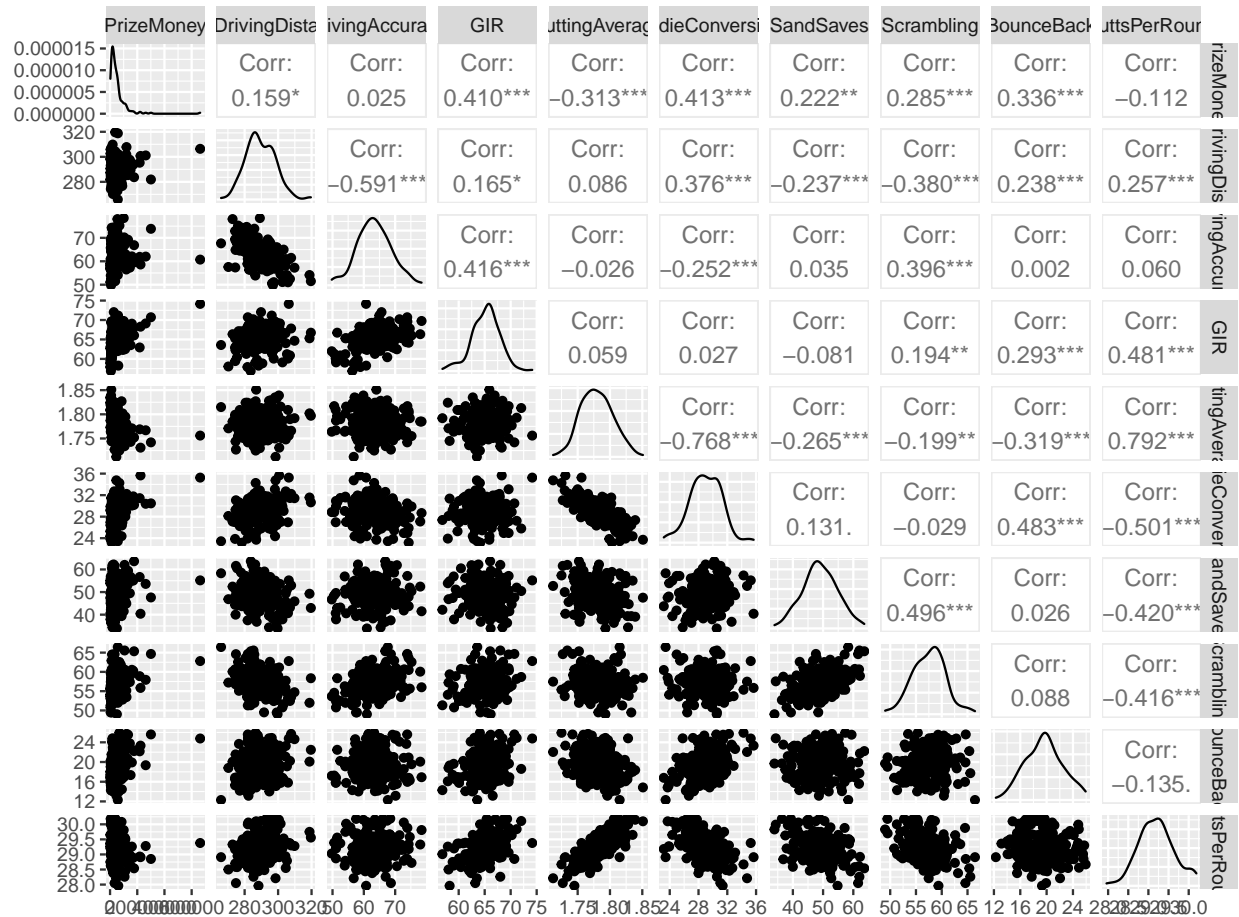
```
# check correlation
cor_df <- cor(raw_df %>% select_if(is.numeric))

corrplot(cor_df,
          type="full",
          order="hclust",
          tl.col="black", tl.srt=45)
```

a. Build a complete first-order model. Evaluate the model using 5-fold cross validation. If necessary, remove a non-significant variable and repeat until you have your final first-order model. Present the model.



```
# check pair plot
ggpairs(raw_df %>% select_if(is.numeric))
```



Let's start building a first-order model. here, we will try to predict based on Player's attributes, how much PrizeMoney can he make.

```
# select numeric columns
num_df <- raw_df %>%
  select_if(is.numeric)

# build a model (baseline)
base_model <- lm(PrizeMoney~DrivingAccuracy+GIR+BirdieConversion+Scrambling,
  data = num_df)

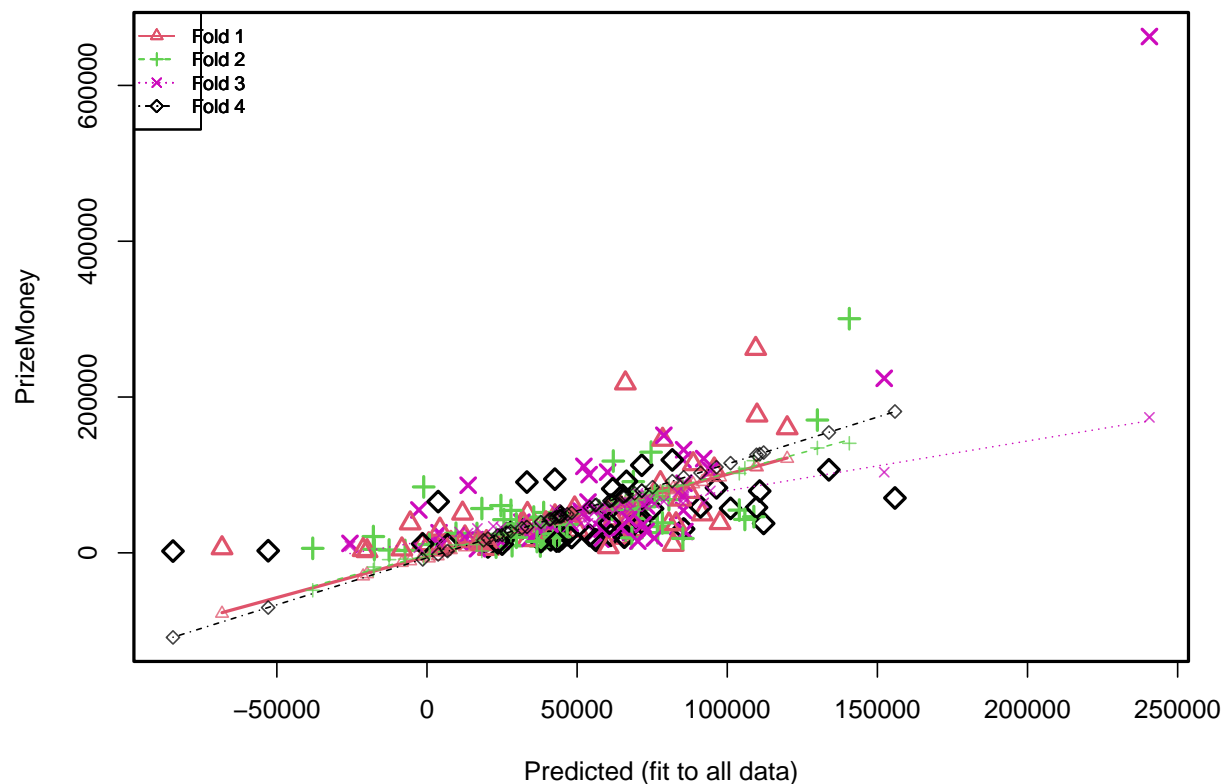
summary(base_model)
```

```
##
## Call:
## lm(formula = PrizeMoney ~ DrivingAccuracy + GIR + BirdieConversion +
##     Scrambling, data = num_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -85429  -27959  -7833   15674  422173
##
## Coefficients:
```

```
##               Estimate Std. Error t value      Pr(>|t|)
## (Intercept)   -1094996.9   109585.4  -9.992 < 0.0000000000000002 ***
## DrivingAccuracy   -1964.1     815.7  -2.408     0.017 *
## GIR              9742.9     1465.9   6.646     0.000000000306 ***
## BirdieConversion  10670.5     1703.7   6.263     0.000000002439 ***
## Scrambling       5670.4     1239.4   4.575     0.000008556442 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 50080 on 191 degrees of freedom
## Multiple R-squared:  0.3984, Adjusted R-squared:  0.3858
## F-statistic: 31.62 on 4 and 191 DF,  p-value: < 0.00000000000000022
```

```
# cross validation
cv_model <- cv.lm(data = num_df,
                  form.lm = formula(PrizeMoney~DrivingAccuracy+GIR+BirdieConversion+Scrambling),
                  plotit = c("Observed", "Residual"), legend.pos = "topleft",
                  m = 4)
```

Small symbols show cross-validation predicted values



```
##
## fold 1
## Observations in test set: 49
##           2           6           7           8          11          13          14
```

```

## Predicted 109477.3 95668.75 11848.51 49184.55 68816.83 42604.705 91689.33
## cvpred 110688.8 96458.47 12023.00 47004.96 65463.12 41791.003 91259.34
## PrizeMoney 262045.0 107294.00 50620.00 57273.00 29567.00 47172.000 49640.00
## CV residual 151356.2 10835.53 38597.00 10268.04 -35896.12 5380.997 -41619.34
## 15 19 24 35 36 41
## Predicted 69849.63 50321.10 44308.45 97604.34 33458.09 67479.99
## cvpred 68686.54 48857.66 43583.53 97178.92 32535.57 65755.07
## PrizeMoney 53610.00 28658.00 27224.00 38455.00 50249.00 45752.00
## CV residual -15076.54 -20199.66 -16359.53 -58723.92 17713.43 -20003.07
## 44 46 47 48 62 63
## Predicted 39605.047 33406.38 82019.24 16883.283 48247.908 66073.08
## cvpred 39856.075 29284.66 83149.91 10229.816 45768.137 63759.71
## PrizeMoney 38275.000 16630.00 10504.00 13262.000 43820.000 217748.00
## CV residual -1581.075 -12654.66 -72645.91 3032.184 -1948.137 153988.29
## 64 65 72 77 79 81
## Predicted 3573.567 -1617.093 7933.424 80578.48 64599.621 20427.45
## cvpred -4140.289 -4675.043 3789.004 80710.11 63335.418 15835.41
## PrizeMoney 5402.000 10528.000 13031.000 36918.00 57824.000 5265.00
## CV residual 9542.289 15203.043 9241.996 -43792.11 -5511.418 -10570.41
## 86 88 93 101 105 108
## Predicted 62302.36 64624.61 82942.71 -19957.12 4329.9761 32159.220
## cvpred 61080.49 64835.00 82234.90 -27103.69 676.1089 32321.177
## PrizeMoney 43173.00 19594.00 37004.00 2426.00 30068.0000 37214.000
## CV residual -17907.49 -45241.00 -45230.90 29529.69 29391.8911 4892.823
## 109 117 121 125 129 141
## Predicted 41437.30 109904.41 612.1707 60387.66 87301.233 -5594.059
## cvpred 40960.96 109999.73 -6875.2049 58143.74 87369.157 -10503.217
## PrizeMoney 26899.00 176523.00 11315.0000 7490.00 78489.000 38046.000
## CV residual -14061.96 66523.27 18190.2049 -50653.74 -8880.157 48549.217
## 143 151 154 166 177 179
## Predicted 78469.64 -8367.754 -21266.86 88662.92 5883.315 77740.67
## cvpred 76274.45 -12614.460 -29983.60 88358.04 1881.503 78065.00
## PrizeMoney 145414.00 4667.000 3816.00 114055.00 9062.000 89770.00
## CV residual 69139.55 17281.460 33799.60 25696.96 7180.497 11705.00
## 181 183 184 187 188 191
## Predicted 12640.251 18148.028 -68260.06 19818.04 119957.32 84465.30
## cvpred 7437.214 14798.705 -77832.22 18198.44 120988.55 84635.71
## PrizeMoney 20064.000 11309.000 6117.00 14098.00 160175.00 68613.00
## CV residual 12626.786 -3489.705 83949.22 -4100.44 39186.45 -16022.71
##
## Sum of squares = 96596380580 Mean square = 1971354706 n = 49
##
## fold 2
## Observations in test set: 49
## 1 3 10 18 23 26
## Predicted 24622.82 -12614.814 66066.89 -17854.07 16635.15 76718.11
## cvpred 24367.73 -8732.368 65410.51 -22012.72 10726.34 79112.86
## PrizeMoney 60661.00 3635.000 23396.00 20911.00 24814.00 33782.00
## CV residual 36293.27 12367.368 -42014.51 42923.72 14087.66 -45330.86
## 31 33 37 38 39 40
## Predicted 38505.95 38853.23 72507.12 39418.94 37750.67 18275.325
## cvpred 39414.17 35632.49 72598.35 37386.11 39375.94 2317.205
## PrizeMoney 15668.00 51770.00 59151.00 18345.00 8734.00 56873.000
## CV residual -23746.17 16137.51 -13447.35 -19041.11 -30641.94 54555.795

```

```

##          45          57          58          60          61          66          69
## Predicted 108852.99 72816.45 74630.8 35557.39 27958.76 104011.92 25768.713
## cvpred   118360.09 77427.98 75903.9 34660.35 22674.39 102055.55 22856.158
## PrizeMoney 46377.00 43951.00 129234.0 45904.00 54477.00 54862.00 15840.000
## CV residual -71983.09 -33476.98 53330.1 11243.65 31802.61 -47193.55 -7016.158
##          87          90          91          96          104          107          110
## Predicted 70314.13 140652.2 23010.77 28344.63 62046.51 68708.87 76838.35
## cvpred   67738.15 140599.3 24843.28 34573.45 62291.02 66804.74 73367.32
## PrizeMoney 56058.00 300555.0 7331.00 9149.00 117801.00 91406.00 25918.00
## CV residual -11680.15 159955.7 -17512.28 -25424.45 55509.98 24601.26 -47449.32
##          111          115          119          122          127          132
## Predicted 25631.26 -7299.596 -38049.09 85227.71 -17537.14 105864.70
## cvpred   26071.30 -8031.807 -48065.02 87244.09 -18180.15 108492.78
## PrizeMoney 42589.00 3025.000 5777.00 18513.00 4444.00 42890.00
## CV residual 16517.70 11056.807 53842.02 -68731.09 22624.15 -65602.78
##          133          139          140          144          145          146
## Predicted 9653.397 29749.07 36641.43 42158.68 57311.871 80585.81
## cvpred   10146.379 23776.13 34098.59 45635.01 55060.849 85889.20
## PrizeMoney 25135.000 37100.00 14527.00 24379.00 53634.000 68345.00
## CV residual 14988.621 13323.87 -19571.59 -21256.01 -1426.849 -17544.20
##          149          152          158          162          164          165
## Predicted 68248.89 777.2415 29781.93 44174.86 78409.11 42447.56
## cvpred   74443.22 -1741.1376 34302.33 45515.86 78936.21 39084.07
## PrizeMoney 19200.00 10715.0000 19973.00 20502.00 38471.00 19997.00
## CV residual -55243.22 12456.1376 -14329.33 -25013.86 -40465.21 -19087.07
##          171          185          186          189          192
## Predicted 46676.16 -1091.278 75922.392 61704.098 130009.74
## cvpred   46078.13 -6508.421 79428.195 61141.544 134662.32
## PrizeMoney 36289.00 84604.000 72623.000 55581.000 170460.00
## CV residual -9789.13 91112.421 -6805.195 -5560.544 35797.68
##
## Sum of squares = 87964361969      Mean square = 1795191061      n = 49
##
## fold 3
## Observations in test set: 49
##          4          9          12          16          22          25
## Predicted 57997.68 13704.64 58116.01 67755.28 92159.17 83467.39
## cvpred   47083.19 25316.09 56683.00 57165.31 64136.75 77552.07
## PrizeMoney 17516.00 86782.00 44080.00 26129.00 120927.00 33471.00
## CV residual -29567.19 61465.91 -12603.00 -31036.31 56790.25 -44081.07
##          29          49          51          52          54          55
## Predicted 73158.9954 53620.70 85483.00 85259.30 10868.55 55993.83
## cvpred   59390.6298 37954.14 69402.47 63570.95 26701.05 54386.94
## PrizeMoney 60073.0000 65174.00 132327.00 119444.00 13865.00 26301.00
## CV residual 682.3702 27219.86 62924.53 55873.05 -12836.05 -28085.94
##          68          73          74          76          83          84
## Predicted 31592.603 60155.02 66406.01 4011.872 85878.36 -2707.036
## cvpred   31848.156 57973.17 46632.71 22372.642 77016.62 6381.382
## PrizeMoney 39356.000 103594.00 57216.00 25804.000 27361.00 55014.000
## CV residual 7507.844 45620.83 10583.29 3431.358 -49655.62 48632.618
##          89          92          94          95          99          112
## Predicted 85391.54 53990.60 37606.494 44905.15 51334.21 62841.43
## cvpred   73421.94 45521.39 34691.538 50572.11 37957.41 55475.66
## PrizeMoney 54513.00 100398.00 27673.000 29296.00 53530.00 18494.00

```

```

## CV residual -18908.94 54876.61 -7018.538 -21276.11 15572.59 -36981.66
##          113      114      126      128      131      134
## Predicted -25647.112 34303.598 75723.85 16785.51 4170.275 42643.18
## cvpred      8591.756 27715.851 63314.68 31291.29 12589.382 55185.69
## PrizeMoney 12110.000 18721.000 18838.00 5285.00 8272.000 26532.00
## CV residual 3518.244 -8994.851 -44476.68 -26006.29 -4317.382 -28653.69
##          135      136      137      142      147      148      150
## Predicted 85613.89 47703.622 22086.58 152277.5 24678.33 12734.95 52252.62
## cvpred 72113.98 39626.527 34002.48 103535.2 32263.01 20894.45 47979.35
## PrizeMoney 89312.00 37869.000 11376.00 224027.0 14558.00 16455.00 111028.00
## CV residual 17198.02 -1757.527 -22626.48 120491.8 -17705.01 -4439.45 63048.65
##          155      156      157      159      167      168
## Predicted 51640.637 72008.45 64585.26 74200.7053 73003.79 70228.66
## cvpred 49754.164 61398.99 64197.61 68608.6551 69400.58 76351.45
## PrizeMoney 51005.000 36428.00 32843.00 69173.0000 27657.00 15012.00
## CV residual 1250.836 -24970.99 -31354.61 564.3449 -41743.58 -61339.45
##          169      173      174      176      178      194
## Predicted 67233.81 94382.72 78884.75 41009.953 240598.2 58267.25
## cvpred 64564.30 79527.88 66143.48 35689.817 173881.2 48096.42
## PrizeMoney 42958.00 105997.00 150889.00 36861.000 662771.0 30344.00
## CV residual -21606.30 26469.12 84745.52 1171.183 488889.8 -17752.42
##
## Sum of squares = 310309714409 Mean square = 6332851314 n = 49
##
## fold 4
## Observations in test set: 49
##          5      17      20      21      27      28
## Predicted 41197.02 18842.600 48163.74 110805.29 40706.59 112118.48
## cvpred 43253.98 16187.617 51281.29 126698.61 42840.73 128710.82
## PrizeMoney 16683.00 11989.000 19683.00 79316.00 20322.00 37751.00
## CV residual -26570.98 -4198.617 -31598.29 -47382.61 -22518.73 -90959.82
##          30      32      34      42      43      50
## Predicted 42583.34 71535.55 69123.10 37937.75 31645.9420 43950.75
## cvpred 44966.45 79449.43 76393.68 39554.57 31745.1894 46395.10
## PrizeMoney 94571.00 112443.00 37735.00 14499.00 31371.0000 15187.00
## CV residual 49604.55 32993.57 -38658.68 -25055.57 -374.1894 -31208.10
##          53      56      59      67      70      71
## Predicted 65130.749 54202.83 101098.8 85466.71 -84595.47 71541.16
## cvpred 71920.593 58597.32 115125.9 97001.67 -108563.34 79952.75
## PrizeMoney 73819.000 22340.00 57092.0 30656.00 2240.00 38188.00
## CV residual 1898.407 -36257.32 -58033.9 -66345.67 110803.34 -41764.75
##          75      78      80      82      85      97
## Predicted 61852.81 20292.99 26495.839 56013.17 65542.26 -52881.74
## cvpred 67896.86 18270.79 25823.173 61037.14 72323.22 -70246.41
## PrizeMoney 82196.00 7583.00 24724.000 16927.00 20612.00 2692.00
## CV residual 14299.14 -10687.79 -1099.173 -44110.14 -51711.22 72938.41
##          98      100      102      103      106      116
## Predicted 56401.66 91103.16 155850.0 44848.86 109741.65 96414.63
## cvpred 61685.45 102719.98 181435.3 46965.61 125906.95 110007.84
## PrizeMoney 15964.00 58953.00 70421.0 18085.00 58189.00 83483.00
## CV residual -45721.45 -43766.98 -111014.3 -28880.61 -67717.95 -26524.84
##          118      120      123      124      130      138
## Predicted 65781.32 27882.972 44476.824 61248.14 75144.02 46727.73
## cvpred 73044.04 27512.094 46936.669 67306.88 84286.33 49557.08

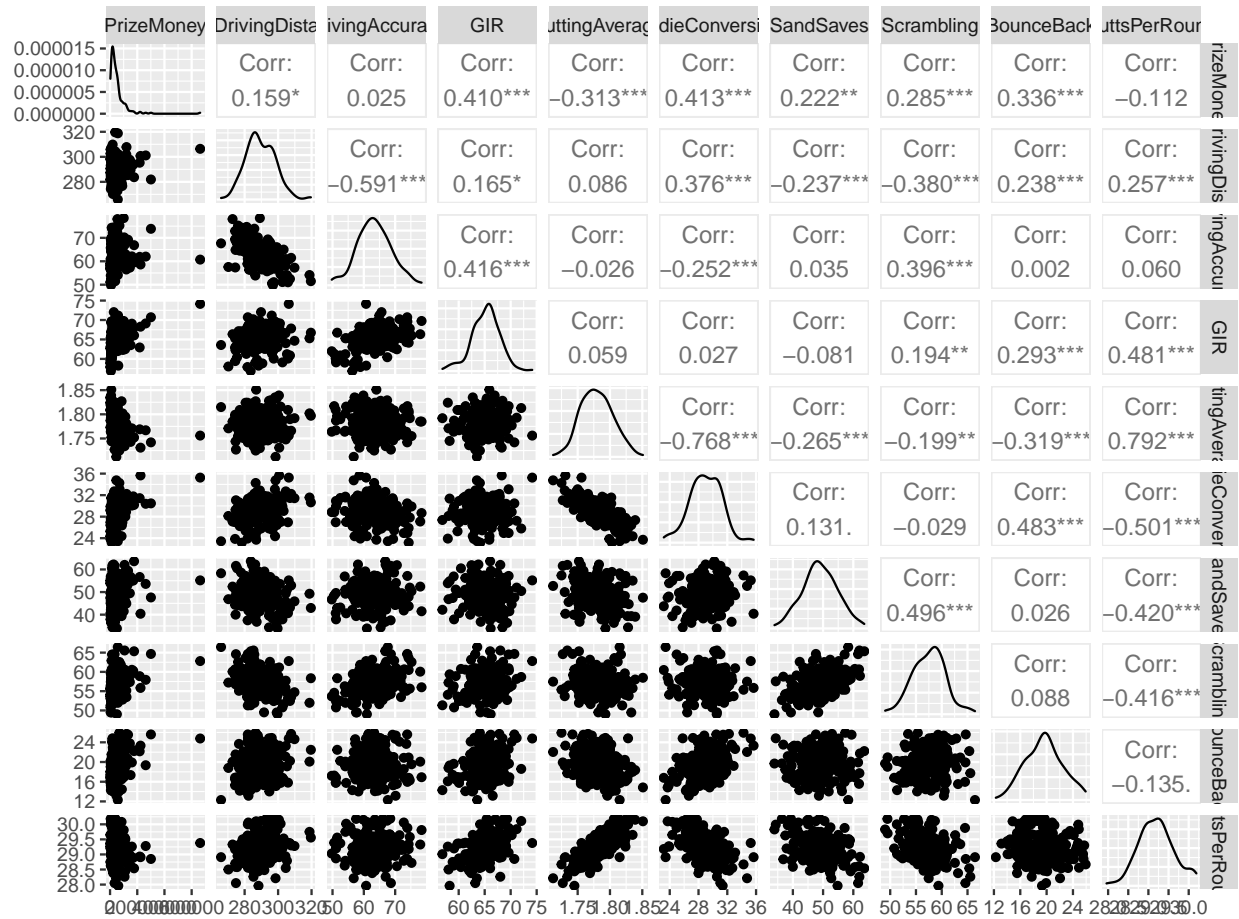
```



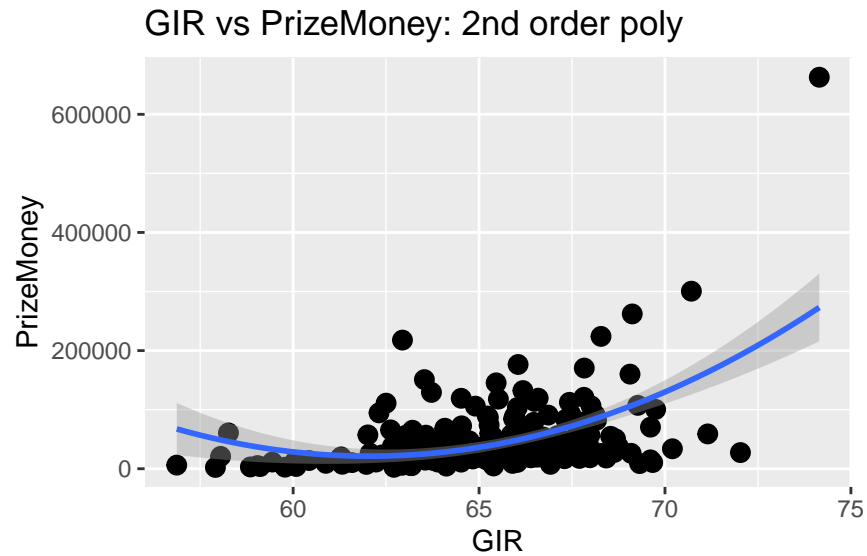
```
## PrizeMoney    20188.00 26123.000 41390.000  22467.00  56693.00  23403.00
## CV residual  -52856.04 -1389.094 -5546.669 -44839.88 -27593.33 -26154.08
##              153         160         161         163         170         172
## Predicted    81690.36 44337.06034 66430.47  60836.73 -1424.039 133847.00
## cvpred       92037.17 47113.71067 73828.37  66619.87 -8474.102 154466.12
## PrizeMoney   119240.00 47046.00000 91808.00  56305.00 11421.000 106577.00
## CV residual   27202.83  -67.71067 17979.63 -10314.87 19895.102 -47889.12
##              175         180         182         190         193         195         196
## Predicted    43164.21  3729.020  25025.13  6840.089 23591.71  60791.44 33277.00
## cvpred       46196.38 -2005.631  22976.60  2305.937 22542.64  66954.52 33238.05
## PrizeMoney    15098.00 65783.000  11187.00 10354.000 12803.00  38043.00 90824.00
## CV residual  -31098.38 67788.631 -11789.60  8048.063 -9739.64 -28911.52 57585.95
##
## Sum of squares = 95370706618      Mean square = 1946340951      n = 49
##
## Overall (Sum over all 49 folds)
##           ms
## 3011434508
```

```
# pair plot
ggpairs(num_df, size=.5)
```

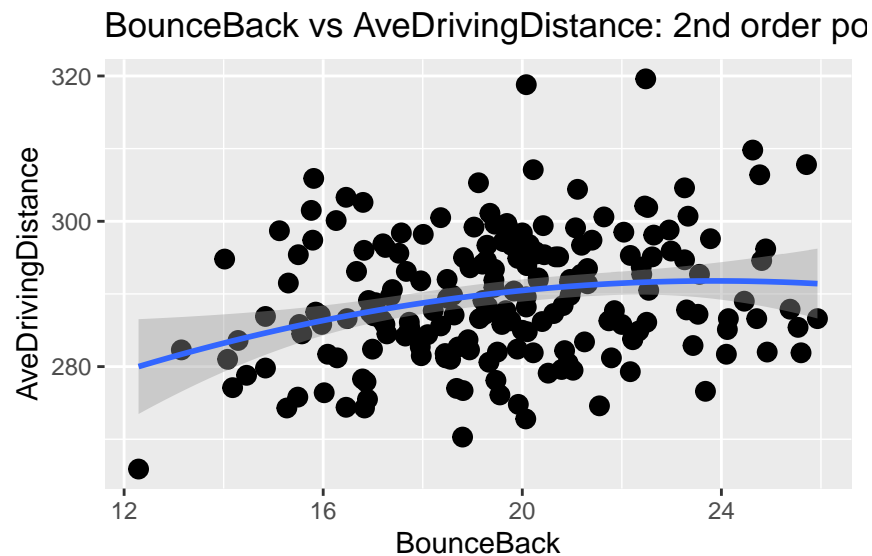
b. Evaluate scatterplots to determine which second-order terms should be tested. Test them using 5-fold cross validation and add them one-by-one until you arrive at a model you feel is appropriate. Present the model.



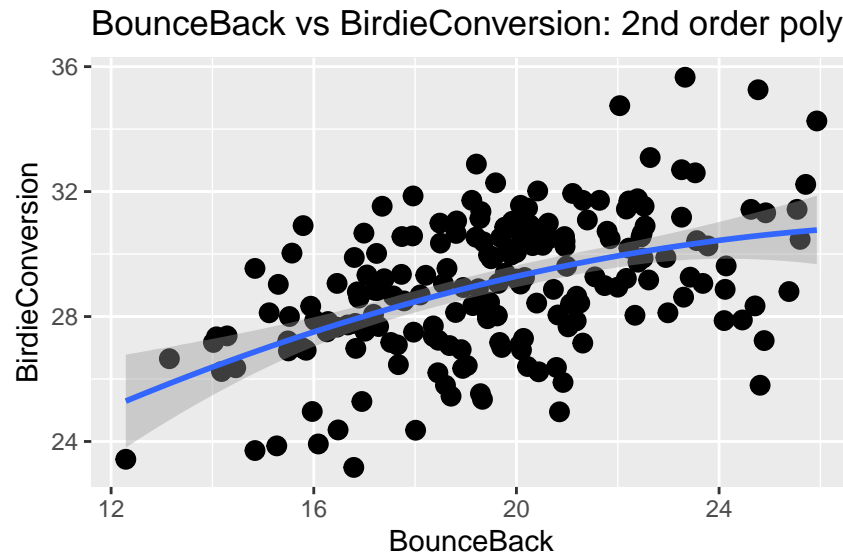
```
# scatter plots
plt_1 <- ggplot(data = num_df, aes(x = GIR, y = PrizeMoney))
plt_1 + geom_point(size=3) +
  geom_smooth(method = "lm", formula = y ~ poly(x, 2, raw = TRUE)) +
  ggtitle("GIR vs PrizeMoney: 2nd order poly")
```



```
plt_1 <- ggplot(data = num_df, aes(x = BounceBack, y = AveDrivingDistance))
plt_1 + geom_point(size=3) +
  geom_smooth(method = "lm", formula = y ~ poly(x, 2, raw = TRUE)) +
  ggtitle("BounceBack vs AveDrivingDistance: 2nd order poly")
```



```
plt_1 <- ggplot(data = num_df, aes(x = BounceBack, y = BirdieConversion))
plt_1 + geom_point(size=3) +
  geom_smooth(method = "lm", formula = y ~ poly(x, 2, raw = TRUE)) +
  ggtitle("BounceBack vs BirdieConversion: 2nd order poly")
```



```
# try second order model
sec_ordr_model <- lm(PrizeMoney~(SandSaves+GIR+BirdieConversion)^2, data = num_df)

summary(sec_ordr_model)
```

```
##
## Call:
## lm(formula = PrizeMoney ~ (SandSaves + GIR + BirdieConversion)^2,
##     data = num_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -131379  -21075   -6305   14861  184661
##
## Coefficients:
##              Estimate Std. Error t value      Pr(>|t|)
## (Intercept)   8445009.3  1012279.1   8.343 0.00000000000000150
## SandSaves     -40082.5   13989.8  -2.865   0.004640
## GIR          -115968.5   14125.1  -8.210 0.00000000000000338
## BirdieConversion -285772.6  30201.7  -9.462 < 0.00000000000000002
## SandSaves:GIR      259.5     185.0   1.402   0.162445
## SandSaves:BirdieConversion  865.8     223.3   3.877   0.000146
## GIR:BirdieConversion  3891.4     415.9   9.358 < 0.00000000000000002
##
## (Intercept)          ***
## SandSaves             **
## GIR                   ***
## BirdieConversion      ***
## SandSaves:GIR
## SandSaves:BirdieConversion ***
## GIR:BirdieConversion  ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 41370 on 189 degrees of freedom
## Multiple R-squared:  0.5938, Adjusted R-squared:  0.5809
## F-statistic: 46.04 on 6 and 189 DF,  p-value: < 0.00000000000000022
```

```
# add terms
sec_df <- num_df %>%
  mutate(AveDrvDistSec = AveDrivingDistance^2,
         DrvAccSec = DrivingAccuracy^2,
         GIRSec = GIR^2,
         BouncBckSec = BounceBack^2)

model_2 <- lm(PrizeMoney~BouncBckSec+GIRSec+BounceBack+BirdieConversion+GIR,
             data = sec_df)

summary(model_2)
```

```
##
## Call:
## lm(formula = PrizeMoney ~ BouncBckSec + GIRSec + BounceBack +
##     BirdieConversion + GIR, data = sec_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -113508  -25116   -3667   13324   304616
##
## Coefficients:
##              Estimate Std. Error t value    Pr(>|t|)
## (Intercept)   6290703.7  1183754.1   5.314 0.000000298288 ***
## BouncBckSec     1147.4     344.4    3.332   0.00104 **
## GIRSec         1608.6     283.6    5.672 0.000000051837 ***
## BounceBack    -44174.0    13709.9  -3.222   0.00150 **
## BirdieConversion 11596.6     1773.4    6.539 0.000000000557 ***
## GIR          -199534.9    36826.5  -5.418 0.000000180825 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 47140 on 190 degrees of freedom
## Multiple R-squared:  0.4699, Adjusted R-squared:  0.4559
## F-statistic: 33.68 on 5 and 190 DF,  p-value: < 0.00000000000000022
```

```
# add interaction terms
thr_df <- sec_df %>%
  mutate(AvgDrvD_BouncBck = AveDrivingDistance*BounceBack,
         DrvAcc_GIR = DrivingAccuracy*GIR,
         PuttAvg_Gir = PuttingAverage*GIR,
         PuttAvg_BouncBck = PuttingAverage*BounceBack,
         PuttAvg_Scrmb = PuttingAverage*Scrambling,
         Scrmb_BouncBck = Scrambling*BounceBack,
         SndSvs_Scrmb = SandSaves*Scrambling) %>%
  dplyr::select(-c(Scrambling, PuttsPerRound, BounceBack))

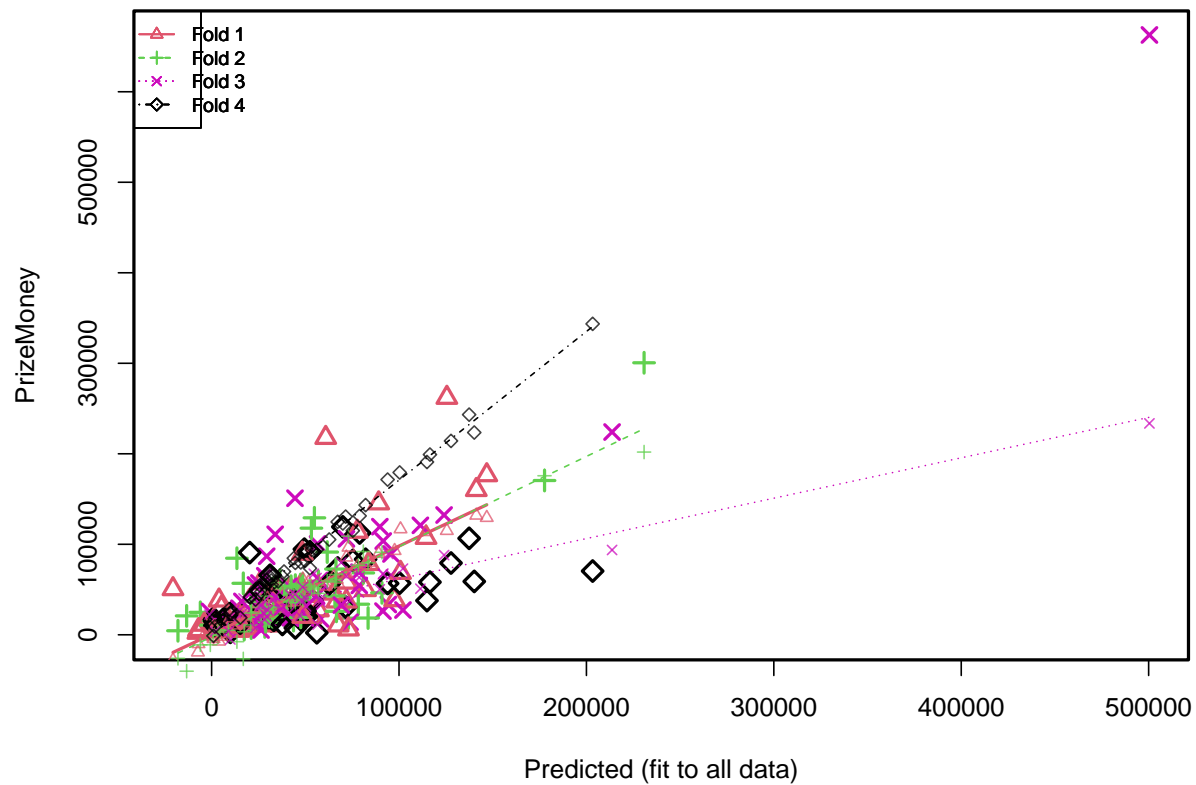
model_3 <- lm(PrizeMoney~., data = thr_df)

summary(model_3)
```

```
##
## Call:
## lm(formula = PrizeMoney ~ ., data = thr_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -132898  -19469   -1252   13954  162350
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -21236344.23   6162605.32  -3.446  0.000710 ***
## AveDrivingDistance    29741.03    18419.43   1.615  0.108157
## DrivingAccuracy     52351.48    15224.66   3.439  0.000728 ***
## GIR             121479.42     88612.67   1.371  0.172131
## PuttingAverage  12494032.77   2886857.42   4.328 0.00002506254 ***
## BirdieConversion    9052.88     2940.44   3.079  0.002408 **
## SandSaves      -11296.81     7317.91  -1.544  0.124432
## AveDrvDistSec     -59.25        32.93  -1.799  0.073680 .
## DrvAccSec         347.43       104.76   3.316  0.001105 **
## GIRSec           1967.91       312.83   6.291 0.00000000238 ***
## BouncBckSec       611.47       320.00   1.911  0.057633 .
## AvgDrvD_BouncBck   217.77      143.47   1.518  0.130815
## DrvAcc_GIR       -1506.39      305.74  -4.927 0.00000189927 ***
## PuttAvg_Gir      -153217.47    47078.24  -3.255  0.001359 **
## PuttAvg_BouncBck  -84807.79    26861.57  -3.157  0.001871 **
## PuttAvg_Scrmb    -16577.83     5245.97  -3.160  0.001854 **
## Scrmb_BouncBck    1124.35      346.55   3.244  0.001406 **
## SndSvs_Scrmb      212.28      126.21   1.682  0.094337 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 39130 on 178 degrees of freedom
## Multiple R-squared:  0.6578, Adjusted R-squared:  0.6251
## F-statistic: 20.12 on 17 and 178 DF, p-value: < 0.00000000000000022
```

```
# cross validation
cv_sec_model <- CVlm(data = thr_df,
                     form.lm = formula(PrizeMoney~.),
                     m = 4)
```

Small symbols show cross-validation predicted values



```
##
## fold 1
## Observations in test set: 49
##      2      6      7      8     11     13     14
## Predicted 125525.9 114423.954 -20615.93 26031.22 40232.20 35070.493 82142.73
## cvpred    115000.8 113737.133 -28097.96 29458.10 35286.23 54060.569 77070.04
## PrizeMoney 262045.0 107294.000 50620.00 57273.00 29567.00 47172.000 49640.00
## CV residual 147044.2 -6443.133 78717.96 27814.90 -5719.23 -6888.569 -27430.04
##      15      19      24      35      36      41
## Predicted 47453.28 44068.379 56970.23 97645.69 41954.907 65158.24
## cvpred    43601.67 36304.491 58455.55 92853.37 41647.658 64109.49
## PrizeMoney 53610.00 28658.000 27224.00 38455.00 50249.000 45752.00
## CV residual 10008.33 -7646.491 -31231.55 -54398.37 8601.342 -18357.49
##      44      46      47      48      62      63
## Predicted 32356.856 535.8664 67499.17 14358.32 29923.08 60889.14
## cvpred    33206.462 -2262.0122 56530.42 27349.05 24039.38 53400.27
## PrizeMoney 38275.000 16630.0000 10504.00 13262.00 43820.00 217748.00
## CV residual 5068.538 18892.0122 -46026.42 -14087.05 19780.62 164347.73
##      64      65      72      77      79      81
## Predicted -7005.432 29842.5 1031.250 71895.82 72036.846 17390.88
## cvpred    -10046.184 40079.6 -4462.864 85602.14 67171.379 21238.31
## PrizeMoney 5402.000 10528.0 13031.000 36918.00 57824.000 5265.00
## CV residual 15448.184 -29551.6 17493.864 -48684.14 -9347.379 -15973.31
##      86      88      93     101     105     108
```

```

## Predicted      51655.72  53070.12  66793.97  -7305.663  5242.526  20068.09
## cvpred        57954.25  47833.94  61091.90  -19294.576  -1960.122  12845.57
## PrizeMoney    43173.00  19594.00  37004.00   2426.000  30068.000  37214.00
## CV residual   -14781.25 -28239.94 -24087.90  21720.576  32028.122  24368.43
##              109      117      121      125      129      141
## Predicted    35370.016 146822.51  2136.900  18752.07  83830.512  3959.518
## cvpred       29086.304 129385.82  7380.533  19768.63  79810.694 -7281.394
## PrizeMoney   26899.000 176523.00 11315.000   7490.00  78489.000  38046.000
## CV residual  -2187.304  47137.18  3934.467 -12278.63 -1321.694  45327.394
##              143      151      154      166      177      179
## Predicted     89154.48 14435.659  1564.737  77737.54  9775.817  48427.42
## cvpred        89654.58 10580.604  8259.098  75069.58  18408.556  48737.12
## PrizeMoney   145414.00  4667.000  3816.000 114055.00  9062.000  89770.00
## CV residual   55759.42 -5913.604 -4443.098  38985.42 -9346.556  41032.88
##              181      183      184      187      188      191
## Predicted     48649.53 -3926.8235  73029.20 15505.579 141227.09 100800.37
## cvpred        61361.97 -118.7371  96588.58 16109.054 131919.75 116793.29
## PrizeMoney    20064.00 11309.0000   6117.00 14098.000 160175.00  68613.00
## CV residual  -41297.97 11427.7371 -90471.58 -2011.054  28255.25 -48180.29
##
## Sum of squares = 95938616703      Mean square = 1957930953      n = 49
##
## fold 2
## Observations in test set: 49
##              1          3          10          18          23          26
## Predicted    36443.207  8990.173  49794.58 -13328.28 -6017.608  78279.55
## cvpred       53573.944  4989.405  41177.98 -40236.94 -11130.060  76882.30
## PrizeMoney   60661.000  3635.000  23396.00  20911.00  24814.000  33782.00
## CV residual   7087.056 -1354.405 -17781.98  61147.94  35944.060 -43100.30
##              31          33          37          38          39          40          45
## Predicted    43691.33 33103.53 57025.21  73004.63  28391.76  16900.04  90905.52
## cvpred       45430.75 30472.50 45769.88 108845.64  28199.55 -26600.05  91135.25
## PrizeMoney   15668.00 51770.00 59151.00  18345.00   8734.00  56873.00  46377.00
## CV residual  -29762.75 21297.50 13381.12 -90500.64 -19465.55  83473.05 -44758.25
##              57          58          60          61          66          69
## Predicted    46332.006  54852.64 52174.823 48115.306 44672.96   751.02360
## cvpred       49820.926  52424.94 54003.906 55556.455 35987.39  -53.90664
## PrizeMoney   43951.000 129234.00 45904.000 54477.000 54862.00 15840.00000
## CV residual  -5869.926  76809.06 -8099.906 -1079.455 18874.61 15893.90664
##              87          90          91          96          104          107          110
## Predicted    48639.80 230765.03 21130.63 4456.974  53246.11 61693.13  66623.51
## cvpred       38707.01 201895.96 23992.64 3049.633  50622.10 59495.95  61216.81
## PrizeMoney   56058.00 300555.00  7331.00 9149.000 117801.00 91406.00  25918.00
## CV residual  17350.99  98659.04 -16661.64 6099.367  67178.90 31910.05 -35298.81
##              111          115          119          122          127          132
## Predicted    38989.786  3366.764 17397.43  83498.36 -17950.83  65797.21
## cvpred       50677.369  5515.055  3280.68  79498.29 -26063.14  58401.08
## PrizeMoney   42589.000  3025.000  5777.00  18513.00   4444.00  42890.00
## CV residual  -8088.369 -2490.055  2496.32 -60985.29  30507.14 -15511.08
##              133          139          140          144          145          146          149
## Predicted    34373.15 20899.06  28790.1 26022.553 42402.33  80952.96  47554.53
## cvpred       57694.89 10879.31 29556.6 30642.886 35874.50  91948.32  40768.97
## PrizeMoney   25135.00 37100.00 14527.0 24379.000 53634.00  68345.00  19200.00
## CV residual  -32559.89 26220.69 -15029.6 -6263.886 17759.50 -23603.32 -21568.97

```



```

##          152          158          162          164          165          171
## Predicted      -687.8284  28364.99  30630.83  47582.312  32528.86  40038.804
## cvpred        -11118.1922  42743.63  30839.58  42571.392  30242.77  38855.571
## PrizeMoney    10715.0000  19973.00  20502.00  38471.000  19997.00  36289.000
## CV residual   21833.1922 -22770.63 -10337.58 -4100.392 -10245.77 -2566.571
##          185          186          189          192
## Predicted    13500.206  66356.28  47431.9535  177650.813
## cvpred       -7620.203  66530.14  55411.5171  175718.721
## PrizeMoney   84604.000  72623.00  55581.0000  170460.000
## CV residual  92224.203  6092.86   169.4829  -5258.721
##
## Sum of squares = 68171605068      Mean square = 1391257246      n = 49
##
## fold 3
## Observations in test set: 49
##          4          9          12          16          22          25          29
## Predicted    58148.81  29394.50  32772.725  91434.65  111402.8  94289.34  57791.63
## cvpred       36372.34  20270.17  37959.168  66786.45  50901.8  89266.20  39143.95
## PrizeMoney   17516.00  86782.00  44080.000  26129.00  120927.0  33471.00  60073.00
## CV residual  -18856.34  66511.83  6120.832  -40657.45  70025.2  -55795.20  20929.05
##          49          51          52          54          55          68          73
## Predicted    28368.99  124045.01  89767.86  73877.49  54514.57  47287.72  91567.54
## cvpred       16771.78  88075.36  50264.01  37618.58  67433.15  20863.38  67658.73
## PrizeMoney   65174.00  132327.00  119444.00  13865.00  26301.00  39356.00  103594.00
## CV residual  48402.22  44251.64  69179.99  -23753.58  -41132.15  18492.62  35935.27
##          74          76          83          84          89          92          94
## Predicted    25233.38  -1111.995  102104.62  23411.49  78791.248  56536.35  47980.86
## cvpred       16250.34  22261.983  73063.81  7611.11  63395.707  11280.83  38487.14
## PrizeMoney   57216.00  25804.000  27361.00  55014.00  54513.000  100398.00  27673.00
## CV residual  40965.66  3542.017  -45702.81  47402.89  -8882.707  89117.17  -10814.14
##          95          99          112          113          114          126
## Predicted    14588.403  41256.70  50145.04  10010.135  29970.959  42018.73
## cvpred       26003.892  24342.99  40085.10  -5157.676  27184.216  44101.69
## PrizeMoney   29296.000  53530.00  18494.00  12110.000  18721.000  18838.00
## CV residual  3292.108  29187.01  -21591.10  17267.676  -8463.216  -25263.69
##          128          131          134          135          136          137          142
## Predicted    26371.41  9025.244  26322.135  95701.25  27660.63  1888.618  213682.03
## cvpred       33288.34  4091.210  31665.454  66380.80  24254.27  3828.593  93691.68
## PrizeMoney   5285.00  8272.000  26532.000  89312.00  37869.00  11376.000  224027.00
## CV residual  -28003.34  4180.790  -5133.454  22931.20  13614.73  7547.407  130335.32
##          147          148          150          155          156          157          159
## Predicted    17066.11  10074.310  33920.67  50432.93  36641.597  69202.8  78605.69
## cvpred       40088.50  20462.979  42485.94  31366.38  27522.616  79827.9  46749.22
## PrizeMoney   14558.00  16455.000  111028.00  51005.00  36428.000  32843.0  69173.00
## CV residual  -25530.50  -4007.979  68542.06  19638.62  8905.384  -46984.9  22423.78
##          167          168          169          173          174          176          178
## Predicted    48632.30  22695.09  55995.55  71920.72  44488.28  16147.02  500420.6
## cvpred       52777.23  40649.24  62679.95  64873.25  44736.30  23523.87  233567.4
## PrizeMoney   27657.00  15012.00  42958.00  105997.00  150889.00  36861.00  662771.0
## CV residual  -25120.23  -25637.24  -19721.95  41123.75  106152.70  13337.13  429203.6
##          194
## Predicted    37253.055
## cvpred       28890.178
## PrizeMoney   30344.000

```

```

## CV residual 1453.822
##
## Sum of squares = 270559263230    Mean square = 5521617617    n = 49
##
## fold 4
## Observations in test set: 49
##      5      17      20      21      27      28
## Predicted 23649.79 9891.795 25627.34 127742.1 23441.69 114911.8
## cvpred    50360.75 24035.508 54566.43 214215.0 38902.04 190915.3
## PrizeMoney 16683.00 11989.000 19683.00 79316.0 20322.00 37751.0
## CV residual -33677.75 -12046.508 -34883.43 -134899.0 -18580.04 -153164.3
##      30      32      34      42      43      50
## Predicted 49505.842 78973.02 30997.38 20577.71 29456.83 31824.54
## cvpred    92901.535 131366.05 64260.31 41109.56 60568.11 59987.01
## PrizeMoney 94571.000 112443.00 37735.00 14499.00 31371.00 15187.00
## CV residual 1669.465 -18923.05 -26525.31 -26610.56 -29197.11 -44800.01
##      53      56      59      67      70      71
## Predicted 67272.16 38644.9 100344.4 71520.10 56133.95 53488.45
## cvpred    124782.36 69875.3 179345.6 130541.51 94118.69 93841.22
## PrizeMoney 73819.00 22340.0 57092.0 30656.00 2240.00 38188.00
## CV residual -50963.36 -47535.3 -122253.6 -99885.51 -91878.69 -55653.22
##      75      78      80      82      85      97
## Predicted 75347.36 44672.51 10932.552 47557.92 49093.49 10015.89
## cvpred    115026.57 79424.35 26322.898 79939.85 91474.86 23061.97
## PrizeMoney 82196.00 7583.00 24724.000 16927.00 20612.00 2692.00
## CV residual -32830.57 -71841.35 -1598.898 -63012.85 -70862.86 -20369.97
##      98      100      102      103      106      116
## Predicted 33208.48 140149.4 203318.9 994.5391 116500.6 82171.18
## cvpred    66298.99 223471.0 343551.5 -1164.1277 199127.2 143314.29
## PrizeMoney 15964.00 58953.0 70421.0 18085.0000 58189.0 83483.00
## CV residual -50334.99 -164518.0 -273130.5 19249.1277 -140938.2 -59831.29
##      118      120      123      124      130      138
## Predicted 50524.37 49885.76 31995.19 35501.80 93913.42 9275.927
## cvpred    93619.85 81590.50 55155.44 59062.78 171478.84 27955.728
## PrizeMoney 20188.00 26123.00 41390.00 22467.00 56693.00 23403.000
## CV residual -73431.85 -55467.50 -13765.44 -36595.78 -114785.84 -4552.728
##      153      160      161      163      170      172
## Predicted 70018.444 25502.000 52457.37 62746.32 37765.32 137418.2
## cvpred    123026.409 45325.373 73473.97 105219.73 64430.14 243253.2
## PrizeMoney 119240.000 47046.000 91808.00 56305.00 11421.00 106577.0
## CV residual -3786.409 1720.627 18334.03 -48914.73 -53009.14 -136676.2
##      175      180      182      190      193      195
## Predicted 1612.051 31159.834 6212.218 1739.241 15292.755 43869.35
## cvpred    17648.188 67335.474 19426.545 9059.469 18912.429 84590.00
## PrizeMoney 15098.000 65783.000 11187.000 10354.000 12803.000 38043.00
## CV residual -2550.188 -1552.474 -8239.545 1294.531 -6109.429 -46547.00
##      196
## Predicted 20344.40
## cvpred    42001.29
## PrizeMoney 90824.00
## CV residual 48822.71
##
## Sum of squares = 286208693787    Mean square = 5840993751    n = 49
##

```

```
## Overall (Sum over all 49 folds)
##      ms
## 3677949892
```

```
#
part_c_df <- thr_df %>%
  mutate(gir_sec = poly(GIR, 2, raw=TRUE),
         bird_conv_sec = poly(BirdieConversion, 2, raw=T),
         sand_saves_sec = poly(SandSaves, 2, raw=T)) %>%
  dplyr::select(c(PrizeMoney, GIR, BirdieConversion, SandSaves, gir_sec, bird_conv_sec,
                 sand_saves_sec, Scrmb_BouncBck, PuttAvg_Scrmb,
                 PuttAvg_BouncBck, PuttAvg_Gir, DrvAcc_GIR, BouncBckSec))

# second order model
model_5 <- lm(PrizeMoney~., data = part_c_df)

summary(model_5)
```

c. Beginning from scratch, engineer all possible second-order terms and add them to your dataset. From this dataset, produce a model using backward selection. Evaluate this model using 5-fold cross validation. Do you arrive at the same model as above? Explain.

```
##
## Call:
## lm(formula = PrizeMoney ~ ., data = part_c_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -125736  -20205   -2208   15527   238778
##
## Coefficients: (3 not defined because of singularities)
##              Estimate Std. Error t value    Pr(>|t|)
## (Intercept)   6656717.34 1104322.14   6.028 0.00000000896 ***
## GIR          -176664.40   34768.66  -5.081 0.00000092100 ***
## BirdieConversion -88272.69   26125.62  -3.379   0.000890 ***
## SandSaves      -1567.58    6645.50  -0.236   0.813785
## gir_sec1              NA          NA      NA         NA
## gir_sec2       1152.99     274.61   4.199 0.00004186107 ***
## bird_conv_sec1       NA          NA      NA         NA
## bird_conv_sec2    1674.61     447.27   3.744   0.000242 ***
## sand_saves_sec1       NA          NA      NA         NA
## sand_saves_sec2     30.37      67.63   0.449   0.653952
## Scrmb_BouncBck    1098.05     325.08   3.378   0.000893 ***
## PuttAvg_Scrmb    -10141.07    3652.70  -2.776   0.006070 **
## PuttAvg_BouncBck -49555.66   12607.44  -3.931   0.000120 ***
## PuttAvg_Gir      21654.82    7494.30   2.890   0.004325 **
## DrvAcc_GIR        -21.42      11.66  -1.836   0.067956 .
## BouncBckSec       643.00     309.79   2.076   0.039333 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 42510 on 183 degrees of freedom
## Multiple R-squared:  0.5847, Adjusted R-squared:  0.5574
## F-statistic: 21.47 on 12 and 183 DF,  p-value: < 0.00000000000000022
```

Now, let's try backward selection.

```
# backward selection
bckwrд_selctn <- stepAIC(model_5, direction = "backward")
```

```
## Start:  AIC=4190.3
## PrizeMoney ~ GIR + BirdieConversion + SandSaves + gir_sec + bird_conv_sec +
##      sand_saves_sec + Scrmb_BouncBck + PuttAvg_Scrmb + PuttAvg_BouncBck +
##      PuttAvg_Gir + DrvAcc_GIR + BouncBckSec
##
##
## Step:  AIC=4190.3
## PrizeMoney ~ GIR + BirdieConversion + gir_sec + bird_conv_sec +
##      sand_saves_sec + Scrmb_BouncBck + PuttAvg_Scrmb + PuttAvg_BouncBck +
##      PuttAvg_Gir + DrvAcc_GIR + BouncBckSec
##
##
## Step:  AIC=4190.3
## PrizeMoney ~ GIR + gir_sec + bird_conv_sec + sand_saves_sec +
##      Scrmb_BouncBck + PuttAvg_Scrmb + PuttAvg_BouncBck + PuttAvg_Gir +
##      DrvAcc_GIR + BouncBckSec
##
##
## Step:  AIC=4190.3
## PrizeMoney ~ gir_sec + bird_conv_sec + sand_saves_sec + Scrmb_BouncBck +
##      PuttAvg_Scrmb + PuttAvg_BouncBck + PuttAvg_Gir + DrvAcc_GIR +
##      BouncBckSec
##
##
##          Df    Sum of Sq      RSS      AIC
## <none>                330726784077 4190.3
## - sand_saves_sec      2  9087838897 339814622974 4191.6
## - DrvAcc_GIR          1  6093120367 336819904444 4191.9
## - BouncBckSec         1  7785553418 338512337495 4192.9
## - PuttAvg_Scrmb       1 13930246485 344657030562 4196.4
## - PuttAvg_Gir         1 15089169972 345815954049 4197.0
## - Scrmb_BouncBck      1 20619348233 351346132310 4200.2
## - PuttAvg_BouncBck    1 27922307163 358649091240 4204.2
## - bird_conv_sec       2 44350444173 375077228250 4211.0
## - gir_sec             2 49812186522 380538970599 4213.8
```

```
print(bckwrд_selctn$anova)
```

```
## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## PrizeMoney ~ GIR + BirdieConversion + SandSaves + gir_sec + bird_conv_sec +
##      sand_saves_sec + Scrmb_BouncBck + PuttAvg_Scrmb + PuttAvg_BouncBck +
```

```
##      PuttAvg_Gir + DrvAcc_GIR + BouncBckSec
##
## Final Model:
## PrizeMoney ~ gir_sec + bird_conv_sec + sand_saves_sec + Scrmb_BouncBck +
##      PuttAvg_Scrmb + PuttAvg_BouncBck + PuttAvg_Gir + DrvAcc_GIR +
##      BouncBckSec
##
##
##              Step Df      Deviance Resid. Df   Resid. Dev      AIC
## 1
## 2      - SandSaves  0 0.0000000000      183 330726784077 4190.303
## 3 - BirdieConversion 0 0.0001220703      183 330726784077 4190.303
## 4      - GIR      0 0.0000000000      183 330726784077 4190.303
```

Let's see how the final model is performing.

```
model_final <- lm(PrizeMoney ~ gir_sec + bird_conv_sec + sand_saves_sec + Scrmb_BouncBck +
  PuttAvg_Scrmb + PuttAvg_BouncBck + PuttAvg_Gir + DrvAcc_GIR +
  BouncBckSec, data = part_c_df)

summary(model_final)
```

```
##
## Call:
## lm(formula = PrizeMoney ~ gir_sec + bird_conv_sec + sand_saves_sec +
##      Scrmb_BouncBck + PuttAvg_Scrmb + PuttAvg_BouncBck + PuttAvg_Gir +
##      DrvAcc_GIR + BouncBckSec, data = part_c_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -125736  -20205   -2208   15527  238778
##
## Coefficients:
##              Estimate Std. Error t value      Pr(>|t|)
## (Intercept)   6656717.34 1104322.14   6.028 0.00000000896 ***
## gir_sec1      -176664.40   34768.66  -5.081 0.00000092100 ***
## gir_sec2         1152.99    274.61   4.199 0.00004186107 ***
## bird_conv_sec1  -88272.69   26125.62  -3.379   0.000890 ***
## bird_conv_sec2   1674.61    447.27   3.744   0.000242 ***
## sand_saves_sec1 -1567.58   6645.50  -0.236   0.813785
## sand_saves_sec2    30.37     67.63   0.449   0.653952
## Scrmb_BouncBck   1098.05    325.08   3.378   0.000893 ***
## PuttAvg_Scrmb  -10141.07   3652.70  -2.776   0.006070 **
## PuttAvg_BouncBck -49555.66  12607.44  -3.931   0.000120 ***
## PuttAvg_Gir     21654.82   7494.30   2.890   0.004325 **
## DrvAcc_GIR       -21.42     11.66  -1.836   0.067956 .
## BouncBckSec      643.00    309.79   2.076   0.039333 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 42510 on 183 degrees of freedom
## Multiple R-squared:  0.5847, Adjusted R-squared:  0.5574
## F-statistic: 21.47 on 12 and 183 DF, p-value: < 0.00000000000000022
```

From comparison, it is clear that we've arrived the model from earlier. This is because of the data used to build the model. We've used the data which yields the best model possible with features available to us.

As the same data has been used to perform stepwise model selection, it will not be able to achieve local maxima or minima of the metric. Yet, it will follow a particular path by adding or removing the variables from the iteration.

d. You have used two procedures to build a second-order model. Compare these two procedures. Which do you think is “best”? Explain. In the first method, we first identify the features that are significant by building a full model with all the features. Then, gradually, we remove the features which are not significant. This is a iterative process where we remove features one-by-one to get the best version of the model. However, in the second method, we build a model using stepwise selection where we pass in a full model object and select the direction for stepwise search. In this method, we build a multiple versions of model based on its AIC (prediction error, similar to adj R-squared) and features.

Building a model using backward or forward selection method gives you more flexibility in terms of manual efforts. This way, we can build multiple versions of model and pick one of our choice which is accurate and less complex. Also, it tries all the combination of model from null model (model with no features) to full model (with all features) by defining the scope. Therefore, stepwise selection is best for building a model.