

“I have done this assignment completely on my own. I have not copied it, nor have I given my solution to anyone else. I understand that if I am involved in plagiarism or cheating I will have to sign an official form that I have cheated and that this form will be stored in my official university record. I also understand that I will receive a grade of **0** for the involved assignment for my first offense and that I will receive a grade of **“F” for the course** for any additional offense.”

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1. Insertion Sort

Instruction count using Method 1.

Code snippet: -

```
while (i < number)
{
    j = i;
    while(j > 0 && array[j] < array[j-1])
    {
        swapping(&array[j],&array[j-1]);
        j--;
    }
    i++;
}
```

As per above code,

The outer loop executes from 1 to Number of input array elements times so N times.

The inner while loop will execute till value of i

$$\begin{aligned} T(n) &= T(n-1) + (n-1) \\ &= T(n-2) + (n-2) + (n-1) \\ &= T(n-3) + (n-3) + (n-2) + (n-1) \\ &\dots\dots\dots \\ &= T(1) + 1 + 2 + 3 + \dots + (n-1) \end{aligned}$$

So to calculate instruction count as per Summation formula,

$$\begin{aligned} \sum_{i=1}^n i &= n(n+1)/2 \\ &= (n^2 + n)/2 \end{aligned}$$

So this proves the insertion sort runs $\Theta(n^2)$.

2. Counting Sort

Instruction count using Method 2.

Code snippet: -

```
while (i < number) {
    int second = array[i];
    second_array[second] = second_array[second] + 1;
    i++;
}
while (i < number) {
    int second = array[i];
    int location = second_array[second] - 1;
    result[location] = second;
    second_array[second] = second_array[second] - 1;
    i++;
}
```

As per above code,

For this while loop will execute from 0 to input array number i.e. N-1 times.

$$T(n) = 1$$

$$T(n) = T(n-1) + 1$$

$$= T(n-2) + 1 + 1$$

$$= T(n-3) + 1 + 1 + 1$$

.....

$$= T(1) + 1+1+1+....+1$$

$$= 1+n-1$$

$$= n$$

So to calculate instruction count as per Summation formula,

$$\sum_{i=1}^n 1 = n$$

So this proves the counting sort runs $\Theta(n)$.

3. Merge Sort

Instruction count using method 1.

Code snippet: -

```
While ((n <= higher) && (x <= middle))
{
    If (array[n] >= array[x]){
        other[j] = array[x];
```

```

        x++;
    }
    else{
        other[j] = array[n];
        n++;
    }
    j++;
}

if(x > middle){
    p=n;
    while(p<=higher){
        other[j] = array[p];
        j++;
        p++;
    }
}
else{
    p=x;
    while(p<=middle){
        other[j] = array[p];
        j++;
        p++;
    }
}
}

```

$$\begin{aligned}
 T(n) &= 2T(n/2) + n \quad \text{For } n=2^k \\
 &= 4[T(n/4) + (n/2)] + 2n \\
 &= 8[T(n/8)] + 3n \\
 &= 2^k[T(n/2^k)] + kn \\
 &= 2^k[T(1)] + n \lg n \quad n=2^k \\
 &= 2^k(1) + n \lg n \\
 &= n + n \lg n
 \end{aligned}$$

So this proves the merge sort runs $\Theta(n \lg n)$.