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[1]: import numpy as np
      from matplotlib.pyplot import randn
      from math import exp
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[2]: def sigmoid(x):
      return 1 / (1 + np.exp(-x))

      def sigmoidDerivative(x):
      return x * (1 - x)
```

```
[3]: class NeuralNetwork:
      def __init__(self, layerSizes):
          self.layerSizes = layerSizes
          self.weights = []
          for i in range(1, len(layerSizes)):
              self.weights.append(np.random.randn(layerSizes[i - 1], layerSizes[i]))

      def forwardPropagation(self, inputData):
          self.activations = [inputData]
          self.zValues = []
          for i in range(len(self.layerSizes) - 1):
              z = np.dot(self.activations[i], self.weights[i])
              self.zValues.append(z)
              activation = sigmoid(z)
              self.activations.append(activation)
          return self.activations[-1]
```

```
      def backwardPropagation(self, inputData, targetOutput, learningRate):
          output = self.forwardPropagation(inputData)
          error = targetOutput - output
          delta = error * sigmoidDerivative(output)

          for i in range(len(self.layerSizes) - 2, -1, -1):
              gradient = np.dot(self.activations[i].T, delta)
              self.weights[i] += learningRate * gradient
              error = np.dot(delta, self.weights[i].T)
              delta = error * sigmoidDerivative(self.activations[i])

      def train(self, inputData, targetOutput, epochs, learningRate):
          for _ in range(epochs):
              self.backwardPropagation(inputData, targetOutput, learningRate)
          return self.forwardPropagation(inputData)
```

```
[4]: X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
      y = np.array([[0], [1], [1], [0]])

      layerSizes = [2, 4, 1]

      nn = NeuralNetwork(layerSizes)

      output = nn.train(X, y, epochs=10000, learningRate=0.1)

      print("Output after training:")
      print(output)
```

Output after training:

```
[[0.11246119]
 [0.92341256]
 [0.92986151]
 [0.03965906]]
```