



INDIAN INSTITUTE OF TECHNOLOGY GANDHINAGAR

MA 202: MATHEMATICS - IV
Semester-II, Academic Year 2022-23

Tutorial Set -3
Question - 10

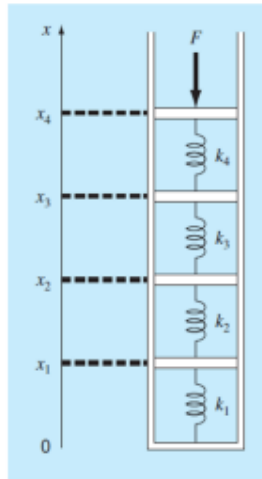
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- In question 10, we are asked to estimate the value of x 's. We are given the spring mass system. I have used the Gauss-Seidel method to compute the values of x . At equilibrium, force-balance equations can be developed defining the interrelationships between the springs. We have given these interrelationships as four equations.
- We have made a coefficient matrix using all equations and then we can use it in the Gauss-Seidel method.

$$\begin{aligned}
 k_2(x_2 - x_1) &= kx_1, \\
 k_3(x_3 - x_2) &= k_2(x_2 - x_1), \\
 k_4(x_4 - x_3) &= k_3(x_3 - x_2), \\
 F &= k_4(x_4 - x_3),
 \end{aligned}$$

where the k 's are spring constants. If k_1 through k_4 are 100, 50, 80, and 200 N/m, respectively, compute the x 's.



→ Gauss-Seidel method of power flow problem is an iterative method used to solve a system of linear equations. In this method we are using simple algebraic equations so that the calculation time for each iteration is less.

Gauss-Seidel Method

➤ **use new x_i at j^{th} iteration as soon as they become available**

$$\begin{cases}
 x_1^j = (b_1 - a_{12}x_2^{j-1} - a_{13}x_3^{j-1} - a_{14}x_4^{j-1}) / a_{11} \\
 x_2^j = (b_2 - a_{21}x_1^{new} - a_{23}x_3^{j-1} - a_{24}x_4^{j-1}) / a_{22} \\
 x_3^j = (b_3 - a_{31}x_1^j - a_{32}x_2^j - a_{34}x_4^{j-1}) / a_{33} \\
 x_4^j = (b_4 - a_{41}x_1^j - a_{42}x_2^j - a_{43}x_3^j) / a_{44}
 \end{cases}$$

$$\mathcal{E}_{a,i} = \left| \frac{x_i^j - x_i^{j-1}}{x_i^j} \right| \times 100\% < \varepsilon_s \quad \text{for all } x_i$$

→ I took the coefficient matrix A and B as an input and applied the above iterations on it to compute the solutions of the equations.

```
% Gauss Seidel Iteration method
% Call the function by giving two matrix as a input
function Xr = T10_20110131(A,B)
% Matrix A(n*n)
% Matrix B(n*1)           % System Ax=B
n = size(B);               % Calculating the size of matrix B
p = n(1);                  % Define a number of rows in matrix B
tol = 0.0001;              % define a value of tolerance
Err = ones(p,1);           % Define a error column matrix
X = zeros(p,1);            % Define a initial guess of solution
C = zeros(p,1);            % Define a dummy column matrix for calculations
% Run a loop to find final result by applying the condition of Gauss
% Seidel iteration method
while max(Err) > tol
    for i = 1:p
        C(i,1) = X(i,1);
        X(i,1) = (1/A(i,i)) * (B(i,1) - sum(A(i,:) * X(:,1)) + A(i,i)*X(i,1))
        Err(i,1) = abs(C(i,1) - X(i,1));
        C(i,1) = X(i,1);
    end
end
disp('Solution by Gauss Seidel Iteration Method is:')
Xr = X;
end
```

Code of Gauss Seidel method

```
>> Xr = T10_20110131([3 -1 0 0;5 -13 8 0;0 2 -7 5;0 0 -1 1],[0;0;0;10])
Solution by Gauss Seidel Iteration Method is:

Xr =

    19.999700343855558
    59.999174182212322
    84.998939288621571
    94.998939288621571

>>
```

Final Simulated output