

Chapter 4. Syntax Analysis II

(Bottom-Up Parsers)

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4.1 Introduction

Disadvantages of Top-Down parser:

- Remove left recursion and thus changing the grammar.
- Hard to generate the intermediate code

Q: is there a better way of parsing without changing the grammar?

A: Yes, parse the string bottom up
(Start from the bottom of the tree and build up)

Ex: Let's consider the following grammar:

R1) $E \rightarrow E + T$

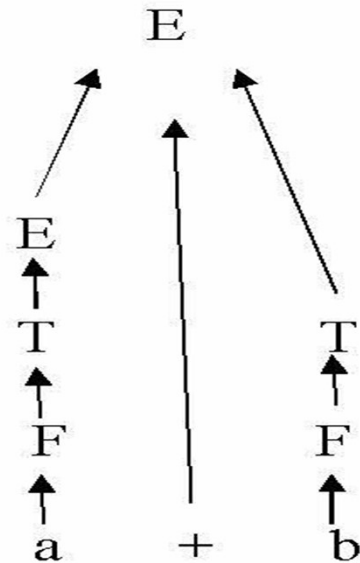
R2) $E \rightarrow T$

R3) $T \rightarrow T * F$

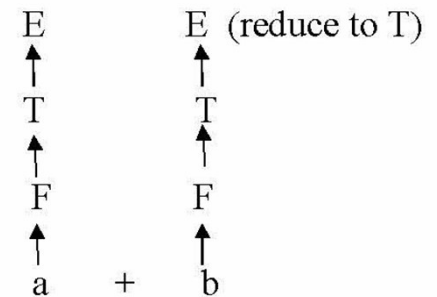
R4) $T \rightarrow F$

R5) $F \rightarrow \text{id}$

And parse the string $a + b$



But we also could
have done this way!!

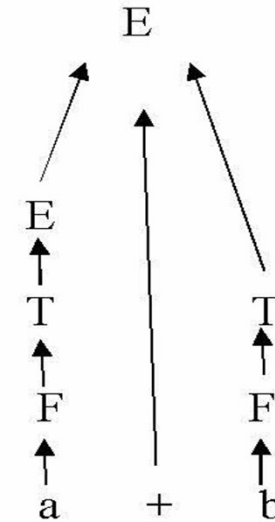


But it leads to nowhere

How do we know which
Way???

Now let's consider a derivation
for $a + b$ from right most
nonterminal (RMD)

		E
R1) $E \rightarrow E + T$	1) \Rightarrow	$E + T$
R2) $E \rightarrow T$	2) \Rightarrow	$E + F$
R3) $T \rightarrow T * F$	3) \Rightarrow	$E + \text{id (b)}$
R4) $T \rightarrow F$	4) \Rightarrow	$T + b$
R5) $F \rightarrow \text{id}$	5) \Rightarrow	$F + b$
	6) \Rightarrow	$a + b$



RMD shows how to reduce in reverse
It tells us that in (1) that we need to reduce
according
to $E \rightarrow E + T$ but NOT $E \rightarrow T$

**Conclusion: We have to look at the RMD to see which
reduction we need to apply In order to parse to
bottom-up**

- R1) $E \rightarrow E + T$
- R2) $E \rightarrow T$
- R3) $T \rightarrow T * F$
- R4) $T \rightarrow F$
- R5) $F \rightarrow id$

Def: Handle

A handle is the right hand side of a production which reduced to get to the preceding step of the RMD

Ex.

E	
E + T	(handle: T or E+T?)
E + F	(F)
E + id (b)	(id)
T + b	(T)
F + b	(F)
a + b	(id)



	E	(RMD)
1) =>	E + T	
2) =>	E + F	
3) =>	E + id (b)	
4) =>	T + b	
5) =>	F + b	
6) =>	a + b	

So, bottom-up parser is about finding the handles and reduce until the top of the tree is found

Formal Def: Handle

For β to be a handle of the sentential form $\alpha\beta\omega$ (ω is reserved for all terminal symbols), we must have

$$\alpha B \omega \Rightarrow \alpha \beta \omega$$

$$S \Rightarrow^* \alpha B \omega$$

This implies that :

$B \rightarrow \beta$ exists and reduction leads to the preceding step of derivation RMD

4.2 Operator Precedence Parser

Simplest Bottom-up (BU) parser, however recognizes the smallest set of CFL. It uses Precedence table, stack and driver to recognize a sentence. The table consists of precedence relations such as

<. . = .>

Ex. For the following grammar

1) $E \rightarrow E + E$

2) $E \rightarrow E * E$

3) $E \rightarrow id$

stack \ token	+	*	Id	\$
+	.>	<.	<.	.>
*	.>	.>	<.	.>
id	.>	.>		.>
\$	<.	<.	<.	

Driver:

- Push \$ onto the stack
- Append \$ at the end of the input string
- Repeat
 - Let t = top most **TERMINAL** symbol in the stack and
 i = the incoming token
 - Find Table [t, i]
 - If **NO** entry then error
 - else if $i .> t$ then
 - push $<.$ and i onto the stack (skip all NTs for $<.$)
 - else { $/* t .> i */$
 - found handle delimited by $<.$ and $.>$
 - if no RHS match to the handle, then error
 - else push LHS of the handle onto the stack
 - }
- Until ($t = \$$ and $i = \$$) or error found

token \ stack	+	*	Id	\$
+	.>	<.	<.	.>
*	.>	.>	<.	.>
id	.>	.>		.>
\$	<.	<.	<.	

- 1) $E \rightarrow E + E$
- 2) $E \rightarrow E * E$
- 3) $E \rightarrow id$

Ex. Parse $a+b*c$ using OPP

Stack	Compare	Input	Production used
\$	<.	a+b*c\$	
\$<.a	.>	+b*c\$	$E \rightarrow id$
\$E	<.	+b*c\$	
\$<.E+	<.	b*c\$	
\$<.E+<.b	.>	*c\$	$E \rightarrow id$
\$<.E+ E	<.	*c\$	
\$<.E+<E*	<.	c\$	
\$<.E+<.E*<.c	.>	\$	$E \rightarrow id$
\$<.E+<.E*E	.>	\$	$E \rightarrow E * E$
\$<.E + E	.>	\$	$E \rightarrow E + E$
\$E		\$	Finished

OPP Evaluation:

Advantage: fast and simple to use

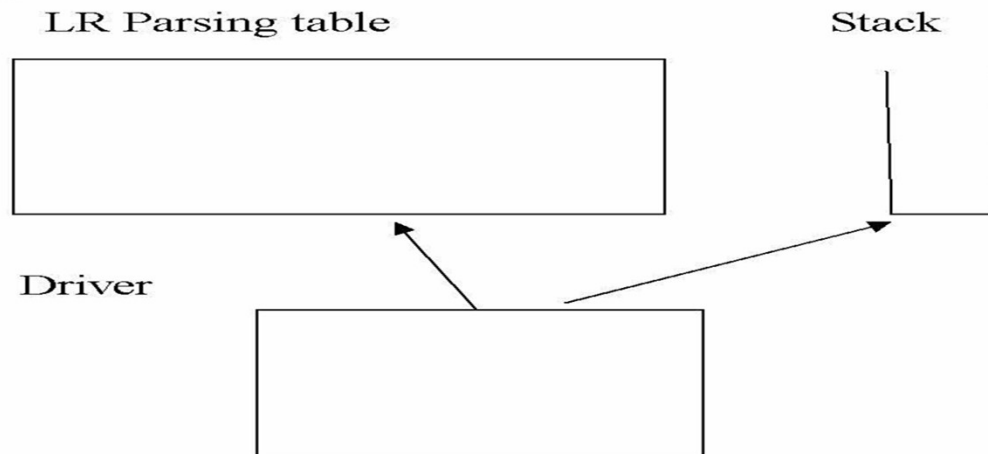
Main Disadvantages:

- Cannot have two consecutive NT on the RHS of the production
- No ϵ production is allowed

4.3 LR parsers

(L = Left-to-right token scan, R= Right most derivation)

Operations:



LR parsing Table: (consists of 3 parts)

States	Terminals.....(Action Part)	NTs.....(Goto Part)

Productions:

1. $E \rightarrow E + T$
2. $E \rightarrow T$
3. $T \rightarrow T * F$
4. $T \rightarrow F$
5. $F \rightarrow (E)$
6. $F \rightarrow id$

State	Action Part						GOTO Part		
	id	+	*	()	\$	E	T	F
0	S5			S4			1	2	3
1		S6				ACCT			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

4 kind of entries:

1. S_n (Shift)
2. R_n (Reduce)
3. N (goto)
4. $Acct$ (Accept)

Driver:

Place \$ at the end of the input string

Push state 0 on to the stack

Repeat

Let q_m be the current state (TOS state) and i the token

Find $x = \text{Table}[Q_m, i]$;

Case x of

$S(Q_n)$: Push (i) and enter q_n , i.e., push (Q_n);

$R(n)$: Reduce by production $\#n$ by popping $2x \#$ of RHS symbols

Let Q_j be the TOS state

Push the LHS L onto the stack

Push $Q_k = \text{Table}[Q_j, L]$ onto the stack

ACCT: Parsing is complete

Empty: error condition

Until ACCT or Error

Productions:

1. $E \rightarrow E + T$
2. $E \rightarrow T$
3. $T \rightarrow T * F$
4. $T \rightarrow F$
5. $F \rightarrow (E)$
6. $F \rightarrow id$

State	Action Part						GOTO Part		
	id	+	*	()	\$	E	T	F
0	S5			S4			1	2	3
1		S6				ACCT			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

Example of Parsing $a+b$

Stack	Input	Table Entry	Action
0	$a+b\$$	S5	Push(a);push(5)
0a5	$+b\$$	R6	$F \rightarrow id$; Table[0,F]=3
0F3	$+b\$$	R4	$T \rightarrow F$; Table[0,T] = 2
0T2	$+b\$$	R2	$E \rightarrow T$; Table[0,E] = 1
0E1	$+b\$$	S6	Push(+),push(6)
0E1+6	$b\$$	S5	Push(b);push(5)
0E1+6b5	$\$$	R6	$F \rightarrow id$; Table[6,F]= 3
0E1+6F3	$\$$	R4	$T \rightarrow F$; Table[6,T] = 9
0E1+6T9	$\$$	R1	$E \rightarrow E+T$;Table[0,E]=1
0E1	$\$$	ACCT	

Question: How do we construct such as Parsing Table?

Need 3 Concepts:

Concept 1: Item

Item is a production with a marker \cdot inserted somewhere on its RHS enclosed in $[\dots\dots\dots]$.

E.g.

Consider the production $E \rightarrow E + T$ then

$[E \rightarrow \cdot E + T]$, $[E \rightarrow E \cdot + T]$, $[E \rightarrow E + \cdot T]$, $[E \rightarrow E + T \cdot]$ are items.

Especially:

$[E \rightarrow \cdot E + T]$ is called the “Initial Item”

$[E \rightarrow E + T \cdot]$ is called the “Completed Item”

Concept 2: Closure (I)

If I is a set of items, then $\text{Closure}(I)$ is given by

1) $I \in \text{Closure}(I)$

2) If $[A \rightarrow \alpha.B\gamma]$ is in the $\text{Closure}(I)$ so far and $B \rightarrow \beta$ then $[B \rightarrow .\beta]$ is in the $\text{Closure}(I)$

E.g. Consider the following “Expression Grammar”

$E \rightarrow E + T, \quad E \rightarrow T, \quad T \rightarrow T * F, \quad T \rightarrow F, \quad F \rightarrow (E), \quad F \rightarrow \text{id}$

Find

- $\text{Closure} (I = \{ [T \rightarrow .T * F] \}) = \{ [T \rightarrow .T * F], [T \rightarrow .T * F], [T \rightarrow .F], [F \rightarrow .\text{id}], [F \rightarrow .(E)] \} = \{ [T \rightarrow .T * F], [T \rightarrow .F], [F \rightarrow .\text{id}], [F \rightarrow .(E)] \}$
- $\text{Closure} ([E \rightarrow E . + T]) = \{ [E \rightarrow E . + T] \}$
- $\text{Closure} ([T \rightarrow T * .F], [F \rightarrow \text{id}.]) = \{ [T \rightarrow T * .F], [F \rightarrow \text{id}.], [F \rightarrow .(E)], [F \rightarrow .\text{id}] \}$

Concepts 3: Transition $N(I, X)$

If I is a set of items and X is ANY grammar symbol (T or NT), then $N(I, X)$ is defined to be Closure set of all items $[A \rightarrow \alpha X \gamma]$ such that $[A \rightarrow \alpha . X \gamma]$ is in I .

E.g.,

$$N(I = \{[E \rightarrow .E + T]\}, E) = \{[E \rightarrow E . + T]\}$$

$$N(I = \{[T \rightarrow T . * F]\}, *) = \{[T \rightarrow T * . F], [F \rightarrow .id], [F \rightarrow .(E)]\}$$

$$N(I = \{[T \rightarrow T * . F]\}, T) = \{ \}$$

4.3.1 Simple LR

Now we are ready to construct the Parsing Table

Step1) Augment the Grammar

Step2) Construct the Transition sets

Step3) Construct the Transition Table

Step4) write out the table

E.g., Expression Grammar:

R1. $E \rightarrow E + T$

R2. $E \rightarrow T$

R3. $T \rightarrow T * F$

R4. $T \rightarrow F$

R5. $F \rightarrow (E)$

R6. $F \rightarrow id$

R1. $E \rightarrow E + T$

R2. $E \rightarrow T$

R3. $T \rightarrow T * F$

R4. $T \rightarrow F$

R5. $F \rightarrow (E)$

R6. $F \rightarrow id$

Step1) Augment the Grammar

R0: $E' \rightarrow E$ (needed whenever more than one production for the Starting Symbol)

Step 2) Construct the Transition Sets

$i0 = \text{State 0} = \text{Def. Closure of Initial item of R0} = ([E' \rightarrow .E])$

$= \{ [E' \rightarrow .E], [E \rightarrow .E+T], [E \rightarrow .T], [T \rightarrow .T*f], [T \rightarrow .F], [F \rightarrow .(E)], [F \rightarrow .id] \}$

Transitions from State 0:

$i1 = N(i0, E) = \{ [E' \rightarrow E.], [E \rightarrow E.+T] \}$

$i2 = N(i0, T) = \{ [E \rightarrow T.], [T \rightarrow T.*F] \}$

$i3 = N(i0, F) = \{ [T \rightarrow F.] \}$

$i4 = N(i0, ()) = \{ [F \rightarrow (.E)], [E \rightarrow .E+T], [E \rightarrow .T], [T \rightarrow .T*F], [T \rightarrow .F], [F \rightarrow .(E)], [F \rightarrow .id] \}$

$i5 = N(i0, id) = \{ [F \rightarrow id.] \}$

R0. $E' \rightarrow E$
R1. $E \rightarrow E + T$
R2. $E \rightarrow T$
R3. $T \rightarrow T * F$
R4. $T \rightarrow F$
R5. $F \rightarrow (E)$
R6. $F \rightarrow id$

Transitions from State 1 = $\{ [E' \rightarrow E.], [E \rightarrow E.+T] \}$

$i6 = N(i1, +) = \{ [E \rightarrow E+.T], [T \rightarrow .T*F], [T \rightarrow .F], [F \rightarrow .(E)], [F \rightarrow .id] \}$

Transitions from State 2 = $\{ [E \rightarrow T.], [T \rightarrow T.*F] \}$

$i7 = N(i2, *) = \{ [T \rightarrow T*.F], [F \rightarrow .(E)], [F \rightarrow .id] \}$

Transition from State 3 = $\{ [T \rightarrow F.] \}$

= $\{ \}$

Transitions from State 4 = $\{ [F \rightarrow (.E)], [E \rightarrow .E+T], [E \rightarrow .T], [T \rightarrow .T*F],$
 $[T \rightarrow .F], [F \rightarrow .(E)], [F \rightarrow .id] \}$

$i8 = N(i4, E) = \{ [F \rightarrow (E.)], [E \rightarrow E.+T] \}$

$N(i4, T) = \{ [E \rightarrow T.], [T \rightarrow T.*F] \} = i2$

$N(i4, F) = \{ [T \rightarrow F.] \} = i3$

$N(i4, () = i4$

$N(i4, id) = \{ [F \rightarrow id.] \} = i5$

R0. $E' \rightarrow E$
R1. $E \rightarrow E + T$
R2. $E \rightarrow T$
R3. $T \rightarrow T * F$
R4. $T \rightarrow F$
R5. $F \rightarrow (E)$
R6. $F \rightarrow id$

Transitions from State 6 = { $[E \rightarrow E+.T]$, $[T \rightarrow .T*F]$, $[T \rightarrow .F]$, $[F \rightarrow .(E)]$, $[F \rightarrow .id]$ }

$i9 = N(i6, T) = \{ [E \rightarrow E+T.] , [T \rightarrow T.*F] \}$

$N(i6, F) = \{ [T \rightarrow F.] \} = i3$

$N(i6, () = i4$

$N(i6, id) = i5$

Transitions from State 7 = { $[T \rightarrow T*.F]$, $[F \rightarrow .(E)]$, $[F \rightarrow .id]$ }

$i10 = N(i7, F) = \{ [T \rightarrow T*F.] \}$

$N(i7, () = i4$

$N(i7, id) = i5$

Transitions from State 8 = { $[F \rightarrow (E.)]$, $[E \rightarrow E.+T]$ }

$i11 = N(i8,)) = \{ [F \rightarrow (E).] \}$

$N(i8, +) = i6$

Transitions from State 9 = { $[E \rightarrow E+T.]$, $[T \rightarrow T.*F]$ }

$N(i9, *) = \{ [T \rightarrow T*.F]$, $[F \rightarrow .(E)]$, $[F \rightarrow .id]$ } = $i7$

No transitions from $i10$ & $i11 \Rightarrow$ finished

Step3) Construct Transition Table

i1 = N (i0, E) = { [E' → E.], [E' → E.+T] }

i2 = N (i0, T) = { [E → T.], [T → T.*F] }

i3 = N (i0, F) = { [T → F.] }

i4 = N (i0, () = { [F → (.E)], [E → .E+T], [E → .T], [T → .T*F], [T → .F], [F → .(E)], [F → .id] }

i5 = N (i0, id) = { [F → id.] }

i6 = N (i1, +) = { [E → E+.T], [T → .T*F], [T → .F], [F → .(E)], [F → .id] }

i7 = N (i2, *) = { [T → T*.F], [F → .(E)], [F → .id] }

i8 = N (i4, E) = { [F → (E.)], [E → E.+T] }

N (i4, T) = { [E → T.], [T → T.*F] } = i2, N (i4, F) = i3, N (i4, () = i4, N (i4, id) = i5

i9 = N (i6, T) = { [E → E+T.], [T → T.*F] }, N (i6, F) = i3, N (i6, () = i4, N (i6, id) = i5

i10 = N (i7, F) = { [T → T*F.] }, N (i7, () = i4, N (i7, id) = i5

i11 = N (i8,)) = { [F → (E).] }, N (i8, +) = i6, N (i9, *) = i7

State	Id	+	*	()	\$	E	T	F
0	5			4			1	2	3
1		6							
2			7						
3									
4	5			4			8	2	3
5									
6	5			4				9	3
7	5			4					10
8		6			11				
9			7						
10									
11									

Step 4) Write out the table

1) Change the entry m in the Action Part to “ S_m ”

2) If a state contains a completed item for R_n then

For each symbol in the follow set of LHS

Put the Reduction rule R_n

(*) Special Case: If a state Q contains the item $[S' \rightarrow S.]$

completed item for R_0 , then the entry for $[Q, \$]$ is “ACCT”

1) Change m to Sm in Action Part

State	Id	+	*	()	\$	E	T	F
0	S5			S4			1	2	3
1		S6							
2			S7						
3									
4	S5			S4			8	2	3
5									
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9			S7						
10									
11									

$i1 = N(i0, E) = \{ [E' \rightarrow E.], [E' \rightarrow E.+T] \}$ (Special case)
 $i2 = N(i0, T) = \{ [E \rightarrow T.], [T \rightarrow T.*F] \}$
 $i3 = N(i0, F) = \{ [T \rightarrow F.] \}$
 $i4 = N(i0, () = \{ [F \rightarrow (.E)], [E \rightarrow .E+T], [E \rightarrow .T], [T \rightarrow .T*F], [T \rightarrow .F], [F \rightarrow .(E)], [F \rightarrow .id] \}$
 $i5 = N(i0, id) = \{ [F \rightarrow id.] \}$
 $i6 = N(i1, +) = \{ [E \rightarrow E+.T], [T \rightarrow .T*F], [T \rightarrow .F], [F \rightarrow .(E)], [F \rightarrow .id] \}$
 $i7 = N(i2, *) = \{ [T \rightarrow T*.F], [F \rightarrow .(E)], [F \rightarrow .id] \}$
 $i8 = N(i4, E) = \{ [F \rightarrow (E.)], [E \rightarrow E.+T] \}$
 $i9 = N(i6, T) = \{ [E \rightarrow E+.T], [T \rightarrow T.*F] \}$
 $i10 = N(i7, F) = \{ [T \rightarrow T*.F.] \}$
 $i11 = N(i8,)) = \{ [F \rightarrow (E).] \}$

R0. $E' \rightarrow E$
R1. $E \rightarrow E + T$
R2. $E \rightarrow T$
R3. $T \rightarrow T * F$
R4. $T \rightarrow F$
R5. $F \rightarrow (E)$
R6. $F \rightarrow id$

2) Find for completed item in each state

• State 2 has a completed item $[E \rightarrow T.]$ for R2

Follow (E) = {+, \$,)} \Rightarrow Table [2, {+, \$,)}] = R2

• State 3 has a completed item $[T \rightarrow F.]$ for R4

Follow (T) = {*, +,), \$} \Rightarrow Table [3, {*, +,), \$}] = R4

• State 5 has a completed item $[F \rightarrow id.]$ for R6

Follow(F) = {*, +,), \$} \Rightarrow Table [5, {*, +,), \$}] = R6

• State 9 has a completed item $[E \rightarrow E+T.]$ for R1

Follow (E) = {+, \$,)} \Rightarrow Table [9, {+, \$,)}] = R1

• State 10 has a completed item $[T \rightarrow T*F.]$ for R3

Follow (T) = {*, +,), \$} \Rightarrow Table [10, {*, +,), \$}] = R3

• State 11 has a completed item $[F \rightarrow (E).]$ for R5

Follow(F) = {*, +,), \$} \Rightarrow Table [11, {*, +,), \$}] = R5

(*) State 1 has a completed item $[E' \rightarrow E.] \Rightarrow$ Table [1, \$] = ACCT

Result:

State	Id	+	*	()	\$	E	T	F
0	S5			S4			1	2	3
1		S6				ACCT			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

Ex 2)

Consider the following

Grammar

R0) $S' \rightarrow S$

R1) $S \rightarrow E = E$

R2) $S \rightarrow id$

R3) $E \rightarrow E + id$

R4) $E \rightarrow id$

Step2) Transition Sets

$I_0 = \text{Closure} ([S' \rightarrow .S]) = \{ [S' \rightarrow .S], [S \rightarrow .E = E], [S \rightarrow .id], [E \rightarrow .E + id], [E \rightarrow .id] \}$

$I_1 = N(I_0, S) = \{ [S' \rightarrow S.] \}$

$I_2 = N(I_0, E) = \{ [S \rightarrow E . = E], [E \rightarrow E . + id] \}$

$I_3 = N(I_0, id) = \{ [S \rightarrow id.], [E \rightarrow id.] \}$

$I_4 = N(I_2, =) = \{ [S \rightarrow E = .E], [E \rightarrow .E + id], [E \rightarrow .id] \}$

$I_5 = N(I_2, +) = \{ [E \rightarrow E + .id] \}$

$I_6 = N(I_4, E) = \{ [S \rightarrow E = E.], [E \rightarrow E . + id] \}$

$I_7 = N(I_4, id) = \{ [E \rightarrow id.] \}$

$I_8 = N(I_5, id) = \{ [E \rightarrow E + id.] \}$

$N(I_6, +) = \{ [E \rightarrow E + .id] \} = I_5$

$I_0 = \text{Closure} ([S' \rightarrow \cdot S]) = \{ [S' \rightarrow \cdot S], [S \rightarrow \cdot E = E], [S \rightarrow \cdot \text{id}], [E \rightarrow \cdot E + \text{id}], [E \rightarrow \cdot \text{id}] \}$

$I_1 = N(I_0, S) = \{ [S' \rightarrow S \cdot] \}$

$I_2 = N(I_0, E) = \{ [S \rightarrow E \cdot = E], [E \rightarrow E \cdot + \text{id}] \}$

$I_3 = N(I_0, \text{id}) = \{ [S \rightarrow \text{id} \cdot], [E \rightarrow \text{id} \cdot] \}$

$I_4 = N(I_2, =) = \{ [S \rightarrow E = \cdot E], [E \rightarrow \cdot E + \text{id}], [E \rightarrow \cdot \text{id}] \}$

$I_5 = N(I_2, +) = \{ [E \rightarrow E + \cdot \text{id}] \}$

$I_6 = N(I_4, E) = \{ [S \rightarrow E = E \cdot], [E \rightarrow E \cdot + \text{id}] \}$

$I_7 = N(I_4, \text{id}) = \{ [E \rightarrow \text{id} \cdot] \}$

$I_8 = N(I_5, \text{id}) = \{ [E \rightarrow E + \text{id} \cdot] \}$

$I_5 = N(I_6, +) = \{ [E \rightarrow E + \text{id} \cdot] \}$

Step 3) Transition Table

	Id	=	+	\$	S	E
0	3				1	2
1						
2		4	5			
3						
4	7					6
5	8					
6			5			
7						
8						

Step4) Write out the Table

1) $m \Rightarrow S_m$ in Action Part

2) Just want to consider for State 3

• State 3 = { [S \rightarrow id.], [E \rightarrow id.] } has two completed items:

[S \rightarrow id.] for R2 and [E \rightarrow id.] for R4

Compute Follow (S) = { \$ } and Follow (E) = { =, +, \$ }

\Rightarrow Table [3, \$] = R2 and Table[3, { =, +, \$ }] = R4

R0) S' \rightarrow S

R1) S \rightarrow E = E

R2) S \rightarrow id

R3) E \rightarrow E + id

R4) E \rightarrow id

	Id	=	+	\$	S	E
0	S3				1	2
1				ACCT		
2		S4	S5			
3		R4	R4	R2/R4		
4	S7					6
5	S8					
6			S5			
7						
8						

➤ There is a conflict in Table[3, \$] = {R2/R4} Called Reduce/Reduce Conflict.
That is, if the stack has State 3 and input is \$, there are two possibilities R2 and R4

	Id	=	+	\$	S	E
0	S3				1	2
1				ACCT		
2		S4	S5			
3		R4	R4	(R2/R4)		
4	S7					6
5	S8					
6			S5			
7						
8						

Let's examine further: Consider a string "a" and try to parse

Stack	Input	Action
0	a\$	S3
0a3	\$	R2 or R4 (Choose R2) S → id
0S1	\$	ACCT

Stack	Input	Action
0	a\$	S3
0a3	\$	R2 or R4 (Choose R4) E → id
0E2	\$	Error????

What does it mean ? => R4 should NOT be allowed in the first place

The conflict occurred because the technique we utilized is not powerful enough. We need a more powerful method

Canonical LR

4.3.2) Canonical LR

Item: $[A \rightarrow \beta.\gamma ; l]$ a.k.a Canonical Item,
with core $A \rightarrow \beta.\gamma$ and l = look ahead set (LAS).

The idea is : Reduce for the complete items in LAS, rather than the follow set.

Modifications from SLR:

1. Our Starting State $I_0 = [S' \rightarrow . S ; \{\$ \}]$
2. For each item $[A \rightarrow \alpha.B\gamma ; l]$ in the closure set do
For each production $B \rightarrow .\beta$ do
Create the initial item $[B \rightarrow .\beta ; t]$ with $t = \bigcup x \in l \text{ First}(\gamma x)$
If the cores are the same, merge items by merging the LASs
3. Reduce for completed items in each state for tokens in the LAS rather than Follow set

Example: Construct CLR from the following productions.

Step1) Augment the grammar with R0

R0) $S' \rightarrow S$ R1) $S \rightarrow E = E$ R2) $S \rightarrow id$ R3) $E \rightarrow E + id$ R4) $E \rightarrow id$

Step 2) Transition Sets for LR states

$I_0 = \text{Closure} \{ [S' \rightarrow .S; \{\$\}] \} = \{ [S' \rightarrow .S; \{\$\}], [S \rightarrow .E=E; \{\$\}], [S \rightarrow .id; \{\$\}], [E \rightarrow .E+id; \{=\}], [E \rightarrow .id; \{=\}], [E \rightarrow .E+id; \{+\}], [E \rightarrow .id; \{+\}] \}$

$= \{ [S' \rightarrow .S; \{\$\}], [S \rightarrow .E=E; \{\$\}], [S \rightarrow .id; \{\$\}], [E \rightarrow .E+id; \{=,+\}], [E \rightarrow .id; \{+,=\}] \}$

Transitions from I0

$$I1 = N(I0, S) = \{ [S' \rightarrow S.]; \{\$ \} \}$$

$$I2 = N(I0, E) = \{ [S \rightarrow E.=E; \{\$ \}], [E \rightarrow E.+id; \{+, =\}] \}$$

$$I3 = N(I0, id) = \{ [S \rightarrow id.; \{\$ \}], [E \rightarrow id.; \{=, +\}] \}$$

Transitions from I2

$$I4 = N(I2, =) = \{ [S \rightarrow E=.E; \{\$ \}], [E \rightarrow .E+id; \{\$ \}], [E \rightarrow .id; \{\$ \}], [E \rightarrow .E+id; \{+\}], [E \rightarrow .id; \{+\}] \}$$

$$= \{ [S \rightarrow E=.E; \{\$ \}], [E \rightarrow .E+id; \{+, \$ \}], [E \rightarrow .id; \{+, \$ \}] \}$$

$$I5 = N(I2, +) = \{ [E \rightarrow E+.id; \{=, +\}] \}$$

Transitions from I4

$$I6 = N(I4, E) = \{[S \rightarrow E=E.; \{\$\}], [E \rightarrow E.+id; \{+, \$\}]\}$$

$$I7 = N(I4, id) = \{[E \rightarrow id.; \{+, \$\}]\}$$

Transitions from I5

$$I8 = N(I5, id) = \{[E \rightarrow E+id.; \{=, +\}]\}$$

Transitions from I6

$$I9 = N(I6, +) = \{[E \rightarrow E+.id; \{+, \$\}]\}$$

Transitions from I9

$$I10 = N(I9, id) = \{[E \rightarrow E+id.; \{+, \$\}]\}$$

Step 3) Transition Table

	Id	=	+	\$	S	E
0	3				1	2
1						
2		4	5			
3						
4	7					6
5	8					
6			9			
7						
8						
9	10					
10						

Step 4) Write out the table

1) $m \rightarrow S_m$ in the action part

2) Let's just consider:

• State 3: $\{ [S \rightarrow id.; \{\$ \}], [E \rightarrow id.; \{ =, + \}] \}$ has two completed items.

$[S \rightarrow id.]$ for R2 with $I = \{\$ \} \Rightarrow \text{Table } [3, \$] = R2$

$[E \rightarrow id.]$ for R4 with $I = \{+, =\} \Rightarrow \text{Table } [3, \{+, =\}] = R4$

	Id	=	+	\$	S	E
0	S3				1	2
1				ACCT		
2		S4	S5			
3		R4	R4	R2		
4	S7					6
5	S8					
6			S9			
7			R4	R4		
8		R2	R2			
9	S10					
10			R3	R3		

•The result: The conflict in state 3 is GONE!!

Observations:

1. More states than SLR (machine got bigger) : from 9 to 11
2. However, some LR state are similar (i.e., same cores) with different LAS

$I_5 = \{ [E \rightarrow E + .id; \{+, =\}]$

$I_9 = \{ [E \rightarrow E + .id; \{+, \$\}]$

Q: Can we make machine smaller? (same number of states as SLR)

Yes, LALR (Look Ahead LR)

4.3.3) LALR Parser

The simplest way to construct the LALR states is:

- 1) Find CLR states
- 2) Merge all states ($S_1, S_2 \dots S_n$) having same core sets by taking the unions of all LASs and say that the resulting state is Q

Example: of our grammar

$I_5 = \{ [E \rightarrow E + .id; \{=, +\}] \}$ and $I_9 = \{ [E \rightarrow E + .id; \{\$, +\}] \}$ can be merged

$I_5' = \{ [E \rightarrow E + .id; \{=, +, \$\}] \}$

$I_8 = \{ [E \rightarrow E + id.; \{=, +\}] \}$ and $I_{10} = \{ [E \rightarrow E + id.; \{+, \$\}] \}$ can be merged

$I_8' = \{ [E \rightarrow E + id.; \{=, +, \$\}] \}$

So it gives us 9 LALR states in total, same as SLR states

4.4 Error Handling

If there is a syntax error, your parser should do

- Generate a “meaningful” error message
- Recover from the error

a) Error message

Assume LR parser, current state is N and token = I, then

Table[N, i] = empty is an error.

In this case, we could look at the Table [N, x] = Not empty and announce all x tokens

State	Id	+	*	()	\$	E	T	F
0	S5			S4			1	2	3
1		S6				ACCT			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

Ex. Current state = 5 and token (=> error => look for entry

b) Error recovery is more “tricky”

One way to do is to insert a fake token e.g., $a(b+c) \Rightarrow$ will generate an error message of missing an operator \Rightarrow Insert any operator and move on

State	Id	+	*	()	\$	E	T	F
0	S5			S4			1	2	3
1		S6				ACCT			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

Ex. Current state = 5 and token (\Rightarrow fake token +, -, *

But what if the parser assumes wrong \Rightarrow But what if the parser assumes wrong \Rightarrow (e.g., state 4, multiple different entries \Rightarrow

Will generate message which will be hard to understand

4.5 Symbol Table

A Database for symbol that occur during the compilation process.
It also provides set of procedures such as, lookup(), insert(), remove(), list()
etc

4.5.1 Organization of the table

- Array :

Adv: Simplest and no overhead (pointers)

Disadv: fixed size, search $O(N)$

- Linked List

Adv: Expandable

DisAdv: Overhead (Pointers), search $O(N)$

- Binary Search Tree

Adv: Expandable, Search $O(\log N)$

Disadv: Overhead (2 pointers), House-keeping for Binary Search Tree

- Hash Table (Most compiler use this) = Bucket + LL

Adv: Expandable, Search $O(\lambda)$ = average bucket size

If hash function $h(x)$ is good the bucket size will be good.

Some $h(x)$ = mode function, middle square function etc

4.5.2 Scope issues

To make variables visible correctly

- No Scope => All variables are global (Basic)
- Totally Separate => All local = No nesting is allowed
- Nested scope : Nesting allowed

How Symbol table handles the scopes:

- No scope: All names (variables must be distinct)
- Totally Separate: Same names are allowed if scopes are different

- Nest Scope (many PLs)

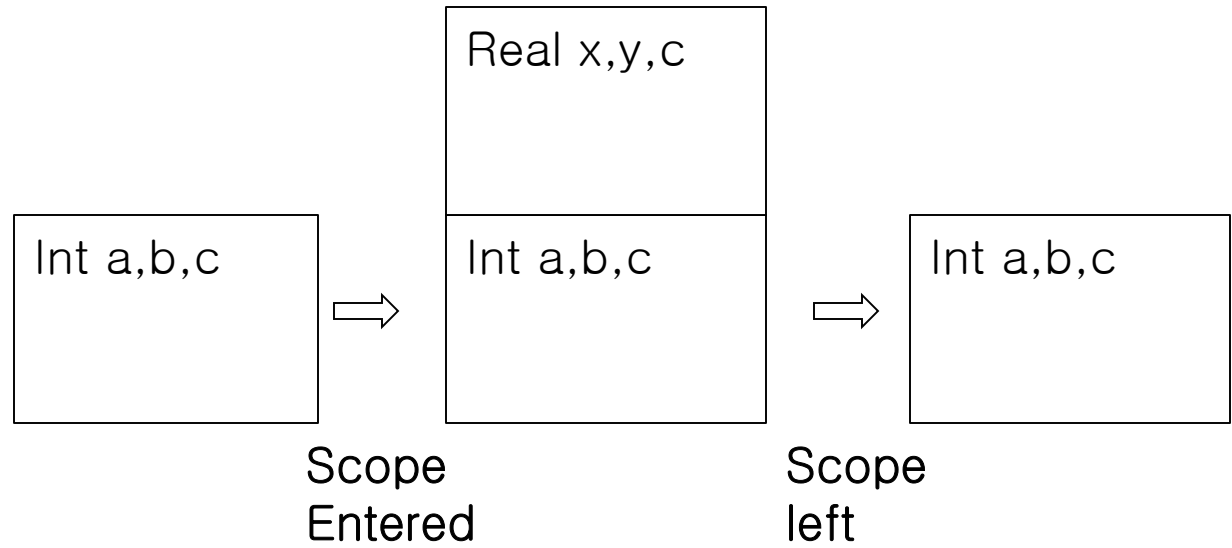
Use of dynamic (growing and shrinking) symbol table, i.e.,

If a scope is entered the table grows by the symbols of the scope

And if scope is left the table shrinks (STACK)

Example:

```
{  
  int a,b, c;  
  .....  
  {  
    real x,y,c;  
    .....  
    c= /* real */  
  
  }  
  
  ...c = /* int */  
}
```



END