EE583 Pattern Recognition HW5

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1 Question 1

3 different experiments are conducted. In each experiment, ten models are individually used to calculate the accuracy, or equivalently misclassification loss.

1.1 Default settings

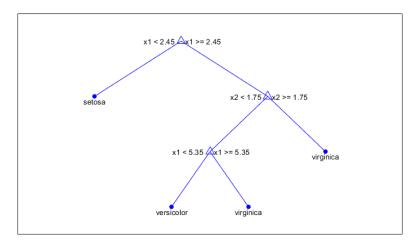


Figure 1: Visualization of the first tree

This 3 split tree resulted in a loss of 0.0267.

1.2 Maximum number of Splits Restriction

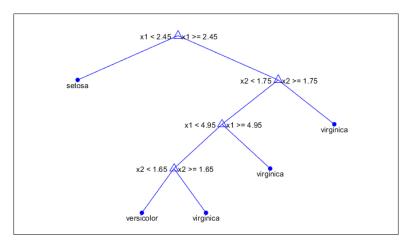


Figure 2: Visualization of the second tree

For this experiment the resultant number of splits was higher than the first one. Therefore, it resulted in less misclassification loss of 0.0240.

1.3 Maximum number of Splits Restriction

Changing the split criterion from Gini's diversity index to deviance resulted in the improvement of the accuracy.

- 2 Question 2
- 3 Question 3
- 4 Question 4

5 APPENDIX

The code given in this section is shared @**Q**.

5.1 Q1

```
%%
2 clear; clc;
  chdir('...')
  addpath ('export_fig')
  chdir ('HW5')
  rng (101)
  %%
  load fisheriris.mat
  feats = meas(:, 3:4);
  Y = species;
11
  tree_model = fitctree (feats, species, 'CrossVal', 'on');
12
   view (tree_model.Trained {1}, 'Mode', 'graph')
  Ls = [];
  \begin{array}{cccc} \textbf{for} & i & = & 1:10 \end{array}
15
       model = tree_model.Trained{i};
16
       preds = predict(model, feats);
17
       confusion matrix = confusionmat (species, preds);
18
       accuracy = sum(diag(confusion matrix))/sum(sum(confusion matrix))
19
       loss = 1 - accuracy;
20
       Ls(end+1) = loss;
21
  end
22
  mean loss default = mean(Ls);
^{23}
24
  %%
25
  tree_model = fitctree (feats, species, 'CrossVal', 'on', 'MaxNumSplits',7)
26
   view (tree model. Trained {1}, 'Mode', 'graph')
27
  Ls = [];
28
  for i = 1:10
29
       model = tree model.Trained{i};
30
       preds = predict(model, feats);
31
       confusion matrix = confusionmat (species, preds);
32
       accuracy = sum(diag(confusion matrix))/sum(sum(confusion matrix))
33
       loss = 1 - accuracy;
34
       Ls(end+1) = loss;
35
36
  mean_loss_restricted_splits = mean(Ls);
37
  %%
38
  tree_model = fitctree (feats, species, 'CrossVal', 'on', 'SplitCriterion',
      'deviance');
  view (tree model. Trained {1}, 'Mode', 'graph')
  Ls = |\cdot|;
41
  for i = 1:10
```

```
model = tree model.Trained{i};
43
       preds = predict(model, feats);
44
       confusion matrix = confusionmat (species, preds);
45
       accuracy = sum (diag (confusion_matrix))/sum (sum (confusion_matrix))
46
       loss = 1 - accuracy;
47
       Ls(end+1) = loss;
48
49
  mean_loss_split_criterion = mean(Ls);
50
  figHandles = findall(0, 'Type', 'figure');
52
53
  for i = 1:numel(figHandles)
54
       export_fig(['Q1_',num2str(i)], '-png', figHandles(i), '-append')
55
  end
56
57
  hTree=findall(0, 'Tag', 'tree viewer');
  % close (hTree)
59
60
  mean loss default
61
  mean\_loss\_restricted\_splits
62
  mean loss split criterion
```

5.2 Q2

```
1 clc, clear;
2 load fisheriris.mat
  feats = meas(:,3:4);
 Y = species;
  rng(101)
5
  % Cross varidation (train: 50%, test: 50%)
  cv = cvpartition(size(feats,1),'HoldOut',0.5);
  idx = cv.test;
9
10
  % Separate to training and test data
11
  feats Train = feats(~idx,:);
  feats Test = feats(idx,:);
  Y \text{ Train} = Y(\tilde{idx});
14
  Y_{\text{Test}} = Y(idx);
15
16
  % To amplify the difference of the classification success, the number
17
       o f
  % splits are restricted for a single tree to also highlight the
      a da boost
  % success
19
  t = templateTree('MaxNumSplits',1);
20
  Mdl = fitcensemble (feats_Train, Y_Train, 'Method', 'AdaBoostM2', ...
21
       'Learners',t,'NumLearningCycles',25);
22
  view (Mdl. Trained {1}, 'Mode', 'graph')
23
  preds = predict (Mdl. Trained {1}, feats Test);
24
  confusionmatrix = confusionmat(Y_Test, preds);
25
  first\_tree\_accuracy = sum(diag(confusionmatrix))/sum(sum(
26
      confusion matrix))
  preds = predict (Mdl, feats Test);
  confusionmatrix = confusionmat(Y_Test, preds);
  ensemble_tree_accuracy = sum(diag(confusionmatrix))/sum(sum(
29
      confusion matrix))
30
31
32
  accs = [];
33
  for lr = 10.^{-1} - 8:0
34
       t = templateTree('MaxNumSplits',1);
35
       Mdl = fitcensemble (feats_Train, Y_Train, 'Method', 'AdaBoostM2', ...
36
       'Learners', t, 'NumLearningCycles', 25, 'LearnRate', lr);
37
       preds = predict(Mdl, feats Test);
       confusionmatrix = confusionmat(Y_Test, preds);
39
       model\_accuracy = sum(diag(confusionmatrix))/sum(sum(
40
          confusionmatrix));
       accs(end+1) = model \ accuracy;
41
  end
42
43
  figure
```

```
plot(-8:0,1-accs)

ylim([0 0.5])

title('Misclassification Rate vs Learning Rate')

ylabel('Misclassification Rate')

xlabel('Learning Rate Power')
```

5.3 Q3

```
1 clc, clear;
2 load fisheriris.mat
  feats = meas(:, 3:4);
_{4} Y = species;
  rng (101)
  % Cross varidation (train: 50%, test: 50%)
  cv = cvpartition(size(feats,1),'HoldOut',0.5);
  idx = cv.test;
9
10
  % Separate to training and test data
11
  feats Train = feats(~idx,:);
  feats Test = feats(idx,:);
  Y \text{ Train} = Y(\tilde{idx});
14
  Y_Test = Y(idx);
15
16
  Mdl = TreeBagger (25, feats, Y, 'OOBPrediction', 'On', ...
17
       'Method', 'classification', 'SampleWithReplacement', 'on');
18
19
20
  view (Mdl. Trees {1}, 'Mode', 'graph')
21
  preds = predict(Mdl.Trees{1},feats_Test);
22
  confusionmatrix = confusionmat(Y Test, preds);
23
  first tree accuracy = sum(diag(confusionmatrix))/sum(sum(
24
      confusion matrix))
  preds = predict(Mdl, feats Test);
^{25}
  confusionmatrix = confusionmat(Y_Test, preds);
  ensemble\_tree\_accuracy = sum(diag(confusionmatrix))/sum(sum(
      confusionmatrix))
```

5.4 Q4

```
1 load lawdata
  rhohat = corr(lsat, gpa);
  %%
4
  rng default; % For reproducibility
  jackrho = jackknife(@corr,lsat,gpa);
  meanrho = mean(jackrho);
  yyaxis left
  plot (lsat)
9
  ylabel ('LSAT')
10
  hold on
11
  yyaxis right
12
  plot (gpa)
  h = ylabel ('GPA', 'Rotation', 270);
14
  xlabel ('Samples')
  h. Position (1) = 16.5; % change horizontal position of ylabel
  legend('LSAT,GPA')
17
   title ({['Real Correlation: ',num2str(rhohat)],['Estimated Correlation
         , num2str(meanrho)])
19
  n = length(lsat);
20
  biasrho = (n-1) * (meanrho-rhohat)
21
22
23
  %%
24
  rng default; % For reproducibility
^{25}
  jackmed = jackknife (@median, lsat);
26
  meanmed lsat = mean(jackmed);
27
  n = length(lsat);
28
  bias lsat median = (n-1) * (meanmed <math>lsat-median(lsat))
  jackmed = jackknife (@median, gpa);
31
  meanmed gpa = mean(jackmed);
32
  figure
33
  yyaxis left
34
  hp1 = plot(lsat);
35
  ylabel ('LSAT')
  hold on
37
  yyaxis right
38
  hp2 = plot(gpa);
  legend ([hp1,hp2], 'LSAT', 'GPA')
  xlabel ('Samples')
  h = ylabel('GPA', 'Rotation', 270);
  h. Position (1) = 16.5; % change horizontal position of ylabel
  n = length(gpa);
  bias gpa median = (n-1) * (meanmed gpa-median(gpa))
  title ({['Real medians: ',num2str(median(lsat)),' - ',num2str(median(
      gpa))],['Estimated medians: ',num2str(meanmed_lsat),' - ',num2str(
      meanmed_gpa)],['Jackknife Estimate Bias for LSAT & GPA: ',num2str(
```