EXTENDS Naturals, FiniteSets, Sequences, TLC

The history of history for the client, used by the model checker to verify sequential consistency VARIABLE history

The history of events received by the client, used by the model checker to verify sequential consistency VARIABLE events

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The state invariant checks that the client's history never go back in time
StateInvariant \triangleq
     \land \forall c \in \text{DOMAIN } history:
         \land \forall k \in \text{DOMAIN } history[c]:
            \land \forall r \in \text{DOMAIN } history[c][k]:
                 r > 1 \Rightarrow history[c][k][r] \geq history[c][k][r-1]
 The events invariant checks that events are sequential
EventInvariant \triangleq
     \land \forall c \in \text{DOMAIN } events:
         \land \forall k \in \text{DOMAIN } events[c]:
            \land \forall r \in \text{DOMAIN } events[c][k]:
                 r > 1 \Rightarrow events[c][k][r] > events[c][k][r-1]
 Record a read to the history
RecordRead(c, k, v) \triangleq
     \land \lor \land c \in \text{DOMAIN } history
            \land k \in \text{DOMAIN } history[c]
            \land history' = [history \ EXCEPT \ ![c][k] = Append(history[c][k], v)]
         \lor \land c \in DOMAIN \ history
            \land k \notin \text{DOMAIN } history[c]
            \land history' = [history \ EXCEPT \ ![c] = history[c] @@(k:>\langle v\rangle)]
         \lor \land c \notin DOMAIN \ history
            \land history' = history @@(c:> [i \in \{k\} \mapsto \langle v \rangle])
Record an event to the history
RecordEvent(c, k, v) \triangleq
     \land \lor \land c \in \text{DOMAIN} \ events
            \land k \in \text{DOMAIN } events[c]
            \land events' = [events \ EXCEPT \ ![c][k] = Append(events[c][k], v)]
         \lor \land c \in \text{DOMAIN} \ events
            \land k \notin \text{DOMAIN } events[c]
            \land events' = [events \ EXCEPT \ ![c] = events[c] @@(k:>\langle v\rangle)]
         \lor \land c \notin DOMAIN \ events
            \land events' = events @@(c:>[i \in \{k\} \mapsto \langle v \rangle])
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