EXTENDS Naturals, Sequences, Controller, Device

```
VARIABLE step
```

```
A sequence of all variables vars \triangleq \langle mastership Vars, node Vars, message Vars, stream Vars, device Vars \rangle
```

The invariant asserts that the device will not allow a write from an older master if it has already accepted a write from a newer master. This is determined by comparing the *mastership* terms of accepted writes. For this invariant to hold, terms may only increase in the history of writes.

```
TypeInvariant \stackrel{\triangle}{=}
      \land \forall x \in 1 .. Len(history) :
            \forall y \in x \dots Len(history) :
                 \land history[x].term \leq history[y].term
                 \land history[x].term = history[y].term \Rightarrow history[x].node = history[y].node
Init \triangleq
      \wedge term = 0
      \land master = Nil
      \wedge backups = \langle \rangle
      \land events = [n \in Nodes \mapsto \langle \rangle]
      \land mastership = [n \in Nodes \mapsto [term \mapsto 0, master \mapsto Nil, backups \mapsto \langle \rangle]]
      \wedge streamId = 0
      \land sentTerm = [n \in Nodes \mapsto 0]
      \land isMaster = [n \in Nodes \mapsto FALSE]
      \land requestStream = [n \in Nodes \mapsto [id \mapsto 0, state \mapsto Closed]]
      \land requests = [n \in Nodes \mapsto \langle \rangle]
      \land responseStream = [n \in Nodes \mapsto [id \mapsto 0, state \mapsto Closed]]
      \land responses = [n \in Nodes \mapsto \langle \rangle]
      \land election = [n \in Nodes \mapsto 0]
      \wedge state = Stopped
      \wedge history = \langle \rangle
Next \stackrel{\triangle}{=}
     \vee \exists n \in Nodes : OpenStream(n)
         \land UNCHANGED \langle device Vars \rangle
      \vee \exists n \in Nodes : CloseStream(n)
         \land UNCHANGED \langle device Vars \rangle
      \vee \exists n \in Nodes : ConnectStream(n)
         \land UNCHANGED \langle mastership Vars, node Vars \rangle
      \vee \exists n \in Nodes : DisconnectStream(n)
         \land UNCHANGED \langle mastership Vars, node Vars \rangle
      \vee \exists n \in Nodes : JoinMastershipElection(n)
         \land UNCHANGED \langle device Vars \rangle
      \vee \exists n \in Nodes : LeaveMastershipElection(n)
```

```
\land UNCHANGED \langle device Vars \rangle
     \vee \exists n \in Nodes : LearnMastership(n)
        \land UNCHANGED \langle device Vars \rangle
     \lor \exists n \in Nodes : SendMasterArbitrationUpdate(n)
         \land UNCHANGED \langle device Vars \rangle
     \vee \exists n \in Nodes : HandleMasterArbitrationUpdate(n)
         \land UNCHANGED \langle mastership Vars, node Vars \rangle
     \lor \exists n \in Nodes : ReceiveMasterArbitrationUpdate(n)
         \land UNCHANGED \langle device Vars \rangle
     \vee \exists n \in Nodes : SendWriteRequest(n)
        \land UNCHANGED \langle device Vars \rangle
     \vee \exists n \in Nodes : HandleWrite(n)
         \land UNCHANGED \langle mastership Vars, node Vars \rangle
     \vee \exists n \in Nodes : ReceiveWriteResponse(n)
         \land UNCHANGED \langle device Vars \rangle
     \vee Shutdown
         \land UNCHANGED \langle mastership Vars, node Vars \rangle
     \vee Startup
         \land UNCHANGED \langle mastership Vars, node Vars \rangle
Spec \triangleq Init \wedge \Box [Next]_{vars}
```

^{*} Last modified Wed Mar 27 15:51:45 PDT 2019 by jordanhalterman

^{*} Created Thu Feb 14 11:33:03 PST 2019 by jordanhalterman