EXTENDS Naturals, FiniteSets, Sequences, TLC

The set of all ONOS nodes CONSTANTS Nodes

Stream states
CONSTANTS Open, Closed

 $\begin{array}{c} {\rm Master~arbitration~message~types} \\ {\rm CONSTANTS~} Master Arbitration Update \end{array}$ 

Write message types
CONSTANTS WriteRequest, WriteResponse

Response status constants
CONSTANTS Ok, AlreadyExists, PermissionDenied

Empty value
CONSTANT Nil

The current state of mastership elections VARIABLES term, master, backups

The current mastership event queue for each node VARIABLE events

The current mastership state for each node

VARIABLE masterships

Whether the node has received a Master Arbitration Update indicating it is the current master VARIABLE is Master

The state of all streams and their requests and responses VARIABLE streams, requests, responses

The current set of elections for the device, the greatest of which is the current master  $VARIABLE\ elections$ 

The current set of terms for each open stream for the device VARIABLE terms

The term of the last successful write to the device VARIABLE lastTerm

Counting variables used to enforce state constraints  ${\tt VARIABLES}\ master ship Changes,\ stream Changes,\ message Count$ 

A history of successful writes to the switch used for model checking

```
Mastership/consensus related variables mastership Vars \triangleq \langle term, master, backups, mastership Changes \rangle
Node related variables node Vars \triangleq \langle events, masterships, isMaster \rangle
Stream related variables stream Vars \triangleq \langle streams, stream Changes \rangle
Message related variables message Vars \triangleq \langle requests, responses, message Count \rangle
Device related variables device Vars \triangleq \langle elections, terms, last Term, history \rangle
A sequence of all variables vars \triangleq \langle mastership Vars, node Vars, stream Vars, message Vars, device Vars \rangle
```

## Helpers

```
Returns a sequence with the head removed Pop(q) \stackrel{\triangle}{=} SubSeq(q, 2, Len(q))
```

Returns a sequences with the element at the given index removed  $Drop(q, i) \stackrel{\Delta}{=} SubSeq(q, 1, i-1) \circ SubSeq(q, i+1, Len(q))$ 

Returns the set of values in f $Range(f) \stackrel{\Delta}{=} \{f[x] : x \in DOMAIN f\}$ 

Returns the maximum value from a set or undefined if the set is empty  $Max(s) \stackrel{\Delta}{=} \text{CHOOSE } x \in s : \forall y \in s : x \geq y$ 

 $max(s) = cnooper x \in s \cdot \forall y \in s \cdot x \geq y$ 

This section models the messaging between controller nodes and the device. Messaging is modelled on TCP, providing strict ordering between controller and device via sequences. The 'requests' sequence represents the messages from controller to device for each node, and the 'responses' sequence represents the messages from device to each node. Requests and responses are always received from the head of the queue and are never duplicated or reordered.

```
Sends request 'm' on the stream for node 'n' SendRequest(n, m) \triangleq \\ \wedge requests' = [requests \ \text{EXCEPT !}[n] = Append(requests[n], m)] \\ \wedge messageCount' = messageCount + 1
```

Indicates whether a request of type 't' is at the head of the queue for node 'n'

```
HasRequest(n, t) \triangleq Len(requests[n]) > 0 \land requests[n][1].type = t
Returns the next request in the queue for node 'n'
NextRequest(n) \stackrel{\Delta}{=} requests[n][1]
Discards the request at the head of the queue for node 'n'
DiscardRequest(n) \stackrel{\triangle}{=} requests' = [requests \ EXCEPT \ ![n] = Pop(requests[n])]
Sends response 'm' on the stream for node 'n'
SendResponse(n, m) \triangleq
    \land responses' = [responses \ EXCEPT \ ![n] = Append(responses[n], m)]
    \land messageCount' = messageCount + 1
 Indicates whether a response of type 't' is at the head of the queue for node 'n'
HasResponse(n, t) \triangleq Len(responses[n]) > 0 \land responses[n][1].type = t
Returns the next response in the queue for node 'n'
NextResponse(n) \stackrel{\triangle}{=} responses[n][1]
 Discards the response at the head of the queue for node 'n'
DiscardResponse(n) \stackrel{\Delta}{=} responses' = [responses \ EXCEPT \ ![n] = Pop(responses[n])]
Indicates whether the stream for node 'n' is Open
IsStreamOpen(n) \stackrel{\Delta}{=} streams[n].state = Open
 Indicates whether the stream for node 'n' is Closed
IsStreamClosed(n) \stackrel{\Delta}{=} streams[n].state = Closed
```

This section models the mastership election service used by the controller to elect masters. Mastership changes through join and leave steps. Mastership is done through a consensus service, so these steps are atomic. When a node joins or leaves the mastership election, events are queued to notify nodes of the mastership change. Nodes learn of mastership changes independently of the state change in the consensus service.

Node 'n' joins the mastership election

If the current 'master' is Nil, set the master to node 'n', increment the 'term', and send a master-ship change event to each node. If the current 'master' is non-Nil, append node 'n' to the sequence of 'backups'.

Node 'n' leaves the mastership election

If node 'n' is the current 'master' and a backup exists, increment the 'term', promote the first backup to master, and send a mastership change event to each node. If node 'n' is the current 'master' and no backups exist, set the 'master' to Nil. If node 'n' is in the sequence of 'backups', simply remove it.

```
LeaveMastershipElection(n) \triangleq
    \land \ \lor \ \land \ master = n
          \wedge \vee \wedge Len(backups) > 0
                \wedge term' = term + 1
                \wedge master' = backups[1]
                \wedge backups' = Pop(backups)
                \land events' = [i \in Nodes \mapsto Append(events[i], [i])
                                                       term \mapsto term',
                                                       master \mapsto master',
                                                       backups \mapsto backups'[)]
              \lor \land Len(backups) = 0
                \land \mathit{master'} = \mathit{Nil}
                ∧ UNCHANGED ⟨term, backups, events⟩
       \lor \land n \in Range(backups)
          \land backups' = Drop(backups, CHOOSE j \in DOMAIN backups : backups[j] = n)
          \land UNCHANGED \langle term, master, events \rangle
    \land mastershipChanges' = mastershipChanges + 1
    ∧ UNCHANGED ⟨masterships, isMaster, stream Vars, message Vars, device Vars⟩
```

This section models controller-side mastership arbitration. The controller nodes receive mastership change events from the mastership service and send master arbitration requests to the device. Additionally, master nodes can send write requests to the device.

```
Returns master node 'n' election\_id for mastership term 'm' MasterElectionId(m) \stackrel{\triangle}{=} m.term + Cardinality(Nodes)
```

Returns backup node 'n'  $election\_id$  for mastership term 'm'

 $BackupElectionId(n, m) \triangleq m.term + Cardinality(Nodes) - CHOOSE \ i \in DOMAIN \ m.backups : m.backups[i] =$ 

Returns the mastership term for MasterArbitrationUpdate 'm'

```
MasterTerm(m) \stackrel{\Delta}{=} m.election\_id - Cardinality(Nodes)
```

Node 'n' receives a mastership change event from the mastership service

When a mastership change event is received, the node's local mastership state is updated. If the mastership term has changed, the node will set a flag to push the mastership change to the device in the master arbitration step.

```
LearnMastership(n) \triangleq
    IN
           \lor \land e.term > m.term
              \land masterships' = [masterships \ EXCEPT \ ! [n] = [
                                       term
                                              \mapsto e.term,
                                      master \mapsto e.master,
                                       backups \mapsto e.backups
           \lor \land e.term = m.term
              \land masterships' = [masterships \ EXCEPT \ ![n] = [
                                      term
                                              \mapsto e.term,
                                      master \mapsto e.master,
                                      backups \mapsto e.backups
    \land events' = [events \ EXCEPT \ ![n] = Pop(events[n])]
    \(\triangle \) UNCHANGED \(\langle master \), is Master, stream Vars, message Vars, device Vars\(\rangle \)
```

Node 'n' sends a MasterArbitrationUpdate to the device

If the node has an open stream to the device and a valid mastership state, a MasterArbitrationUpdate is sent to the device. If the node is a backup, the request's 'election\_id' is set to (mastership term) + (number of nodes) – (backup index). If the node is the master, the 'election\_id' is set to (mastership term) + (number of nodes). This is done to avoid  $election\_ids \leq 0$ . Note that the actual protocol requires a  $(device\_id, role\_id, election\_id)$  tuple, but  $(device\_id, role\_id)$  have been excluded from this model as we're modelling interaction only within a single  $(device\_id, role\_id)$  and thus they're irrelevant to correctness. The mastership term is sent in MasterArbitrationUpdate requests for model checking.

```
SendMasterArbitrationUpdate(n) \triangleq \\ \land IsStreamOpen(n) \\ \land LET \ m \triangleq masterships[n] \\ s \triangleq streams[n] \\ \text{IN} \\ \land m.term > 0 \\ \land s.term < m.term \\ \land \lor \land m.master = n \\ \land SendRequest(n, [\\ type \mapsto MasterArbitrationUpdate, \\ election\_id \mapsto MasterElectionId(m), \\ term \mapsto m.term]) \\ \lor \land m.master \neq n \\ \land n \in Range(m.backups)
```

```
 \land SendRequest(n, [\\ type \qquad \mapsto MasterArbitrationUpdate,\\ election\_id \mapsto BackupElectionId(n, m),\\ term \qquad \mapsto m.term])\\ \land streams' = [streams \ \text{EXCEPT} \ ![n].term = m.term]\\ \land \ \text{UNCHANGED} \ \langle mastership Vars, \ events, \ masterships, \ isMaster, \ deviceVars, \ streamChanges, \ responses\rangle
```

Node 'n' receives a MasterArbitrationUpdate from the device

If the node has an open stream with a MasterArbitrationUpdate, determine whether the local node is the master. If the MasterArbitrationUpdate 'status' is Ok, the 'election\_id' matches the last requested mastership term, and 'n' is the master for that term, update the node's state to master. Otherwise, the mastership request is considered out of date.

Note that the separate 'isMaster' state is maintained to indicate whether the \*device\* considers this node to be the current master, and this is necessary for the safety of the algorithm. Both the node and the device must agree on the role of the node.

```
ReceiveMasterArbitrationUpdate(n) \stackrel{\Delta}{=}
     \land IsStreamOpen(n)
     \land HasResponse(n, MasterArbitrationUpdate)
     \land \text{ LET } r \stackrel{\triangle}{=} NextResponse(n) \\ m \stackrel{\triangle}{=} masterships[n] 
             s \triangleq streams[n]
       ΙN
             \vee \wedge r.status = Ok
                \land m.master = n
                \land m.term = MasterTerm(r)
                \wedge s.term = m.term
                \land isMaster' = [isMaster \ EXCEPT \ ![n] = TRUE]
             \lor \land \lor r.status \neq Ok
                   \vee m.master \neq n
                    \forall s.term \neq m.term
                    \vee m.term \neq MasterTerm(r)
                \wedge isMaster' = [isMaster \ EXCEPT \ ![n] = FALSE]
     \land DiscardResponse(n)
     \land UNCHANGED \langle events, masterships, mastership Vars, device Vars, stream Vars, requests, message Count <math>\rangle
```

Master node 'n' sends a WriteRequest to the device

To write to the device, the node must have an open stream, must have received a mastership change event from the mastership service (stored in 'masterships') indicating it is the master, and must have received a MasterArbitrationUpdate from the switch indicating it is the master (stored in 'isMaster') for the same term as was indicated by the mastership service. The term is sent with the WriteRequest for model checking.

```
SendWriteRequest(n) \stackrel{\triangle}{=} \\ \land IsStreamOpen(n) \\ \land \text{LET } m \stackrel{\triangle}{=} masterships[n] \\ \text{IN} \\ \land m.term > 0 \\ \land m.master = n
```

```
 \land isMaster[n] \\ \land SendRequest(n, [\\ type \qquad \mapsto WriteRequest, \\ election\_id \mapsto MasterElectionId(m), \\ term \qquad \mapsto m.term]) \\ \land \text{UNCHANGED} \ \langle mastershipVars, \ nodeVars, \ deviceVars, \ streamVars, \ responses} \rangle \\ \\ \text{Node 'n' receives a write response from the device} \\ \\ ReceiveWriteResponse(n) \stackrel{\triangle}{=} \\ \land IsStreamOpen(n) \\ \land HasResponse(n, \ WriteResponse) \\ \land \text{LET} \ m \stackrel{\triangle}{=} NextResponse(n) \\ \text{IN} \\ \lor m.status = Ok \\ \lor m.status = PermissionDenied} \\ \land DiscardResponse(n) \\ \land \text{UNCHANGED} \ \langle mastershipVars, \ nodeVars, \ deviceVars, \ streamVars, \ requests, \ messageCount \rangle \\ \end{aligned}
```

This section models a P4 Runtime device. For the purposes of this spec, the device has two functions: determine a master controller node and accept writes. Mastership is determined through MasterArbitrationUpdates sent by the controller nodes. The 'election\_id's provided by controller nodes are stored in 'elections', and the master is computed as the node with the highest 'election\_id' at any given time. The device will only allow writes from the current master node.

```
Returns the highest election ID for the given elections DeviceElectionId(e) \triangleq Max(Range(e))

Returns the master for the given elections DeviceMaster(e) \triangleq

IF Cardinality(\{i \in Range(e) : i > 0\}) > 0 THEN

CHOOSE n \in DOMAIN \ e : e[n] = DeviceElectionId(e)

ELSE
```

Opens a new stream between node 'n' and the device

Nil

When a stream is opened, the 'streams' state for node 'n' is set to *Open*. Stream creation is modelled as a single step to reduce the state space.

```
\begin{aligned} &ConnectStream(n) \triangleq \\ & \land IsStreamClosed(n) \\ & \land streams' = [streams \ \texttt{EXCEPT} \ ![n].state = Open] \\ & \land streamChanges' = streamChanges + 1 \\ & \land \texttt{UNCHANGED} \ \langle mastership Vars, \ node Vars, \ device Vars, \ message Vars \rangle \end{aligned}
```

Closes an open stream between node 'n' and the device

When a stream is closed, the 'streams' state for node 'n' is set to Closed, any 'election\_id' provided by node 'n' is forgotten, and the 'requests' and 'responses' queues for the node are cleared. Additionally, if the stream belonged to the master node, a new master is elected and a MasterArbitrationUpdate is sent on the streams that remain in the Open state. The MasterArbitrationUpdate will be sent to the new master with a 'status' of Ok and to all slaves with a 'status' of AlreadyExists.

```
CloseStream(n) \triangleq
    \land IsStreamOpen(n)
    \land elections' = [elections \ EXCEPT \ ![n] = 0]
    \wedge terms' = [terms \ EXCEPT \ ![n] = 0]
    \land streams' = [streams \ EXCEPT \ ![n] = [state \mapsto Closed, \ term \mapsto 0]]
    \land \ requests' = [requests \ \texttt{EXCEPT} \ ! [n] = \langle \rangle]
    \land LET oldMaster \triangleq DeviceMaster(elections)
             newMaster \triangleq DeviceMaster(elections')
       IN
            \lor \land oldMaster \neq newMaster
               \land responses' = [i \in DOMAIN \ streams' \mapsto
                                     IF streams'[i].state = Open then
                                         If i = newMaster then
                                              Append(responses[i], [
                                                                \mapsto MasterArbitrationUpdate,
                                                  type
                                                                \mapsto Ok.
                                                  election\_id \mapsto DeviceElectionId(elections')])
                                              Append(responses[i], [
                                                  type
                                                                \mapsto MasterArbitrationUpdate,
                                                  status
                                                                \mapsto AlreadyExists,
                                                  election\_id \mapsto DeviceElectionId(elections')])
                                      ELSE
               \land messageCount' = messageCount + 1
            \lor \land oldMaster = newMaster
               \land responses' = [responses \ EXCEPT \ ![n] = \langle \rangle]
               \land UNCHANGED \langle messageCount \rangle
    \land streamChanges' = streamChanges + 1
    \land UNCHANGED \langle mastership Vars, node Vars, last Term, history <math>\rangle
```

The device receives and responds to a MasterArbitrationUpdate from node 'n'

If the 'election\_id' is already present in the 'elections' and does not already belong to node 'n', the stream is <code>Closed</code> and 'requests' and 'responses' are cleared for the node. If the 'election\_id' is not known to the device, it's added to the 'elections' state. If the change results in a new master being elected by the device, a <code>MasterArbitrationUpdate</code> is sent on all <code>Open</code> streams. If the change does not result in a new master being elected by the device, node 'n' is returned a

Master Arbitration Update. The device master will always receive a

Master Arbitration Update response with 'status' of Ok, and slaves will always receive a 'status' of Already Exists.

```
HandleMasterArbitrationUpdate(n) \stackrel{\Delta}{=}
    \land IsStreamOpen(n)
    \land HasRequest(n, MasterArbitrationUpdate)
    \wedge LET m \stackrel{\triangle}{=} NextRequest(n)
            \lor \land m.election\_id \in Range(elections)
               \land elections[n] \neq m.election\_id
               \land streams' = [streams \ EXCEPT \ ![n] = [state \mapsto Closed, \ term \mapsto 0]]
               \land requests' = [requests \ EXCEPT \ ![n] = \langle \rangle]
               \land responses' = [responses \ EXCEPT \ ![n] = \langle \rangle]
               \land UNCHANGED \langle deviceVars, streamChanges, messageCount \rangle
            \lor \land m.election\_id \notin Range(elections)
               \land elections' = [elections \ EXCEPT \ ![n] = m.election\_id]
               \wedge terms' = [terms \ EXCEPT \ ! [n] = m.term]
               \land LET oldMaster \triangleq DeviceMaster(elections)
                       newMaster \triangleq DeviceMaster(elections')
                 ΙN
                       \lor \land oldMaster \neq newMaster
                          \land responses' = [i \in \text{DOMAIN } streams \mapsto
                                               IF streams[i].state = Open THEN
                                                    If i = newMaster then
                                                        Append(responses[i], [
                                                                          \mapsto MasterArbitrationUpdate,
                                                             type
                                                             status
                                                             election\_id \mapsto DeviceElectionId(elections')])
                                                    ELSE
                                                        Append(responses[i], [
                                                                          \mapsto MasterArbitrationUpdate,
                                                             type
                                                             status
                                                                          \mapsto AlreadyExists,
                                                             election\_id \mapsto DeviceElectionId(elections')])
                                                ELSE
                                                    responses[i]]
                         \land messageCount' = messageCount + 1
                       \lor \land oldMaster = newMaster
                          \wedge \vee \wedge n = newMaster
                                \land SendResponse(n, [
                                       type
                                                     \mapsto MasterArbitrationUpdate,
                                                    \mapsto Ok.
                                       status
                                       election\_id \mapsto DeviceElectionId(elections')])
                             \lor \land n \neq newMaster
                                \land SendResponse(n, [
                                                     \mapsto MasterArbitrationUpdate,
                                       type
                                                    \mapsto AlreadyExists,
                                       election\_id \mapsto DeviceElectionId(elections')])
               ∧ UNCHANGED ⟨stream Vars⟩
```

```
\land DiscardRequest(n)
 \land UNCHANGED \ \langle mastership Vars, node Vars, lastTerm, history \rangle
```

The device receives a WriteRequest from node 'n'

The WriteRequest is accepted if:

- \* The 'election\_id' for node 'n' matches the 'election\_id' for its stream
- \* Node 'n' is the current master for the device
- \* If node 'n' provided a 'term', the 'term' is greater than or equal to the highest term received by the device

When the WriteRequest is accepted, the 'lastTerm' is updated and the term of the node that sent the request is recorded for model checking. If the WriteRequest is rejected, a PermissionDenied response is returned.

```
HandleWrite(n) \triangleq
    \land IsStreamOpen(n)
    \land HasRequest(n, WriteRequest)
    \wedge \text{ LET } m \stackrel{\triangle}{=} NextRequest(n)
            \lor \land elections[n] = m.election\_id
               \land DeviceMaster(elections) = n
               \wedge \vee terms[n] = 0
                   \lor \land terms[n] \ge lastTerm
                     \wedge lastTerm' = terms[n]
               \land history' = Append(history, [node \mapsto n, term \mapsto m.term])
               \land SendResponse(n, [
                       type \mapsto WriteResponse,
                      status \mapsto Ok)
            \lor \land \lor elections[n] \neq m.election\_id
                   \lor DeviceMaster(elections) \neq n
                  \lor \land terms[n] > 0
                     \land \ terms[n] < lastTerm
               \land SendResponse(n, 
                       type \mapsto WriteResponse,
                       status \mapsto PermissionDenied)
               \land UNCHANGED \langle lastTerm, history \rangle
    \wedge DiscardRequest(n)
    ∧ UNCHANGED ⟨mastership Vars, node Vars, elections, terms, stream Vars⟩
```

The invariant asserts that the device will not allow a write from an older master if it has already accepted a write from a newer master. This is determined by comparing the mastership terms of accepted writes. For this invariant to hold, terms may only increase in the history of writes.

```
TypeInvariant \triangleq \\ \land \forall x \in 1 .. Len(history) : \\ \forall y \in x .. Len(history) : \\ history[x].term \leq history[y].term \\ \land \forall x \in 1 .. Len(history) :
```

```
\forall y \in x ... Len(history) :
 history[x].term = history[y].term \Rightarrow history[x].node = history[y].node
```

```
Init \; \stackrel{\scriptscriptstyle \Delta}{=} \;
      \wedge term = 0
     \land master = Nil
     \wedge backups = \langle \rangle
      \land events = [n \in Nodes \mapsto \langle \rangle]
     \land masterships = [n \in Nodes \mapsto [term \mapsto 0, master \mapsto Nil, backups \mapsto \langle \rangle]]
     \land isMaster = [n \in Nodes \mapsto FALSE]
     \land streams = [n \in Nodes \mapsto [state \mapsto Closed, term \mapsto 0]]
      \land requests = [n \in Nodes \mapsto \langle \rangle]
      \land responses = [n \in Nodes \mapsto \langle \rangle]
      \land elections = [n \in Nodes \mapsto 0]
      \land terms = [n \in Nodes \mapsto 0]
      \wedge lastTerm = 0
      \land mastershipChanges = 0
     \wedge streamChanges = 0
      \land \ messageCount = 0
      \wedge history = \langle \rangle
Next \triangleq
     \vee \exists n \in Nodes : ConnectStream(n)
      \vee \exists n \in Nodes : CloseStream(n)
     \vee \exists n \in Nodes : JoinMastershipElection(n)
     \vee \exists n \in Nodes : LeaveMastershipElection(n)
      \vee \exists n \in Nodes : LearnMastership(n)
      \vee \exists n \in Nodes : SendMasterArbitrationUpdate(n)
      \vee \exists n \in Nodes : HandleMasterArbitrationUpdate(n)
      \vee \exists n \in Nodes : ReceiveMasterArbitrationUpdate(n)
      \vee \exists n \in Nodes : SendWriteRequest(n)
      \vee \exists n \in Nodes : HandleWrite(n)
      \vee \exists n \in Nodes : ReceiveWriteResponse(n)
Spec \stackrel{\triangle}{=} Init \wedge \Box [Next]_{vars}
```

 $<sup>\</sup>backslash * \ {\bf Modification} \ {\bf History}$ 

<sup>\\*</sup> Last modified Wed Feb 20 17:53:13 PST 2019 by jordanhalterman

<sup>\\*</sup> Created Thu Feb 14 11:33:03 PST 2019 by jordanhalterman