

Given file ElGamal.py

Encryption function mathematically gives

$$t = (h^k \times m) \text{ modulo } p$$
$$r = (g^k) \text{ modulo } p$$

Decryption function mathematically gives

$$m = (r^{q-s} \times t) \text{ modulo } p$$

But using given encryption function we can create our own decryption

$$m = ((h^k)^{-1} \times t) \text{ modulo } p$$

Thus we need to find k, where  $1 < k < 2^{16} - 1$  as given in encryption function and we are already given  $r = (g^k) \text{ modulo } p$ , so we iterate over powers of g and find the k.

Then for k such that  $r = (g^k) \text{ modulo } p$  ;

We calculate the following:  $h^k$

Take inverse of  $h^k$  over  $\text{modulo } p$  which is  $(h^k)^{-1}$

And finally using the function  $m = ((h^k)^{-1} \times t) \text{ modulo } p$  gives us the message m.