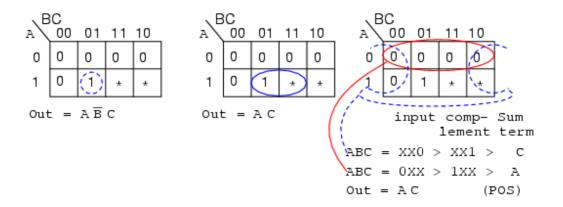
DON'T CARE CELLS IN THE KARNAUGH MAP

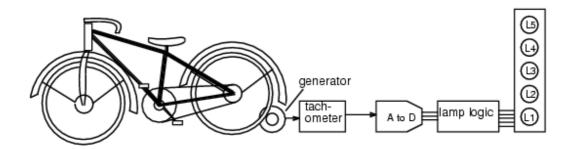
Up to this point we have considered logic reduction problems where the input conditions were completely specified. That is, a 3-variable truth table or Karnaugh map had $2^n = 2^3$ or 8-entries, a full table or map. It is not always necessary to fill in the complete truth table for some real-world problems. We may have a choice to not fill in the complete table.

For example, when dealing with BCD (Binary Coded Decimal) numbers encoded as four bits, we may not care about any codes above the BCD range of (0, 1, 2...9). The 4-bit binary codes for the hexadecimal numbers (Ah, Bh, Ch, Eh, Fh) are not valid BCD codes. Thus, we do not have to fill in those codes at the end of a truth table, or K-map, if we do not care to. We would not normally care to fill in those codes because those codes (1010, 1011, 1100, 1101, 1110, 1111) will never exist as long as we are dealing only with BCD encoded numbers. These six invalid codes are *don't cares* as far as we are concerned. That is, we do not care what output our logic circuit produces for these don't cares.

Don't cares in a Karnaugh map, or truth table, may be either 1s or 0s, as long as we don't care what the output is for an input condition we never expect to see. We plot these cells with an asterisk, *, among the normal 1s and 0s. When forming groups of cells, treat the don't care cell as either a 1 or a 0, or ignore the don't cares. This is helpful if it allows us to form a larger group than would otherwise be possible without the don't cares. There is no requirement to group all or any of the don't cares. Only use them in a group if it simplifies the logic.



Above is an example of a logic function where the desired output is 1 for input ABC = 101 over the range from 000 to 101. We do not care what the output is for the other possible inputs (110, 111). Map those two as don't cares. We show two solutions. The solution on the right Out = AB'C is the more complex solution since we did not use the don't care cells. The solution in the middle, Out=AC, is less complex because we grouped a don't care cell with the single 1 to form a group of two. The third solution, a Product-Of-Sums on the right, results from grouping a don't care with three zeros forming a group of four 0s. This is the same, less complex, Out=AC. We have illustrated that the don't care cells may be used as either 1s or 0s, whichever is useful.

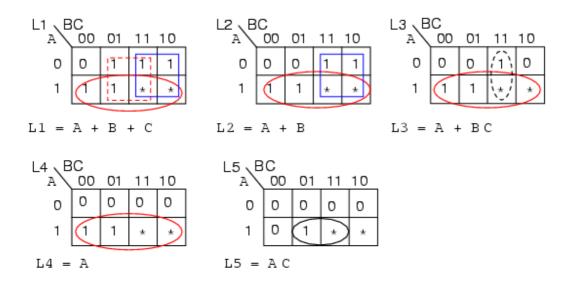


The electronics class of Lightning State College has been asked to build the lamp logic for a stationary bicycle exhibit at the local science museum. As a rider increases his pedaling speed, lamps will light on a bar graph display. No lamps will light for no motion. As speed increases, the lower lamp, L1 lights, then L1 and L2, then, L1, L2, and L3, until all lamps light at the highest speed. Once all the lamps illuminate, no further increase in speed will have any effect on the display.

A small DC generator coupled to the bicycle tire outputs a voltage proportional to speed. It drives a tachometer board which limits the voltage at the high end of speed where all lamps light. No further increase in speed can increase the voltage beyond this level. This is crucial

because the downstream A to D (Analog to Digital) converter puts out a 3-bit code, **ABC**, 2^3 or 8-codes, but we only have five lamps. **A** is the most significant bit, **C** the least significant bit.

The lamp logic needs to respond to the six codes out of the A to D. For **ABC=000**, no motion, no lamps light. For the five codes (**001** to **101**) lamps L1, L1&L2, L1&L2&L3, up to all lamps will light, as speed, voltage, and the A to D code (ABC) increases. We do not care about the response to input codes (**110**, **111**) because these codes will never come out of the A to D due to the limiting in the tachometer block. We need to design five logic circuits to drive the five lamps.



Since, none of the lamps light for **ABC=000** out of the A to D, enter a **0** in all K-maps for cell **ABC=000**. Since we don't care about the never to be encountered codes (**110**, **111**), enter asterisks into those two cells in all five K-maps.

Lamp L5 will only light for code **ABC=101**. Enter a **1** in that cell and five **0**s into the remaining empty cells of L5 K-map.

L4 will light initially for code **ABC=100**, and will remain illuminated for any code greater, **ABC=101**, because all lamps below L5 will light when L5 lights. Enter **1**s into cells **100** and **101** of the L4 map so that it will light for those codes. Four **0**'s fill the remaining L4 cells

L3 will initially light for code **ABC=011**. It will also light whenever L5 and L4 illuminate. Enter three **1**s into cells **011**, **100**, **101** for L3 map. Fill three **0**s into the remaining L3 cells.

L2 lights for **ABC=010** and codes greater. Fill **1**s into cells **010**, **011**, **100**, **101**, and two **0**s in the remaining cells.

The only time L1 is not lighted is for no motion. There is already a 0 in cell **ABC=000**. All the other five cells receive 1s.

Group the 1's as shown above, using don't cares whenever a larger group results. The L1 map shows three product terms, corresponding to three groups of 4-cells. We used both don't cares in two of the groups and one don't care on the third group. The don't cares allowed us to form groups of four.