

ANALYSIS OF A TRANSISTOR AMPLIFIER USING H-PARAMETERS

To form a transistor amplifier it is only necessary to connect an external load and signal source as indicated in fig. 1 and to bias the transistor properly.

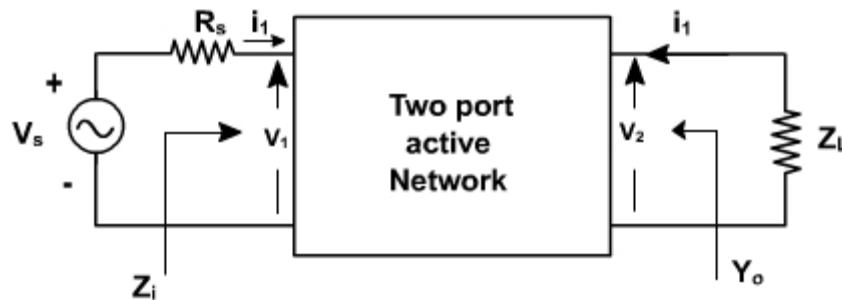


Fig. 1

Consider the two-port network of CE amplifier. R_S is the source resistance and Z_L is the load impedance. h -parameters are assumed to be constant over the operating range. The ac equivalent circuit is shown in fig. 2. (Phasor notations are used assuming sinusoidal voltage input). The quantities of interest are the current gain, input impedance, voltage gain, and output impedance.

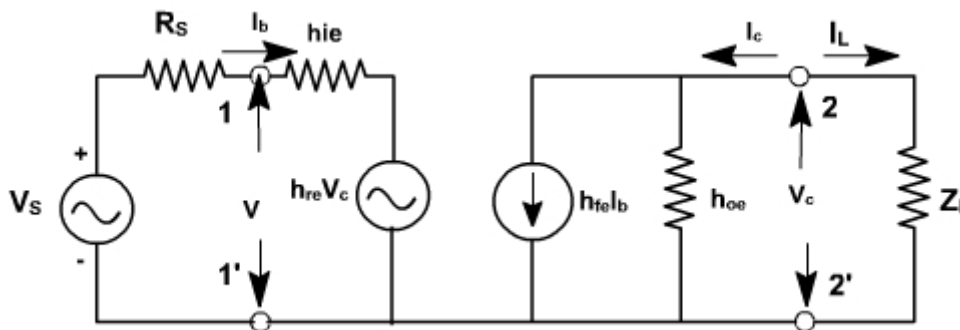


Fig. 2

Current gain:

For the transistor amplifier stage, A_i is defined as the ratio of output to input currents.

$$A_i = \frac{I_L}{I_b} = \frac{-I_c}{I_b} \quad (I_L + I_c = 0 \quad \therefore I_L = -I_c)$$

$$I_c = h_{fe} I_b + h_{oe} V_c$$

$$V_c = I_L Z_L = -I_c Z_L$$

$$\therefore I_c = h_{fe} I_b + h_{oe} (-I_c Z_L)$$

$$\text{or } \frac{I_c}{I_b} = \frac{h_{fe}}{1 + h_{oe} Z_L}$$

$$\therefore A_i = - \frac{h_{fe}}{1 + h_{oe} Z_L}$$

Input Impedence:

The impedance looking into the amplifier input terminals (1,1') is the input impedance Z_i

$$Z_i = \frac{V_b}{I_b}$$

$$V_b = h_{ie} I_b + h_{re} V_c$$

$$\frac{V_b}{I_b} = h_{ie} + h_{re} \frac{V_c}{I_b}$$

$$= h_{ie} - \frac{h_{re} I_c Z_L}{I_b}$$

$$\therefore Z_i = h_{ie} + h_{re} A_i Z_L$$

$$= h_{ie} - \frac{h_{re} h_{fe} Z_L}{1 + h_{oe} Z_L}$$

$$\therefore Z_i = h_{ie} - \frac{h_{re} h_{fe}}{Y_L + h_{oe}} \quad (\text{since } Y_L = \frac{1}{Z_L})$$

Voltage gain:

The ratio of output voltage to input voltage gives the gain of the transistors.

$$A_v = \frac{V_c}{V_b} = - \frac{I_c Z_L}{V_b}$$

$$\therefore A_v = \frac{I_b A_i Z_L}{V_b} = \frac{A_i Z_L}{Z_i}$$

Output Admittance:

It is defined as

$$Y_0 = \left. \frac{I_c}{V_c} \right|_{V_s=0} = 0$$

$$I_c = h_{fe} I_b + h_{oe} V_c$$

$$\frac{I_c}{V_c} = h_{fe} \frac{I_b}{V_c} + h_{oe}$$

when $V_s = 0$, $R_s \cdot I_b + h_{ie} \cdot I_b + h_{re} V_c = 0$.

$$\frac{I_b}{V_c} = - \frac{h_{re}}{R_s + h_{ie}}$$

$$\therefore Y_0 = h_{oe} - \frac{h_{re} h_{fe}}{R_s + h_{ie}}$$

Voltage amplification taking into account source impedance (R_s) is given by

$$A_{VS} = \frac{V_c}{V_s} = \frac{V_c}{V_b} * \frac{V_b}{V_s} \quad \left(V_b = \frac{V_s * Z_i}{R_s + Z_i} \right)$$

$$= A_V \cdot \frac{Z_i}{Z_i + R_s}$$

$$= \frac{A_i Z_L}{Z_i + R_s}$$

A_v is the voltage gain for an ideal voltage source ($R_s = 0$).

Consider input source to be a current source I_s in parallel with a resistance R_s as shown in fig. 3.

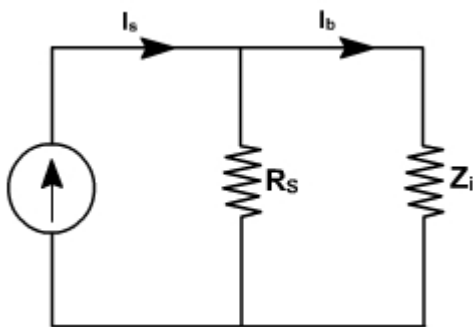


Fig. 3

In this case, overall current gain A_{I_s} is defined as

$$\begin{aligned}
 A_{I_s} &= \frac{I_L}{I_s} \\
 &= -\frac{I_c}{I_s} \\
 &= -\frac{I_c}{I_b} * \frac{I_b}{I_s} \quad \left(I_b = \frac{I_s * R_s}{R_s + Z_i} \right) \\
 &= A_I * \frac{R_s}{R_s + Z_i} \\
 \text{If } R_s \rightarrow \infty, \quad A_{I_s} &\rightarrow A_I
 \end{aligned}$$