

Signals and classification of signals

A signal is a function representing physical quantity or variable and typically it contains information about the behavior or nature of the phenomenon. For instance, in a RC circuit the signal may represent the voltage across the capacitor or the current flowing in the resistor. Mathematically, a signal is represented as a function of an independent variable t . Usually t represents time. Thus, a signal is denoted by $x(t)$.

A. Continuous-Time and Discrete-Time Signals: A signal $x(t)$ is a *continuous-time* signal if t is a continuous variable. If t is a discrete variable, that is, $x(t)$ is defined at discrete times, then $x(t)$ is a *discrete-time* signal. Since a discrete-time signal is defined at discrete times, a discrete-time signal is often identified as a *sequence* of numbers, denoted by $\{x[n]\}$ or $x[n]$, where $n = \text{integer}$. Illustrations of a continuous-time signal $x(t)$ and of a discrete-time signal $x[n]$ are shown in Fig.

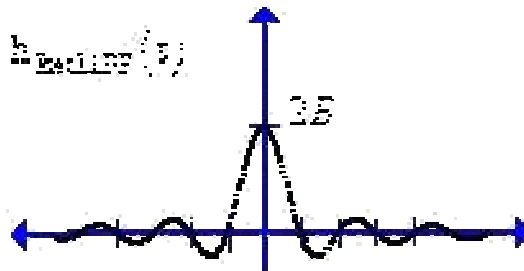


Figure 1.4

A discrete-time signal $x[n]$ may represent a phenomenon for which the independent variable is inherently discrete. For instance, the daily closing stock market average is by its nature a signal that evolves at discrete points in time (that is, at the close of each day). On the other hand a discrete-time signal $x[n]$ may be obtained by *sampling* a continuous-time

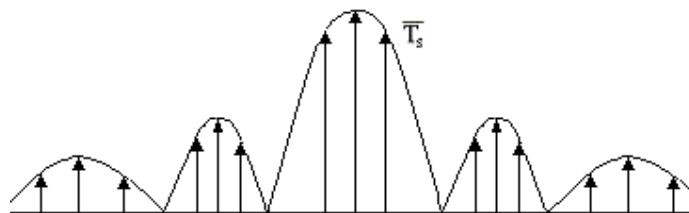


Figure 1.5

signal $x(t)$ such as $x(t_0)$, $x(t_1)$, ..., $x(t_n)$, ...

B. Analog and Digital Signals: If a continuous-time signal $x(t)$ can take on any value in the continuous interval (a, b) ,

where a may be $-\infty$ and b may be ∞ then the continuous-time signal $x(t)$ is called an *analog* signal. If a discrete-time signal $x[n]$ can take on only a finite number of distinct values, then we call this signal a *digital* signal.

C. Real and Complex Signals: A signal $x(t)$ is a *real* signal if its value is a real number, and a signal $x(t)$ is a *complex* signal if its value is a complex number. A general complex signal $x(t)$ is a function of the form

$$x(t) = x_l(t) + jx_c(t)$$

D. Deterministic and Random Signals:

Deterministic signals are those signals whose values are completely specified for any given time. Thus, a deterministic signal can be modeled by a known function of time t .

Random signals are those signals that take random values at any given time and must be characterized statistically. Random signals will not be discussed in this text.

E. Even and Odd Signals:

A signal $x(t)$ or $x[n]$ is referred to as an *even* signal if

$$x(-t) = x(t)$$

A signal $x(t)$ or $x[n]$ is referred to as an *odd* signal if

$$x(-t) = -x(t)$$

Examples of even and odd signals:

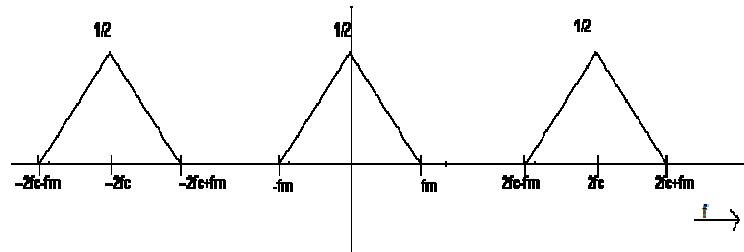


Figure 1.6 Even signal

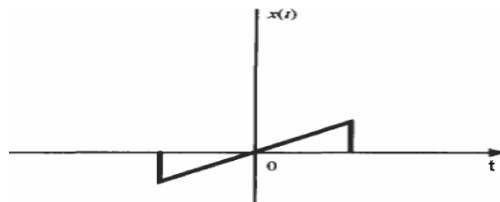


Figure 1.7 Odd signal

F. Periodic and Nonperiodic Signals:

A continuous-time signal $x(t)$ is said to be *periodic with period T* if there is a positive nonzero value of T for which

$$x(t) = x(t+T)$$

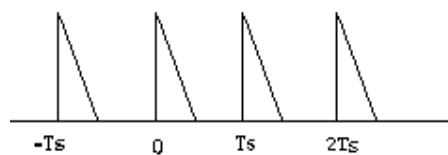


Figure 1.8

Otherwise it is called aperiodic signal.