

TABLE C.4 χ^2 distribution. Values of the reduced chi-square $\chi^2_{\nu} = \chi^2 / \nu$ corresponding to the probability $P_{\chi}(\chi^2; \nu)$ of exceeding χ^2 vs. the number of degrees of freedom ν

| | P | | | | | | | | | |
|-----|---------|---------|---------|--------|--------|-------|-------|-------|--|--|
| ν | 0.99 | 0.98 | 10.95 | 0.90 | 0.80 | 0.70 | 0.60 | 0.50 | | |
| 1 | 0.00016 | 0.00063 | 0.00393 | 0.0158 | 0.0642 | 0.148 | 0.275 | 0.45 | | |
| 2 | 0.0100 | 0.0202 | 0.0515 | 0.105 | 0.223 | 0.357 | 0.511 | 0.69 | | |
| 3 | 0.0383 | 0.0617 | 0.117 | 0.195 | 0.335 | 0.475 | 0.623 | 0.78 | | |
| 4 | 0.0742 | 0.107 | 0.178 | 0.266 | 0.412 | 0.549 | 0.688 | 0.83 | | |
| 5 | 0.111 | 0.150 | 0.229 | 0.322 | 0.469 | 0.600 | 0.731 | 0.87 | | |
| 6 | 0.145 | 0.189 | 0.273 | 0.367 | 0.512 | 0.638 | 0.762 | 0.89 | | |
| 7 | 0.177 | 0.223 | 0.310 | 0.405 | 0.546 | 0.667 | 0.785 | 0.90 | | |
| 8 | 0.206 | 0.254 | 0.342 | 0.436 | 0.574 | 0.691 | 0.803 | 0.91 | | |
| 9 | 0.232 | 0.281 | 0.369 | 0.463 | 0.598 | 0.710 | 0.817 | 0.92 | | |
| 10 | 0.256 | 0.306 | 0.394 | 0.487 | 0.618 | 0.727 | 0.830 | 0.93 | | |
| 11 | 0.278 | 0.328 | 0.416 | 0.507 | 0.635 | 0.741 | 0.840 | 0.94 | | |
| 12 | 0.298 | 0.348 | 0.436 | 0.525 | 0.651 | 0.753 | 0.848 | 0.94 | | |
| 13 | 0.316 | 0.367 | 0.453 | 0.542 | 0.664 | 0.764 | 0.856 | 0.949 | | |
| 14 | 0.333 | 0.383 | 0.469 | 0.556 | 0.676 | 0.773 | 0.863 | 0.953 | | |
| 15 | 0.349 | 0.399 | 0.484 | 0.570 | 0.687 | 0.781 | 0.869 | 0.95 | | |
| 16 | 0.363 | 0.413 | 0.498 | 0.582 | 0.697 | 0.789 | 0.874 | 0.959 | | |
| 17 | 0.377 | 0.427 | 0.510 | 0.593 | 0.706 | 0.796 | 0.879 | 0.96 | | |
| 18 | 0.390 | 0.439 | 0.522 | 0.604 | 0.714 | 0.802 | 0.883 | 0.963 | | |
| 19 | 0.402 | 0.451 | 0.532 | 0.613 | 0.722 | 0.808 | 0.887 | 0.965 | | |
| 20 | 0.413 | 0.462 | 0.543 | 0.622 | 0.729 | 0.813 | 0.890 | 0.967 | | |
| 22 | 0.434 | 0.482 | 0.561 | 0.638 | 0.742 | 0.823 | 0.897 | 0.970 | | |
| 24 | 0.452 | 0.500 | 0.577 | 0.652 | 0.753 | 0.831 | 0.902 | 0.972 | | |
| 26 | 0.469 | 0.516 | 0.592 | 0.665 | 0.762 | 0.838 | 0.907 | 0.974 | | |
| 28 | 0.484 | 0.530 | 0.605 | 0.676 | 0.771 | 0.845 | 0.911 | 0.976 | | |
| 30 | 0.498 | 0.544 | 0.616 | 0.687 | 0.779 | 0.850 | 0.915 | 0.978 | | |
| 32 | 0.511 | 0.556 | 0.627 | 0.696 | 0.786 | 0.855 | 0.918 | 0.979 | | |
| 34 | 0.523 | 0.567 | 0.637 | 0.704 | 0.792 | 0.860 | 0.921 | 0.980 | | |
| 36 | 0.534 | 0.577 | 0.646 | 0.712 | 0.798 | 0.864 | 0.924 | 0.982 | | |
| 38 | 0.545 | 0.587 | 0.655 | 0.720 | 0.804 | 0.868 | 0.926 | 0.983 | | |
| 40 | 0.554 | 0.596 | 0.663 | 0.726 | 0.809 | 0.872 | 0.928 | 0.983 | | |
| 42 | 0.563 | 0.604 | 0.670 | 0.733 | 0.813 | 0.875 | 0.930 | 0.984 | | |
| 44 | 0.572 | 0.612 | 0.677 | 0.738 | 0.818 | 0.878 | 0.932 | 0.985 | | |
| 46 | 0.580 | 0.620 | 0.683 | 0.744 | 0.822 | 0.881 | 0.934 | 0.986 | | |
| 48 | 0.587 | 0.627 | 0.690 | 0.749 | 0.825 | 0.884 | 0.936 | 0.986 | | |
| 50 | 0.594 | 0.633 | 0.695 | 0.754 | 0.829 | 0.886 | 0.937 | 0.987 | | |
| 60 | 0.625 | 0.662 | 0.720 | 0.774 | 0.844 | 0.897 | 0.944 | 0.989 | | |
| 70 | 0.649 | 0.684 | 0.739 | 0.790 | 0.856 | 0.905 | 0.949 | 0.990 | | |
| 80 | 0.669 | 0.703 | 0.755 | 0.803 | 0.865 | 0.911 | 0.952 | 0.992 | | |
| 90 | 0.686 | 0.718 | 0.768 | 0.814 | 0.873 | 0.917 | 0.955 | 0.993 | | |
| 100 | 0.701 | 0.731 | 0.779 | 0.824 | 0.879 | 0.921 | 0.958 | 0.993 | | |
| 20 | 0.724 | 0.753 | 0.798 | 0.839 | 0.890 | 0.928 | 0.962 | 0.994 | | |
| 140 | 0.743 | 0.770 | 0.812 | 0.850 | 0.898 | 0.934 | 0.965 | 0.995 | | |
| 160 | 0.758 | 0.784 | 0.823 | 0.860 | 0.905 | 0.938 | 0.968 | 0.996 | | |
| 80 | 0.771 | 0.796 | 0.833 | 0.868 | 0.910 | 0.942 | 0.970 | 0.996 | | |
| 200 | 0.782 | 0.806 | 0.841 | 0.874 | 0.915 | 0.945 | 0.972 | 0.997 | | |

TABLE C.4 χ^2 distribution (continued)

| ν | <u> </u> | | | | | | | | | |
|-----|----------|-------|-------|-------|-------|-------|-------|--------|--|--|
| | 0.40 | 0.30 | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 | 0.001 | | |
| 1 | 0.708 | 1.074 | 1.642 | 2.706 | 3.841 | 5.412 | 6.635 | 10.827 | | |
| 2 | 0.916 | 1.204 | 1.609 | 2.303 | 2.996 | 3.912 | 4.605 | 6.908 | | |
| 3 | 0.982 | 1.222 | 1.547 | 2.084 | 2.605 | 3.279 | 3.780 | 5.423 | | |
| 4 | 1.011 | 1.220 | 1.497 | 1.945 | 2.372 | 2.917 | 3.319 | 4.617 | | |
| 5 | 1.026 | 1.213 | 1.458 | 1.847 | 2.214 | 2.678 | 3.017 | 4.102 | | |
| 6 | 1.035 | 1.205 | 1.426 | 1.774 | 2.099 | 2.506 | 2.802 | 3.743 | | |
| 7 | 1.040 | 1.198 | 1.400 | 1.717 | 2.010 | 2.375 | 2.639 | 3.475 | | |
| 8 | 1.044 | 1.191 | 1.379 | 1.670 | 1.938 | 2.271 | 2.511 | 3.266 | | |
| 9 | 1.046 | 1.184 | 1.360 | 1.632 | 1.880 | 2.187 | 2.407 | 3.097 | | |
| 10 | 1.047 | 1.178 | 1.344 | 1.599 | 1.831 | 2.116 | 2.321 | 2.959 | | |
| 11 | 1.048 | 1.173 | 1.330 | 1.570 | 1.789 | 2.056 | 2.248 | 2.842 | | |
| 12 | 1.049 | 1.168 | 1.318 | 1.546 | 1.752 | 2.004 | 2.185 | 2.742 | | |
| 13 | 1.049 | 1.163 | 1.307 | 1.524 | 1.720 | 1.959 | 2.130 | 2.656 | | |
| 14 | 1.049 | 1.159 | 1.296 | 1.505 | 1.692 | 1.919 | 2.082 | 2.580 | | |
| 15 | 1.049 | 1.155 | 1.287 | 1.487 | 1.666 | 1.884 | 2.039 | 2.513 | | |
| 16 | 1.049 | 1.151 | 1.279 | 1.471 | 1.644 | 1.852 | 2.000 | 2.453 | | |
| 17 | 1.048 | 1.148 | 1.271 | 1.457 | 1.623 | 1.823 | 1.965 | 2.399 | | |
| 18 | 1.048 | 1.145 | 1.264 | 1.444 | 1.604 | 1.797 | 1.934 | 2.35 | | |
| 19 | 1.048 | 1.142 | 1.258 | 1.432 | 1.586 | 1.773 | 1.905 | 2.30 | | |
| 20 | 1.048 | 1.139 | 1.252 | 1.421 | 1.571 | 1.751 | 1.878 | 2.26 | | |
| 22 | 1.047 | 1.134 | 1.241 | 1.401 | 1.542 | 1.712 | 1.831 | 2.19 | | |
| 24 | 1.046 | 1.129 | 1.231 | 1.383 | 1.517 | 1.678 | 1.791 | 2.13 | | |
| 26 | 1.045 | 1.125 | 1.223 | 1.368 | 1.496 | 1.648 | 1.755 | 2.07 | | |
| 28 | 1.045 | 1.121 | 1.215 | 1.354 | 1.476 | 1.622 | 1.724 | 2.03 | | |
| 30 | 1.044 | 1.118 | 1.208 | 1.342 | 1.459 | 1.599 | 1.696 | 1.99 | | |
| 32 | 1.043 | 1.115 | 1.202 | 1.331 | 1.444 | 1.578 | 1.671 | 1.95 | | |
| 34 | 1.042 | 1.112 | 1.196 | 1.321 | 1.429 | 1.559 | 1.649 | 1.91 | | |
| 36 | 1.042 | 1.109 | 1.191 | 1.311 | 1.417 | 1.541 | 1.628 | 1.88 | | |
| 38 | 1.041 | 1.106 | 1.186 | 1.303 | 1.405 | 1.525 | 1.610 | 1.86 | | |
| 40 | 1.041 | 1.104 | 1.182 | 1.295 | 1.394 | 1.511 | 1.592 | 1.83 | | |
| 42 | 1.040 | 1.102 | 1.178 | 1.288 | 1.384 | 1.497 | 1.576 | 1.81 | | |
| 44 | 1.039 | 1.100 | 1.174 | 1.281 | 1.375 | 1.485 | 1.562 | 1.79 | | |
| 46 | 1.039 | 1.098 | 1.170 | 1.275 | 1.366 | 1.473 | 1.548 | 1.77 | | |
| 48 | 1.038 | 1.096 | 1.167 | 1.269 | 1.358 | 1.462 | 1.535 | 1.75 | | |
| 50 | 1.038 | 1.094 | 1.163 | 1.263 | 1.350 | 1.452 | 1.523 | 1.73 | | |
| 60 | 1.036 | 1.087 | 1.150 | 1.240 | 1.318 | 1.410 | 1.473 | 1.66 | | |
| 70 | 1.034 | 1.081 | 1.139 | 1.222 | 1.293 | 1.377 | 1.435 | 1.60 | | |
| 80 | 1.032 | 1.076 | 1.130 | 1.207 | 1.273 | 1.351 | 1.404 | 1.56 | | |
| 90 | 1.031 | 1.072 | 1.123 | 1.195 | 1.257 | 1.329 | 1.379 | 1.52 | | |
| 100 | 1.029 | 1.069 | 1.117 | 1.185 | 1.243 | 1.311 | 1.358 | 1.49 | | |
| 120 | 1.027 | 1.063 | 1.107 | 1.169 | 1.221 | 1.283 | 1.325 | 1.44 | | |
| 140 | 1.026 | 1.059 | 1.099 | 1.156 | 1.204 | 1.261 | 1.299 | 1.41 | | |
| 160 | 1.024 | 1.055 | 1.093 | 1.146 | 1.191 | 1.243 | 1.278 | 1.38 | | |
| 180 | 1.023 | 1.052 | 1.087 | 1.137 | 1.179 | 1.228 | 1.261 | 1.35 | | |
| 200 | 1.022 | 1.050 | 1.083 | 1.130 | 1.170 | 1.216 | 1.247 | 1.33 | | |