

**Example 1:** Do the points  $(3, 2)$ ,  $(-2, -3)$  and  $(2, 3)$  form a triangle? If so, name the type of triangle formed.

**Solution:** Let us apply the distance formula to find the distances  $PQ$ ,  $QR$ , and  $PR$ , where  $P(3, 2)$ ,  $Q(-2, -3)$  and  $R(2, 3)$  are the given points. We have

$$PQ = \sqrt{(3 + 2)^2 + (2 + 3)^2} = \sqrt{5^2 + 5^2} = \sqrt{50} = 7.07 \text{ (approx.)}$$

$$QR = \sqrt{(-2 - 2)^2 + (-3 - 3)^2} = \sqrt{(-4)^2 + (-6)^2} = \sqrt{52} = 7.21 \text{ (approx.)}$$

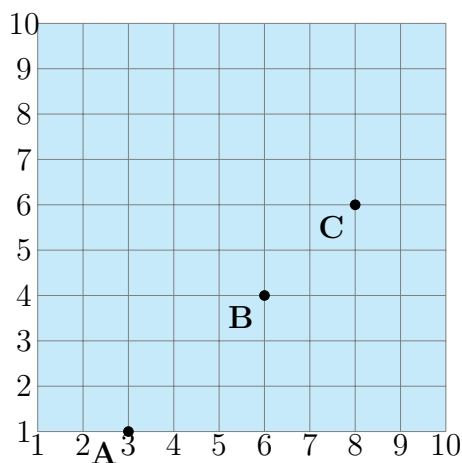
$$PR = \sqrt{(3 - 2)^2 + (2 - 3)^2} = \sqrt{1^2 + (-1)^2} = \sqrt{2} = 1.41 \text{ (approx.)}$$

Since the sum of any two of these distances is greater than the third distance, the points  $P$ ,  $Q$ , and  $R$  form a triangle.

Also,  $PQ^2 + PR^2 = QR^2$ . By the converse of Pythagoras' theorem, we have  $\angle P = 90^\circ$ .

Therefore,  $\triangle PQR$  is a right triangle.

**Example 3 :** Fig. 7.6 shows the arrangement of desks in a classroom. Ashima, Bharti and Camella are seated at  $A(3, 1)$ ,  $B(6, 4)$ , and  $C(8, 6)$  respectively. Do you think they are seated in a line? Give reasons for your answer.



**Fig. 7.6**

**Solution :** Using the distance formula, we have

$$AB = \sqrt{(6-3)^2 + (4-1)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$BC = \sqrt{(8-6)^2 + (6-4)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

$$AC = \sqrt{(8-3)^2 + (6-1)^2} = \sqrt{25+25} = \sqrt{50} = 5\sqrt{2}$$

Since  $AB + BC = 3\sqrt{2} + 2\sqrt{2} = 5\sqrt{2} = AC$ , we can say that the points A, B and C are collinear. Therefore, they are seated in a line.