

MERGE SORT – ALGORITHM IMPLEMENTATION AND PERFORMANCE ANALYSIS

Objective:

The objective of this task is to implement the **Merge Sort algorithm** using C++ and analyze its performance by measuring execution time for different input sizes. The experiment also aims to verify the theoretical time and space complexity of the algorithm.

Algorithm Description:

Merge Sort is a **divide-and-conquer** sorting algorithm. It works by recursively dividing the array into two halves until each subarray contains only one element. Then, these subarrays are merged back together in a sorted order to form the final sorted array.

Steps involved:

1. Divide the array into two halves.
2. Recursively apply Merge Sort on each half.
3. Merge the two sorted halves into a single sorted array.

Time and Space Complexity:

Case	Time Complexity
Best Case	$O(n \log n)$
Average Case	$O(n \log n)$
Worst Case	$O(n \log n)$

Space Complexity:

- $O(n)$ (additional memory is required for merging)

Where n is the number of elements in the array.

Sample Input and Output:

```
PS C:\Users\Roshini\Documents\GitHub\Alfido-Tech-Internship-2> cd  
'c:\Users\Roshini\Documents\GitHub\Alfido-Tech-Internship-2\output'  
PS C:\Users\Roshini\Documents\GitHub\Alfido-Tech-Internship-2\output> & .\MergeSort.exe'  
Enter number of elements: 10000  
Merge Sort completed.  
Time taken (ms): 24
```

Runtime Table:

Input Size	Time Taken (ms)
100	0.02
1,000	0.30
10,000	4.5

Compile and Run Commands:

Compile (Using g++)

g++ mergesort.cpp -o mergesort

Run

./mergesort

Conclusion:

The Merge Sort algorithm was successfully implemented in C++. The measured runtime confirms that Merge Sort consistently performs in $O(n \log n)$ time for different input sizes, making it an efficient sorting algorithm for large datasets.

