

E-way Set Associative Cache (Here: E = 2)

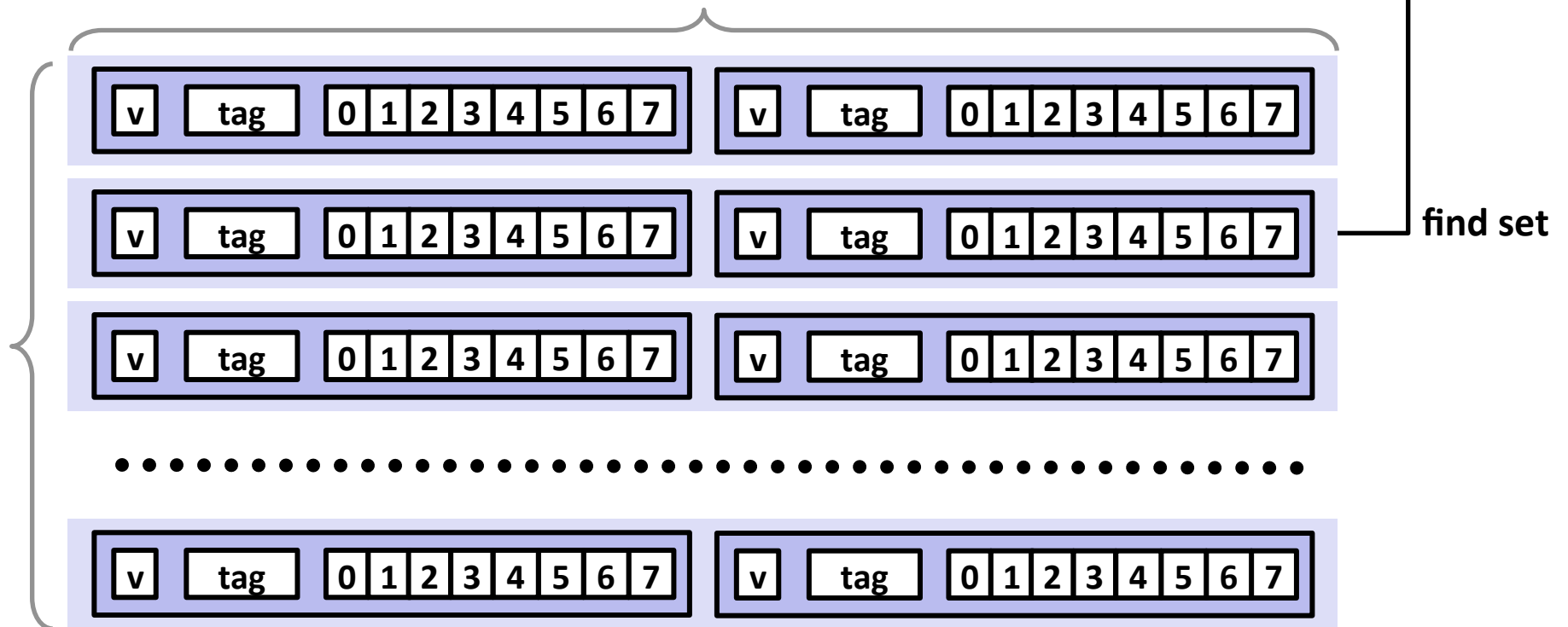
E = 2: Two lines per set

Assume: cache block size 8 bytes

Address of short int:

t bits	0...01	100
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2 lines per set

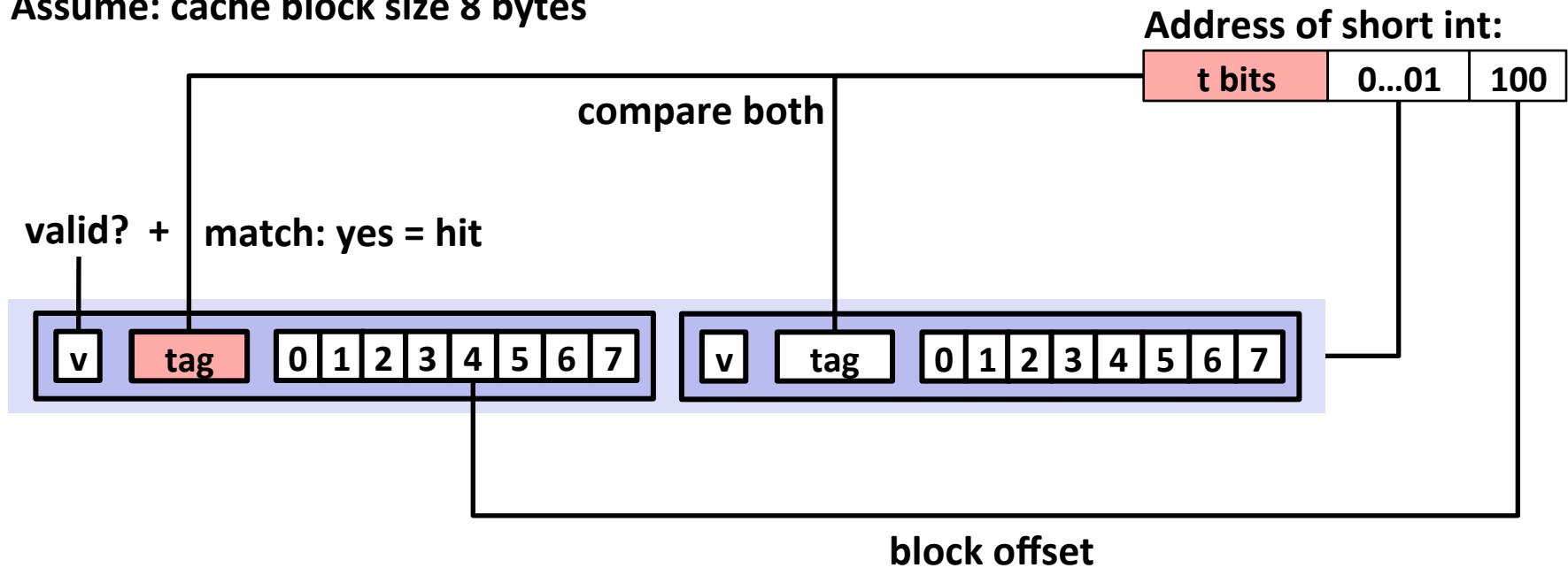


S sets

E-way Set Associative Cache (Here: E = 2)

E = 2: Two lines per set

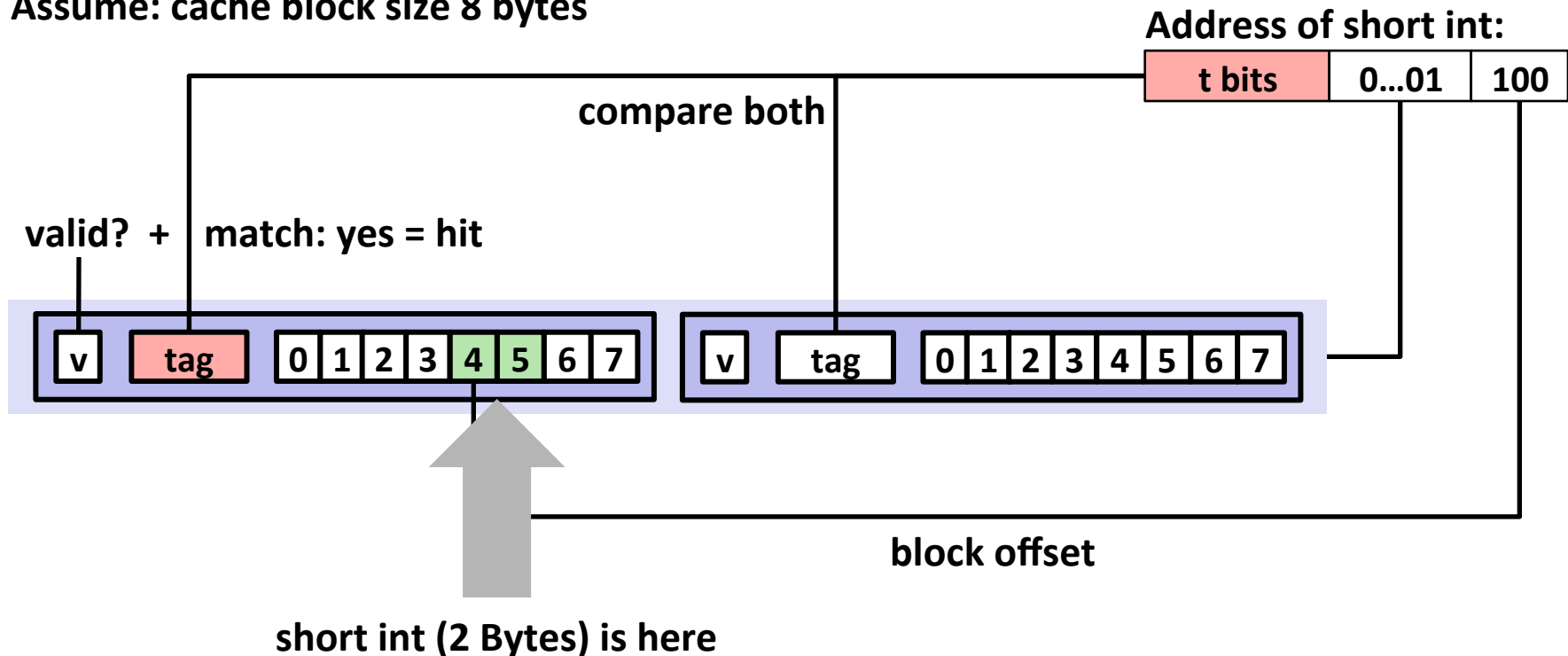
Assume: cache block size 8 bytes



E-way Set Associative Cache (Here: E = 2)

E = 2: Two lines per set

Assume: cache block size 8 bytes



No match:

- One line in set is selected for eviction and replacement
- Replacement policies: random, least recently used (LRU), ...

2-Way Set Associative Cache Simulation

t=2	s=1	b=1
xx	x	x

M=16 byte addresses, B=2 bytes/block,
S=2 sets, E=2 blocks/set

Address trace (reads, one byte per read):

0	[00 <u>0</u> 0] ₂ ,	miss
1	[00 <u>0</u> 1] ₂ ,	hit
7	[0 <u>1</u> 11] ₂ ,	miss
8	[10 <u>0</u> 0] ₂ ,	miss
0	[00 <u>0</u> 0] ₂	hit

	v	Tag	Block
Set 0	1	00	M[0-1]
	1	10	M[8-9]
Set 1	1	01	M[6-7]
	0		

What about writes?

■ Multiple copies of data exist:

- L1, L2, L3, Main Memory, Disk

■ What to do on a write-hit?

- **Write-through** (write immediately to memory)
- **Write-back** (defer write to memory until replacement of line)
 - Need a dirty bit (line different from memory or not)

■ What to do on a write-miss?

- **Write-allocate** (load into cache, update line in cache)
 - Good if more writes to the location follow
- **No-write-allocate** (writes straight to memory, does not load into cache)

■ Typical

- Write-through + No-write-allocate
- **Write-back + Write-allocate**

Why Index Using Middle Bits?

Direct mapped: One line per set
Assume: cache block size 8 bytes

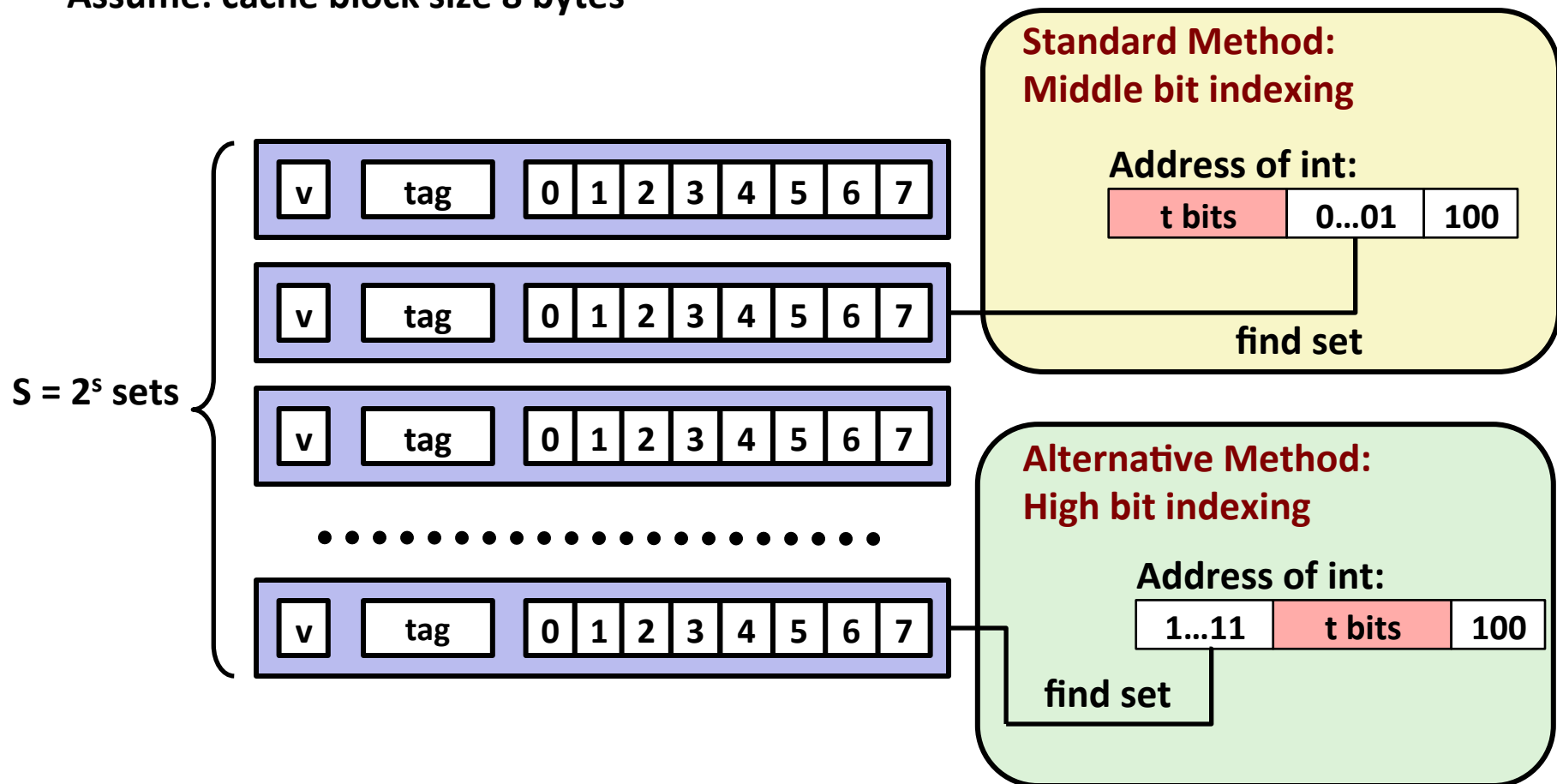
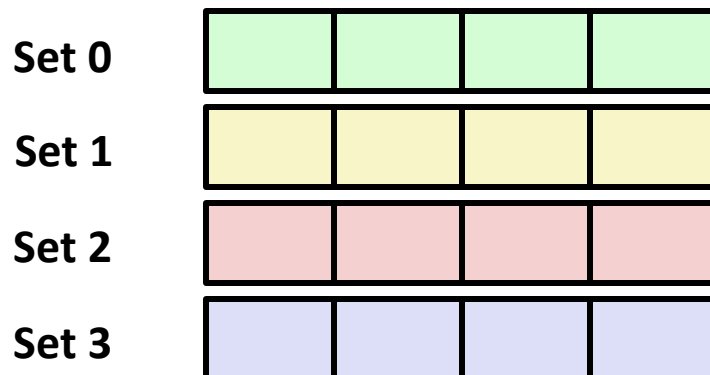


Illustration of Indexing Approaches

- **64-byte memory**
 - 6-bit addresses
- **16 byte, direct-mapped cache**
- **Block size = 4 (4 sets)**
- **2 bits tag, 2 bits index, 2 bits offset**



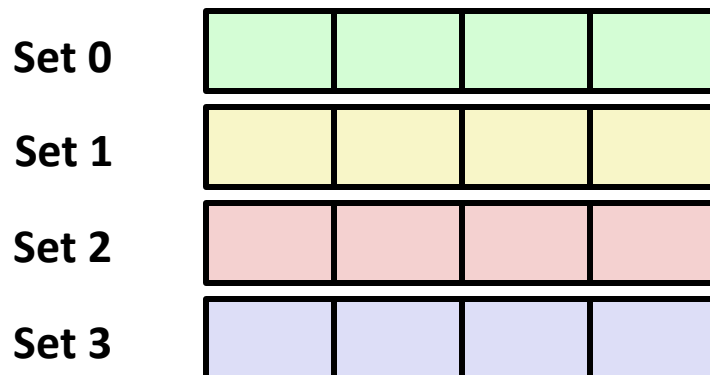
				0000xx
				0001xx
				0010xx
				0011xx
				0100xx
				0101xx
				0110xx
				0111xx
				1000xx
				1001xx
				1010xx
				1011xx
				1100xx
				1101xx
				1110xx
				1111xx

Middle Bit Indexing

■ Addresses of form **TTSSBB**

- **TT** Tag bits
- **SS** Set index bits
- **BB** Offset bits

■ Makes good use of spatial locality



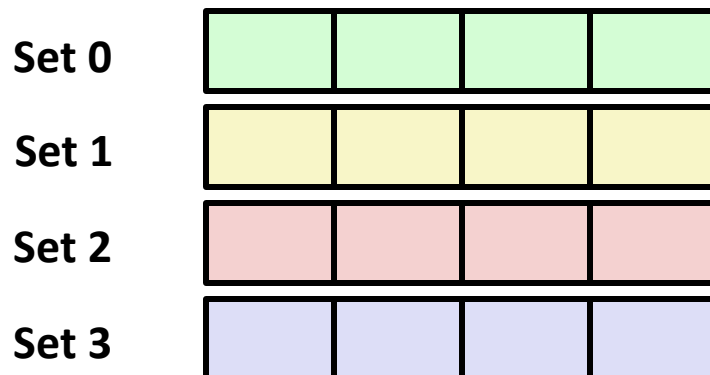
				0000xx
				0001xx
				0010xx
				0011xx
				0100xx
				0101xx
				0110xx
				0111xx
				1000xx
				1001xx
				1010xx
				1011xx
				1100xx
				1101xx
				1110xx
				1111xx





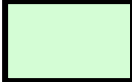
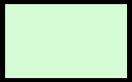
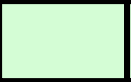
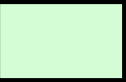
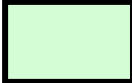
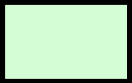
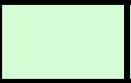
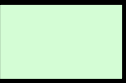
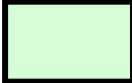
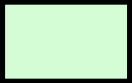
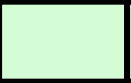
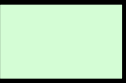
















































High Bit Indexing

■ Addresses of form **SS****TT****BB**

- **SS** Set index bits
- **TT** Tag bits
- **BB** Offset bits

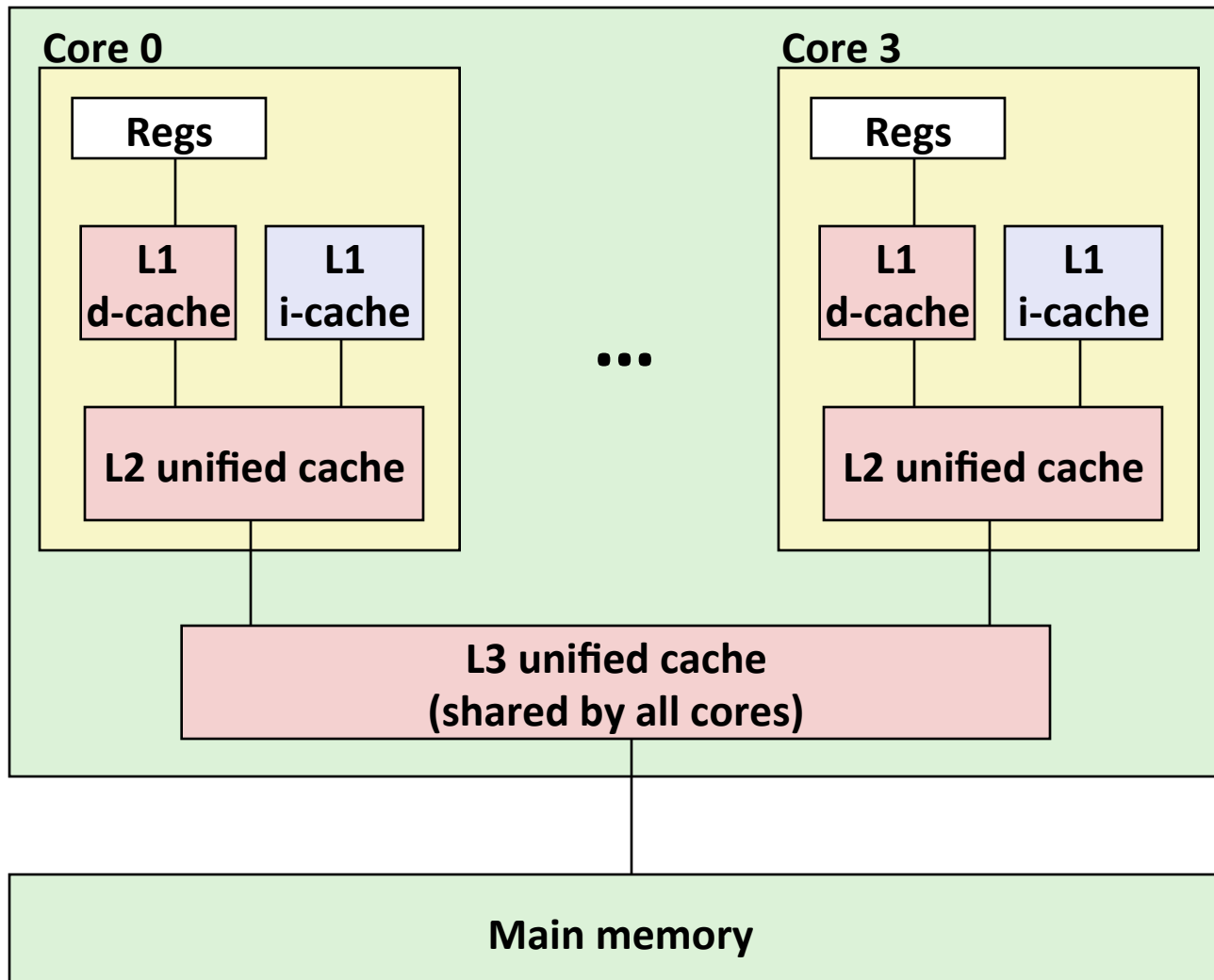
■ Program with high spatial locality would generate lots of conflicts



				0000xx
				0001xx
				0010xx
				0011xx
				0100xx
				0101xx
				0110xx
				0111xx
				1000xx
				1001xx
				1010xx
				1011xx
				1100xx
				1101xx
				1110xx
				1111xx

Intel Core i7 Cache Hierarchy

Processor package



L1 i-cache and d-cache:
32 KB, 8-way,
Access: 4 cycles

L2 unified cache:
256 KB, 8-way,
Access: 10 cycles

L3 unified cache:
8 MB, 16-way,
Access: 40-75 cycles

Block size: 64 bytes for
all caches.

Example: Core i7 L1 Data Cache

32 kB 8-way set associative

64 bytes/block

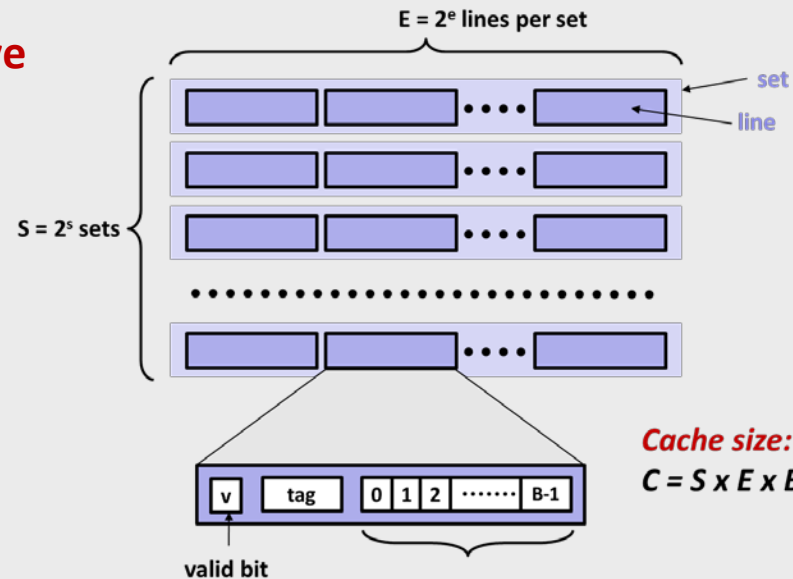
47 bit address range

B =

S = , s =

E = , e =

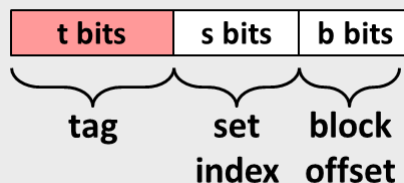
C =



Cache size:
 $C = S \times E \times B$ data bytes

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

Address of word:



Block offset: . bits

Set index: . bits

Tag: . bits

Stack Address:

0x00007f7262a1e010

Block offset:

0x??

Set index:

0x??

Tag:

0x??

Example: Core i7 L1 Data Cache

32 kB 8-way set associative

64 bytes/block

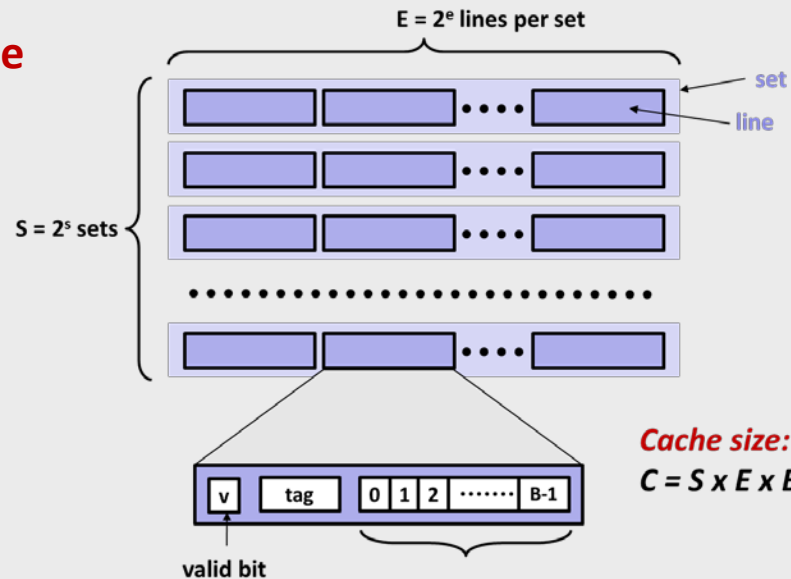
47 bit address range

$B = 64$

$S = 64, s = 6$

$E = 8, e = 3$

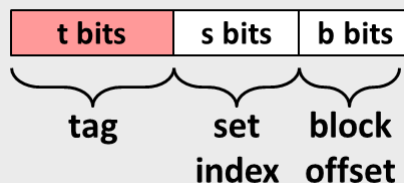
$C = 64 \times 64 \times 8 = 32,768$



Cache size:
 $C = S \times E \times B$ data bytes

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

Address of word:



Block offset: 6 bits

Set index: 6 bits

Tag: 35 bits

Stack Address:

0x00007f7262a1e010

0000 0001 0000

Block offset: **0x10**

Set index: **0x0**

Tag: **0x7f7262a1e**

Cache Performance Metrics

■ Miss Rate

- Fraction of memory references not found in cache (misses / accesses)
= $1 - \text{hit rate}$
- Typical numbers (in percentages):
 - 3-10% for L1
 - can be quite small (e.g., $< 1\%$) for L2, depending on size, etc.

■ Hit Time

- Time to deliver a line in the cache to the processor
 - includes time to determine whether the line is in the cache
- Typical numbers:
 - 4 clock cycle for L1
 - 10 clock cycles for L2

■ Miss Penalty

- Additional time required because of a miss
 - typically 50-200 cycles for main memory (Trend: increasing!)

Let's think about those numbers

- **Huge difference between a hit and a miss**
 - Could be 100x, if just L1 and main memory

- **Would you believe 99% hits is twice as good as 97%?**
 - Consider:
 - cache hit time of 1 cycle
 - miss penalty of 100 cycles

 - Average access time:
 - 97% hits: $1 \text{ cycle} + 0.03 \times 100 \text{ cycles} = 4 \text{ cycles}$
 - 99% hits: $1 \text{ cycle} + 0.01 \times 100 \text{ cycles} = 2 \text{ cycles}$

- **This is why “miss rate” is used instead of “hit rate”**

Writing Cache Friendly Code

- **Make the common case go fast**
 - Focus on the inner loops of the core functions
- **Minimize the misses in the inner loops**
 - Repeated references to variables are good (**temporal locality**)
 - Stride-1 reference patterns are good (**spatial locality**)

Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories