

## Assignment

### Probability Distributions

1. Simultaneously 10 coins were tossed, the probability of getting head for each coin is 0.6. What is the probability of getting 4 heads?
2. Three employees are randomly selected. The probability a single employee is between 180 and 185 cm is 0.1157.
  - a) What is the probability that all three are between 180 and 185 cm height?
  - b) What is the probability that none are between 180 and 185 cm?
3. Let's do a "shock" study and select 4 students. Let's name them as
  - a) Carol
  - b) Zack
  - c) Sarah
  - d) James
  - a. What exactly be the chance one of them will be success? Assume that 35% of the students a success.
  - b. Verify the situation where Carol is the only one to refuse to give the most severe shock has probability  $(0.3) * (0.65)^3$
4. On observing 59 Passengers or fewer at station who are constantly using mobile in a sample of 400. If the true portion of passengers on using mobile is  $p = 0.20$ . Use the normal approximation to estimate the probability of passengers using mobile 59 or fewer?
5. A survey indicates that for each trip Zack goes on for shopping in mall and spends an average  $\mu=45$  minutes with a standard deviation of  $\sigma=12$  minutes. The length of time spent in the mall is normally distributed and is represented by the variable  $x$ .

If 200 shoppers enter the mall, how many shoppers would you expect to be in the mall for each interval of time listed below?

  - a) Between 24 and 54 minutes
  - b) More than 39 minutes

6. A truck from Gati has to carry load from Mumbai to Chennai. The amount of diesel consumed is normally distributed random variable  $X$ , with  $\mu = 5.7$ ,  $\sigma = 0.5$ . Freight management wants to find the amount of fuel to fill so that there will be 0.99 probability that truck reaches Chennai on time.
7. Consider 80% of all business start-ups in the IT industry in the city report that they generate a profit in their first year. If a sample of 10 new IT business start-ups are selected, find the probability that exactly seven will generate a profit in their first year.
8. A roulette wheel consisting of 38 numbers 1 through 36, 0, and double 0. If Sam always bets that the outcome will be one of the numbers 1 through 12, what is the probability that Sam will lose his first 5 bets?
9. Ram got fever and has gone for diagnostic centre for test. A diagnostic test has a 0.95 probability of giving a positive result when tested on person affected with typhoid and 0.10 probability of giving as (false) positive when applied to non-typhoid.

It is estimated that 0.5% of the population are suffering from typhoid. If a person is selected from the population and suppose a test is conducted on him where we have no relevant information relating to fever.

**Calculate the following probabilities:**

- A. that the test result will be positive;
  - B. that, given a positive result, the person is suffering from typhoid;
  - C. that, given a negative result, the person is a non-typhoid;
  - D. that the person will be misclassified.
10. Brooklyn High School's A level is normally distributed. The total data which is 95% is between the age 15.6 and 18.4. Can you find the mean and standard deviation?
  11. For a job interview a test has been taken and the final results have a mean of 70 and a standard deviation of 10. If normally distributed what percent of the job seekers.
    - a) Test score higher than 80?
    - b) Should pass the test (Test score  $\geq 60$ )?
    - c) Should fail the test (Test score  $< 60$ )

12. The longevity of musical instruments used by musicians has a normal distribution with mean of 12 months and standard deviation of 2 months. Find the probability that an instrument used by musicians will last.