

Air cargo problem. Heuristic report

Artificial Intelligence Nanodegree

Summary

1. Truly informed planning searches algorithms (*astar_search with h_ignore_preconditions* and *astar_search with h_pg_levelsum*)¹ provide optimal solution in all considered problems and use for it less number of node expansions
2. The best results in term of optimality and time demonstrate *astar_search with h_ignore_preconditions* algorithm
3. However, *astar_search with h_pg_levelsum* algorithm also provides optimal solution and is best in term of number of node expansions. Unfortunately, the computational time of heuristic is big and as a result the total computational time is considerable.
4. Between uninformed algorithms, **optimal solution** in reasonable time **can provide breadth_first_search** (best in this class in term of optimality, time and new nodes quantity) and *uniform_cost_search algorithm/Astar_with_h_1* (optimal, but less efficient than BFS) .
5. The algorithms which are not provided optimal solution seem to be impractical due to huge gap between proposed and optimal solution
6. We should note that the most reasonable cause of fail of some algorithms based on h_1 heuristic it is heuristic, not the algorithms itself.² It would be perspective to test these algorithms with more meaning heuristics.

Problem 1. Result analysis

1. The first problem is very small and simple, so we can test each algorithm and define it applicability for the problem space before to test it on problems that are more complex.
2. The results of tests are in the table below:

| # | Algoritm Name | Time | Length | Expansion | Goal Test | New Nodes |
|----|---|------|--------|-----------|-----------|-----------|
| 1 | breadth_first_search | 0.15 | 6 | 43 | 56 | 180 |
| 2 | breadth_first_tree_search | 4.8 | 6 | 1458 | 1459 | 5960 |
| 3 | depth_first_graph_search | 0.05 | 12 | 12 | 13 | 48 |
| 4 | depth_limited_search | 0.37 | 50 | 101 | 271 | 414 |
| 5 | uniform_cost_search | 0.2 | 6 | 55 | 57 | 224 |
| 6 | recursive_best_first_search with h_1 | 14.9 | 6 | 4229 | 4230 | 17029 |
| 7 | greedy_best_first_graph_search with h_1 | 0.02 | 6 | 7 | 9 | 28 |
| 8 | astar_search with h_1 | 0.18 | 6 | 55 | 57 | 224 |
| | astar_search with | | | | | |
| 9 | h_ignore_preconditions | 0.12 | 6 | 31 | 33 | 126 |
| 10 | astar_search with h_pg_levelsum | 2.8 | 6 | 11 | 13 | 50 |

Table 1. Problem 1 results

¹ We cannot consider *astar_search with h_1* as a truly informed algorithm because h_1 heuristic doesn't provide any useful information. In fact the results of this algorithm in term of optimality and nodes are equal to *uniform_cost_search*. The time is a little bit slower due to additional computations resources to add constant. Due to this we will not consider this algorithm in our analysis.

² For example, RBFS is described by Peter Norvig as "RBFS (recursive best-first search) and SMA* (simplified memory-bounded A*) are robust, optimal search algorithms that use limited amounts of memory; given enough time, they can solve problems that A* cannot solve because it runs out of memory." See "Artificial intelligence a modern approach" 3rd edition, section 3.7 "Summary" for more information

3. From these results we can made the following conclusions:
 - a. Breadth_first_tree_search is impractical for usage. Usage of tree search instead of grid search means unnecessary repeating of already done steps³ Due to this it is impossible to use it for problems that are more complex⁴.
 - b. recursive_best_first_search with h_1 cannot run efficiently without reasonable heuristic. As h_1 is not reasonable heuristic, number of nodes expanded is huge and it failed to search more complex problem
 - c. depth_limited_search provides unreasonable solution (50 moves instead of possible 6 is not relevant solution) and number of expanded nodes is big.

Problem 2 and 3. Result analysis

1. To understand the efficiency of algorithms on more complex problems it is useful to analyze problem 2 and problem 3 together. Below are the results of computations⁵

| # | Algorithm Name | Time | Length | Expansion | Goal Test | New Nodes |
|----|--|---|--------|-----------|-----------|-----------|
| 1 | breadth_first_search | 66.7 | 9 | 3343 | 4609 | 30509 |
| 2 | breadth_first_tree_search | cannot be computed within reasonable time | | | | |
| 3 | depth_first_graph_search | 13.7 | 575 | 582 | 583 | 5211 |
| 4 | depth_limited_search | cannot be computed within reasonable time | | | | |
| 5 | uniform_cost_search | 147.9 | 9 | 4852 | 4854 | 44030 |
| 6 | recursive_best_first_search with h_1 | cannot be computed within reasonable time | | | | |
| 7 | greedy_best_first_graph_search with h_1 | 31.6 | 15 | 990 | 992 | 8910 |
| 8 | astar_search with h_1 | 159.8 | 9 | 4852 | 4854 | 44030 |
| 9 | astar_search with h_ignore_preconditions | 39.5 | 9 | 1166 | 1168 | 10651 |
| 10 | astar_search with h_pg_levelsum | 265 | 9 | 86 | 88 | 841 |

Table 2. Problem 2 results

| # | Algorithm Name | Time | Length | Expansion | Goal Test | New Nodes |
|----|--|---|--------|-----------|-----------|-----------|
| 1 | breadth_first_search | 461.5 | 12 | 14663 | 18098 | 129631 |
| 2 | breadth_first_tree_search | cannot be computed within reasonable time | | | | |
| 3 | depth_first_graph_search | 17.3 | 596 | 627 | 628 | 5176 |
| 4 | depth_limited_search | cannot be computed within reasonable time | | | | |
| 5 | uniform_cost_search | 1009.4 | 12 | 18235 | 18237 | 159716 |
| 6 | recursive_best_first_search with h_1 | cannot be computed within reasonable time | | | | |
| 7 | greedy_best_first_graph_search with h_1 | 294.8 | 22 | 5615 | 5617 | 49438 |
| 8 | astar_search with h_1 | 1143.6 | 12 | 18235 | 18237 | 159716 |
| 9 | astar_search with h_ignore_preconditions | 205 | 12 | 3816 | 3818 | 34216 |
| 10 | astar_search with h_pg_levelsum | 1724.6 | 12 | 404 | 406 | 3718 |

Table 3. Problem 3 results

2. As we can see, when the problem increase, non-optimal algorithms became impractical (for example, greedy_best_first_graph_search with h_1 became two time less optimal during problem 3 and consequently it is non reasonable to use it for practical problems)

³ For more information see "Artificial intelligence a modern approach" 3rd edition, section 3.3 "Searching for solution"

⁴ To prove this state for this algorithms and for other, I try to run search for problem 2 and 3, but it failed to compute it in reasonable time

⁵ If the algorithm name font is green, it is best algorithm to solve the problem. If is red – unacceptable. If is black – not best, but can be used for the problem

3. Though, breadth_first_search algorithm is acceptable for problem 3, it is obvious if the problem became more complex it is failed to solve within reasonable time due to state complexity (and uniform_cost_search already fail to pass 10 minutes limit)
4. Finally, as we can see in the results above, *ignore_preconditions* heuristic can reduce path to solve as much as 3-5 times, comparing with uninformed search, and provide reasonable time for computation. As a result **astar_search with h_ignore_preconditions** is the winner in our test
5. h_pg_levelsum heuristic is the best in term of path search (it is 10 time less comparing with *ignore_preconditions* heuristic). However it is hard to compute and as a result, total calculation time of algorithm with this heuristic is very slow and it is became unpractical to use it on complex problem (problem 3 and more complex problems)

Optimal solution review

1. In general case the following algorithms let find the optimal sequence:
 - a. breadth_first_search
 - b. uniform_cost_search/ astar_search with h_1
 - c. astar_search with h_ignore_preconditions
 - d. astar_search with h_pg_levelsum
2. However, in the simplest problem (problem 1), optimal solution was find by greedy best first search (not the case for more complex problems)
3. In tables below are optimal sequences which were identified for each problem:

| Problem | Optimal sequence |
|------------------|---|
| Problem 1 | Load(C1, P1, SFO) Load(C2, P2, JFK) Fly(P1, SFO, JFK) Fly(P2, JFK, SFO) Unload(C1, P1, JFK) Unload(C2, P2, SFO) |
| Problem 2 | Load(C1, P1, SFO) Load(C2, P2, JFK) Load(C3, P3, ATL) Fly(P1, SFO, JFK) Fly(P2, JFK, SFO) Fly(P3, ATL, SFO) Unload(C1, P1, JFK) Unload(C2, P2, SFO) Unload(C3, P3, SFO) |

| Problem | Optimal sequence |
|------------------|--|
| Problem 3 | Load(C1, P1, SFO) Load(C2, P2, JFK) Fly(P1, SFO, ATL) Fly(P2, JFK, ORD) Load(C3, P1, ATL) Load(C4, P2, ORD) Fly(P1, ATL, JFK) Fly(P2, ORD, SFO) Unload(C1, P1, JFK) Unload(C3, P1, JFK) Unload(C2, P2, SFO) Unload(C4, P2, SFO) |