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1) Explain one tailed and two tailed test and type 1 and type 2 errors?

a) One Tailed Test: A one-tailed test is a statistical test in which the critical area of a distribution is one-sided so that it is either greater than or less than a certain value, but not both. If the sample being tested falls into the one-sided critical area, the alternative hypothesis will be accepted instead of the null hypothesis. A one-tailed test is also known as a directional hypothesis or directional test. Key Features: • A one-tailed test is a statistical hypothesis test set up to show that the sample mean would be higher or lower than the population mean, but not both. • When using a one-tailed test, the analyst is testing for the possibility of the relationship in one direction of interest, and

completely disregarding the possibility of a relationship in another direction. • Before running a one-tailed test, the analyst must set up a null hypothesis and an alternative hypothesis and establish a probability value (p-value).

Two-Tailed Test:

In statistics, a two-tailed test is a method in which the critical area of a distribution is two-sided and tests whether a sample is greater than or less than a certain range of values. It is used in null hypothesis testing and testing for statistical significance. If the sample being tested falls into either of the critical areas, the alternative hypothesis is accepted instead of the null hypothesis.

Key Features: • In statistics, a two-tailed test is a method in which the critical area of a distribution is two-sided and tests whether a sample is greater or less than a range of values.

- It is used in null-hypothesis testing and testing for statistical significance.
- If the sample being tested falls into either of the critical areas, the alternative hypothesis is accepted instead of the

null hypothesis.

- By convention two-tailed tests are used to determine significance at the 5% level, meaning each side of the distribution is cut at 2.5%.

Type 1 & Type 2 error:

A Type I error means rejecting the null hypothesis when it's actually true. It means concluding that results are statistically significant when, in reality, they came about purely by chance or because of unrelated factors. The risk of committing this error is the significance level (α or α) you choose. That's a value that you set at the beginning of your study to assess the statistical probability of obtaining your results (p value). A Type II error means not rejecting the null hypothesis when it's actually false. This is not quite the same as "accepting" the null hypothesis, because hypothesis testing can only tell you whether to reject the null hypothesis.

Instead, a Type II error means failing to conclude there was an effect when there actually was. In reality, your study may not have

had enough statistical power to detect an effect of a certain size.

Null Hypothesis is True false

Rejected

Type I error	correct decision
False Positive	true negative
Probability = α	probability = $1 - \beta$

Not Rejected

Correct decision	Type II error
True negative	false negative
Probability = $1 - \alpha$	probability = $1 - \beta$

The significance level is usually set at 0.05 or 5%. This means that your results only have a 5% chance of occurring, or less, if the null hypothesis is actually true.

To reduce the Type I error probability, you can simply set a lower significance level.

2) Samples of 100 voters are asked which of four candidates they would vote for in an election. The number supporting each candidate is given below:

Higgins Seardon White Charlton

41 19 24 16

Do the data suggest that all candidates are equally popular? [Chi-square = 14.96, With 3 d.f.: p < 0.05]

Sol:

Null Hypothesis: H_0 = There is no preference for any of the candidate.

Therefore, we would expect roughly equal no of votes = $100/4 = 25$ per candidate

Alternative Hypothesis: H_1

H_1 not equal to H_0

Calculations:

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

O	E	O-E	$(O-E)^2$	$(O-E)^2/E$
41	25	16	256	10.24
19	25	-6	36	1.44
24	25	-1	1	0.04
16	25	-9	81	3.24
$\sum (O-E)^2$				$= 14.96$
				E

Critical value:

The Critical Value of Chi-square at 0.05 level of significance with 3

Degrees of freedom is 7.82.

Therefore value = 7.82

Calculated value = 14.52 //

Conclusion:

Calculated value > theoretical value

$$14.52 > 7.82$$

Therefore Null Hypothesis is accepted.

That voters are not preferring any of the candidate from four.

3) The random samples are drawn from two normal populations and there are

$$X_1: 65\ 67\ 74\ 76\ 84\ 86\ 88\ 94\ 95$$

$$X_2: 65\ 66\ 74\ 78\ 84\ 85\ 89\ 94\ 96\ 95\ 98$$

test whether two samples have the same variance of 5% level of significance ($f=3.11$ at 5) ($V_1=8$ & $V_2=10$)

Let us take the hypothesis is that two populations have the same variant

applying F -Test.

$$F = \frac{S_1^2}{S_2^2}$$

$$X_1 \quad X_1 = \mu - \mu_1 \quad X_{12} \quad X_2 \quad X_2 = \bar{X}_2 - \bar{X}_2$$

sq

65	65-81=-14	256	65	65-84=-19	361
67	67-81=-7	196	66	66-84=-18	324
74	74-81=-7	49	74	74-84=-10	100
76	76-81=-5	25	78	78-84=-6	36
84	84-81=3	9	84	84-84=0	0
86	86-81=5	25	85	85-84=1	1
88	88-81=7	49	89	89-84=5	25
			94	94-84=10	100
94	94-81=13	169	96	96-84=12	144
			95	95-84=12	144
95	95-81=14	196	98	95-84=14	196

$$E_{\chi^2} = 729 \quad E_{\chi^2} = 0 \quad E_{\chi^2/2} = 974 \quad E_{\chi^2/2} = 924 \quad E_{\chi^2/2} = 0 \quad E_{\chi^2/2/2} = 1309$$

$$X_1 = E_{\chi^2}/n_1 = 729/9 = 81$$

$$X_2 = E_{\chi^2}/n_2 = 924/11 = 84$$

$$\chi^2/2 = E_{\chi^2/2}/n_1 - 1 = 974/9 - 1 = 121.75$$

$$\chi^2/2/2 = E_{\chi^2/2/2}/n_2 - 1 = 1309/11 - 1 = 130.9$$

$$T = 121.75/130.9$$

$$T = 0.930$$

For $V_1 = 81$ $V_2 = 10$ $T = 3.11$ at 5% level of significance

Calculated value is = 0.93

Tabulated value is = 3.11

Calculated value < Tabulated