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Program Structures & Algorithms

Fall 2021

Assignment No. 2

- **Task:**

  Part 1) Implement three methods of class called Timer. Timer is invoked from a class called Benchmark_Timer which implements the Benchmark interface.

  Part 2) Implement InsertionSort (in the InsertionSort class) by simply looking up the insertion code used by Arrays.sort.

  Part 3) Implement a main program (or you could do it via your own unit tests) to actually run the following benchmarks: measure the running times of this sort, using four different initial array ordering situations: random, ordered, partially-ordered and reverse-ordered.

- **Relationship Conclusion:**

  The Order of Growth for Randomly Ordered Array of Size N is $\approx N^{1.36}$

  The Order of Growth for Ordered Array of Size N is $\approx N^{0.80}$

The Order of Growth for Reverse Ordered Array of Size N is ≈ $N^{1.53}$

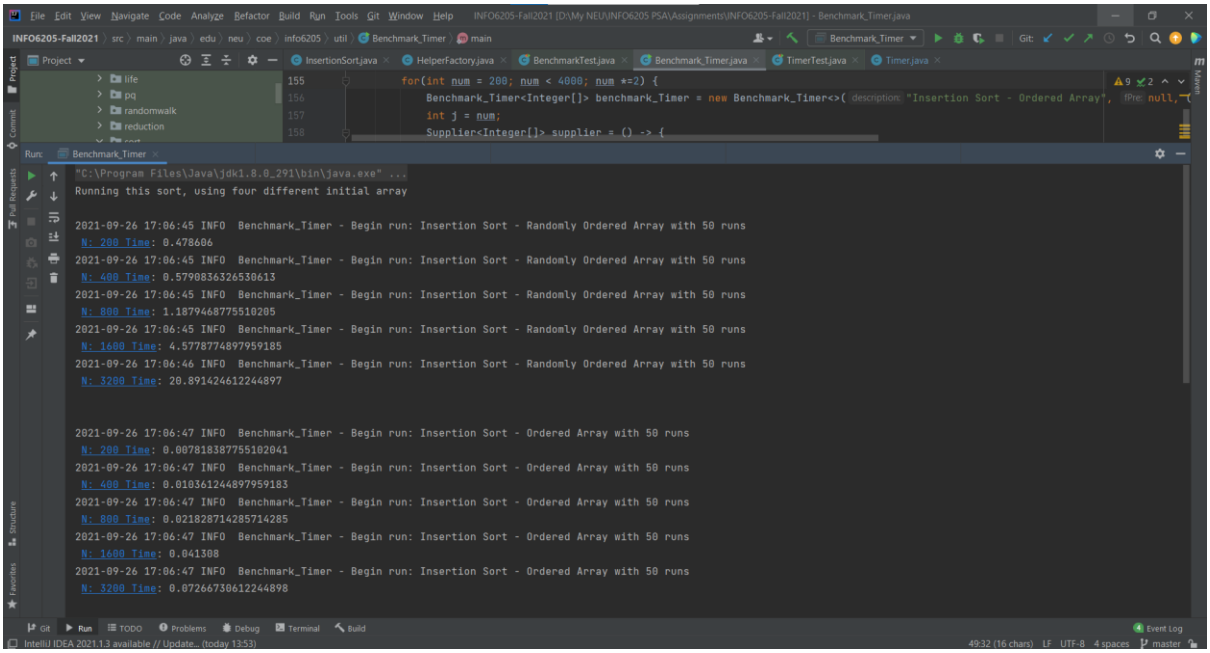
The Order of Growth for Partially Ordered Array of Size N is ≈ $N^{1.09}$

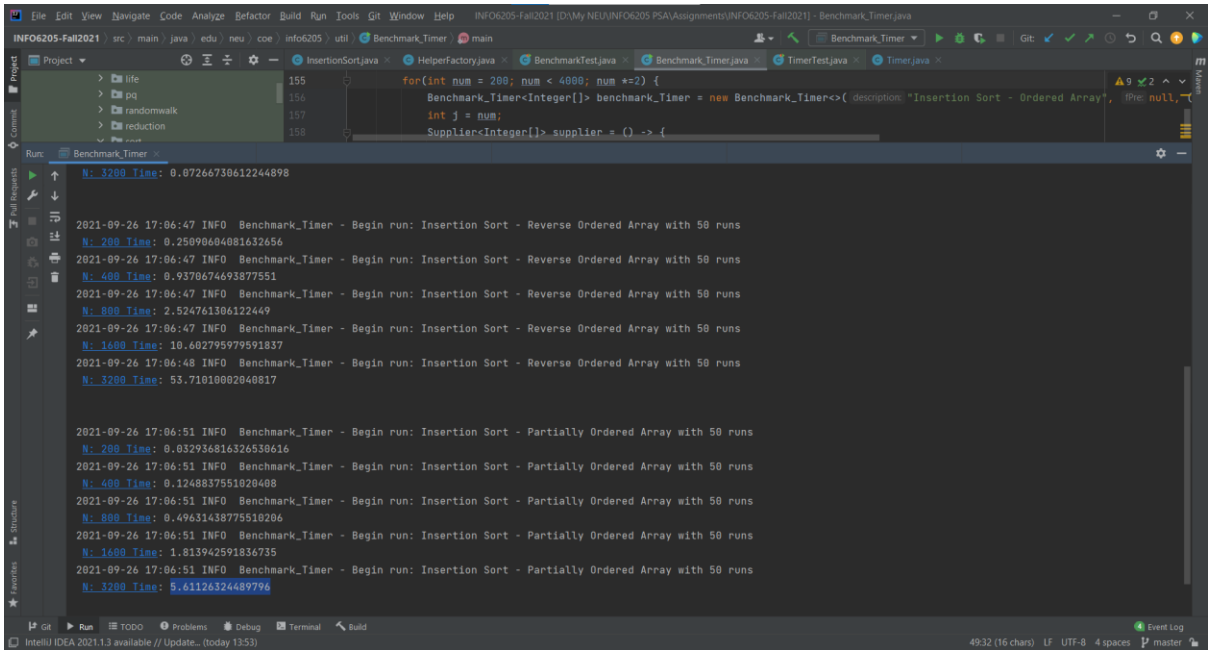
The Order of growth, based on running time of insertion sort is:

Ordered < Partially Ordered < Randomly Ordered < Reverse Ordered

- **Evidence to support the conclusion:**

1. **Output (Snapshot of Code output in the terminal)**

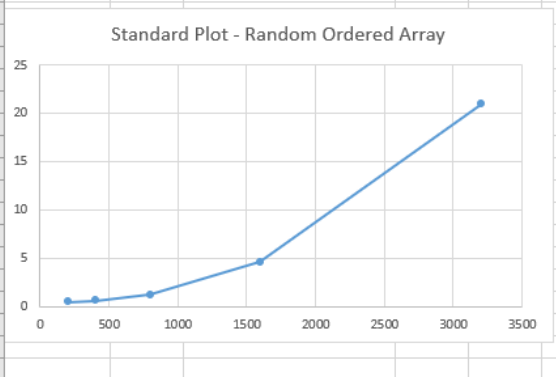


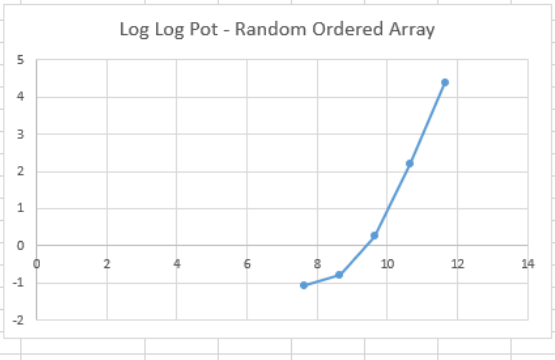


2. Graphical Representation

Random Ordered Array:

1	Running this sort, using four different initial array					
2						
3	Insertion Sort - Random Orderd Array					
4						
5	Length of Arra	Time	lg(Len(Array))	lg(Time)	Log-Ratio	Slop
6	200	0.47861	7.64385619	-1.0631	-7.1902	
7	400	0.57908	8.64385619	-0.7882	-10.967	0.27493
8	800	1.18795	9.64385619	0.24847	38.8129	1.03663
9	1600	4.57788	10.64385619	2.19468	4.84985	1.94621
10	3200	20.8914	11.64385619	4.38484	2.65548	2.19016
11					Avg Slope	1.36198
12						
13						
14						





Initial input size is 200 and increased upto 3200. Calculated the running time of the soring algorithm Random Orderly.

Using Doubling Hypothesis:

For Function $T(N) = aN\hat{}b$

N = Input Size

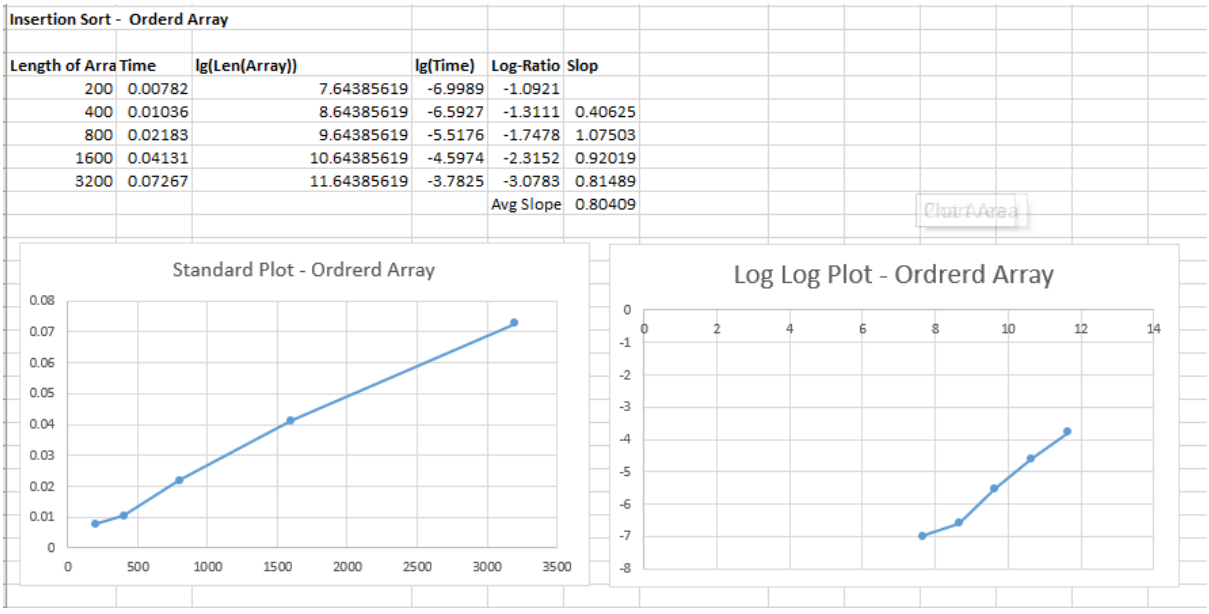
a = Constant

b = slope of the log-log graph

The average slope for Randomly Ordered Array is: 1.36

The Equation of such a line is:

$$\text{llg}\big(T(N)\big) = \ aN^{1.36}$$



Insertion Sort - Orderd Array					
Length of Arra	Time	lg(Len(Array))	lg(Time)	Log-Ratio	Slop
200	0.00782	7.64385619	-6.9989	-1.0921	
400	0.01036	8.64385619	-6.5927	-1.3111	0.40625
800	0.02183	9.64385619	-5.5176	-1.7478	1.07503
1600	0.04131	10.64385619	-4.5974	-2.3152	0.92019
3200	0.07267	11.64385619	-3.7825	-3.0783	0.81489
				Avg Slope	0.80409

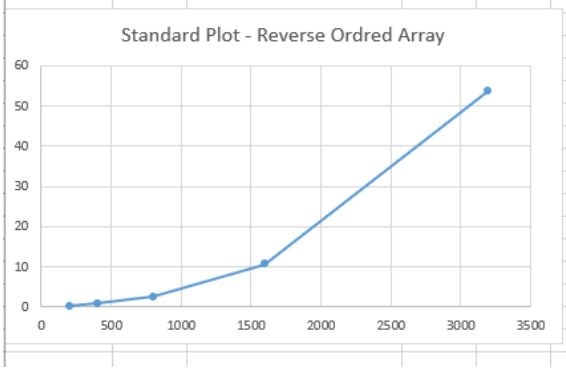
The average slope for Ordered Array is: 0.80

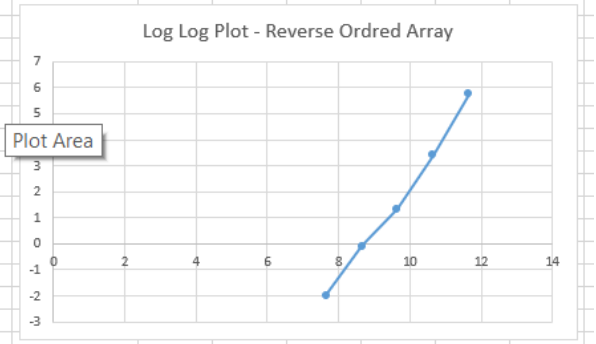
The Equation of such a line is:

$$\text{llg}\big(T(N)\big) = \ aN^{0.80}$$

Insertion Sort - Reverse Orderd Array

Length of Arra	Time	lg(Len(Array))	lg(Time)	Log-Ratio	Slop
200	0.25091	7.64385619	-1.9948	-3.8319	0
400	0.93707	8.64385619	-0.0938	-92.176	1.90101
800	2.52476	9.64385619	1.33615	7.21766	1.42992
1600	10.6028	10.64385619	3.40637	3.12469	2.07023
3200	53.7101	11.64385619	5.74712	2.02603	2.34075
				Avg Slope	1.54838





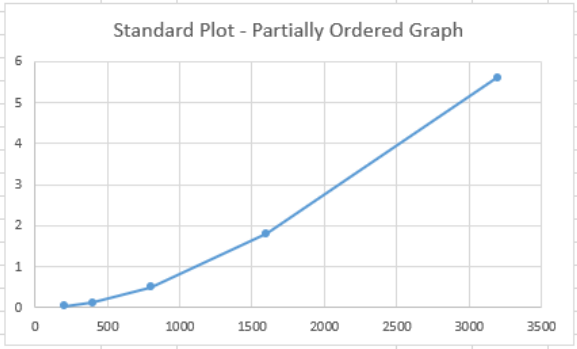
The average slope for Reverse Ordered Array is: 1.54

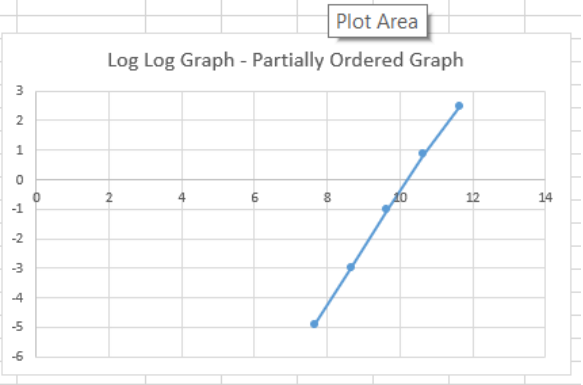
The Equation of such a line is:

$$\text{lg}\big(T(N)\big) = \ aN^{1.54}$$

Insertion Sort - Partially Orderd Array

Length of Arra	Time	lg(Len(Array))	lg(Time)	Log-Ratio	Slop
200	0.03294	7.64385619	-4.9242	-1.5523	0
400	0.12488	8.64385619	-3.0013	-2.88	0
800	0.49631	9.64385619	-1.0107	-9.542	1.99067
1600	1.81394	10.64385619	0.85913	12.3891	1.8698
3200	5.61126	11.64385619	2.48833	4.67939	1.6292
				Avg Slope	1.09793





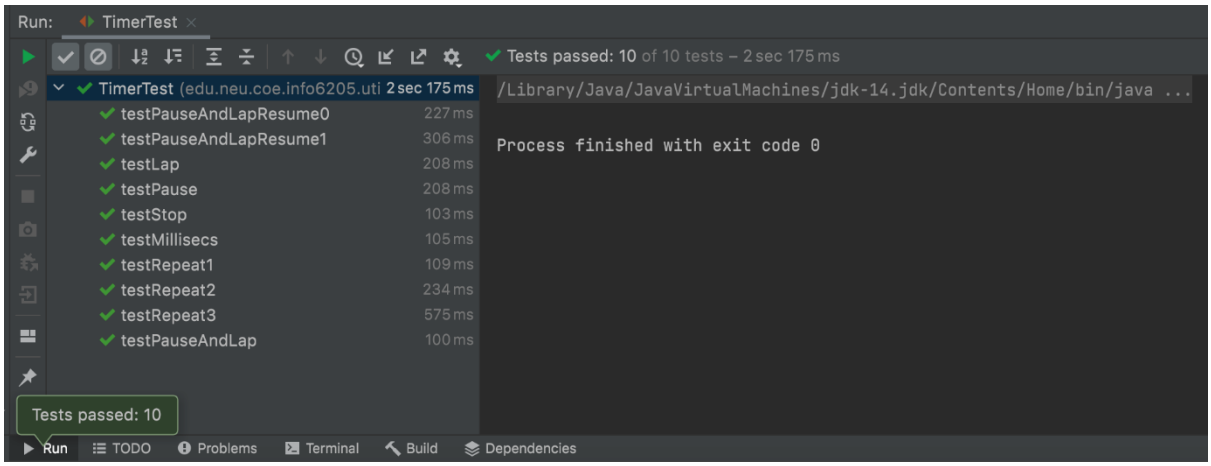
The average slope for Partially Ordered Array is: 1.09

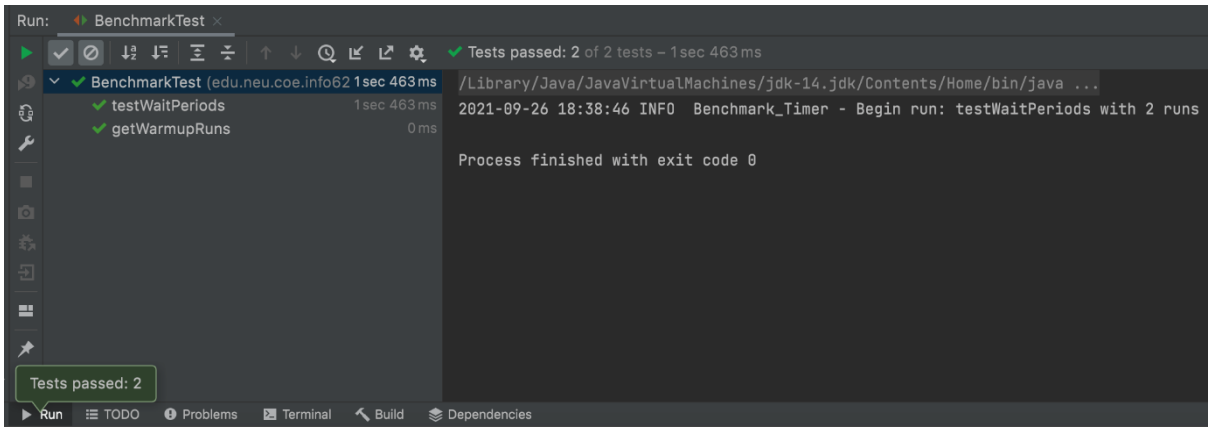
The Equation of such a line is:

$$\text{lg}\big(T(N)\big) = \ aN^{1.09}$$

- **Unit tests result:**

Part 1 : Timer Test





Part 2: Insertion Sort