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Program Structures & Algorithms

Fall 2021

Assignment No. 3

- ◉ **Task:** Implement height-weighted Quick Union with Path Compression.

Step 1 a): Fill in the sections // TO BE IMPLEMENTED

b): Check all the unit tests.

Step 2: Using your implementation of UF_HWQUPC, develop a UF ("union-find") client that takes an integer value n from the command line to determine the number of "sites."

Step 3: Determine the relationship between the number of objects (n) and the number of pairs (m) generated

- ◉ **Relationship Conclusion:**

$$\text{The number of pairs}(m) \approx \frac{1}{2} N \ln(N)$$

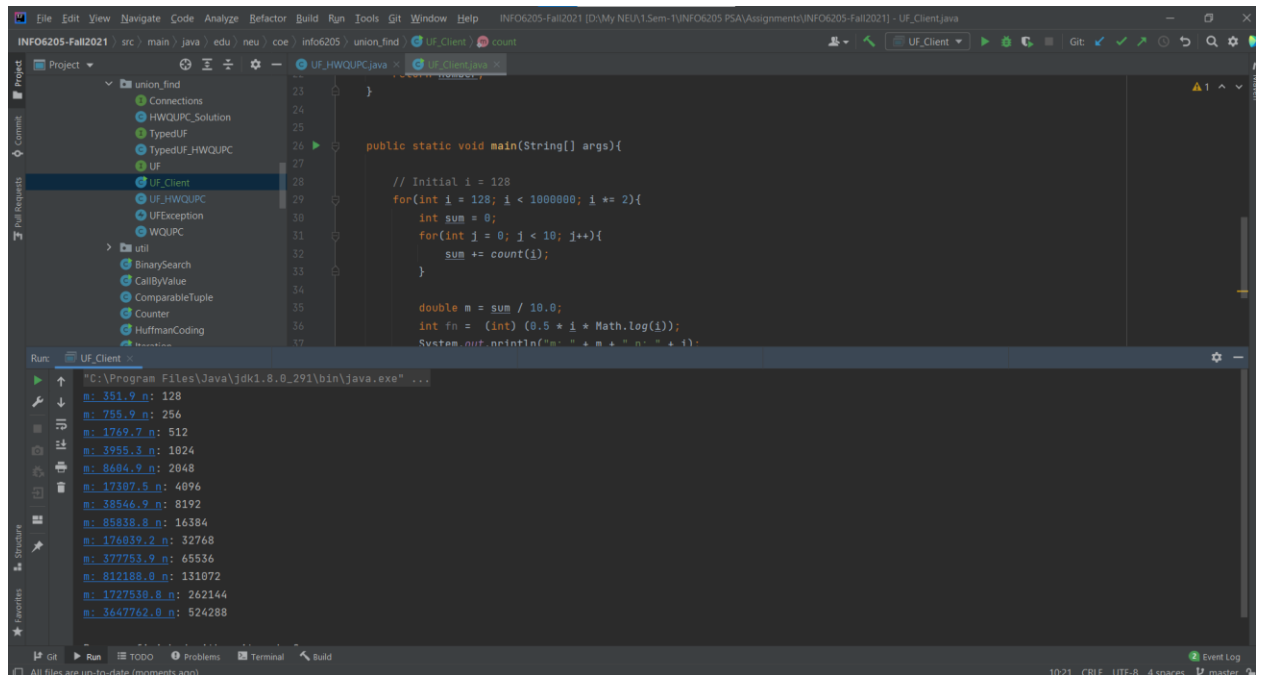
The relationship between the number of objects(n) and the number of pairs(m) generated is the above relation.

I pasted the table and line graph to justify the relationship.

We can observe that the relation between N vs M graph is very similar to N vs NlogN graph even for large values.

◉ Evidence to support the conclusion:

Output (Snapshot of Code output in the terminal):



The screenshot shows an IDE with a project named 'INFO6205-Fall2021'. The code editor displays the 'UF_Client.java' file, which contains a 'main' method. The code calculates the sum of values for 'i' from 128 to 1000000, where each value is calculated as $0.5 * i + \text{Math.log}(i)$. The terminal output shows the results of these calculations for various values of 'i'.

```
public static void main(String[] args){  
    // Initial i = 128  
    for(int i = 128; i < 1000000; i += 2){  
        int sum = 0;  
        for(int j = 0; j < 10; j++){  
            sum += count(i);  
        }  
  
        double m = sum / 10.0;  
        int fn = (int) (0.5 * i + Math.log(i));  
        System.out.println("m: " + m + " n: " + i);  
    }  
}
```

Run: UF_Client

```
m: 351.9 n: 128  
m: 755.9 n: 256  
m: 1769.7 n: 512  
m: 3955.3 n: 1024  
m: 8604.9 n: 2048  
m: 17307.5 n: 4096  
m: 38546.9 n: 8192  
m: 85838.8 n: 16384  
m: 176039.2 n: 32768  
m: 364776.2 n: 524288
```

Console Output:

m: 351.9 n: 128

m: 755.9 n: 256

m: 1769.7 n: 512

m: 3955.3 n: 1024

m: 8604.9 n: 2048

m: 17307.5 n: 4096

m: 38546.9 n: 8192

m: 85838.8 n: 16384

m: 176039.2 n: 32768

m: 377753.9 n: 65536

m: 812188.0 n: 131072

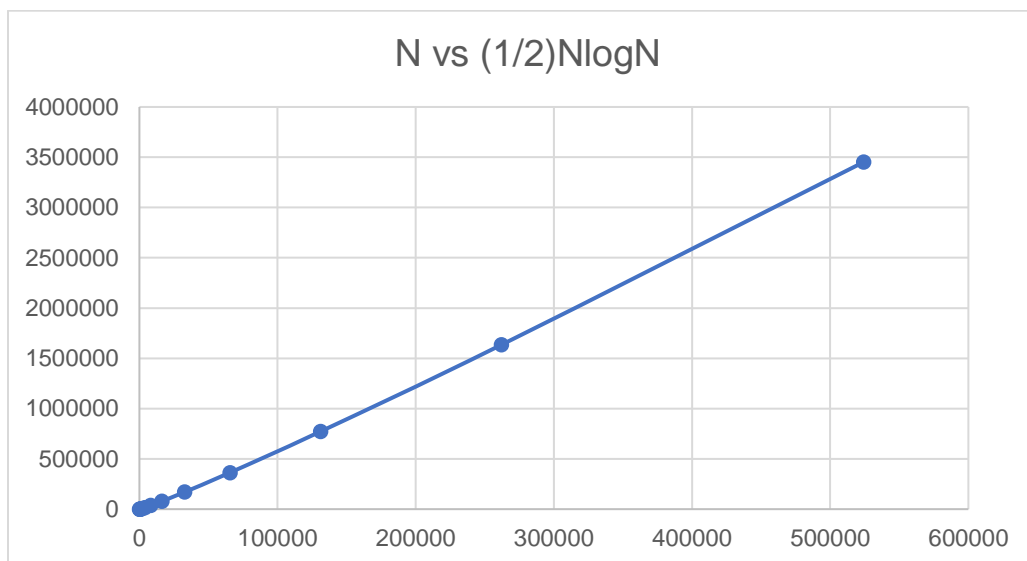
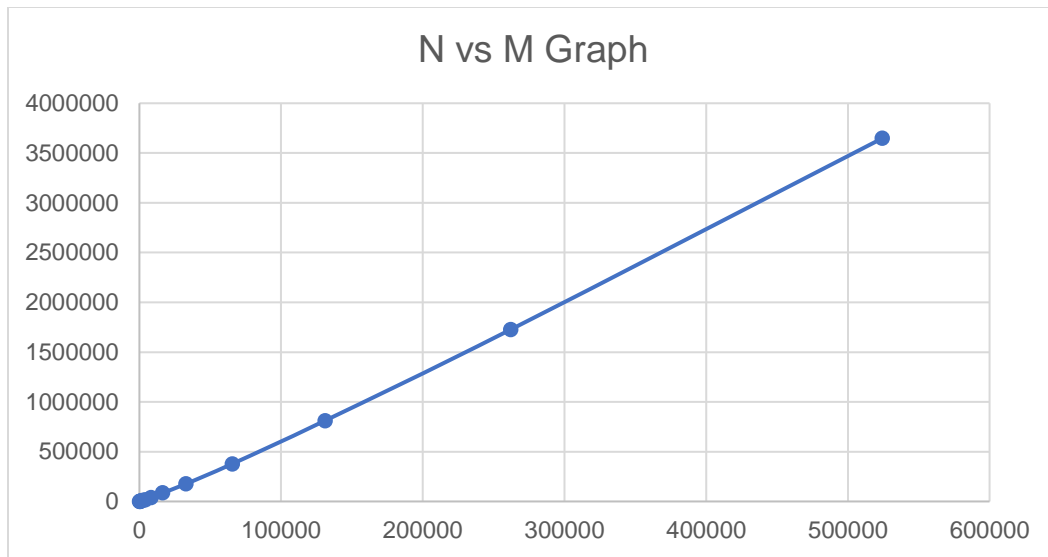
m: 1727530.8 n: 262144

m: 3647762.0 n: 524288

Process finished with exit code 0

Graphical Representation

Number of Objects (n)	Number of Pairs(m)	$(1/2)n\log n$
128	351.9	310.5299369
256	755.9	709.7827129
512	1769.7	1597.011104
1024	3955.3	3548.913564
2048	8604.9	7807.609842
4096	17307.5	17034.78511
8192	38546.9	36908.70107
16384	85838.8	79495.66384
32768	176039.2	170347.8511
65536	377753.9	363408.749
131072	812188	772243.5916
262144	1727530.8	1635339.371
524288	3647762	3452383.116



◉ **Unit tests result:**

