Homework 6

ISyE 6420 Spring 2020



Course Material for ISyE6420 by Brani Vidakovic is licensed under a Creative Commons Attribution-NonCommercial 4.0 International License.

Due April 12, 2020, 11:55pm. HW6 is not time limited except the due date. Late submissions will not be accepted.

Use of all available electronic and printed resources is allowed except direct communication that violates Georgia Tech Academic Integrity Rules.

1. Rinderpest Virus in Rabbits with Missing Data. Temperatures (temp) were recorded in a rabbit at various times (time) after the rabbit was inoculated with rinderpest virus (the data modified from Carter and Mitchell, 1958). Rinderpest (RP) is an infectious viral disease of cattle, domestic buffalo, and some species of wildlife; it is commonly referred to as cattle plague. It is characterized by fever, oral erosions, diarrhea, lymphoid necrosis, and high mortality.

Time after injection	Temperature
(time in hrs)	$(\texttt{temp in } \circ F)$
24	102.8
32	104.5
48	106.5
56	107.0
NA	107.1
70	105.1
72	103.9
75	NA
80	103.2
96	102.1

- (a) Using WinBUGS and properly accounting for the missing data demonstrate that a linear regression with one predictor (time) gives relatively low Bayesian R^2 . What are estimators of the missing data? Does the 95% Credible Set for the slope contain 0? Comment.
- (b) Include time2 (squared time) as the second predictor, making the regression quadratic in variables, but still linear in coefficients. Show that this regression has a larger Bayesian

 R^2 . What are the estimators of missing data? Do the 95% Credible Sets for parameters in the quadratic model contain 0? Comment.

Hint: To have cleaner codes, do the modeling in (a) and (b) in two separate WinBUGS programs.

2. Bladder Cancer Data. An exercise in the book Pagano and Gauvreau (2000) ¹ features data on 86 patients who after surgery were assigned to placebo or chemotherapy (thiopeta). Endpoint was the time to cancer recurrence (in months).

Variables are: time, group (0 - placebo, 1- chemotherapy), and observed (0 - recurrence not observed, 1 - recurrence observed). This data is given in files bladerc.csv|dat|xlsx. Data are given in WinBUGS format bladderBUGS.csv|dat|xlsx. The starter file bladderc0.odc contains data and also initial values for parameters and censored observations.

Assume that observed times are exponentially distributed with the rate parameter λ_i depending on the covariate group, as

$$\lambda_i = \exp\{\beta_0 + \beta_1 \times \operatorname{group}_i\}$$

After β_0 and β_1 are estimated, since the variable group takes values 0 or 1, the means for the placebo and treatment times become

$$\mu_0 = \frac{1}{\exp{\{\beta_0\}}} = \exp{\{-\beta_0\}}$$

$$\mu_1 = \frac{1}{\exp{\{\beta_0 + \beta_1\}}} = \exp{\{-\beta_0 - \beta_1\}},$$

respectively. The censored data are modeled as exponentials left truncated by the censoring time. Use noninformative priors on β_0 and β_1 .

- (a) Is the 90% Credible Set for $\mu_1 \mu_0$ all positive?
- (b) What is the posterior probability of hypothesis $H: \mu_1 > \mu_0$?
- (c) Comment on the benefits of the treatment (a paragraph).

¹Bladder cancer data from M Pagano and K Gauvreau, "Principles of Biostatistics, 2nd Ed. Duxbury 2000. Chapter 21, Exercise 9, page 512.