Is There a Replication Crisis in Finance?

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Abstract

Several papers argue that financial economics faces a replication crisis because the majority of studies cannot be replicated or are the result of multiple testing of too many factors. We develop and estimate a Bayesian model of factor replication, which leads to different conclusions. The majority of asset pricing factors: (1) can be replicated, (2) can be clustered into 13 themes, the majority of which are significant parts of the tangency portfolio, (3) work out-of-sample in a new large data set covering 93 countries, and (4) have evidence that is strengthened (not weakened) by the large number of observed factors.

Keywords: asset pricing, factors, data mining, replication, multiple testing, external validity, empirical Bayes, Bayesian statistics

 ${\rm JEL~Codes:~G11,~G12,~G14,~G15,~G4,~C5}$

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Several research fields face replication crises (or credibility crises), including medicine (Ioannidis, 2005), psychology (Nosek et al., 2012), management (Bettis, 2012), experimental economics (Maniadis et al., 2017), and now also financial economics. Challenges to the replicability of finance research take two basic forms:

- 1. No internal validity. Most studies cannot be replicated with the same data (e.g., because of coding errors or faulty statistics) or are not robust in the sense that the main results cannot be replicated using slightly different methodologies and/or slightly different data. E.g., Hou et al. (2020) state:
 - "Most anomalies fail to hold up to currently acceptable standards for empirical finance."
- 2. No external validity. Most studies may be robustly replicated, but are spurious and driven by "p-hacking," that is, finding significant results by testing multiple hypotheses without controlling the false discovery rate. Such spurious results are not expected to replicate in other samples or time periods, in part because the sheer number of factors is simply too large, and too fast growing, to be believable. E.g., Cochrane (2011) asks for a consolidation of the "factor zoo," and Harvey et al. (2016) states:

"most claimed research findings in financial economics are likely false." 2

We examine both of these challenges theoretically and empirically. We conclude that neither criticism is tenable. The majority of factors do replicate, do survive joint modeling of all factors, do hold up out-of-sample, are strengthened (not weakened) by the large number of observed factors, are further strengthened by global evidence, and the number of factors can be understood as multiple versions of a smaller number of themes.

¹Hamermesh (2007) contrasts "pure replication" and "scientific replication." Pure replication is, "checking on others' published papers using their data," also called "reproduction" by Welch (2019). Scientific replication uses, "different sample, different population and perhaps similar, but not identical model." We focus on scientific replication. We propose a new modeling framework to jointly estimate factor alphas, we use robust factor construction methods that are applied uniformly to all factors, and we test both internal and external validity of prior factor research in several dimensions, including out-of-sample time series replication and international sample replication. In complementary and contemporaneous work, Chen and Zimmermann (2020a) consider pure replication, attempting to use the same data and methods as the original papers for a large number of factors. They are able to reproduce nearly 100% of factors, but Hou et al. (2020) challenge the scientific replication and Harvey et al. (2016) challenge validity due to multiple testing.

²Similarly, Linnainmaa and Roberts (2018) state "the majority of accounting-based return anomalies,

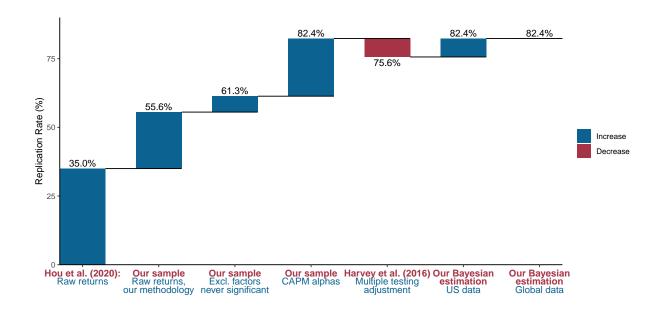


Figure 1: Replication Rates Versus the Literature

Note: This figure summarizes analyses throughout the paper. Refer to Section 3 for estimation details.

These conclusions rely on new theory and data: First, we show that factors must be understood in light of economic theory and we develop a Bayesian model that offers a very different interpretation of the evidence on factor replication. Second, we put together a new global data set of 153 factors across 93 countries. To help advance replication in finance, we have made this data set easily accessible to researchers via a direct open-source link to WRDS, including meticulous documentation of the data and the underlying code base.

Replication results. Figure 1 illustrates our main results and how they relate to the literature in a sequence of steps. It presents the "replication rate," that is, the percent of factors with a statistically significant average excess return. The starting point of Figure 1—shown as the first bar on the left—is the 35% replication rate reported in the expansive factor replication study of Hou et al. (2020).

The second bar in Figure 1 shows a 55.6% baseline replication rate in our main sample of US factors. It is based on significant OLS t-statistics for average raw factor returns, in direct comparability to the 35% calculation from Hou et al. (2020). This difference arises because our sample is longer, we add 15 factors to our sample that were previously studied in the literature but not studied by Hou et al. (2020), and due to minor conservative factor

construction details that we believe robustify factor behavior.³ We discuss this decomposition further in Section 2, where we detail our factor construction choices and discuss why we prefer them.

The Hou et al. (2020) sample includes a number of factors that the original studies found to be insignificant.⁴ We exclude these when calculating the replication rate. After we make this adjustment, the replication rate rises to 61.3%, shown in the third bar in Figure 1.

Alpha, not raw return. Hou et al. (2020) analyze and test factors' raw returns, but if we wish to learn about "anomalies," economic theory dictates the use of risk-adjusted returns. Raw return gives a misleading inference for the factor if it differs from the alpha: When the raw return is significant, but the alpha is not, it simply means that the factor is taking risk exposure and the risk premium is significant, which does not indicate anomalous returns of the factor. Likewise, when the raw return is insignificant, but the alpha is significant, then the factor's efficacy is masked by its risk exposure. An example of this is the low-beta anomaly, where theory predicts that the alpha of a dollar-neutral low-beta factor is positive, but its raw return is negative or close to zero (Frazzini and Pedersen, 2014). In this case, the "failure to replicate" of Hou et al. (2020) is, in fact, support for the betting-against-beta theory. We analyze alpha to the CAPM, which is the clearest theoretical benchmark model that is not mechanically linked to other so-called anomalies in the list of replicated factors. The fourth bar in Figure 1 shows that the replication rate rises to 82.4% based on tests of factors' CAPM alpha.

Multiple testing and our Bayesian model. The first four bars in Figure 1 are based on individual ordinary least squares (OLS) t-statistics for each factor. But Harvey et al. (2016) rightly point out that this type of analysis suffers from a multiple testing (MT) problem. Harvey et al. (2016) recommend MT adjustments that raise the threshold for a t-statistic to be considered statistically significant. We report one such MT correction using

 $^{^3}$ We use tercile spreads while they use deciles; we use tercile breakpoints from all stocks above the NYSE 20^{th} percentile (i.e., non-micro-caps), they use straight NYSE breakpoints; we always lag accounting data four months, they use a mixture of updating schemes; we exclude IBES factor due to their relatively short history; we use capped value-weighting they use straight value-weights; We look at returns over a 1 month holding period, they use 1, 6 and 12 months. In appendix C we detail how each change affects the replication rate.

⁴We identify 34 factors from Hou et al. (2020) for which the original paper did not find a significant alpha or did not study factor returns (see appendix Table J.1).

a leading method proposed by Benjamini and Yekutieli (2001). Accounting for MT in this manner, we find that the replication rate drops to 75.6% (the fifth bar of Figure 1). For comparison, Hou et al. (2020) consider a similar adjustment and find that their replication rate drops from 35% with OLS to 18% after MT correction.

However, common frequentist MT corrections can be unnecessarily crude. Our handling of the MT problem is different. We propose a Bayesian framework for the joint behavior of all the factors, resulting in an MT correction that sacrifices much less power than its frequentist counterpart (which we demonstrate via simulation).⁵ To understand the benefits of our approach, note first that we impose a prior that all alphas are expected to be zero. The role of the Bayesian prior is conceptually similar to that of frequentist MT corrections—it imposes conservatism on statistical inference and controls the false discovery rate. Second, our joint factor model allows us to conduct inference for all factor alphas simultaneously. The joint structure among factors leverages dependence in the data in order to draw more informative statistical inferences (relative to conducting independent individual tests). Our zero-alpha prior shrinks alpha estimates of all factors, thereby leading to fewer discoveries (i.e., a lower replication rate), with similar conservatism as a frequentist MT correction. At the same, however, the model allows us to learn more about the alpha of any individual factor, borrowing estimation strength across all factors. The improved precision of alpha estimates for all factors can increase the number of discoveries. Which effect dominates when we construct our final Bayesian model—the conservative shrinkage to the prior or the improved precision of alphas—is an empirical question.

In our sample, we find that the two effects exactly offset, which is why the Bayesian multiple testing view delivers a replication rate identical to the OLS-based rate. Specifically, our estimated replication rate rises to 82.4% (the sixth bar of Figure 1) using our Bayesian approach to the MT problem.⁶ The intuition behind this surprising result is simply that

⁵A large statistics literature (see Gelman et al., 2013, and references therein) explains how Bayesian estimation naturally combats MT problems and Gelman et al. (2012) conclude that "the problem of multiple comparisons can disappear entirely when viewed from a hierarchical Bayesian perspective." Chinco et al. (2020) use a Bayesian estimation framework similar to ours for a different (but conceptually related) problem. They infer the distribution of coefficients in a stock return prediction model to calculate what they dub the "anomaly base rate."

⁶Our Bayesian approach leads to an even larger increase in the replication rate when using pure valueweighted returns (see Figure C.1 of the appendix) and when considering global evidence outside the US (as

having many factors (a "factor zoo") can be a strength rather than a weakness when assessing the replicability of factor research. It is obvious that our posterior is tighter when a factor has performed better and has a longer time series. But the posterior is further tightened if similar factors have also performed well, and if additional data shows that these factors have performed well in many other countries.⁷

Benefits of our model beyond the replication rate. One of the key benefits of Bayesian statistics is that one recovers not just a point estimate but the entire posterior distribution of parameters. The posterior allows us to make any possible probability calculation about parameters. For example, in addition to the replication rate, we also calculate the posterior probability of false discoveries (false discovery rate, FDR) and the posterior expected fraction of true factors. Moreover, we calculate Bayesian confidence intervals (also called credibility intervals) for each of these estimates. We find that our 82.4% replication rate has a tight posterior standard error of 2.8%. The posterior Bayesian FDR is only 0.1% with a 95% confidence interval of [0.0%, 1.0%], demonstrating the small risk of false discoveries. The expected fraction of true factors is 94.0% with a posterior standard error of 1.3%.

Global replication. Having found a high degree of internal validity of prior research, we next consider external validity across countries and over time. Regarding the former, we investigate how our conclusions are affected when we extend the data to include all factors in a large global panel of 93 countries. The last bar in Figure 1, shows that, based on the global sample, the final replication rate is 82.4%. This estimate is based on the Bayesian model extended to incorporate the joint behavior of international data. Because it accounts for the global correlation structure among factors, the model recognizes that international evidence is not independent out-of-sample evidence, and uses only the incremental global evidence to update the overall replicability assessment. And it continues to account for multiple testing. The global result reflects that factor performance in the US replicates well in an extensive cross section of countries. Serving as our final estimate, the global factor replication rate

we show later, in Figure 6).

⁷Taking this intuition further, we can glean additional information from studying whether factors work in other asset classes, as has been done for value and momentum (Asness et al., 2013), betting against beta (Frazzini and Pedersen, 2014), time series momentum (Moskowitz et al., 2012), and carry (Koijen et al., 2018).

more than doubles that of Hou et al. (2020) by grounding our tests in economic theory and modern Bayesian statistics. We conclude from the global analysis that factor research demonstrates external validity in the cross section of countries.

Post-publication performance. McLean and Pontiff (2016) find that US factor returns "are 26% lower out-of-sample and 58% lower post-publication." Our Bayesian framework shows that, given a prior belief of zero alpha but an OLS alpha ($\hat{\alpha}$) that is positive, then our posterior belief about alpha lies somewhere between zero and $\hat{\alpha}$. Hence, a positive but attenuated post-publication alpha is the expected outcome based on Bayesian learning, rather than a sign of non-reproducibility. Further, when comparing factors cross-sectionally, the prediction of the Bayesian framework is that higher pre-publication alphas, if real, should be associated with higher post-publication alphas on average. And that is what we find. We present new and significant cross-sectional evidence that factors with higher in-sample alpha generally have higher out-of-sample alpha. The attenuation in the data is somewhat stronger than predicted by our Bayesian model. We conclude that factor research demonstrates external validity in the time series, but there appears to be some decay of the strongest factors that could be due to arbitrage or data mining.⁹

Publication bias. We also address the issue that factors with strong in-sample performance are more likely to be published while poorly performing factors are more likely to be unobserved in the literature. Publication bias can influence our full-sample Bayesian evidence through the empirical Bayes estimation of prior hyperparameters. To account for this bias, we show how to pick a prior distribution that is unaffected by publication bias by using only out-of-sample data or estimates from Harvey et al. (2016). Using such priors, the full-sample alphas are shrunk more heavily toward zero. The result is a slight drop in US the replication rate to 81.5%. If we add an extra degree of conservatism to the prior, the replication rate drops to 79.8%. Further, our out-of-sample evidence across time and across countries is not subject to publication bias.

⁸Extending the evidence to global stock markets, Jacobs and Müller (2020) find that "the United States is the only country with a reliable post-publication decline in long-short returns." Chen and Zimmermann (2020b) use Bayesian methods to estimate bias-corrected post-publication performance and find that average returns drop by only 12% after publication in US data.

⁹Data prior to the sample used in original studies also constitutes out-of-sample evidence (Linnainmaa and Roberts, 2018; Ilmanen et al., 2021). Our external validity conclusions are the same when we also include pre-original-study out-of-sample evidence.

Multidimensional challenge: A Darwinian view of the factor zoo. Harvey et al. (2016) challenge the sheer number of factors and Cochrane (2011) refers to as "the multidimensional challenge." We argue that the factor research universe should not be viewed as hundreds of distinct factors. Instead, factors cluster into a relatively small number of highly correlated themes, and this property features prominently in our Bayesian modeling approach. We propose a factor taxonomy that algorithmically classifies factors into 13 themes possessing a high degree of within-theme return correlation and economic concept similarity, and low across-theme correlation. The emergence of themes, in which factors are minor variations on a related idea, is intuitive. For example, each value factor is defined by a specific valuation ratio, but there are many plausible ratios. Considering their variations is not spurious alpha-hacking, particularly when the "correct" value signal construction is debatable.

We estimate a replication rate of greater than 50% in 11 of the 13 themes (based on the Bayesian model including MT adjustment), the exceptions being "low leverage," and "size" factor themes. We also analyze which themes matter when simultaneously controlling for all other themes. To do so, we estimate the expost tangency portfolio of 13 themerepresentative portfolios. We find that 10 of the 13 themes enter into the tangency portfolio with significantly positive weights, where the three displaced themes are "profitability," "investment," and "size."

Why, the profession asks, have we arrived at a "factor zoo"?¹⁰ The answer, evidently, is because the risk-return tradeoff is complex and difficult to measure. The complexity manifests in our inability to isolate a single, silver bullet characteristic that pins down the risk-return tradeoff. Classifying factors into themes, we trace the economic culprits to roughly a dozen concepts. This is already a multidimensional challenge, but it is compounded by the fact that within a theme there are many detailed choices for how to configure the economic concept, which results in highly correlated within-theme factors. Together, the themes (and the factors in them) each make slightly different contributions to our collective understanding of markets. A more positive take on the factor zoo is *not* as a collective exercise in data

 $^{^{10}}$ See Bryzgalova et al. (2019), Chordia et al. (2020), Kelly et al. (2019), Kozak et al. (2020), Green et al. (2017), and Feng et al. (2020) for other perspectives on high-dimensional asset pricing problems, and Chen (2020) for an argument why p-hacking cannot explain the existence of so many significant factors.

mining and false discovery; instead, it is a natural outcome of a decentralized effort in which researchers make contributions that are correlated with, but incrementally improve on, the shared body of knowledge.

Economic implications. Our findings have broad implications for finance researchers and practitioners. We confirm that the body of finance research contains a multitude of replicable information about the drivers of expected returns. Further, we show that investors would have profited from factors deemed significant by our Bayesian method, but deemed insignificant by the frequentist MT method proposed by Harvey et al. (2016). Indeed, Figure 2 plots the returns of the subset of factors discovered by our method but discarded by the frequentist method. These factors produce an annualized information ratio (IR) of 0.93 in the US and 1.10 globally (ex. US) over the full sample, with t-statistics above five. If we restrict analysis to the sample after that of Harvey et al. (2016), the performance differential remains large and significant. These findings show strong external validity (post original publications, post Harvey et al. (2016), different countries) and significant economic benefits of exploiting the joint information in all factor returns rather than simply applying a high cutoff for t-statistics. 11 We also show how the optimal risk-return profile has improved over time as factors have been discovered. In other words, the Sharpe ratio of the tangency portfolio has meaningfully increased over time as truly novel drivers of returns have been discovered. These findings can help inform asset pricing theory.

1 A Bayesian Model of Factor Replication

This section presents our Bayesian model for assessing factor replicability. We first draw out some basic implications of the Bayesian framework for interpreting evidence on individual factor alphas, then present a hierarchical structure for simultaneously modeling factors in a variety themes and across many countries.

¹¹The out-of-sample performance across all significant factors under empirical Bayes is also highly significant as shown in Appendix Figure D.1.

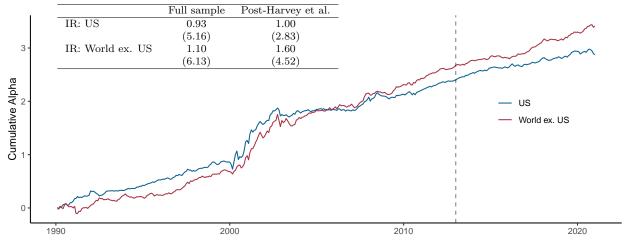


Figure 2: Out-of-sample performance of marginally significant factors

Note: The figure shows the cumulative CAPM alpha of an average of factors significant under our empirical Bayes framework, but not with the Benjamini-Yekutieli adjustment suggested by Harvey et al. (2016). The significance cutoffs are re-estimated each year with the available data. Factors are eligible for inclusion after the sample period in the original paper, so all returns are out-of-sample. The table shows the information ratio (alpha divided by residual volatility) for the full sample (1990-2020) and the post-Harvey et al. (2016) sample (2013-2020) with t-statistics in parentheses. The dashed line is at December 2012.

1.1 Learning About Alpha: The Bayes Case

Posterior Alpha

We begin by considering an excess return factor f_t . A study of "anomalous" factor returns requires a risk benchmark, without which we cannot separate distinctive factor behavior from run of the mill risk compensation. We assume a CAPM benchmark due to its history as a factor research benchmark for decades, and because it is not mechanically related to any of the factors that we attempt to replicate (in contrast to, say, the model of Fama and French, 1993, which by construction explains size and value factors). A factor's net performance versus the excess market factor (r_t^m) is its α :

$$f_t = \alpha + \beta r_t^m + \varepsilon_t. \tag{1}$$

Our Bayesian prior is that the alpha is normally distributed with mean zero and variance τ^2 , or $\alpha \sim N(0, \tau^2)$. The mean of zero implies that CAPM holds on average, and τ governs potential deviations from CAPM. Intuitively, the higher the confidence in the prior, the lower is τ . The error term, $\varepsilon_t \sim N(0, \sigma^2)$, has volatility σ , is independent and identically

distributed over time, and σ and β are observable.¹²

The risk-adjusted return, α , is estimated as the average market-adjusted factor return from T periods of data:

$$\hat{\alpha} = \frac{1}{T} \sum_{t} (f_t - \beta r_t^m) = \alpha + \frac{1}{T} \sum_{t} \varepsilon_t.$$
 (2)

This observed ordinary least squares (OLS) estimate $\hat{\alpha}$ is distributed $N(\alpha, \sigma^2/T)$ given the true alpha, α . From Bayes' rule, we can compute the posterior distribution of the true alpha given the data evidence and prior. The posterior exhaustively describes the Bayesian's beliefs about alpha at a future time t > T given the past experience, including the posterior expected factor performance,

$$E(\alpha|\hat{\alpha}) = E\left(f_t - \beta r_t^m \middle| \hat{\alpha}\right). \tag{3}$$

We derive the posterior alpha distribution via Bayes' rule (the derivation, which is standard, is shown in Appendix A). The posterior alpha is normal with mean

$$E(\alpha|\hat{\alpha}) = \kappa \hat{\alpha} \tag{4}$$

where κ is a shrinkage factor given by

$$\kappa = \frac{\tau^2}{\tau^2 + \sigma^2/T} = \frac{1}{1 + \frac{\sigma^2}{\tau^2 T}} \in (0, 1)$$
 (5)

and the posterior variance is

$$\operatorname{Var}(\alpha|\hat{\alpha}) = \kappa \frac{\sigma^2}{T} = \frac{1}{\frac{1}{\sigma^2/T} + \frac{1}{\tau^2}}.$$
 (6)

The first insight from this posterior is that a Bayesian predicts future returns will have

¹²Here we seek to derive some simple expressions that illustrate the economic implications of Bayesian logic. In the empirical implementation, we use slightly richer model, as discussed further below. The empirical implementation normalizes factors so that σ is given at 10% for all factors, while β must be estimated, but this does not affect the economic points that we make in this section.

smaller alpha (in absolute value) than the OLS estimate $\hat{\alpha}$, because the posterior mean $(\kappa \hat{\alpha})$ must lie between $\hat{\alpha}$ and the prior mean of zero. Said differently, a large observed alpha might be due to luck and, given the prior, we expect that at least part of this performance indeed is luck. The more data we have (higher T), the less shrinkage there is (i.e., κ closer to 1). Likewise, the stronger is the prior of zero alpha (i.e., lower τ), the heavier is the shrinkage. We can think of the prior τ in terms of the number of time periods of evidence that it corresponds to. That is, the posterior mean, $E(\alpha|\hat{\alpha})$, corresponds to first observing σ^2/τ^2 time periods with an average alpha of zero, followed by T time periods with a average alpha of $\hat{\alpha}$.

When evaluating out-of-sample evidence, a positive, but lower, alpha is sometimes interpreted as a sign of replication failure. But this is the expected outcome from the Bayesian perspective (i.e., based on the latest posterior), and can be fully consistent with a high degree of replicability. In fact, we show later that the comparatively low post-publication factor performance documented by McLean and Pontiff (2016) turns out to be consistent with the posterior a Bayesian would have formed given published results. Thus, post-publication results have tended to confirm the Bayesian's beliefs and as a result the Bayesian posterior alpha estimate has been extraordinarily stable over time (see Section 3.2).

Alpha-hacking

Because out-of-sample alpha attenuation is not generally a sign of replication failure, we may want a more direct probe for non-replicability. We can build such a test into our Bayesian framework by embedding scope for "alpha-hacking," or selectively reporting or manipulating data to artificially make the alpha seem larger. We represent this idea using the following distribution of factor returns in the in-sample time period t = 1, ..., T:

$$f_t = \alpha + \beta r_t^m + \underbrace{\tilde{\varepsilon}_t + u}_{\varepsilon_t}. \tag{7}$$

Here, $\tilde{\varepsilon}_t \sim N(0, \sigma^2)$ captures usual return shocks and $u \sim N(\bar{\varepsilon}, \sigma_u^2)$ represents return inflation due to alpha-hacking. The total in-sample return shock ε_t is normally distributed, $N(\bar{\varepsilon}, \bar{\sigma}^2)$, where $\bar{\varepsilon} \geq 0$ is the alpha-hacking bias, and the variance $\bar{\sigma}^2 = \sigma^2 + \sigma_u^2 \geq \sigma^2$ is elevated due to

the artificial noise created by alpha-hacking.¹³ Naturally, the false benefits of alpha-hacking disappear in out-of-sample data, or in other words $\varepsilon_t \sim N(0, \sigma^2)$ for t > T. The Bayesian accounts for alpha-hacking as follows:

Proposition 1 (Alpha-hacking) The posterior alpha with alpha-hacking is given by

$$E(\alpha|\hat{\alpha}) = -\kappa_0 + \kappa^{hacking} \hat{\alpha} \tag{8}$$

where $\kappa^{hacking} = \frac{1}{1 + \frac{\bar{\sigma}^2}{\tau^2 T}} \leq \kappa$ and $\kappa_0 = \kappa^{hacking} \bar{\varepsilon} \geq 0$. Further, $\kappa^{hacking} \to 0$ in the limit of "pure alpha-hacking," $\tau \to 0$ or $\bar{\sigma} \to \infty$.

The Bayesian posterior alpha accounts for alpha-hacking in two ways. First, the estimated alpha is shrunk more heavily toward zero since the factor κ^{hacking} is now smaller. Second, the alpha is further discounted by the intercept term κ_0 due to the bias in the error terms.

We examine alpha-hacking empirically in Section 3.2 in light of Proposition 1. We consider a cross-sectional regression of factors' out-of-sample (e.g., post-publication) alphas on their in-sample alphas, looking for the signatures of alpha-hacking in the form of a negative intercept term or a slope coefficient that is too small. In addition, Section 3.3 shows how to estimate the Bayesian model in a way that is less susceptible to the effects of alpha hacking and Appendix A presents additional theoretical results characterizing alpha-hacking.

1.2 Hierarchical Bayesian Model

Shared Alphas: The Case of Complete Pooling

We now embed a critical aspect of factor research into our Bayesian framework: Factors are often correlated and conceptually related to each other. For concreteness, we begin with a setting in which the researcher has access to "domestic" evidence in (1) as well as "global" evidence from an international factor, f_t^g , with known exposure β^g to the global market index r_t^g :

$$f_t^g = \alpha + \beta^g r_t^g + \varepsilon_t^g. \tag{9}$$

 $^{^{13}}$ We note that this elevated variance cannot be detected by looking at the in-sample variance of residual returns since the alpha-hacking term u does not depend on time t.

Here, we assume that the true alpha for this global factor is the same as the domestic alpha. In other words, we have complete "pooling" of information about alpha across the two samples. As an alternative interpretation, the researcher could have access to two related factors, say two different value factors in the same country, and assume that they have the same alpha because they capture the same investment principle.

The global shock, ε_t^g , is normally distributed $N(0, \sigma^2)$, and ε_t^g and ε_t are jointly normal with correlation ρ .¹⁴ The estimated alpha based on the global evidence is simply its market-adjusted return:

$$\hat{\alpha}^g = \frac{1}{T} \sum_t \left(f_t^g - \beta^g r_t^g \right). \tag{10}$$

To see the power of global evidence (or, more generally, the power of observing related strategies), we consider the posterior when observing both the domestic and global evidence.

Proposition 2 (The Power of Shared Evidence) The posterior alpha given the domestic estimate, $\hat{\alpha}$, and the global estimate, $\hat{\alpha}^g$, is normally distributed with mean

$$E(\alpha|\hat{\alpha}, \hat{\alpha}^g) = \kappa^g \left(\frac{1}{2}\hat{\alpha} + \frac{1}{2}\hat{\alpha}^g\right). \tag{11}$$

The global shrinkage parameter is

$$\kappa^g = \frac{1}{1 + \frac{\sigma^2}{\tau^2 T} \frac{1+\rho}{2}} \in [\kappa, 1] \tag{12}$$

which decreases with the correlation ρ , attaining the minimum value, $\kappa^g = \kappa$, when $\rho = 1$. The posterior variance is lower when observing both domestic and global evidence:

$$Var(\alpha|\hat{\alpha}) \ge Var(\alpha|\hat{\alpha}, \hat{\alpha}^g). \tag{13}$$

Naturally, the posterior depends on the average alpha observed domestically and globally. Furthermore, the combined alpha is shrunk toward the prior of zero. The shrinkage factor κ^g

¹⁴The framework can be generalized to a situation where the global shocks have a different volatility and sample length. In this case, the Bayesian posterior puts more weight on the sample with lower volatility and longer sample.

is smaller (heavier shrinkage) if the markets are more correlated because the global evidence provides less new information. With low correlation, the global evidence adds a lot of independent information, shrinkage is lighter, and the Bayesian becomes more confident in the data and less reliant on the prior. The proposition shows that, if a factor has been found to work both domestically and globally, then the Bayesian expects stronger out-of-sample performance than a factor that has only worked domestically (or has only been analyzed domestically).

Two important effects are at play here, and both are important for understanding the empirical evidence presented below: The domestic and global alphas are shrunk both toward each other and toward zero. For example, suppose that a factor worked domestically but not globally, say $\hat{\alpha}=10\%>\hat{\alpha}^g=0\%$. Then the overall evidence points to an alpha of $\frac{1}{2}\hat{\alpha}+\frac{1}{2}\hat{\alpha}^g=5\%$, but shrinkage toward the prior results in a lower posterior, say, 2.5%. Hence, the Bayesian expects future factor returns in both regions of 2.5%. That shared alphas are shrunk together is a key feature of a joint model, and it generally leads to different conclusions than when factors are evaluated independently. Next we consider a perhaps more realistic model in which factors are only partially shrunk toward each other.

Hierarchical Alphas: The Case of Partial Pooling

We now consider several factors, numbered i = 1, ..., N. Factor i has a true alpha given by

$$\alpha^i = c + w^i. (14)$$

Here, c is the common component of all alphas, which has a prior distribution given by $N(0, \tau_c^2)$. Likewise, w^i is the idiosyncratic alpha component, which has a prior distribution given by $N(0, \tau_w^2)$, independent of c and across i. Said differently, we can imagine that nature first picks of the overall c from $N(0, \tau_c^2)$ and then picks the factor-specific α^i from $N(c, \tau_w^2)$.

This hierarchical model is a realistic compromise between assuming that all factor alphas are completely different (using equation (4) for each alpha separately) and assuming that they are all the same (using Proposition 2). Rather than assuming no pooling or complete pooling, the hierarchical model allows factors to have a common component and an idiosyncratic

component.

Suppose we observe factor returns of

$$f_t^i = \alpha^i + \beta^i r_t^m + \varepsilon_t^i \tag{15}$$

where ε_t^i are normally distributed with mean 0 and variance σ^2 and $\operatorname{Cor}(\varepsilon_t^i, \varepsilon_t^j) = \rho \geq 0$ for all i, j.¹⁵ Computing the observed alpha estimates as above, $\hat{\alpha}^i = \frac{1}{T} \sum_t (f_t^i - \beta^i r_t^m)$, we derive the posterior in the following result.¹⁶

Proposition 3 (Hierarchical Alphas) The posterior alpha of factor i given the evidence on all factors is normally distributed with mean

$$E(\alpha^{i}|\hat{\alpha}^{1},\dots,\hat{\alpha}^{N}) = \frac{1}{1 + \frac{\rho\sigma^{2}}{\tau_{c}^{2}T} + \frac{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}{\tau_{c}^{2}N}} \hat{\alpha}^{\cdot} + \frac{1}{1 + \frac{(1-\rho)\sigma^{2}}{\tau_{w}^{2}T}} \left(\hat{\alpha}^{i} - \frac{1}{1 + \frac{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}{(\tau_{c}^{2} + \rho\sigma^{2}/T)N}} \hat{\alpha}^{\cdot}\right),$$
(16)

where $\hat{\alpha} = \frac{1}{N} \sum_{i} \hat{\alpha}^{j}$ is average alpha. When the number of factors N grows, the limit is

$$\lim_{N \to \infty} E(\alpha^i | \hat{\alpha}^1, \dots, \hat{\alpha}^N) = \frac{1}{1 + \frac{\rho \sigma^2}{\tau_c^2 T}} \hat{\alpha}^\cdot + \frac{1}{1 + \frac{(1 - \rho)\sigma^2}{\tau_c^2 T}} \left(\hat{\alpha}^i - \hat{\alpha}^\cdot \right). \tag{17}$$

The posterior variance of factor i's alpha using the information in all factor returns is lower than the posterior variance when looking at this factor in isolation:

$$Var(\alpha^i|\hat{\alpha}^1,\dots,\hat{\alpha}^N) < Var(\alpha^i|\hat{\alpha}^i). \tag{18}$$

¹⁵Alternatively, we can write the error terms in a similar way to how we write the alphas in (14), namely $\varepsilon_t^i = \sqrt{\rho}\,\tilde{\varepsilon}_t + \sqrt{1-\rho}\,\tilde{\varepsilon}_t^i$, where $\tilde{\varepsilon}_t^i$ are idiosyncratic shocks that are independent across factors and of the common shock $\tilde{\varepsilon}_t$, with $\mathrm{Var}(\tilde{\varepsilon}_t^i) = \mathrm{Var}(\tilde{\varepsilon}_t) = \sigma^2$. We note that we require (the empirically realistic case) that $\rho \geq 0$ since we cannot have an arbitrarily large number of normal random variables with equal negative correlation (because the corresponding variance-covariance matrix would not be positive semi-definite for large enough N).

 $^{^{16}}$ The general hierarchical model is used extensively in the statistics literature, see, e.g., Gelman et al. (2013), but to our knowledge the results in Proposition 3 are not in the literature.

The posterior variance is decreasing in N and, as $N \to \infty$, its limit is

$$\operatorname{Var}(\alpha^{i}|\hat{\alpha}^{1},\dots,\hat{\alpha}^{N}) \searrow \frac{\rho\sigma^{2}}{T} \frac{1}{1 + \frac{\rho\sigma^{2}}{\tau_{c}^{2}T}} + \frac{(1-\rho)\sigma^{2}}{T} \frac{1}{1 + \frac{(1-\rho)\sigma^{2}}{\tau_{w}^{2}T}}.$$
(19)

The main insight of this proposition is that having data on many factors is helpful for estimating the alpha of any of them. Intuitively, the posterior for any individual alpha depends on all of the other observed alphas because they are all informative about the common alpha component. That is, the other observed alphas tell us whether alpha exists in general or, said another way, tell us if the CAPM appears to be violated in general. Further, the factor's own observed alpha tells us whether this specific factor appears to be especially good or bad. Using all of the factors jointly reduces posterior variance for all alphas. In summary, the joint model with hierarchical alphas has the dual benefits of identifying the common component in alphas and tightening confidence intervals by sharing information among factors.

To understand the proposition in more detail, consider first the (unrealistic) case in which all factor returns have independent shocks ($\rho = 0$). In this case, we essentially know the overall alpha when we see many uncorrelated factors. Indeed, the average observed alpha becomes a precise estimator of the overall alpha with more and more observed factors, $\hat{\alpha} \to c$. Since we essentially know the overall alpha in this limit, the first term in (17) becomes $1 \times \hat{\alpha}$ when $\rho = 0$ meaning that we don't need any shrinkage here. The second term is the outperformance of factor i above the average alpha, and this outperformance is shrunk toward our prior of zero. Indeed, the outperformance is multiplied by a number less than one, and this multiplier naturally decreases in the return volatility σ and decreases in our conviction in the prior (increases in τ_w).

The posterior variance is also intuitive in the case of $\rho = 0$. The posterior variance is clearly lower compared to only observing the performance of factor i itself:

$$\operatorname{Var}(\alpha^{i}|\hat{\alpha}^{1},\hat{\alpha}^{2}\ldots) = \frac{\sigma^{2}}{T} \frac{1}{1 + \frac{\sigma^{2}}{\tau_{v}^{2}T}} < \frac{\sigma^{2}}{T} \frac{1}{1 + \frac{\sigma^{2}}{(\tau_{c}^{2} + \tau_{v}^{2})T}} = \operatorname{Var}(\alpha^{i}|\hat{\alpha}^{i})$$
(20)

based on (19) and (6). With partial pooling, the posterior variance decreases because the

denominator on the left does not have τ_c^2 , reflecting that uncertainty about the general alpha has been eliminated by observing many factors.

In the realistic case where factor returns are correlated $(\rho > 0)$, we see that both the average alpha $\hat{\alpha}$ and factor i's outperformance $\hat{\alpha}^i - \hat{\alpha}$ are shrunk toward the prior of zero. This is because we cannot precisely estimate the overall alpha even with an infinite number of correlated factors—the correlated part never vanishes. Nevertheless, we still shrink the confidence interval, $\operatorname{Var}(\alpha^i|\hat{\alpha}^1,\ldots,\hat{\alpha}^N) \leq \operatorname{Var}(\alpha^i|\hat{\alpha}^i)$, since more information is always better than less.

Multi-level Hierarchical Model

The model development to this point is simplified to draw out its intuition. Our empirical implementation is based on a more realistic (and slightly more complex) model that takes into account that factors naturally belong to different economic themes and to different regions.

In our global analysis, we have N different characteristic signals (e.g., book-to-market) across K regions, for a total of NK factors (e.g., US, developed, and emerging markets versions of book-to-market). Each of the N signals belongs to a smaller number of J theme clusters, where one cluster consists of various value factors, another consists of various momentum factors, and so on. One level of our hierarchical model allows for partially shared alphas among factors in the same theme cluster. Another level allows for commonality across regions among factors associated with the same underlying characteristic, capturing for example the connection between the book-to-market factor in different markets.

Mathematically, this means that an individual factor i has an alpha of

$$\alpha^i = \alpha^o + c^j + s^n + w^i. (21)$$

Concretely, suppose factor $i \in \{1, ..., NK\}$ is the book-to-market factor in the US region. Part of its alpha is driven by a component that is common to all factors, α^o , which we dogmatically fix at zero to be conservative. In addition, this factor i belongs to the value cluster $j \in \{1, ..., J\}$, which contributes a cluster-specific alpha $c^j \sim N(0, \tau_c^2)$. Next, since factor i is based on book-to-market characteristic $n \in \{1, ..., N\}$, it has an incremental signal-specific alpha of $s^n \sim N(0, \tau_s^2)$ that is shared across regions—e.g., it's the common behavior among book-to-market factors regardless of geography. Finally, $w^i \sim N(0, \tau_w^2)$ is factor i's idiosyncratic alpha, namely the incremental alpha that is unique to the US version of book-to-market.

We write this model in vector form as 17

$$\alpha = \alpha^o 1_{NK} + Mc + Zs + w \tag{22}$$

where $\alpha = (\alpha^1, \dots, \alpha^{NK})'$, $c = (c^1, \dots, c^J)'$, $s = (s^1, \dots, s^N)'$, $w = (w^1, \dots, w^{NK})'$, M is the $NK \times J$ matrix of cluster memberships, and Z is the $NK \times N$ matrix indicating the characteristic that factor i is based on. In particular, $M_{i,j} = 1$ if factor i is in cluster j and $M_{i,j} = 0$ otherwise. Likewise, $Z_{i,n} = 1$ if factor i is based on characteristic n and $Z_{i,n} = 0$ otherwise. This hierarchical model implies that the prior variance of alpha, denoted Ω , is n

$$\Omega = \operatorname{Var}(\alpha) = MM'\tau_c^2 + ZZ'\tau_s^2 + I_{NK}\tau_w^2.$$
(23)

In some cases, we analyze this model within a single region, K=1 (for example, in our US-only analysis). In this case, there is no difference between signal-specific alphas and idiosyncratic alphas, so we collapse one level of the model by setting $\tau^s=0$ and $s^n=0$ for $n \in \{1, ..., N\}$. In any case, the following result shows how to compute the posterior distribution of all alphas based on the prior uncertainty, Ω , and a general variance-covariance matrix of return shocks, $\Sigma = \text{Var}(\varepsilon)$. This result is at the heart of our empirical analysis.

Proposition 4 In the multi-level hierarchical model, the posterior of the vector of true alphas is normally distributed with posterior mean

$$E(\alpha|\hat{\alpha}) = \left(\Omega^{-1} + T\Sigma^{-1}\right)^{-1} \left(\Omega^{-1} 1_{NK} \alpha_0 + T\Sigma^{-1} \hat{\alpha}\right) \tag{24}$$

¹⁷The notation 1_N refers to an $N \times 1$ vector of ones and I_N is the $N \times N$ identity matrix.

¹⁸Stated differently, each diagonal element of Ω is $\tau_c^2 + \tau_s^2 + \tau_w^2$. Further, if $i \neq k$, then the $(i,k)^{th}$ element of Ω is $\tau_c^2 + \tau_s^2$ if i and k are constructed from the same signal in the same cluster in different regions, it is τ_c^2 if i and k are constructed from different signals in the same cluster, and it is 0 if i and k are in different clusters.

and posterior variance

$$\operatorname{Var}(\alpha|\hat{\alpha}) = \left(\Omega^{-1} + T\Sigma^{-1}\right)^{-1}.$$
 (25)

As noted above, we set the mean prior alpha to zero ($\alpha_0 = 0$) in our empirical implementation. This prior is based on economic theory and leads to a conservative shrinkage toward zero as seen in (24). We note that, in the data, the observed alphas are mostly positive, not centered around zero. However, these positive alphas are related to the way that factors are signed, namely according to the convention in the original paper, which almost always leads to a positive factor return in the original sample. However, if we view this signing convention as somewhat arbitrary, then a symmetry argument implies that a prior of zero is again natural. Said differently, factor means would be centered around zero if we changed signs arbitrarily, so our prior is agnostic about these signs.

1.3 Bayesian Multiple Testing and Empirical Bayes Estimation

Frequentist MT corrections embody a principle of conservatism that seeks to limit false discoveries, controlling the family-wise error rate (FWER) or the false discovery rate (FDR). Leading frequentist methods achieve this by widening confidence intervals and raising p-values, but do not alter the underlying point estimate.

Bayesian Multiple Testing

A large statistics literature describes how Bayesian modeling is effective for making reliable inferences in the face of multiple testing.¹⁹ Drawing on this literature, our hierarchical model is a prime example of how Bayesian methods accomplish their MT correction based on two key model features.

First is the model prior, which imposes statistical conservatism in analogy to frequentist MT methods. It anchors the researcher's beliefs to a sensible default (e.g., all alphas are zero) in case the data are insufficiently informative about the parameters of interest. Reduction

¹⁹See Gelman et al. (2012); Berry and Hochberg (1999); Greenland and Robins (1991); Efron and Tibshirani (2002), among others. See Gelman (2016) for an intuitive, informal discussion of the topic.

of false discoveries is achieved first by shrinking estimates toward the prior. When there is no information in the data, the alpha point estimate is the prior mean and there are no false discoveries. As data evidence accumulates, posterior beliefs migrate away from the prior toward the OLS alpha estimate. In the process, discoveries begin to emerge, though they remain dampened relative to OLS. In the large data limit, Bayesian beliefs converge on OLS with no MT correction, which is justified because in the limit there are no false discoveries. In other words, the prior embodies a particularly flexible form conservatism—the Bayesian model decides how severe of an MT correction to make based on the informativeness of the data.

Second is the hierarchical structure that captures joint behavior of factors. Modeling factors jointly means that each alpha is shrunk toward its cluster mean (i.e., toward related factors), in addition to being shrunk toward the prior of zero. So, if we observe a cluster of factors in which most perform poorly, then this evidence reduces the posterior alpha even for the few factors with strong performance—another form of Bayesian MT correction. In addition to this Bayesian discovery control coming through shrinkage of the posterior mean alpha, the Bayesian confidence interval also plays an important role and changes as a function of the data. Indeed, having data on related factors leads to a contraction of the confidence intervals in our joint Bayesian model. So while alpha shrinkage often has the effect of reducing discoveries, the increased precision from joint estimation has the opposite effect of enhancing statistical power and thus increases discoveries.

In summary, a typical implementation of frequentist MT corrections estimates parameters independently for each factor, leaves these parameters unchanged, but inflates p-values to reduce the number of discoveries. In contrast, our hierarchical model leverages dependence in the data to efficiently learn about all alphas simultaneously. All data therefore helps to determine the center and width of each alpha's confidence interval (Propositions 3 and 4). This leads to more precise estimates with "built-in" Bayesian MT correction.

Empirical Bayes Estimation

Given the central role of the prior, it might seem problematic that the severity of the Bayesian MT adjustment is at the discretion of the researcher. A powerful (and somewhat surprising)

aspect of a hierarchical model is that the prior can be learned in part from the data. This idea is formalized in the idea of "empirical Bayes (EB)" estimation, which has emerged as a major toolkit for navigating multiple tests in high-dimensional statistical settings (Efron, 2012).

The general approach to EB is to specify a multi-level hierarchical model, and then to use the dispersion of estimated effects within each level to learn about the prior parameters for that level. In our setting, the specific implementation of EB is dictated by Proposition 4. We first compute each factor's abnormal return, $\hat{\alpha}$, as the intercept in a CAPM regression on the market excess return. Next, we set the overall alpha prior mean, α^o , to zero to enforce conservatism in our inferences.

From here, the benefits of EB kick in: The realized dispersion in alphas across factors helps to determine the appropriate level of conviction for the prior (that is, the appropriate values for τ_c^2 , τ_s^2 , and τ_w^2). For example, if we compute the average alpha for each cluster, \hat{c}^j (e.g., the average value alpha, the average momentum alpha, and so on), the cross-sectional variation in \hat{c}^j suggests that $\tau_c^2 \cong \frac{1}{J-1} \sum_{j=1}^J (\hat{c}^j - \hat{c}^*)^2$. The same idea applies to τ_s^2 . Likewise, variation in observed alphas after accounting for hierarchical connections is informative about $\tau_w^2 \cong \frac{1}{NK-N-J} \sum_{i=1}^N (\hat{w}^i)^2$, where $\hat{w} = \hat{\alpha} - M\hat{c} - Z\hat{s}$.

The above variances illustrate the point that EB can help calibrate prior variances using the data itself. But those calculations are too crude, because they ignore sampling variation coming from the noise in returns, ε , which has covariance matrix Σ . Empirical Bayes estimates the prior variances by maximizing the prior likelihood function of the observed alphas, $\hat{\alpha} \sim N(0, \Omega(\tau_c, \tau_s, \tau_w) + \hat{\Sigma}/T)$, where the notation emphasizes that Ω depends on τ_c , τ_s , and τ_w according to (23). The likelihood function accounts for sampling variation through the a plug-in estimate of the covariance matrix of factor return shocks, $\hat{\Sigma}$. We collect the resulting hyper-parameters in τ , that is, τ_c, τ_s, τ_w , $\hat{\Sigma}$, and β^i .

Bayesian FDR and FWER

With the EB estimates (τ) on hand, we can compute the posterior distribution of the alphas from Proposition 4. From the posterior, we can in turn compute Bayesian versions of the

 $^{^{20}}$ We discuss the details of our EB estimation procedure in Appendix B.

FDR and FWER. Suppose that we consider a factor to be "discovered" if its z-score is greater than the critical value $\bar{z} = 1.96$:

$$\frac{E(\alpha^{i}|\hat{\alpha}^{1},\dots,\hat{\alpha}^{N},\tau)}{\sqrt{\operatorname{Var}(\alpha^{i}|\hat{\alpha}^{1},\dots,\hat{\alpha}^{N},\tau)}} > \bar{z}.$$
(26)

Equivalently, factor i is discovered if p-null $_i < 2.5\%,^{21}$ where we use the posterior to compute

$$p-\text{null}_i = Pr(\alpha^i < 0 | \hat{\alpha}^1, \dots, \hat{\alpha}^N, \tau). \tag{27}$$

In words, p-null_i is the posterior probability that the null hypothesis is true, which is the Bayesian version of a frequentist p-value. Said differently, it is the posterior probability of a "false discovery," namely the probability that the true alpha is actually non-positive.

We can further compute the Bayesian FDR as:

$$FDR^{Bayes} = E\left(\frac{\sum_{i} 1_{\{i \text{ false discovery}\}}}{\sum_{i} 1_{\{i \text{ discovery}\}}} \middle| \hat{\alpha}^{1}, \dots, \hat{\alpha}^{N}, \tau\right)$$
(28)

where we condition on the data including at least one discovery (so the denominator is not zero), otherwise FDR is set to zero (see Benjamini and Hochberg, 1995).

The following proposition is a novel characterization of the Bayesian FDR, and shows that it is the posterior probability of a false discovery, averaged across all discoveries:

Proposition 5 (Bayesian FDR) Conditional on the parameters of the prior distribution τ and data with at least one discovery, the Bayesian false discovery rate can be computed as:

$$FDR^{Bayes} = \frac{1}{\# discoveries} \sum_{i \text{ discovery}} p\text{-null}_i.$$
 (29)

and is bounded, $FDR^{Bayes} \leq 2.5\%$.

This result shows explicitly how the Bayesian framework controls the false discovery rate without the need for additional MT adjustments.²² The definition of a discovery ensures

 $^{^{21}}$ We use a critical value of 2.5% rather than 5% because the 1.96 cut-off corresponds to a 2-sided test, while false discoveries are only on one side in the Bayesian framework.

²²Efron (2007) includes related analysis but, to our knowledge, this particular result is new.

that at most 2.5% of the discoveries are false according to the Bayesian posterior, which is exactly the right distribution for assessing discoveries from the perspective of the Bayesian. Further, if many of the discovered factors are highly significant (as is the case in our data), then the Bayesian FDR is much lower than 2.5%.²³

We can also compute a Bayesian version of the family-wise error rate, which is the probability of making one or more false discoveries in total:

$$FWER^{Bayes} = Pr\left(\sum_{i} 1_{\{i \text{ false discovery}\}} \ge 1 \middle| \hat{\alpha}^{1}, \dots, \hat{\alpha}^{N}, \tau \right).$$
(30)

If we define a discovery as in (26) using the standard critical value $\bar{z}=1.96$, then we do not necessarily control the family-wise error rate, FWER^{Bayes}, which is a harsh criterion that is concerned with the risk of a single false discovery without regard for the number of missed discoveries. FWER^{Bayes} is a probability that can be computed from the posterior so it is straightforward to choose a critical value \bar{z} to ensure FWER^{Bayes} $\leq 5\%$ or any other level one prefers. The main point is that the Bayesian approach to replication lends itself to any inferential calculation the researcher desires because the posterior is a complete characterization of Bayesian beliefs about model parameters.

A Comparison of Frequentist and Bayesian False Discovery Control

We illustrate the benefits of Bayesian inference for our replication analysis via simulation. We assume a factor generating process based on the hierarchical model above and, for simplicity, consider a single region (as in our empirical US-only analysis), removing s^n and τ_s^2 from equations (21) and (23). We analyze discoveries as we vary the prior variances τ_c and τ_w . The remaining parameters are calibrated to our estimates for the US region in our empirical analysis below.

We simulate an economy with 130 factors in 13 different clusters of 10 factors each, observed monthly over 70 years. We assume that the mean alpha, α^o , is zero. We then draw

²³Proposition 5 formalizes the argument of Greenland and Robins (1991) that "from the empirical-Bayes or Bayesian perspective, multiple comparisons are not really a 'problem.' Rather, the multiplicity of comparisons provides an opportunity to improve our estimates through judicious use of any prior information (in the form of model assumptions) about the ensemble of parameters being estimated."

a cluster alpha from $c^j \sim N(0, \tau_c^2)$ and a factor-specific alpha as $w^i \sim N(0, \tau_w^2)$. Based on these alphas, we generate realized returns by adding Gaussian noise.²⁴

We compute p-values separately using OLS with no adjustment or adjusting with the Benjamini-Yekutieli (BY) method. We also use EB to estimate the posterior alpha distribution, treating τ_c and τ_w as known in order to simplify simulations and focus on the Bayesian updating. For OLS and BY, a discovery occurs when the alpha estimate is positive and the two-sided p-value is below 5%. For EB, we consider it a discovery when the posterior probability that alpha is negative is less that 2.5%. For each pair of τ_c and τ_w , we draw 10,000 simulated samples, and report average discovery rates over all simulations.

Figure 3 reports alpha discoveries based on the OLS, BY, and EB approaches. For each method, we report the true FDR in the top panels (we know the truth since this is a simulation) and the "true discovery rate" ²⁵ in the bottom panels.

When idiosyncratic variation in true alphas is small (left panels with $\tau_w = 0.01\%$) and the variation in cluster alphas is also small (values of τ_c near zero on the horizontal axis), alphas are very small and true discoveries are unlikely. In this case, the OLS false discovery rate can be as high as 25% as seen in the upper left panel. However, both BY and EB successfully correct this problem and lower the FDR. The lower left panel shows that the BY correction pays a high price for its correction in terms of statistical power when τ_c is larger. In contrast, EB exhibits much better power to detect true positives while maintaining a similar false discovery control as BY. In fact, when there are more discoveries to be made in the data (as τ_c increases), EB becomes even more likely to identify true positives than OLS. This is due to the joint nature of the Bayesian model, whose estimates are especially precise compared to OLS due to EB's ability to learn more efficiently from dependent data. This illustrates a point of Greenland and Robins (1991) that "Unlike conventional multiple comparisons, empirical-Bayes and Bayes approaches will alter and can improve point estimates and can

 $^{^{24}}$ The noise covariance matrix has a block structure calibrated to our data, with a correlation of 0.58 among factors in the same cluster and a correlation of 0.02 across clusters. The residual volatility for each factor is 10% per annum.

²⁵We define the true discovery rate to be the number of significantly positive alphas according to, respectively, OLS, BY, and EB divided by the number of truly positive alphas. Given our simulation structure, half of the alphas are expected to be positive in any simulation. Some of these will be small (i.e., economically insignificant) positives, so a testing procedure would require a high degree of statistical power to detect them. This is why the true discovery rate is below one even for high values of τ_c .

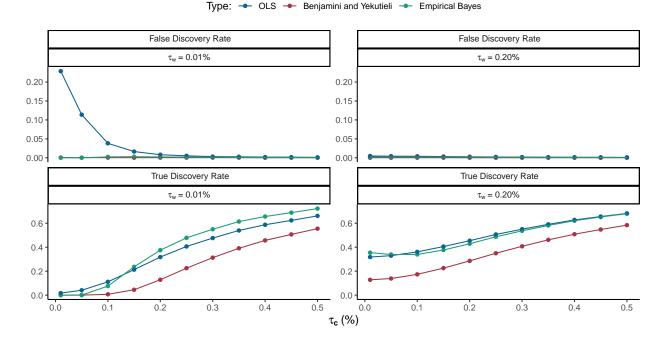


Figure 3: Simulation Comparison of False Discovery Rates

Note: The upper panels show the realized false discovery rate computed as the proportion of discovered factors for which the true alpha is negative, averaged over 10,000 simulations. The lower panels show the true discovery rate computed as the number of discoveries where the true alpha is positive divided by the total number of factors where the true alpha is positive. The left and right panels use low and high values of idiosyncratic variation in alphas (τ_w) , respectively. The x-axis varies cluster alpha dispersion, τ_c .

provide more powerful tests and more precise (narrower) interval estimators." When the idiosyncratic variation is larger ($\tau_w = 0.20\%$), there are many more true discoveries to be made, so the false discovery rate tends to be low even for OLS with no correction. Yet in the lower right panel we continue to see the costly loss of statistical power suffered by the BY correction.

In summary, EB accomplishes a flexible MT adjustment by adapting to the data generating process. When discoveries are rare so that there is a comparatively high likelihood of false discovery, EB imposes heavy shrinkage and behaves similarly to the conservative BY correction. In this case, the benefit of conservatism costs little in terms of power exactly because true discoveries are rare. Yet when discoveries are more likely, EB behaves more like uncorrected OLS, giving it high power to detect discoveries and suffering little in terms of false discoveries because true positives abound.

The limitations of frequentist MT corrections are well studied in the statistics literature.

Berry and Hochberg (1999) note that "these procedures are very conservative (especially in large families) and have been subjected to criticism for paying too much in terms of power for achieving (conservative) control of selection effects." The reason is that, while inflating confidence intervals and p-values indeed reduces the discovery of false positives, it also reduces power to detect true positives.

Much of the discussion around MT adjustments in the finance literature fails to consider the loss of power associated with frequentist corrections. But, as Greenland and Hofman (2019) point out, this tradeoff should be a first-order consideration for a researcher navigating multiple tests, and frequentist MT corrections tend to place an implicit cost on false positives that can be unreasonably large. Unlike some medical contexts for example, there is no obvious motivation for asymmetric treatment of false positives and missed positives in factor research. The finance researcher may be willing to accept the risk of a few false discoveries to avoid missing too many true discoveries. In statistics, this is sometimes discussed in terms of an (abstract) cost of Type I versus Type II errors, ²⁶ but in finance we can make this cost concrete: We can look at the profit of trading on the discovered factors, where the cost of false discoveries is then the resulting extra risk and money lost (Section 3.3).

2 A New Public Data Set of Global Factors

We study a global dataset with 153 factors in 93 countries. In this section, we provide a brief overview of our data construction. We have posted the code along with extensive documentation detailing every implementation choice that we make for each factor.²⁷

Factors

The set of factors we study is based on the exhaustive list compiled by Hou et al. (2020). They study 202 different characteristic signals from which they build 452 factor portfolios. The

²⁶As Greenland and Robins (1991) point out, "Decision analysis requires, in addition to the likelihood function, a loss function, which indicates the cost of each action under the various possible values for the unknown parameter (benefits would be expressed as negative costs). Construction of a loss function requires one to quantify costs in terms of dollars, lives lost, or some other common scale."

²⁷It is available at https://jkpfactors.com/ and at https://github.com/bkelly-lab/ReplicationCrisis.

proliferation is due to treating 1, 6, and 12-month holding periods for a given characteristic as different factors, and due to their inclusion of both annual and quarterly updates of some accounting-based factors. In contrast, we focus on a 1-month holding period for all factors, and we only include the version that updates with the most recent accounting data (which could be either annual or quarterly). Lastly, we exclude a small number of factors for which data is not available globally. This gives us a set of 180 feasible global factors. For this set, we exclude factors based on industry or analyst data because they have comparatively short samples.²⁸ This leaves us with 138 factors. Finally, we add 15 factors studied in the literature that were not included in Hou et al. (2020).

For each characteristic, we build the 1-month holding period factor return within each country as follows. First, in each country and month, we sort stocks into characteristic terciles (top/middle/bottom third) with breakpoints based on non-micro stocks in that country.²⁹ For each tercile, we compute its "capped value weight" return, meaning that we weight stocks by their market equity winsorized at the NYSE 80th percentile. This construction ensures that tiny stocks have tiny weights and any one mega stock does not dominate a portfolio, seeking to create tradable, yet balanced, portfolios.³⁰ The factor is then defined as the high-tercile return minus the low-tercile return, corresponding to the excess return of a long-short zero-net-investment strategy. The factor is long (short) the tercile identified by the original paper to have the highest (lowest) expected return.

We scale all factors such that their monthly idiosyncratic volatility is $10\%/\sqrt{12}$ (i.e., 10% annualized), which ensures cross-sectional stationarity and a prior that factors are similar in terms of their information ratio (i.e., appraisal ratio). Finally, we compute each factor's $\hat{\alpha}^i$ via an OLS regression on a constant and the corresponding region's market portfolio.

For a factor return to be non-missing, we require that it has at least 5 stocks in each of

 $^{^{28} \}rm{Global}$ industry codes (GICS) are only available from 2000 and I/B/E/S data from the mid-1980's (but coverage in early years is somewhat sparse).

²⁹Specifically, we start with all non-micro stocks in a country (i.e., larger than NYSE 20th percentile) and sort them into three groups of equal numbers of stocks based on the characteristic, say book-to-market. Then we distribute the micro-cap stocks into the three groups based on the same characteristic breakpoints. This process ensures that the non-micro stocks are distributed equally across portfolios, creating more tradable portfolios.

³⁰For robustness, Figure C.1 of the appendix reports our replication results to using standard, uncapped value weights to construct factors.

the long and short legs. We also require a minimum of 60 non-missing monthly observations for each country-specific factor for inclusion in our sample. When grouping countries into regions (US, developed ex. US, and emerging) we use the MSCI development classification as of January 7th 2021. When aggregating factors across countries, we use capitalization-weighted averages of the country-specific factors. For the developed and emerging market factors, we require that at least three countries have non-missing factor returns.

Clusters

We group factors into clusters using hierarchical agglomerative clustering (Murtagh and Legendre, 2014). We define the distance between factors as one minus their pairwise correlation and use the linkage criterion of Ward (1963). The correlation is computed based on CAPM-residual returns of US factors signed as in the original paper. Appendix Figure I.1 shows the resulting dendrogram, which illustrates the hierarchical clusters identified by the algorithm. Based on the dendrogram, we choose 13 clusters that demonstrate a high degree of economic and statistical similarity. The cluster names indicate the types of characteristics that dominate each group: Accruals*, Debt Issuance*, Investment*, Leverage*, Low risk, Momentum, Profit Growth, Profitability, Quality, Seasonality, Size*, Skewness*, and Value, where the star (*) indicates that these factors bet against the corresponding characteristic (e.g., accrual factors go long stocks with low accruals while shorting those with high accruals). Appendix Figure I.2 shows that the average within-cluster pairwise correlation is above 0.5 for 9 out of 13 clusters, and Table J.1 provides details on the cluster assignment, sign convention, and original publication source for each factor.

Data and Characteristics

Return data is from CRSP for the US (beginning in 1926) and from Compustat for all other countries (beginning in 1986 for most developed countries).³¹ All accounting data is from Compustat. For international data, all variables are measured in US dollars (based on exchange rates from Compustat) and excess returns are relative to the US treasury bill rate.

 $^{^{31}}$ Appendix Table J.3 shows start date and other information for all countries included in our dataset.

To alleviate the influence of data errors in the international data, we winsorize returns from Compustat at 0.1% and 99.9% each month.

We restrict our focus to common stocks that are identified by Compustat as the primary security of the underlying firm and assign stocks to countries based on the country of their exchange.³² In the US, we include delisting returns from CRSP. If a delisting return is missing and the delisting is for a performance-based reason, we set the delisting return to -30% following Shumway (1997). In the global data, delisting returns are not available, so all performance-based delistings are assigned a return of -30%.

We build characteristics in a consistent way, that sometimes deviates from the exact implementation used in the original reference. For example, for characteristics that use book equity, we always follow the method in Fama and French (1993). Furthermore, we always use the most recent accounting data, whether annual or quarterly. Quarterly income and cash flow items are aggregated over the previous four quarters to avoid distortions from seasonal effects. We assume that accounting data is available four months after the fiscal period end. When creating valuation ratios, we always use the most recent price data following Asness and Frazzini (2013). Section K in the internet appendix contains a detailed documentation of our data set.

Empirical Bayes Estimation

We estimate the hyperparameters and the posterior alpha distributions of our Bayesian model via EB. Appendix B provides details on the EB methodology and the estimated parameters.

3 Empirical Assessment of Factor Replicability

We now report replication results for our global factor sample. We first present an internal validity analysis by studying US factors over the full sample. Then we analyze external validity in the global cross section and in the time series (post-publication factor returns).

³²Compustat identifies primary securities in the US, Canada and rest of the world. This means that some firms can have up to three securities in our data set. In practice, the vast majority of firms (97%) only have one security in our sample at a given point in time.

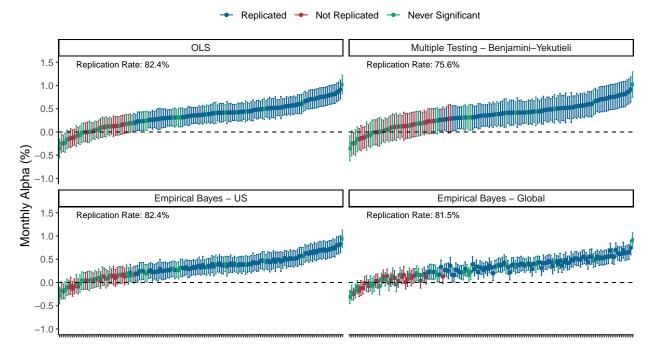


Figure 4: Alpha Distributions for US Factors

Note: The figure reports point estimates and confidence intervals for US factors. The upper left reports OLS estimates. The upper right uses the OLS point estimate but adjusts the confidence interval following the BY procedure. The lower left panel shows our EB posterior confidence intervals using only US data. The lower right continues to show EB results for US factors, but estimates the US factor posterior from global data rather than US-only data. Blue (red) confidence intervals correspond to factors that were significant in the original study in the literature and that we find significant (insignificant) based on the method in each panel. Green intervals correspond to factors that the original study find insignificant or do not evaluate in terms of average return significance. The order of factors is the same in all panels and is arranged from lowest OLS alpha to highest. Table J.2 shows the factor names arranged in the same order.

3.1 Internal Validity

We report full sample performance of US factors in Figure 4. Each panel illustrates the CAPM alpha point estimate of each factor corresponding to the dot at the center of the vertical bars. Vertical bars represent the 95% confidence interval for each estimate. Bar colors differentiate between three types of factors. Blue shows factors that are significant in the original study and remain significant in our full sample. Red shows factors that are significant in the original study but are insignificant in our test. Green shows factors that are not significant in the original study, but are included in the sample of Hou et al. (2020).

The four panels in Figure 4 differ in how the alphas and their confidence intervals are estimated. The upper left panel reports the simple OLS estimate of each alpha, $\hat{\alpha}_{ols}$, and

the 95% confidence intervals based on unadjusted standard errors, $\hat{\alpha}_{\text{ols}} \pm 1.96 \times SE_{\text{ols}}$. The factors are sorted by OLS $\hat{\alpha}$ estimate, and we use this ordering for the other three panels as well. We find that the OLS replication rate is 82.4%, computed as the number of blue factors (98) divided by the sum of red and blue factors (119). Based on OLS tests, factors are highly replicable.

The upper right panel repeats this analysis using the MT adjustment of Benjamini and Yekutieli (2001) (denoted BY), which is advocated by Harvey et al. (2016) and implemented by Hou et al. (2020). This method leaves the OLS point estimate unchanged, but inflates the p-value. We illustrate this visually by widening the alpha confidence interval. Specifically, we find the BY-implied critical value³⁴ in our sample to be a t-statistic of 2.7, and we compute the corresponding confidence interval as $\hat{\alpha}_{\text{ols}} \pm 2.7 \times SE_{\text{ols}}$. We deem a factor as significant according to the BY method if this interval lies entirely above zero. Naturally, this widening of confidence intervals produces a lower replication rate of 75.6%. However, the BY correction does not materially change the OLS-based conclusion that factors appear highly replicable.

The lower left panel is based on our empirical Bayes estimates using the full sample of US factors. For each factor, we use Proposition 4 to compute its posterior mean, $E(\alpha_i|(\hat{\alpha}_j)_{j\text{ any US factor}})$, shown as the dot at the center of the confidence interval. These dots change relative to the OLS estimates, in contrast to BY and other frequentist MT methods that only change the size of the confidence intervals. We also compute the posterior volatility to produce Bayesian confidence intervals, $E(\alpha_i|(\hat{\alpha}_j)_{j\text{ any US factor}}) \pm 1.96 \times \sigma(\alpha_i|(\hat{\alpha}_j)_{j\text{ any US factor}})$. The replication rate based on Bayesian model estimates is 82.4%, larger than BY and, coincidentally, the same as the OLS replication rate. This replication rate has a built-in conservatism from the zero-alpha prior, and it further accounts for the multiplicity of factors because each factor's posterior depends on all of the observed evidence in the US (not just own-factor performance).

The lower right panel again reports EB estimates for US factors, but now we allow the

³³We define $SE_{\rm ols}$ as the diagonal of the alpha covariance matrix $\hat{\Sigma}$, which we estimate according to Appendix B.

 $^{^{34}}$ We compute the BY-implied critical value as the average of the t-statistic of the factor that is just significant based on BY (the factor with the highest BY-adjusted p-value below 5%) and the t-statistic of the factor that is just insignificant (the factor with the lowest BY-adjusted p-value above 5%).

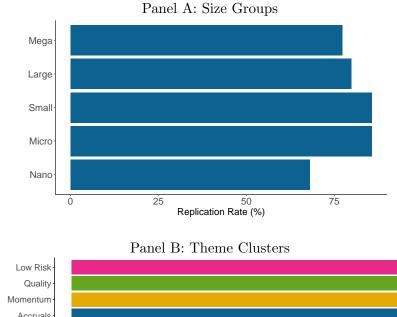
posterior to depend not just on US data, but on data from all over the world. That is, we compute the posterior mean and variance for each US factor conditional on the alpha estimates for all factors in all regions. The resulting replication rate is 81.5%, which is slightly lower than the EB replication rate using only US data. Some posterior means are reduced due to the fact that some factors have not performed as well outside the US, which affects posterior means for the US through the dependence among global alphas. For example, when the Bayesian model seeks to learn the true alpha of the "US change in book equity" factor, the Bayesian's conviction regarding positive alpha is reduced by taking into account that the international version of this factor has underperformed the US version.³⁵

To further assess internal validity, we investigate the replication rate for US factors when those factors are constructed from subsamples based on stock size. One of the leading criticisms of factor research replicability is that results are driven by illiquid small stocks whose behavior in large part reflects market frictions and microstructure as opposed to just economic fundamentals or investor preferences. In particular, Hou et al. (2020) argue that they find a low replication rate because they limit the influence of micro-caps. We find that factors demonstrate a high replication rate throughout the size distribution. Panel A of Figure 5 reports replication rates for US size categories shown in the five bars: mega stocks (largest 20% of stocks based on NYSE breakpoints), large stocks (market capitalization between the 80^{th} and 50^{th} percentile of NYSE stocks), small stocks (between the 50^{th} and 20^{th} percentile), micro stocks (between the 20^{th} and 1^{st} percentile), and nano stocks (market capitalization below the 1^{st} percentile).

We see that the EB replication rates in mega and large stock samples are 77.3% and 79.8%, respectively. This is only marginally lower than the overall US sample replication rate of 82.4%, indicating that criticisms of factor replicability based on arguments around stock size or liquidity are largely groundless. For comparison, small, micro, and nano stocks deliver replication rates of 85.7%, 85.7% and 68.1%, respectively.

In Panel B of Figure 5, we report US factor replication rates by theme cluster. 11 out of 13

 $^{^{35}}$ To provide a few more details on this example, the US factor based on annual change in book equity (be_gr1a) has a posterior volatility of 0.095% using only US data and 0.077% using global data, leading to a tighter confidence interval with the global data. However, the posterior mean is 0.22% using only US data and 0.13% using global data.



Low Risk
Quality
Momentum
Accruals

Debt Issuance
Investment
Value
Skewness
Profit Growth
Profitability
Seasonality
Size
Low Leverage

0 25 50 75 100

Replication Rate (%)

Figure 5: US Replication Rates By Size Group and Theme Cluster

Note: Panel A reports replication rates for US factors formed from subsamples defined by stocks' market capitalization using our EB method. Panel B reports replication rates for US factors in each theme cluster.

themes are replicable with a rate of 50% or better, with the exceptions being the low leverage and size themes. To understand these exceptions, we note that size factors are stronger in emerging markets (bottom panel of Figure G.1) and among micro and nano stocks (bottom panels of Figure G.2). The theoretical foundation of the size effect is a compensation for market illiquidity (Amihud and Mendelson, 1986) and market liquidity risk (Acharya and Pedersen, 2005). Theory predicts that the illiquidity (risk) premium should be the same order of magnitude as the differences in trading costs and these differences are simply much larger in emerging markets and among micro stocks.

Another reason why some factors and themes appear insignificant is that we are not

accounting for other factors. Factors published after 1993 are routinely benchmarked to the Fama-French three-factor model (and, more recently, to the updated five-factor model). Some factors are insignificant in terms of raw return or CAPM alpha, but their alpha becomes significant after controlling for other factors. This indeed explains the lack of replicability for the low leverage theme. While CAPM alphas of low leverage factors are insignificant, we find that it is one of the best performing themes once we account for multiple factors (see Section 3.4 below).

3.2 External Validity

We find a high replication rate in our full-sample analysis, indicating that the large majority of factors are reproducible at least in-sample. We next study the external validity of these results in international data and in post-publication US data.

Global Replication

Figure 6 shows corresponding replication rates around the world. We report replication rates from four testing approaches: (1) OLS with no adjustment; (2) OLS with Benjamini-Yekutieli MT adjustment; (3) the EB posterior conditioning only on factors within a region ("Empirical Bayes – Region"); and (4) EB conditioning on factors in all regions ("Empirical Bayes – All"). Even when using all global data to update the posterior of all factors, the reported Bayesian replication rate applies only to the factors within the stated region.

The first set of bars establishes a baseline by showing replication rates for the US sample, summarizing the results from Figure 4. The next two sets of bars correspond to the developed ex. US sample and the emerging markets sample, respectively.³⁶ Each region factor is a capitalization-weighted average of that factor among countries within a given region, and the replication rate describes the fraction of significant CAPM alphas for these regional factors.

OLS replication rates in developed and emerging markets are generally lower than in

³⁶The developed and emerging samples are defined by the MSCI development classification and include 23 and 27 countries, respectively. The remaining 43 countries in our sample that are classified as neither developed nor emerging by MSCI do not appear in our developed and emerging region portfolios, but they are included in the "world" versions of our factor portfolios.

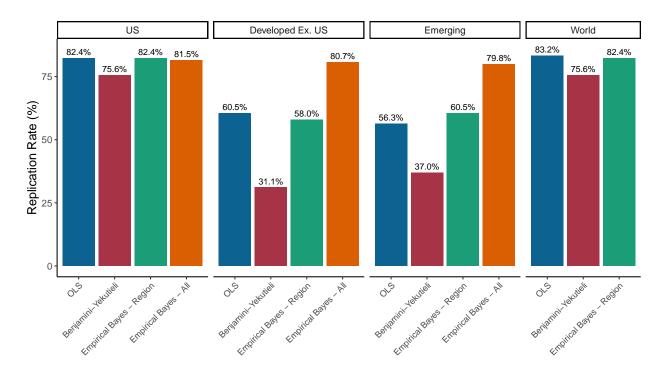


Figure 6: Replication Rates in Global Data

Note: We report replication rates for factors in three global regions (US, developed ex. US, and emerging) and for the world as a whole. A factor in a given region is the capitalization-weighted average factor for countries in that region. We report OLS replication rates with no adjustment and with Benjamini-Yekutieli multiple testing adjustment. We also report replication rates based on the empirical Bayes posterior. We consider two EB methods. In both methods, the replication rate refers only to factors within the region of interest, but the posterior is computed by conditioning either on data from that region alone ("Empirical Bayes – Region") or on the full global sample ("Empirical Bayes – All"). We deem a factor successfully replicated if its 95% confidence interval excludes zero for a given method.

the US, and the frequentist Benjamini-Yekutieli correction has an especially large negative impact on replication rate. This is a case in which the Bayesian approach to MT is especially powerful. Even though the alphas of all regions are shrunk toward zero, the global information set helps EB achieve a high degree of precision, narrowing the posterior distribution around the shrunk point estimate. We can see this in increments. First, the EB replication rate using region-specific data ("Empirical Bayes – Region" in the figure) is just below the OLS replication rate but much higher than the Benjamini-Yekutieli rate. When the posterior leverages global data ("Empirical Bayes – All" in the figure), the replication rate is higher still, reflecting the benefits of sharing information across regions, as recommended by the dependence among alphas in the hierarchical model.

Finally, we use the global model to compute, for each factor, the capitalization-weighted

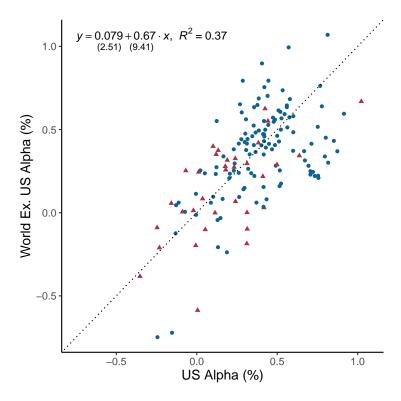


Figure 7: US Factor Alphas Versus World Ex. US

Note: The figure compares OLS alphas for US factors versus their international counterpart. Each world ex. US factor is a capitalization-weighted average of the factor in all other countries of our sample. Blue points correspond to factors that were significant in the original study in the literature, while red points are those for which the original paper did not find a significant effect (or did not study the factor in terms of average return significance). The dotted line is the 45° line. The figure also reports a regression of world ex. US alpha on US alpha.

average alpha across all countries in our sample ("World" in the figure). Using data from around the world, we find a Bayesian replication rate of 82.4%.

Why do international OLS replication rates differ from the US? This is due primarily to the the fact that foreign markets have shorter time samples. Point estimates are similar in magnitude for the US and international data. Figure 7 shows the alpha of each US factor against the alpha of the corresponding factor for the world ex. US universe. The data cloud aligns closely with the 45° line, demonstrating the close similarity of alpha magnitudes in the two samples. But shorter international samples widen confidence intervals, and this is the primary driver of the drop in OLS replication rates outside the US.

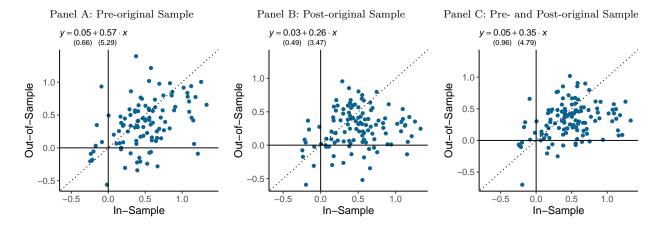


Figure 8: In-Sample versus Out-of-Sample Alphas for US Factors

Note: The figure plots OLS alphas for US factors during the in-sample period (i.e., the period studied in the original publication) versus out-of-sample alphas. In Panel A, out-of-sample is the time period before the in-sample period. In Panel B, out-of-sample is the time period before the in-sample period. In Panel C, out-of-sample includes both the time period before and after the in-sample period. We require at least five years of out-of-sample data for a factor to be included, amounting to 102, 115 and 119 factors in panel A, B and C. The figure also reports feasible GLS estimates of out-of-sample alphas on in-sample alphas. To implement feasible GLS, we assume that the error variance-covariance matrix is proportional to the full-sample CAPM residual variance-covariance matrix, $\hat{\Sigma}/T$, described in section B. The dotted line is the 45° line.

Time Series Out-of-Sample Evidence

McLean and Pontiff (2016) document the intriguing fact that, following publication, factor performance tends to decay. They estimate an average post-publication decline of 58% in factor returns. In our data, the average in-sample alpha is 0.49% per month and the average out-of-sample alpha is 0.26% when looking post-original sample, implying a decline of 47%.

We gain further economic insight by looking at these findings cross-sectionally. Figure 8 makes a cross-sectional comparison of the in-sample and out-of-sample alphas of our US factors. The in-sample period is the sample studied in the original reference. The out-of-sample period in Panel A is the time period before the start of in-sample period, while in Panel B it is the period following the in-sample period. Panel C defines out-of-sample as the combined data from the periods before and after the originally studied sample. We find that 82.6% of the US factors that were significant in the original publication also have positive returns in the pre-original sample, 83.3% are positive in the post-original sample, and 87.4% are positive in the combined out-of-sample period. When we regress out-of-sample alphas on in-sample alphas using GLS, we find a slope coefficient of 0.57, 0.26, and 0.35 in Panels

A, B, and C, respectively. The slopes are highly significant (ranging from t = 3.5 to t = 5.3) indicating that in-sample alphas contain something "real" rather than being the outcome of pure data mining, as factors that performed better in-sample also tend to perform better out-of-sample.

The significantly positive slope allows us to reject the hypothesis of "pure alpha-hacking," which would imply a slope of zero, as seen in Proposition 1. Further, the regression intercept is positive, while alpha-hacking of the form studied in Proposition 1 would imply a negative intercept.

That the slope coefficient is positive and less than one is consistent with basic Bayesian logic of equation (4). As we emphasize in Section 1, a Bayesian would expect at least some attenuation in out-of-sample performance. This is because the published studies report the OLS estimate, while Bayesian beliefs shrink the OLS estimate toward the zero-alpha prior. More specifically, with no alpha hacking or arbitrage, the Bayesian expects a slope of approximately 0.9 using equation (5) and our EB hyperparameters (see appendix Table B.1).³⁷ Hence, the slope coefficients in Figure 8 are too low relative to this Bayesian benchmark. In addition to the moderate slope, there is evidence that the dots in Figure 8 have a concave shape (as seen more clearly in appendix Figure D.2). These results indicate that, while we can rule out pure alpha-hacking (or p-hacking), there is some evidence that the highest in-sample alphas may either be data-mined or arbitraged down.

From the Bayesian perspective, another interesting evaluation of time series external validity is to ask whether the new information contained in out-of-sample data moves the posterior alpha toward zero or not. Imagine a Bayesian observing the arrival of factor data in real time. As new data arrives, she updates her beliefs for all factors based on the information in the full cross section of factor data. In the top panel of Figure 9, we show how the Bayesian's posterior of the average alpha would have evolved in real time.³⁸ We focus on all the World factors that are available since at least 1955 and significant in the original

 $[\]overline{^{37}}$ The slope is $\kappa = 1/(1+\sigma^2/(T\tau^2)) = 0.9$, where $\sigma^2 = 10\%^2/12$, the average in-sample period length is T = 420 months, and $\tau^2 = \tau_c^2 + \tau_w^2 = (0.35\%)^2 + (0.21\%)^2 = (0.41\%)^2$.

38Here we keep τ_c and τ_w fixed at their full-sample values of 0.37% and 0.23% to mimic the idea of given

³⁸Here we keep τ_c and τ_w fixed at their full-sample values of 0.37% and 0.23% to mimic the idea of given decision maker who starts with a given prior and updates this view based on new data, while keeping the prior fixed. Figure D.3 shows that the figure is almost the same with rolling estimates of τ_c and τ_w , and Figure D.4 shows that this consistency arises because the rolling estimates are relatively stable.

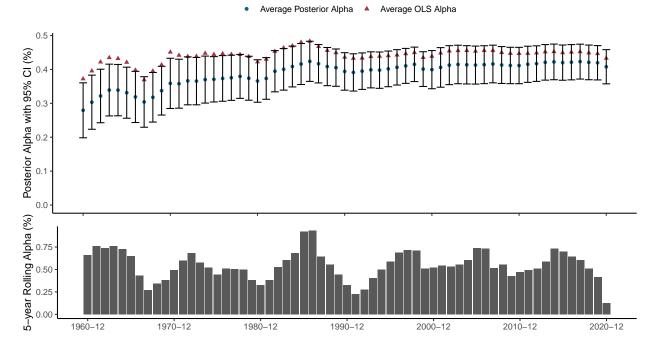


Figure 9: World Factor Alpha Posterior Distribution Over Time

Note: The top panel reports the CAPM alpha and 95% posterior confidence interval for an equal-weighted portfolio of World factors based on EB posteriors re-estimated in December each year. That is, each blue dot is $E(\frac{1}{N}\sum_i \alpha^i|$ data until time t) and the vertical lines are ± 2 times the posterior volatility. Triangles show average OLS alpha at each point in time, $\frac{1}{N}\sum_i \hat{\alpha}^i_{t^i_0,t}$, estimated using data through date t. The bottom panel reports the average monthly alpha for all factors in a rolling 5-year window. The results are based on factors found to be significant in the original paper with data available since 1955.

paper. Starting in 1960, we re-estimate the hierarchical model using the empirical Bayes estimator in December of each year. The plot shows the CAPM alpha and corresponding 95% confidence interval of an equal-weighted portfolio of the available factors. The posterior mean alpha becomes relatively stable from the mid 1980s, around 0.4% per month. And, as data evidence has accumulated over time, the confidence interval narrows by a third, from about 0.16% wide in 1960 to 0.10% in 2020.

To understand the posterior alpha, Figure 9 also shows the average OLS alpha as triangles and the bottom panel in Figure 9 reports the rolling 5-year average monthly alpha among all these factors. We see that the EB posterior is below the OLS estimate, which occurs because the Bayesian posterior is shrunk toward the zero prior. Naturally, periods of good performance increase the posterior mean as well as the OLS estimate, and vice versa for poor performance. Over time, the OLS estimate moves nearer to the Bayesian posterior mean.

To further understand why the posterior alpha is relatively stable with a tightening confidence interval, consider the following simple example. Suppose a researcher has T=10 years of data for factors with an OLS alpha estimate of $\hat{\alpha}=10\%$ with standard error σ/\sqrt{T} . Further, assume their zero-alpha prior is equally as informative as their 10-year sample (i.e., $\tau=\sigma/\sqrt{T}$). Then the shrinkage factor is $\kappa=1/2$ using equation (5). So, after observing the first ten years with $\hat{\alpha}=10\%$, the Bayesian expects a future alpha of $E(\alpha|\hat{\alpha})=5\%$ (equation (4)). What happens if this Bayesian belief is confirmed by additional data, namely that the factor realizes an alpha of 5% over the next 10 years? In this case, the full-sample OLS of alpha is $\hat{\alpha}=7.5\%$, but now the shrinkage factor becomes $\kappa=2/3$ because the sample length doubles, T=20. This results in a posterior alpha of $E(\alpha|\hat{\alpha})=7.5\% \cdot 2/3=5\%$. Naturally, when beliefs are confirmed by additional data, the posterior mean does not change. Nevertheless, we learn something from the additional data, because our conviction increases as the posterior variance is reduced. If $\sigma=0.1$, the posterior volatility $\sqrt{\text{Var}(\alpha|\hat{\alpha})}=\sigma\sqrt{\frac{\kappa}{T}}$ goes from 2.2% with 10 years of data to 1.8% with 20 years of data, and the confidence interval, $[E(\alpha|\hat{\alpha})\pm2\sqrt{\text{Var}(\alpha|\hat{\alpha})}]$, is reduced from [0.5%, 9.5%] to [1.3%, 8.7%].

3.3 Bayesian Multiple Testing

A great advantage of Bayesian methods for tackling challenges in multiple testing is that, from the posterior distribution, we can make explicit probability calculations for essentially any inferential question. We simulate from our EB posterior to investigate the false discovery and family-wise error rates among the set of global factors that were significant in the original study. We define a false discovery as a factor where we claim that the alpha is positive, but where the true alpha is negative.³⁹

First, based on Proposition 5, we calculate the Bayesian FDR in our sample as the average posterior probability of a false discovery, p-null, among all discoveries. We find that $FDR^{Bayes} = 0.1\%$, meaning that we expect roughly one discovery in 1000 to be a false positive given our Bayesian hierarchical model estimates. The posterior standard error for

³⁹In particular, we define a discovery as a factor for which the posterior probability of the true alpha being negative is less than 2.5%. With this definition, we start with 153 world factors, then focus on the 119 factors that were significant in the original studies, and, out of these, 98 are considered discoveries.

FDR^{Bayes} is 0.3% with a confidence interval of [0,1%]. In other words, the model generates a highly conservative MT adjustment in the sense that once a factor is found to be significant, we can be relatively confident that the effect is genuine.

We can also use the posterior to make other inference calculations. We compute the FWER, which we define as the probability of at least one false discovery. We simulate 1,000,000 draws of the vector of alphas that were deemed to be discoveries from the EB posterior and compute

$$FWER^{Bayes} = \frac{1}{1,000,000} \sum_{s=1}^{1,000,000} 1_{\{n_s \ge 1\}} = 5.5\%$$

where n_s is the number of false discoveries in simulation s. In other words, the probability of at least one alpha having the wrong sign is 5.5%. The FWER^{Bayes} is naturally much higher than the FDR^{Bayes} given the extreme conservatism built into the FWER's definition of false discovery. Whether it is too high is subjective. A nice aspect of our approach is that a researcher can control the FWER^{Bayes} as desired. For example, using a t-statistic threshold of 2.78 rather than 1.96 leads to FWER^{Bayes} = 0.8%.

From the posterior, we can also compute the expected fraction of discovered factors that are "true," which is in general different than the replication rate. The replication rate is the fraction of factors having $E(\alpha_i|\text{data})/\sigma(\alpha_i|\text{data}) > 1.96$, while the expected fraction of true factors is $\frac{1}{n}\sum_i E(1_{\alpha_i>0}|\text{data}) = \frac{1}{n}\sum_i Pr(\alpha_i>0|\text{data})$. The replication rate gives a conservative take on the number of true factors—the expected fraction of true factors is typically higher than the replication rate. To understand this conservatism, consider an example in which all factors have a 90% posterior probability of being true. These would all individually be counted as "not replicated," but they would contribute to a high expected fraction of true factors. Indeed, we estimate that the expected fraction of factors with truly positive alphas is 94% (with a posterior standard error of 1.3%), notably higher than our estimated replication rate.

Economic Benefits of More Powerful Tests

MT adjustments should ultimately be evaluated by whether they lead to better decisions. It is important to balance the relative costs of false positives versus false negatives, and the appropriate tradeoff depends on the context of the problem (Greenland and Hofman, 2019). We apply this general principle in our context by directly measuring costs in terms of investment performance.

Specifically, we can compute the difference in out-of-sample investment performance from investing using factors chosen with different methods. We compare two alternatives. One is the BY decision rule advocated by Harvey et al. (2016), which is a frequentist MT method that successfully controls false discoveries relative to OLS, but in doing so sacrifices power (the ability to detect true positives). The second alternative is our EB method, whose false discovery control typically lies somewhere between BY and unadjusted OLS. EB uses the data sample itself to decide whether its discoveries should behave more similarly to BY or to unadjusted OLS.

For investors, the optimal decision rule is the one that leads to the best performance out-of-sample. For the most part, the set of discovered factors for BY and EB coincide. It is only in marginal cases where they disagree which, in our sample, occurs when EB makes a discovery that BY deems insignificant. Therefore, to evaluate MT approaches in economic terms, we track the out-of-sample performance of factors included by EB but excluded by BY. If the performance of these is negative on average, then the BY correction is warranted and preferred by the investor.

We find that the out-of-sample performance of factors discovered by EB but not BY is positive on average and highly significant. The alpha for these marginal cases is 0.35% per month among US factors $(t=5.1).^{40}$ This estimate suggests that the BY decision rule is too conservative. An investor using the rule would fail to invest in factors that subsequently have a high out-of-sample return.

Another way to see that the BY decision rule is too conservative comes from the connec-

 $^{^{40}}$ For the developed ex. US sample, the monthly alpha for marginal cases is 0.24% per month (t = 5.3), and for the emerging sample it is 0.27% (t = 3.7), in favor of the EB decision rule. Appendix Table E.1 reports additional details for this analysis.

tion between Sharpe ratio and t-statistics: $t = SR\sqrt{T}$. If we have a factor with an annual Sharpe ratio of 0.5, an investor using the 1.96 cutoff would in expectation invest in the factor after 15 years. An investor using the 2.78 cutoff, would not start investing until observing the factor for 31 years.

Addressing Unobserved Factors, Publication Bias, and other Biases

A potential concern with our replication rate is that the set of factors that make it into the literature is a selected sample. In particular, researchers may have tried many different factors, some of which are observed in the literature, while others are unobserved because they never got published. Unobserved factors may have worse average performance if poor performance makes publication more difficult or less desirable. Alternatively, unobserved factors could have strong performance if people chose to trade on them in secret rather than publishing them. Either way, we next show how unobserved factors can be addressed in our framework.

The key insight is that the performance of factors across the universe of observed and unobserved factors is captured in our prior parameters τ_c, τ_w . Indeed, large values of these priors correspond to a large dispersion of alphas (that is, a lot of large alphas "out there") while small values means that most true alphas are close to zero. Therefore, smaller τ 's lead to a stronger shrinkage toward zero for our posterior alphas, leading to fewer factor "discoveries" and a lower replication rate. Figure 10 shows how our estimated replication rate depends on the most important prior parameter, τ_c , based on the τ_w that we estimated from the data.⁴¹

In Figure 10, we show how the replication rate varies with τ_c in precise quantitative terms. Note that while the replication rate indeed rises with τ_c , the differences are small in magnitude across a large range of τ_c values, demonstrating robustness of our conclusions about replicability.

This stable replication rate in Figure 10 also suggests that the replication rate among the observed factors would be similar even if we had observed the unobserved factors. The figure highlights several key values of τ_c : Both the value of τ_c that we estimated from the

⁴¹ Figure F.1 in the appendix shows that the results are robust to alternative values of τ_w .

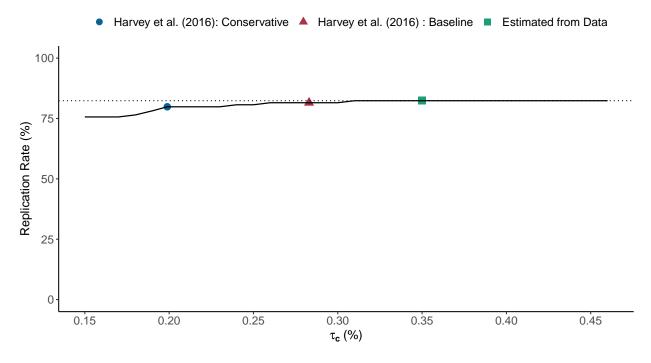


Figure 10: Replication Rate with Prior Estimated in Light of Unobserved Factors

Note: The figure shows how the replication rate in the US varies when changing the τ_c parameter. The τ_w parameter is fixed at the estimate value of 0.21%. The dotted line shows our replication rate of 82.4%. The green square, highlights the value estimated in the data $\tau_c = 0.35\%$. The red triangle and the blue circle highlights values that are found by estimating the empirical Bayes model according to assumptions about unobserved factors from Harvey et al. (2016). The values are $\tau_c = 0.28\%$ in the baseline scenario and $\tau_c = 0.20\%$ in the conservative scenario. A description of this approach can be found in Appendix F.

observed data (as explained in Appendix B) and values that adjust for unobserved data in different ways.

We adjust τ_c for unobserved factors as follows. We simulate a data set that proxies for the full set of factors in the population (including those unobserved), and then estimate the τ 's that match this sample. One set of simulations is constructed to match the baseline scenario of Harvey et al. (2016) (Table 5.A, row 1), which estimates that researchers have tried M=1,297 factors, of which 39.6% of have zero alpha and the rest have a Sharpe ratio of 0.44. We also consider the more conservative scenario of Harvey et al. (2016) (Table 5.B, row 1), which implies that researchers have tried M=2,458 factors, of which 68.3% have zero alpha. Appendix F has more details on these simulations. The result, as seen in Figure 10, is that values of τ_c that correspond to these scenarios from Harvey et al. (2016) still lead to a conclusion of a high replication rate in our factor universe. The replication rate

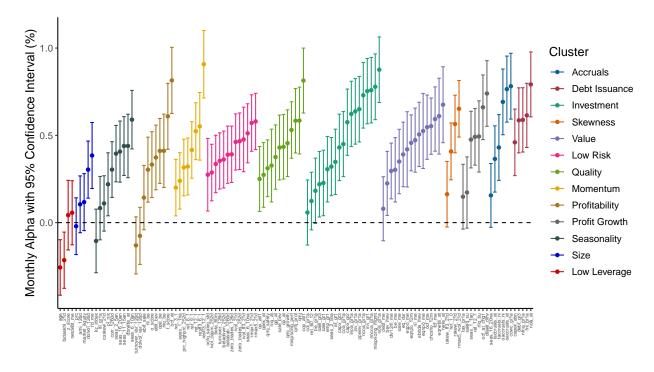


Figure 11: World Alpha Posterior By Factor and Cluster

Note: The figure reports the EB posterior 95% confidence interval for the true alpha of a world factor create as a capitalization weighted average of all country specific factors in our dataset. We only include factors that the original paper finds significant.

is 81.5%, and 79.8% for the prior hyperparameters implied by the baseline and conservative scenario respectively.

A closely related bias is that factors may suffer from alpha-hacking as discussed in Section 1.1 (Proposition 1), which makes realized in-sample factor returns too high. To account for this bias, we estimate the prior hyper-parameters using only out-of-sample data. These estimated values are $\tau_c = 0.27\%$ and $\tau_w = 0.22\%$. These hyper-parameters are similar to those implied by the baseline scenario of Harvey et al. (2016) as seen in Figure 10. With these hyper-parameters, the replication rate is 81.5%.

3.4 Economic Significance of Factors

Which factors (and which themes) are the most impactful anomalies in economic terms? We investigate this question by identifying which factors matter most from an investment performance standpoint.

Figure 11 shows the alpha confidence intervals for all world factors, sorted by the median

posterior alpha within clusters. This illustration is similar to Figure 4, but now we focus on the world instead of the US factors, and here we sort factors into clusters. We also focus on factors that the original studies conclude are significant. We see that world factor alphas tend to be economically large, often above 0.3% per month, and tend to be highly significant, in most clusters. The exception is the low leverage cluster, where we also saw a low replication rate in preceding analyses.

By Region and By Size

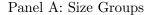
We next consider which factors are most economically important across global regions and across stock size groups. In Panel A of Figure 12, we construct factors using only stocks in the five size subsamples presented earlier in Figure 5; namely mega, large, small, micro, and nano stock samples. For each sample, we calculate cluster-level alphas as the equal-weighted average alpha of rank-weighted factors within the cluster. We see, perhaps surprisingly, that the ordering and magnitude of alphas is broadly similar across size groups. The Spearman rank correlation of alphas for mega caps versus micro caps is 73%. Only the nano stock sample, defined as stocks below the 1^{st} percentile of the NYSE size distribution (which amounted to 458 out of 4356 stocks in the US at the end of 2020), exhibits notable deviation from the other groups. The Spearman rank correlation between alphas of mega caps and nano caps is 36%.

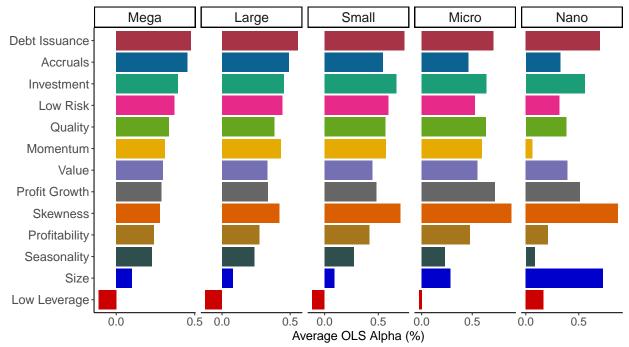
Panel B of Figure 12 shows cluster-level alphas across regions. Again, we find consistency in alphas across the globe, with the obvious standout being the size theme, which is much more important in emerging markets than in developed markets. US factor alphas share a 62% Spearman correlation with the developed ex. US sample, and a 43% correlation with the emerging markets sample.

Controlling for Other Themes

We have focused so far on whether factors (or clusters) possess significant positive alpha relative to the market. The limitation of studying factors in terms of CAPM alpha is that it

⁴²Rank-weighting is similar to equal-weighting and used here to illustrate the performance of typical stocks in each size group. See equation (1) in Asness et al. (2013).





Panel B: Regions

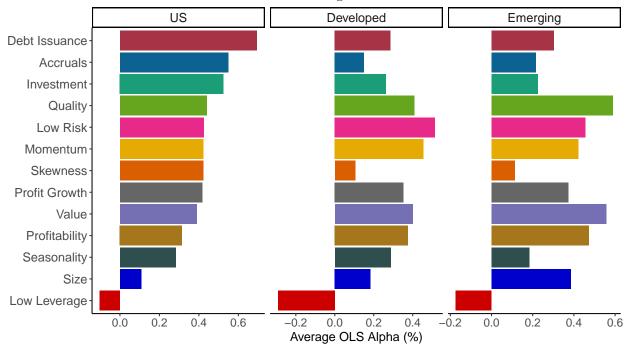


Figure 12: Alphas By Geographic Region and Stock Size Group

Note: The figure reports average cluster-level alphas for factors formed from subsamples defined by different stock market capitalization groups (Panel A) and regions (Panel B).

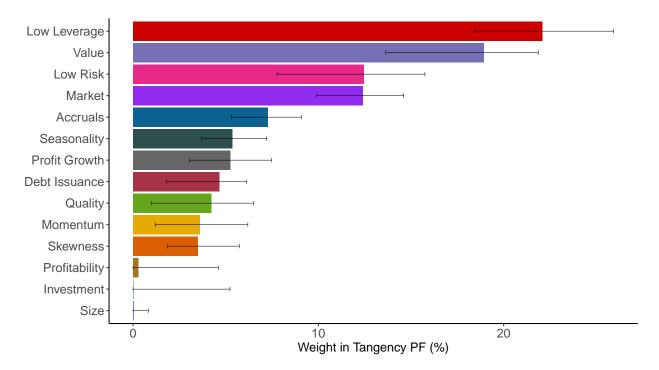


Figure 13: Tangency Portfolio Weights

Note: The return are from the US portfolios. We compute the cluster return as the equal weighted return of all factors with data available at a given point in time. We further add the US market return. We estimate the tangency weights following the method of Britten-Jones (1999) with a non-negativity constraint. The error bars are the 90% confidence intervals based on 10,000 bootstrap samples and the percentile method. The data starts in 1952 to ensure that all cluster have non-missing observations.

does not control for duplicate behavior other than through the market factor. Economically important factors are those that have large impact on an investor's overall portfolio, and this requires understanding which clusters contribute alpha while controlling for all others.

To this end, we estimate cluster weights in a tangency portfolio that invests jointly in all cluster-level portfolios. We test the significance of the estimated weights using the method of Britten-Jones (1999). In addition to our 13 cluster-level factors, we also include the market portfolio as a way of benchmarking factors to the CAPM null. Lastly, we constrain all weights to be non-negative (because we have signed the factors to have positive expected returns according to the findings of the original studies).

Figure 13 reports the estimated tangency portfolio weights and their 90% bootstrap confidence intervals. When a factor has a significant weight in the tangency portfolio, it means that it matters for an investor, even controlling for all the other factors. We see that all but three clusters are significant in this sense. We also see that conclusions about

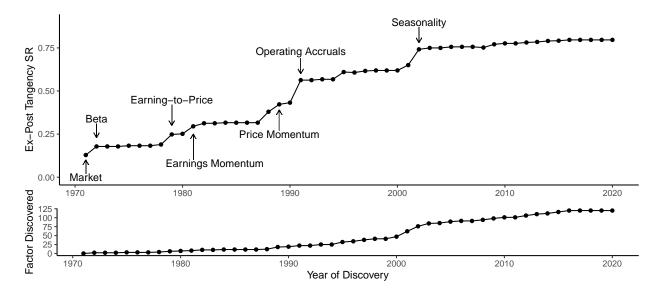


Figure 14: The Evolution of the Tangency Sharpe ratio

Note: The top panel shows the Sharpe ratio on the ex-post tangency portfolio. A factor is included in the tangency portfolio only after the end of the sample in which the factor was studied in the original publication (and we only include factors that were found to be significant in the original paper). We highlight selected factors that significantly improve the optimal portfolio, starting with the market portfolio. We use the longest available balanced US sample, 1972–2020 (that is, when all factors are available).

cluster importance change when clusters are studied jointly. For example, value factors become stronger when controlling for other effects because of their hedging benefits relative to momentum, quality, and low leverage. More surprisingly, the low leverage cluster becomes one of the most heavily weighted clusters, in large part due to its ability to hedge value and low risk factors. The hedging performance of value and low leverage clusters is clearly discernible in Appendix table I.2, which shows the average pairwise correlations among factors within and across clusters.⁴³ Appendix H provides further performance attribution of the tangency portfolio at the factor level.⁴⁴

Evolution of Finance Factor Research

The number of published factors has increased over time as seen in the bottom panel of Figure 14. But, to what extent have these new factors continued to add new insights versus repackaging existing information?

 $^{^{43}}$ Appendix Tables H.1 and H.2 show how tangency portfolio weights vary by region and by size group.

⁴⁴Figure H.3 shows the performance of each cluster in combination with the market portfolio, figure H.4 shows how the optimal portfolio changes when one cluster is excluded and figure H.6 shows the importance of each factor for the optimal portfolio.

To address this question, we consider how the optimal risk-return tradeoff has evolved over time as factors have been discovered. Specifically, Figure 14 computes the monthly Sharpe ratio of the ex-post tangency portfolio that only invests in factors discovered by a certain point in time.⁴⁵ The starting point (on the left) of the analysis is the 0.13 Sharpe ratio of the market portfolio in the US sample 1972-2020 when all factors are available. The ending point (on the right) is the 0.80 Sharpe ratio of the tangency portfolio that invests the optimal weights across all factors over the same US sample period.⁴⁶ In between, we see how the Sharpe ratio of the tangency portfolio has evolved as factors have been discovered. The improvement is gradual over time, but we also see occasional large increases when researchers have discovered especially impactful factors (usually corresponding to new themes in our classification scheme). An example is the operating accruals factor proposed by Sloan (1996), which increased the tangency Sharpe ratio from 0.43 to 0.56. More recently, the seasonality factors of Heston and Sadka (2008) increase the Sharpe ratio from 0.65 to 0.74.

4 Conclusion: Finance Research Posterior

We introduce a hierarchical Bayesian model of alphas that emphasizes the joint behavior of factors and provides a more powerful multiple testing adjustment than common frequentist methods. Based on this framework, we re-visit the evidence on replicability in factor research and come to substantially different conclusions versus the prior literature. We find that US equity factors have a high degree of internal validity in the sense that over 80% of factors remain significant after modifications in factor construction that make all factors consistent, more implementable, while still capturing the original signal (Hamermesh, 2007) and after accounting for multiple testing concerns (Harvey et al., 2016; Harvey, 2017).

We also provide new evidence demonstrating a high degree of external validity in factor research. In particular, we find highly similar qualitative and quantitative behavior in a

⁴⁵We estimate tangency portfolio weights following the method of Pedersen et al. (2021), which offers a sensible approach to mean-variance optimization for high dimensional data. Estimation details are provided in Appendix H.

⁴⁶The high Sharpe ratio partly reflects the fact that we are doing an in-sample optimization. If we instead do a pseudo out-of-sample analysis via cross-validation, we find a monthly Sharpe ratio of 0.56.

large sample of 153 factors across 93 countries as we find in the US. We also show that, within the US, factors exhibit a high degree of consistency between their published insample results and out-of-sample data not considered in the original studies. We show that some out-of-sample factor decay is to be expected in light of Bayesian posteriors based on publication evidence. Therefore, the new evidence from post-publication data largely confirms the Bayesian's beliefs, which has led to relatively stable Bayesian alpha estimates over time.

In addition to providing a powerful tool for replication, our Bayesian framework has several additional applications. For example, the model can be used to correctly interpret out-of-sample evidence, look for evidence of alpha-hacking, compute the expected number of false discoveries and other relevant statistics based on the posterior, analyze portfolio choice taking into account both estimation uncertainty and return volatility, and evaluate asset pricing models.

Finally, the code, data, and meticulous documentation for our analysis are available online. Our large global factor data set and the underlying stock-level characteristics are easily accessible to researchers by using our publicly available code and its direct link to WRDS. Our database will be updated regularly with new data releases and code improvements. We hope that our methodology and data will help promote credible finance research.

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A Appendix: Additional Results and Proofs

Additional Results on Alpha Hacking

We consider the situation where the researcher has in-sample data from time 1 to time T and an out-of-sample (oos) period from time T+1 to $T+T^{oos}$. The researcher may have used alpha-hacking during the in-sample period, but this does not affect the out-of-sample period. The researcher is interested in the posterior alpha based on the total evidence, in-sample and out-of-sample, which is useful for predicting factor performance in a future time period (that is, a time period that is out-of-sample relative to the existing out-of-sample period).

Proposition 6 (Out-of-sample alpha) The posterior alpha based on an in-sample data from time 1 to T with alpha-hacking, and an out-of-sample period from T+1 to $T+T^{oos}$ is given by

$$E(\alpha|\hat{\alpha}, \hat{\alpha}^{oos}) = \kappa^{oos} (w(\hat{\alpha} - \bar{\varepsilon}) + (1 - w)\alpha^{oos})$$
(A.1)

where $w = \frac{\sigma^2/T^{oos}}{\bar{\sigma}^2/T + \sigma^2/T^{oos}} \in (0,1)$ is the relative weight on the in-sample period relative to the out-of-sample period, and $\kappa^{oos} = \frac{1}{1+1/(\tau^2([\bar{\sigma}^2/T]^{-1}+[\sigma^2/T^{oos}]^{-1}))}$ is a shrinkage parameter.

We see that, the more alpha hacking the researcher has done (higher $\bar{\sigma}$), the less weight we put on the in-sample period relative to the out-of-sample period. Further, the in-sample period has the non-proportional discounting due to alpha hacking ($\bar{\varepsilon}$), which we don't have for out-of-sample evidence.

So this result formalizes the idea that an in-sample backtest plus live performance is not the same as a longer backtest. For example, 10 years of backtest plus 10 years of live performance is more meaningful that 20 years of backtest with no live performance. The difference is that the oos-performance is free from alpha-hacking.

Proofs and Lemmas

The proofs make repeated use of the following well-known property of multivariate Normally distributed random variable. If x and y are multivariate Normal:

$$\begin{bmatrix} x \\ y \end{bmatrix} \sim N \left(\begin{bmatrix} \mu_x \\ \mu_y \end{bmatrix}, \begin{bmatrix} \Sigma_{xx} & \Sigma_{yx} \\ \Sigma_{xy} & \Sigma_{yy} \end{bmatrix} \right) \tag{A.2}$$

then the conditional distribution of x given y has the following Normal distribution:

$$x|y \sim N\left(\mu_x + \Sigma_{xy}\Sigma_{yy}^{-1}(y - \mu_y), \Sigma_{xx} - \Sigma_{xy}\Sigma_{yy}^{-1}\Sigma_{yx}\right)$$
(A.3)

The proofs also make use of the following two lemmas.

Lemma 1 For random variables x, y, z, it holds that $E(\operatorname{Var}(x|y, z)) \leq E(\operatorname{Var}(x|y))$ and, if the random variables are jointly normal, then $\operatorname{Var}(x|y, z) \leq \operatorname{Var}(x|y)$.

Lemma 2 Let A be an $N \times N$ matrix for which all diagonal elements equal a and all off-diagonal elements equal b, where $a \neq b$ and $a + b(N - 1) \neq 0$. Then the inverse A^{-1} exists and is of the same form:

$$A = \begin{bmatrix} a & b \\ & \ddots & \\ b & a \end{bmatrix} \quad A^{-1} = \begin{bmatrix} c & d \\ & \ddots & \\ d & c \end{bmatrix}$$
 (A.4)

where
$$c = \frac{a+b(N-2)}{(a-b)(a+b(N-1))}$$
 and $d = \frac{-b}{(a-b)(a+b(N-1))}$.

Proof of Lemma 1. Using the definition of conditional variance, we have

$$E(\operatorname{Var}(x|y,z)) = E(E(x^2|y,z)) - E([E(x|y,z)]^2) = E(x^2) - E([E(x|y,z)]^2)$$

Hence, using Jensen's inequality, we have

$$\begin{split} E(\text{Var}(x|y)) - E(\text{Var}(x|y,z)) = & E([E(x|y,z)]^2) - E([E(x|y)]^2) \\ = & E([E(x|y,z)]^2) - E([E(E(x|y,z)|y)]^2) \\ \geq & E([E(x|y,z)]^2) - E(E([E(x|y,z)]^2|y)) = 0 \end{split}$$

The result for normal distributions follows from the fact that normal conditional variances are non-stochastic, i.e., Var(x|y) = E(Var(x|y)). In this case, we can also characterize the extra drop in variance due to conditioning on z using its orthogonal component ε from the regression $z = a + by + \varepsilon$, using similar notation as (A.2):

$$\operatorname{Var}(x|y,z) = \operatorname{Var}(x|y,\varepsilon) = \sum_{x,x} - \sum_{x,(y,\varepsilon)} \sum_{(y,\varepsilon),(y,\varepsilon)}^{-1} \sum_{(y,\varepsilon),(y,\varepsilon)} \sum_{(y,\varepsilon),x}$$

$$= \sum_{x,x} - \sum_{x,y} \sum_{y,y}^{-1} \sum_{y,x} - \sum_{x,\varepsilon} \sum_{\varepsilon,\varepsilon}^{-1} \sum_{\varepsilon,x} = \operatorname{Var}(x|y) - \sum_{x,\varepsilon} \sum_{\varepsilon,\varepsilon}^{-1} \sum_{\varepsilon,x} \sum_{x,y} \sum_{y,y}^{-1} \sum_{x,z} \sum_{x,z}$$

Proof of Lemma 2. The proof follows from inspection: The product of A and its proposed inverse clearly has the same form as A with diagonal elements

$$ac + bd(I - 1) = \frac{a(a + b(N - 2)) - b^{2}(N - 1)}{(a - b)(a + b(N - 1))} = \frac{a^{2} + ab(N - 1) - ab - b^{2}(N - 1)}{(a - b)(a + b(N - 1))} = 1$$

and off-diagonal elements

$$ad + bc + bd(N - 2) = \frac{-ab + b(a + b(N - 2)) - b^{2}(N - 2)}{(a - b)^{2}(a + b(N - 1))^{2}} = 0$$

In other words, AA^{-1} equals the identity, proving the result.

Proof of Equations (4)–(6). The posterior distribution of the true alpha given the observed

factor return is computed using (A.3). The conditional mean is

$$E(\alpha|\hat{\alpha}) = 0 + \frac{\text{Cov}(\alpha, \hat{\alpha})}{\text{Var}(\hat{\alpha})}(\hat{\alpha} - 0) = \frac{\tau^2}{\tau^2 + \sigma^2/T}\hat{\alpha} = \kappa \hat{\alpha}$$

where κ is given by (5) and the posterior variance is

$$\operatorname{Var}(\alpha|\hat{\alpha}) = \operatorname{Var}(\alpha) - \frac{(\operatorname{Cov}(\alpha,\hat{\alpha}))^2}{\operatorname{Var}(\hat{\alpha})} = \tau^2 - \tau^2 \frac{\tau^2}{\tau^2 + \sigma^2/T} = \frac{\tau^2 \sigma^2/T}{\tau^2 + \sigma^2/T} = \kappa \frac{\sigma^2}{T}$$

Proof of Proposition 1. The posterior alpha with alpha-hacking is given via (A.3) as

$$E(\alpha|\hat{\alpha}) = 0 + \frac{\text{Cov}(\alpha, \hat{\alpha})}{\text{Var}(\hat{\alpha})}(\hat{\alpha} - E(\hat{\alpha})) = \frac{\tau^2}{\tau^2 + \bar{\sigma}^2/T}(\hat{\alpha} - \bar{\varepsilon}) = -\kappa_0 + \kappa^{\text{hacking}}\hat{\alpha}$$

where
$$\kappa^{\text{hacking}} = \frac{1}{1 + \frac{\bar{\sigma}^2}{\tau^2 T}}$$
, $\kappa_0 = \kappa^{\text{hacking}} \bar{\varepsilon} \geq 0$, and $\kappa^{\text{hacking}} \leq \kappa$ because $\bar{\sigma} \geq \sigma$.

Proof of Proposition 2. The posterior mean given $\hat{\alpha}$ and $\hat{\alpha}^g$ is computed via (A.3) as

$$E(\alpha|\hat{\alpha}, \hat{\alpha}^{g}) = \begin{bmatrix} \tau^{2} & \tau^{2} \end{bmatrix} \begin{bmatrix} \tau^{2} + \sigma_{T}^{2} & \tau^{2} + \rho \sigma_{T}^{2} \\ \tau^{2} + \rho \sigma_{T}^{2} & \tau^{2} + \sigma_{T}^{2} \end{bmatrix}^{-1} \begin{bmatrix} \hat{\alpha} \\ \hat{\alpha}^{g} \end{bmatrix}$$

$$= \frac{1}{\det} \begin{bmatrix} \tau^{2} & \tau^{2} \end{bmatrix} \begin{bmatrix} \tau^{2} + \sigma_{T}^{2} & -(\tau^{2} + \rho \sigma_{T}^{2}) \\ -(\tau^{2} + \rho \sigma_{T}^{2}) & \tau^{2} + \sigma_{T}^{2} \end{bmatrix} \begin{bmatrix} \hat{\alpha} \\ \hat{\alpha}^{g} \end{bmatrix}$$

$$= \frac{\tau^{2} (1 - \rho) \sigma_{T}^{2}}{\det} (\hat{\alpha} + \hat{\alpha}^{g})$$

$$= \frac{\tau^{2} (1 - \rho)}{\sigma_{T}^{2} (1 - \rho) (1 + \rho) + 2\tau^{2} (1 - \rho)} (\hat{\alpha} + \hat{\alpha}^{g})$$

$$= \kappa^{g} \left(\frac{1}{2} \hat{\alpha} + \frac{1}{2} \hat{\alpha}^{g} \right)$$

using the notation $\sigma_T^2 = \sigma^2/T$ and

$$\det = (\tau^2 + \sigma_T^2)^2 - (\tau^2 + \rho \sigma_T^2)^2 = \sigma_T^2 [\sigma_T^2 (1 - \rho^2) + 2\tau^2 (1 - \rho)].$$

The global shrinkage parameter κ^g is in $[\kappa, 1]$ and decreases with the correlation ρ , attaining the minimum value, $\kappa^g = \kappa$, when $\rho = 1$ as is clearly seen from (12).

The result about the posterior variance follows from Lemma 1.

Proof of Proposition 3. The prior joint distribution of the true and estimated alphas is

given by the following expression, where we focus on factor 1 without loss of generality:

$$\begin{bmatrix} \alpha^{1} \\ \hat{\alpha}^{1} \\ \vdots \\ \hat{\alpha}^{N} \end{bmatrix} \sim N \begin{pmatrix} \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}, \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} & \tau_{c}^{2} + \tau_{w}^{2} & \tau_{c}^{2} & \cdots & \tau_{c}^{2} \\ \tau_{c}^{2} + \tau_{w}^{2} & \tau_{c}^{2} + \tau_{w}^{2} + \sigma^{2}/T & & \tau_{c}^{2} + \rho\sigma^{2}/T \\ \vdots & & \ddots & \\ \tau_{c}^{2} & \tau_{c}^{2} + \rho\sigma^{2}/T & & \tau_{c}^{2} + \tau_{w}^{2} + \sigma^{2}/T \end{bmatrix} \end{pmatrix}$$
(A.5)

The posterior alpha of factor 1 is therefore normally distributed with a mean derived using the standard formula for conditional normal distributions (A.3):

$$E(\alpha^{1}|\hat{\alpha}^{1},\dots,\hat{\alpha}^{N}) = \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix}^{\top} \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} + \sigma^{2}/T & \tau_{c}^{2} + \rho\sigma^{2}/T \\ \vdots \\ \tau_{c}^{2} + \rho\sigma^{2}/T & \tau_{c}^{2} + \tau_{w}^{2} + \sigma^{2}/T \end{bmatrix}^{-1} \begin{bmatrix} \hat{\alpha}^{1} \\ \vdots \\ \hat{\alpha}^{N} \end{bmatrix}$$

We next use Lemma 2 and its notation, i.e., $a = \tau_c^2 + \tau_w^2 + \sigma^2/T$, $b = \tau_c^2 + \rho\sigma^2/T$, and c', d are defined accordingly, where we use the notation c' to avoid confusion with the c in equation (14). This application of Lemma 2 yields

$$\begin{split} E(\alpha^{1}|\hat{\alpha}^{1},\ldots,\hat{\alpha}^{N}) &= \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix}^{\top} \begin{bmatrix} c' & d \\ \ddots & \vdots \\ \hat{\alpha}^{N} \end{bmatrix} \\ &= \begin{bmatrix} \tau_{c}^{2}(c'+d(N-1)) + \tau_{w}^{2}c' \\ \tau_{c}^{2}(c'+d(N-1)) + \tau_{w}^{2}d \\ \vdots \\ \tau_{c}^{2}(c'+d(N-1)) + \tau_{w}^{2}d \end{bmatrix}^{\top} \begin{bmatrix} \hat{\alpha}^{1} \\ \vdots \\ \hat{\alpha}^{N} \end{bmatrix} \\ &= (\tau_{c}^{2}(c'+d(N-1)) + \tau_{w}^{2}d)N\hat{\alpha} + \tau_{w}^{2}(c'-d)\hat{\alpha}^{1} \\ &= (\tau_{c}^{2} \frac{N}{a+b(N-1)} - \tau_{w}^{2} \frac{bN}{(a-b)(a+b(N-1))})\hat{\alpha} + \tau_{w}^{2} \frac{1}{a-b}\hat{\alpha}^{1} \\ &= \frac{\tau_{c}^{2}}{b+\frac{a-b}{N}}\hat{\alpha} + \frac{\tau_{w}^{2}}{a-b}\left(\hat{\alpha}^{1} - \frac{1}{1+\frac{a-b}{bN}}\hat{\alpha}\right) \\ &= \frac{\tau_{c}^{2}}{\tau_{c}^{2} + \rho\sigma^{2}/T + \frac{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}{N}}\hat{\alpha} + \frac{\tau_{w}^{2}}{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}\left(\hat{\alpha}^{1} - \frac{1}{1+\frac{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}(\hat{\alpha}^{2} + \frac{1}{(\tau_{c}^{2} + \rho\sigma^{2}/T)N})}\hat{\alpha}\right) \\ &= \frac{1}{1+\frac{\rho\sigma^{2}}{22T} + \frac{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}{\tau^{2}N}}\hat{\alpha} + \frac{1}{1+\frac{(1-\rho)\sigma^{2}}{22T}}\left(\hat{\alpha}^{1} - \frac{1}{1+\frac{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T}(\hat{\alpha}^{2})}\hat{\alpha}\right) \end{split}$$

The posterior has conditional variance

$$\begin{aligned} \operatorname{Var}(\alpha^{1}|\hat{\alpha}^{1},\ldots,\hat{\alpha}^{N}) = & \tau_{c}^{2} + \tau_{w}^{2} - \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix}^{\top} \begin{bmatrix} c' & d \\ & \ddots \\ d & c' \end{bmatrix} \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix} \\ = & \tau_{c}^{2} + \tau_{w}^{2} - \begin{bmatrix} \tau_{c}^{2}(c' + d(N-1)) + \tau_{w}^{2}c' \\ \tau_{c}^{2}(c' + d(N-1)) + \tau_{w}^{2}d \end{bmatrix}^{\top} \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix} \\ = & \tau_{c}^{2} + \tau_{w}^{2} - (\tau_{c}^{2}(c' + d(N-1)) + \tau_{w}^{2}d) \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix} \\ = & \tau_{c}^{2} + \tau_{w}^{2} - (\tau_{c}^{2}(c' + d(N-1)) + \tau_{w}^{2}d) \begin{bmatrix} \tau_{c}^{2} + \tau_{w}^{2} \\ \tau_{c}^{2} \\ \vdots \\ \tau_{c}^{2} \end{bmatrix} \\ = & \tau_{c}^{2} + \tau_{w}^{2} - (\tau_{c}^{2}(c' + d(N-1)) + \tau_{w}^{2}d) \tau_{c}^{2}(N-1) \\ \rightarrow & \tau_{c}^{2} + \tau_{w}^{2} - (\tau_{c}^{2}(\frac{1}{a-b} - \frac{1}{a-b}) + \tau_{w}^{2}\frac{1}{a-b})(\tau_{c}^{2} + \tau_{w}^{2}) \\ - & (\tau_{c}^{2}\frac{1}{b} - \tau_{w}^{2}\frac{1}{a-b})\tau_{c}^{2} \\ = & \tau_{c}^{2} + \tau_{w}^{2} - \left(\tau_{w}^{4}\frac{1}{a-b} + \tau_{c}^{4}\frac{1}{b}\right) \\ = & \tau_{c}^{2} + \tau_{w}^{2} - \left(\frac{\tau_{w}^{4}}{\tau_{w}^{2} + (1-\rho)\sigma^{2}/T} + \frac{\tau_{c}^{4}}{\tau_{c}^{2} + \rho\sigma^{2}/T}\right) \end{aligned}$$

The last results follow from Lemma 1.

Proof of Proposition 4. We write the joint prior distribution of true and observed alphas in the multi-level hierarchical model as

$$\begin{pmatrix} \alpha \\ \hat{\alpha} \end{pmatrix} \sim N \left(\alpha^0 \, \mathbf{1}_{2NK}, \begin{pmatrix} \Omega & \Omega \\ \Omega & \Omega + \Sigma/T \end{pmatrix} \right) \tag{A.6}$$

The posterior mean vector of true alphas is computed via (A.3):

$$E(\alpha|\hat{\alpha}) = 1_{NK}\alpha_0 + \Omega \left(\Omega + \Sigma/T\right)^{-1} \left(\hat{\alpha} - 1_{NK}\alpha_0\right)$$
$$= \left(\Omega^{-1} + T\Sigma^{-1}\right)^{-1} \left(\Omega^{-1} 1_{NK}\alpha_0 + T\Sigma^{-1}\hat{\alpha}\right)$$

using that $(\Omega + \Sigma/T)^{-1} = \Omega^{-1} - \Omega^{-1} (\Omega^{-1} + T\Sigma^{-1})^{-1} \Omega^{-1}$ by the Woodbury matrix identity. The posterior variance is computed similarly via (A.3) and the same application of the Woodbury matrix identity as

$$\operatorname{Var}(\alpha|\hat{\alpha}) = \Omega - \Omega \left(\Omega + \Sigma/T\right)^{-1} \Omega = \left(\Omega^{-1} + T\Sigma^{-1}\right)^{-1}.$$

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Proof of Proposition 5. Based on the definition of the Bayesian FDR, we have:

$$FDR^{Bayes} = E\left(\frac{\sum_{i} 1_{\{i \text{ false discovery}\}}}{\sum_{i} 1_{\{i \text{ discovery}\}}} \middle| \hat{\alpha}^{1}, \dots, \hat{\alpha}^{N}, \tau\right)$$

$$= \frac{1}{\sum_{i} 1_{\{i \text{ discovery}\}}} E\left(\sum_{i} 1_{\{i \text{ false discovery}\}} \middle| \hat{\alpha}^{1}, \dots, \hat{\alpha}^{N}, \tau\right)$$

$$= \frac{1}{\sum_{i} 1_{\{i \text{ discovery}\}}} \sum_{i} Pr(i \text{ false discovery} \middle| \hat{\alpha}^{1}, \dots, \hat{\alpha}^{N}, \tau)$$

$$= \frac{1}{\# \text{discoveries}} \sum_{i \text{ discovery}} p\text{-null}_{i}$$

$$< 2.5\%$$
(A.7)

Proof of Proposition 6. The posterior mean alpha is

$$E(\alpha|\hat{\alpha}, \hat{\alpha}^{oos}) = \begin{bmatrix} \tau^2 & \tau^2 \end{bmatrix} \begin{bmatrix} \tau^2 + \bar{\sigma}_T^2 & \tau^2 \\ \tau^2 & \tau^2 + \sigma_{oos}^2 \end{bmatrix}^{-1} \begin{bmatrix} \hat{\alpha} - \bar{\varepsilon} \\ \hat{\alpha}^{oos} \end{bmatrix}$$

$$= \frac{1}{\det} \begin{bmatrix} \tau^2 & \tau^2 \end{bmatrix} \begin{bmatrix} \tau^2 + \sigma_{oos}^2 & -\tau^2 \\ -\tau^2 & \tau^2 + \bar{\sigma}_T^2 \end{bmatrix} \begin{bmatrix} \hat{\alpha} - \bar{\varepsilon} \\ \hat{\alpha}^{oos} \end{bmatrix}$$

$$= \frac{\tau^2}{\det} \left(\sigma_{oos}^2 (\hat{\alpha} - \bar{\varepsilon}) + \bar{\sigma}_T^2 \hat{\alpha}^g \right)$$

$$= \frac{\tau^2 (\bar{\sigma}_T^2 + \sigma_{oos}^2)}{\tau^2 (\bar{\sigma}_T^2 + \sigma_{oos}^2) + \bar{\sigma}_T^2 \sigma_{oos}^2} \left(w(\hat{\alpha} - \bar{\varepsilon}) + (1 - w)\alpha^{oos} \right)$$

$$= \frac{\tau^2}{\tau^2 + \bar{\sigma}_T^2 \sigma_{oos}^2 / (\bar{\sigma}_T^2 + \sigma_{oos}^2)} \left(w(\hat{\alpha} - \bar{\varepsilon}) + (1 - w)\alpha^{oos} \right)$$

$$= \frac{1}{1 + \frac{1}{\tau^2 (\bar{\sigma}_T^{-2} + \sigma_{oos}^{-2})}} \left(w(\hat{\alpha} - \bar{\varepsilon}) + (1 - w)\alpha^{oos} \right)$$

using the notation $\bar{\sigma}_T^2 = \bar{\sigma}^2/T,\, \sigma_{oos}^2 = \sigma^2/T^{oos},$ and

$$\det = (\tau^2 + \bar{\sigma}_T^2)(\tau^2 + \sigma_{oos}^2) - \tau^4 = \tau^2(\bar{\sigma}_T^2 + \sigma_{oos}^2) + \bar{\sigma}_T^2\sigma_{oos}^2$$

B Empirical Bayes Estimation

For convenient reference, we restate the multi-level hierarchical model of Section 1. For a factor i in cluster j and corresponding to signal n, the factor is

$$f_t^i = \alpha^i + \beta^i r_t^m + \varepsilon_t^i$$

with

$$\alpha^i = \alpha^o + c^j + s^n + w^i$$

where the alpha components are $\alpha^o = 0$, $c^i \sim N(0, \tau_c^2)$, $s^n \sim N(0, \tau_s^2)$, and $w^i \sim N(0, \tau_w^2)$. We write alpha in vector form as

$$\alpha = \alpha^o 1_{NK} + Mc + Zs + w \tag{B.1}$$

where $\alpha = (\alpha^1, \dots, \alpha^{NK})'$, $c = (c^1, \dots, c^J)'$, $s = (s^1, \dots, s^N)'$, $w = (w^1, \dots, w^{NK})'$, M is the $NK \times J$ matrix of cluster memberships, and Z is the $NK \times N$ matrix indicating the characteristic that factor i is based on. Given the hyperparameters $(\alpha^0, \tau_c, \tau_s, \tau_w)$, the prior mean and covariance matrix of alphas are

$$E[\alpha] = 0, \quad \Omega \equiv \text{Var}(\alpha) = MM'\tau_c^2 + ZZ'\tau_s^2 + I_{NK}\tau_w^2. \tag{B.2}$$

The vector of return shocks is $\varepsilon_t = (\varepsilon_t^1, \dots, \varepsilon_t^{NK})'$ which is distributed $\varepsilon_t \sim N(0, \Sigma)$.

Given this structure, we estimate the model as follows. The vector of factor returns $f_t = (f_t^1, ..., f_t^{NK})'$ has marginal likelihood—that is, after integrating out the uncertain alpha components—that is distributed as

$$f_t \sim N(0, [\Omega + \Sigma])$$

or, equivalently (treating CAPM betas as known), the estimated alphas are distributed 47

$$\hat{\alpha} \sim N(0, [\Omega + \Sigma/T]).$$

The matrices Z and M are given by the factor definition and cluster assignment (Table J.2), respectively. We use a plug-in estimate of the factor CAPM-residual return covariance matrix, denoted $\hat{\Sigma}$ (discussed below). Finally, given $\hat{\Sigma}$, Z, and M, we estimate the hyperparameters of the prior distribution, (τ_c, τ_s, τ_w) via MLE based on the marginal likelihood.

This estimation approach is an example of the empirical Bayes method. It approximates the fully Bayesian posterior calculation (which requires integrating over a hyperprior distribution of hyperparameters, usually an onerous calculation) by setting the hyperparameters to their most likely values based on the marginal likelihood. It is particularly well suited to hierarchical Bayesian models in which parameters for individual observations share some common structure, so that the realized heterogeneity across individual is informative about sensible values for the hyperparameters of the prior. Our model and estimation approach implementation is a minor variation on Bayesian hierarchical normal mean models that are common in Bayesian statistics (textbook treatments include Efron, 2012; Gelman et al., 2013; Maritz, 2018). We conduct sensitivity analysis to ensure that our results are robust to a wide range of hyperparameters (see Figure F.1). Also, we note that our EB methodology is more easily replicable than a full-Bayesian setting with additional hyperpriors as EB relies on a closed-form Bayesian updating rather than a numerical integration.

⁴⁷We abstract from uncertainty in CAPM betas to emphasize the Bayesian updating of alphas. Our conclusions are qualitatively insensitive to accounting for beta uncertainty.

To ensure cross-sectional stationarity, we scale each factor such that their monthly idiosyncratic volatility is $10\%/\sqrt{12}$ (i.e., 10% annualized). To construct a plug-in estimate of the factor residual return covariance matrix, denoted $\hat{\Sigma}$, we face two main empirical challenges. First, the sample covariance is poorly behaved due the relatively large number of factors compared to the number of time series observations. Second, we have an unbalanced panel because different factors come online at different points in time. To address the first challenge, we impose a block equicorrelation structure on Σ based on factors' cluster membership. The correlation between factors in clusters i and j is estimated as the average correlation among all pairs such that one factor is in cluster i and the other is in j. In our global analyses, blocks correspond to region-cluster pairs. To address unbalancedness, we use the bootstrap. In particular, we generate 10,000 bootstrap samples that resample rows of the unbalanced factor return dataset. Each bootstrap sample is, therefore, also unbalanced, and we use this to produce a distribution of alpha estimates. From this we calculate $\hat{\Sigma}/T$ as the covariance of alphas across bootstrap samples (imposing the block equicorrelation structure).

Table B.1 shows the estimated hyperparameters across different samples. While most of our analysis of based on these full-sample estimates, we also consider rolling-estimates of when considering out-of-sample evidence as seen in Figure D.4.

Sample	$ au_c$	$ au_w$	$ au_s$
USA	0.35%	0.21%	
Developed	0.24%	0.18%	
Emerging	0.32%	0.24%	
USA, Developed & Emerging	0.30%	0.19%	0.10%
World	0.37%	0.23%	
World ex. US	0.29%	0.20%	
USA - Mega	0.26%	0.16%	
USA - Large	0.31%	0.18%	
USA - Small	0.44%	0.26%	
USA - Micro	0.48%	0.32%	
USA - Nano	0.42%	0.28%	

Table B.1: Hyperparameters of the prior distribution estimated by maximum likelihood. Here, τ_c is the estimated dispersion in cluster alphas (e.g., the dispersion in the alpha of the value cluster alpha, momentum cluster, and so on). When we estimate a single region, τ_w is the idiosyncratic dispersion of alphas within each cluster. When we jointly estimate several regions, then τ_s is the estimated dispersion in alphas across signals within each cluster, and τ_w is the estimated idiosyncratic dispersion in alphas for factors identified by their signal and region.

⁴⁸As advocated by Engle and Kelly (2012) and Elton et al. (2006), block equicorrelation constrains all pairs of factors in the same block to share a single correlation parameter, and likewise for cross-block correlations. This stabilizes covariance matrix estimates by dramatically reducing the parameterization of the correlation matrix, while leaving the individual variance estimates unchanged.

Internet Appendix

C Differences in Sample and Factor Construction

Here we provide further details on the difference in sample and factor construction vs. Hou et al. (2020) accounting for the difference between the first two bars in Figure 1 in our introduction. To re-iterate, with raw returns and capped value weights, we find a replication rate of 55.6% where as Hou et al. (2020) finds a replication rate of 35%.

This difference has the following decomposition.⁴⁹ First, Hou et al. (2020) focus their analysis on value-weighted factors rather than the standard Fama and French (1993) methodology that gives half the weight to small stocks (or equal-weighting that gives even more weight to small stocks). However, pure value weighting sometimes leads to excessively concentrated portfolios that mask the behavior of factors.⁵⁰ We use a weighting scheme that we refer to as "capped value-weighting" that winsorizes market caps at the NYSE 80th percentile. This weighting is a helpful compromise between pure value-weighting and the Fama-French method since our factors continue to emphasize large stocks, but the capped scheme avoids undue skewness toward a few mega stocks, which in turn produces more robust factor behavior over time and across countries. Capped value weights contribute +9.2% to our higher replication rate. Figure C.1 reproduces Figure 1 with straight value weights.

Second, for each characteristic, Hou et al. (2020) construct three variations on each factor having either 1-month, 6-month, or 12-month holding periods. They treat these as separate factors so that their factor count essentially multiplies their characteristics count by a factor of three. In contrast, we focus on 1-month returns because this is the horizon of interest in almost all of the original studies (and we believe it is the most economically meaningful since it uses the most current data as theory dictates). Our focus on only the 1-month holding period factor for each characteristic contributes +5.0% to our replication rate.

Third, we use a longer sample, which contributes +8.3% to the difference in replication rate. Fourth, we add 15 factors to our sample that were previously studied in the literature but not studied by Hou et al. (2020), which has a no effect on the replication rate.

Finally, we use tercile spreads and breakpoints based on all stocks above the NYSE 20th percentile (i.e., non-micro-caps), while Hou et al. (2020) use decile spreads and breakpoints based on all NYSE stocks. Our more conservative method leads to a -6.0% drop in the replication rate. The remaining +4.1% difference in replication rates is due to minor construction and sample details⁵¹. We discuss this decomposition further in Section 2, where we detail our factor construction choices and discuss why we prefer them.

⁴⁹Note that the attribution to specific changes depends on the order in which the changes are applied.

 $^{^{50}}$ For example, Nokia stock accounted for more than 70% of the total market capitalization in Finland in 1999 and 2000.

⁵¹For example we always lag accounting data four months, they use a mixture of updating schemes and our set of factors is not identical to that in Hou et al. (2020).

Replication Rate with Uncapped Value Weights

In Figure C.1, we show an alternative version of Figure 1 with factors constructed using straight (as opposed to capped) value weights. It shows that all of main our conclusions remain similar. Our ultimate replication rate in this case is 79.8% (based on global data and Bayesian model estimates).

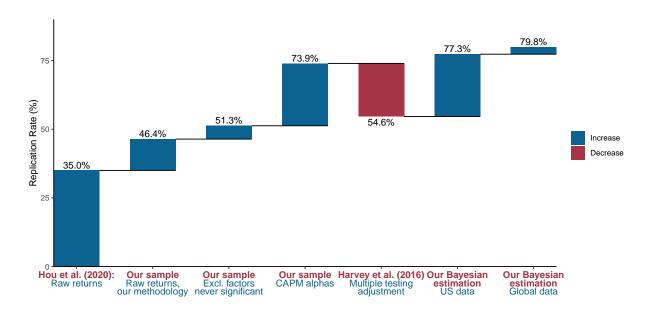


Figure C.1: Replication Rates Versus the Literature (Uncapped Value-weighting)

Note: This figure reproduces the analysis of figure 1 using uncapped value weights to construct factors.

D Additional Time-Series Results

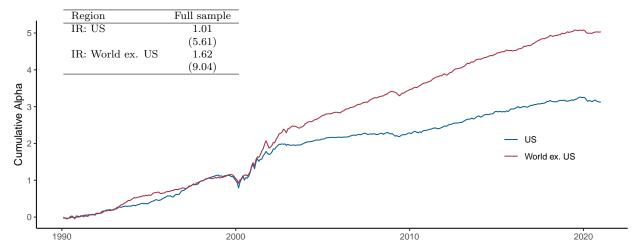


Figure D.1: Out-of-sample performance of significant factors under empirical Bayes

Note: The figure shows the cumulative CAPM alpha of an average of factors significant under our empirical Bayes framework. The significance cutoffs are re-estimated each year with the available data. Factors are eligible for inclusion after the sample period in the original paper, so all returns are out-of-sample. The table shows the information ratio (alpha divided by residual volatility) for the full sample (1990-2020) with t-statistics in parentheses.

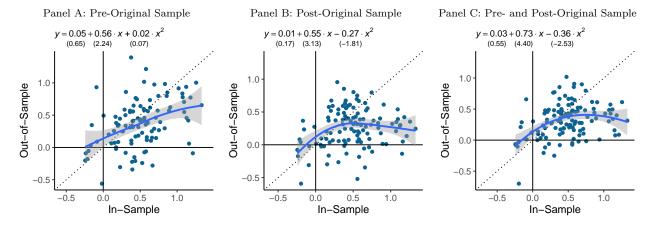


Figure D.2: In-Sample versus Out-of-Sample Alphas for US Factors

Note: The figure plots OLS alphas for US factors during the in-sample period (i.e., the period studied in the original publication) versus out-of-sample alphas. In Panel A, out-of-sample is the time period before the in-sample period. In Panel B, out-of-sample is the time period before the in-sample period. In Panel C, out-of-sample includes both the time period before and after the in-sample period. We require at least five years of out-of-sample data for a factor to be included, amounting to 102, 115 and 119 factors in panel A, B and C. The figure also reports feasible GLS estimates of out-of-sample alphas on in-sample alphas and in-sample alphas squared. To implement feasible GLS, we assume that the error variance-covariance matrix is proportional to the full-sample CAPM residual variance-covariance matrix, $\hat{\Sigma}/T$, described in section B. The blue line is a local polynomial regression fit where observations are weighted by their vicinity to the point on the x-axis. The shaded area is 95% confidence bands. The dotted line is the 45° line.

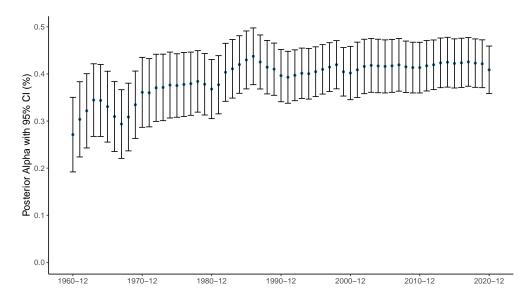


Figure D.3: World Factor Alpha Posterior Distribution Over Time

Note: The figure reports the CAPM alpha and 95% posterior confidence interval for an equal-weighted portfolio of World factors based on EB posteriors re-estimated in December each year. In contrast to figure 9, we re-estimate τ_c and τ_w at each point in time. Figure D.4 shows how the estimated taus evolve over time.

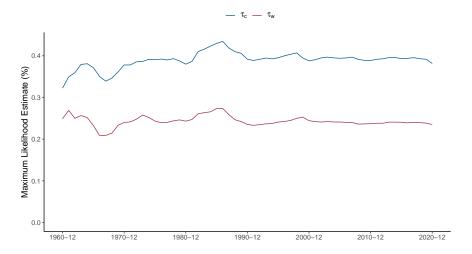


Figure D.4: World Factor Hyperparameters Over Time

Note: The figure reports the τ_c and τ_w used in figure D.3.

E Economic Benefit of More Powerful Tests

Table E.1: The Economic Benefit of More Powerful Tests

	Region			
	US	Developed ex. US	Emerging	
	(1)	(2)	(3)	
Alpha	0.35***	0.24***	0.27***	
	(5.05)	(5.33)	(3.66)	
Market Beta	-0.12^{***}	-0.09^{***}	-0.04***	
	(-4.33)	(-5.68)	(-3.14)	
Observations	540	420	388	
Adjusted R^2	0.17	0.18	0.03	

Note: The dependent variable is an equal-weighted portfolio of factors that are significant under empirical Bayes (EB), but not under OLS with the Benjamini-Yekutieli adjustment (BY). A factor is significant under EB when the probability of a negative alpha is below 2.5%. A factor is significant under BY when the adjusted two-sided p-value is below 5%, and the OLS alpha estimate is positive. Starting in 1959, we update the posterior distribution and the OLS estimates by the end of each year and invest in marginally significant factors over the subsequent year. To avoid lookahead bias, we only use factors after the sample in the original paper has ended. We only consider factors found to be significant by the original reference. The alpha estimates are in percentages, with t-statistics in parentheses. Standard errors are computed following Newey and West (1987) with 6 lags. The stars indicate p-0.1; **p-0.05; **p-0.01.

F Accounting for Publication Bias

Harvey et al. (2016) provides a framework to estimate the total number of factors researchers have tried. The framework is based on t-statistics of published factors and estimation framework to determine the number of unobserved factors.

One set of simulations is constructed to match the baseline scenario of (Harvey et al., 2016, Table 5.A, row 1), which estimates that researchers have tried M=1,297 factors, of which 39.6% of have zero alpha and another is based on the more conservative scenario of (Harvey et al., 2016, Table 5.B, row 1), which implies that researchers have tried 2458 factors, of which 68.3% have zero alpha. Harvey et al. (2016) states that "the average annual Sharpe ratio for these [true] factors is 0.44."

To incorporate these unobserved factors into our framework, we proceed as follows for the baseline scenario. We simulate a total of 1,300 factors in 26 clusters of 50 factors per cluster. We let all factors in 10 clusters have true alphas equal to zero while the remaining clusters have non-zero true alphas. For each of the clusters with non-zero alphas, we set the cluster alpha to $c^j = 0.44 \times 10\%/12$ so that the monthly abnormal return corresponds to an annual Sharpe ratio of 0.44 given the annual volatility of 10%. Finally, we draw each factor's true alpha from $\alpha^i \sim N(c^j, \tau_w^2)$, and then simulate 70 years of monthly returns with within-cluster correlation of 0.58 and 0.02 otherwise. Finally, we estimate prior parameters τ using this data with the same method that we used on the observed data. We repeat this simulation process and compute the average τ_c , which is interpreted as a value that accounts for unobserved factors of the form implied by Harvey et al. (2016). We note that we are implicitly assuming that the unobserved factors belong to different clusters, such that observing new poor performing factors would lead to more shrinkage toward zero via a lower τ_c , but not via different cluster mean returns.

Similarly for the conservative scenario, we simulate a total of 2500 factors in 50 clusters of 50 factors per cluster. We let all factors in 16 clusters have true alphas equal to zero while the remaining clusters have non-zero true alphas as described above. Figure F.1 shows the US replication rate under these alternative hyperparameters of the prior distribution.

⁵²The values are calibrated to match the data on US factors.

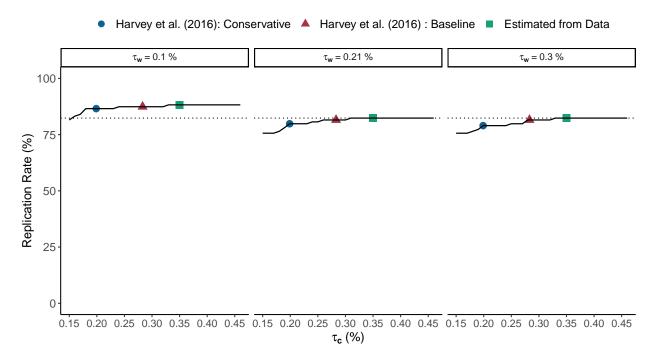


Figure F.1: Replication Rate with Prior Estimated in Light of Unobserved Factors

Note: The figure shows how the replication rate in the US varies when changing the τ_c and τ_w parameter. The dotted line shows our replication rate of 82.4%. The data estimate of τ_w is 0.21%. The green square, highlights the value estimated in the data $\tau_c = 0.35\%$. The red triangle and the blue circle highlights values that are found by estimating the empirical Bayes model according to assumptions about unobserved factors from Harvey et al. (2016). The values are $\tau_c = 0.28\%$ in the baseline scenario and $\tau_c = 0.20\%$ in the conservative scenario. A description of this approach can be found in the appendix, section F.

G Results by Cluster, Region, and Size

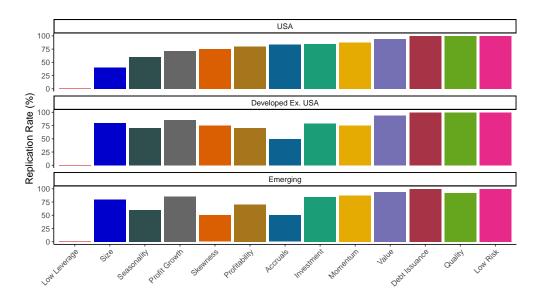


Figure G.1: Replication Rates across Regions by Cluster

Note: Share of factors within each cluster where the 95% posterior intervals does not include zero.

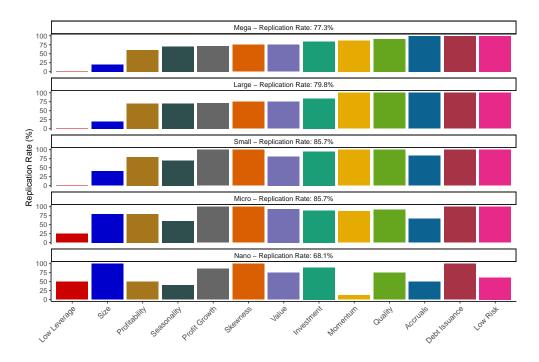


Figure G.2: Replication Rates across Size Groups by Cluster

Note: The figure shows replication rates for US factors created within a size group using rank weights. Mega stocks have a market cap higher than the 80th percentile of NYSE stocks, large stocks are between the 80th and 50th percentile, small stocks are between the 50th and 20th percentile, micro stocks are between the 20th and 1st percentile and nano stocks have a market cap below the 1st percentile of NYSE stocks.

H Further Results on the Tangency Portfolio

In this section, we elaborate on the influence of factors on the tangency portfolio (TPF). Figure H.1 and H.2 shows the tangency weights across regions and size groups. Most notably, the size cluster is much more important outside of the US and among smaller stocks.

The previous TPF analysis, and the results shown in figure 13 has used the 13 cluster level portfolios in addition to the market portfolio as inputs. In the remainder of this section, we build the TPF at the factor level by using the 119 US factors that were found to be significant by an earlier paper. We start the analysis in 1972 to ensure that all factors have non-missing data. The main issue with a factor level analysis, is estimating the covariance matrix. We follow Pedersen et al. (2021) and adjust the covariance matrix by shrinking the correlations towards zero

$$\Sigma_w = \sigma[(1-w)\mathbf{\Omega} + w\mathbf{I}]\sigma$$

where Ω is the sample correlation matrix, σ is a matrix with the sample volatilities on the diagonal and zero elsewhere, \mathbf{I} is the identity matrix and w is a shrinkage parameter. The tangency weights are recovered from the standard formula on the adjusted covariance matrix. This approach requires choosing the shrinkage parameter. Ideally, we want to choose the amount of shrinkage to maximize out-of-sample Sharpe ratio. We implement this intuition via. five-fold cross validation. In each fold, we estimate the tangency weights with a given shrinkage parameter using 4/5 of the data, and compute the realized Sharpe ratio on the remaining 1/5. We repeat this procedure 5 times, and compute the average realized Sharpe ratio for $w \in (0, 0.1, \dots, 1)$. In unreported results, we find that the optimal shrinkage parameter is $w = 0.5^{53}$.

Figure H.3 shows the in-sample Sharpe ratio of the tangency portfolio that are allowed to invest in the market portfolio and factors from one clusters. The dashed line shows the Sharpe ratio of the market portfolio. Figure H.4 shows the in-sample Sharpe ratio attainable after excluding factors from one cluster at a time. Figure H.5 shows the importance of each factor for the cluster TPF. Specifically, we report the drop in the maximal attainable Sharpe ratio within a cluster after excluding one of the cluster factors. Finally, figure H.6 shows the importance of each factor for the TPF that includes all factors. Specifically, we eliminate each factor one at a time and record the resulting drop in the in-sample Sharpe ratio.

⁵³The average monthly out-of-sample Sharpe ratio with w = 0.5 is 0.56 compared to 0.43 from the unconstrained solution (w = 0).

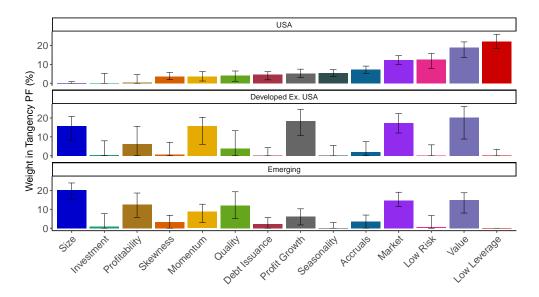


Figure H.1: Tangency Portfolio Weights across Regions

Note: Within each region, we compute the cluster return as the equal weighted return of all factors with data available at a given point in time. We further add the regional market return. We estimate the tangency weights following the method of Britten-Jones (1999) with a non-negativity constraint. The error bars are the 90% confidence intervals based on 10,000 bootstrap samples and the percentile method. The data starts in 1952 for the US, 1987 for Developed ex. US and 1994 for Emerging.

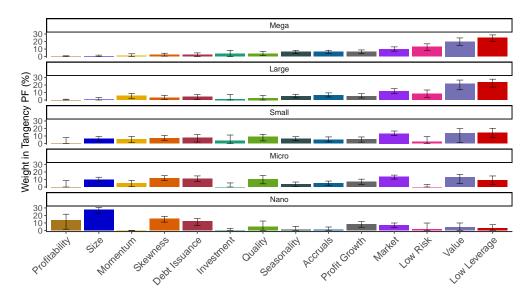


Figure H.2: Tangency Portfolio Weights across Size Groups

Note: Within each size group, we compute the cluster return as the equal weighted return of all factors with data available at a given point in time. We only use US data. We add the US market return. We estimate the tangency weights following the method of Britten-Jones (1999) with a non-negativity constraint. The error bars are the 90% confidence intervals based on 10,000 bootstrap samples and the percentile method. The data starts in 1963.

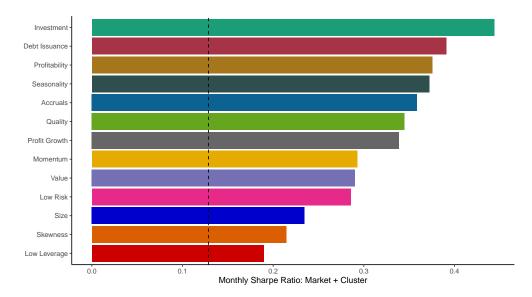


Figure H.3: Market + Cluster

Note: Each bar shows the monthly in-sample Sharpe ratio of a tangency portfolio that is allowed to invest in all factor from one cluster plus the market portfolio. We use the simple enhanced portfolio optimization method from Pedersen et al. (2021), with a shrinkage parameter of w = 0.5. The analysis is done on US factors from 1972 to 2020.

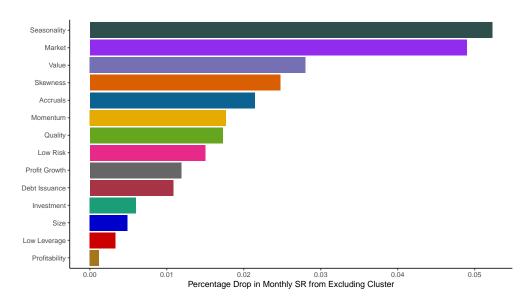


Figure H.4: Excluding One Cluster

Note: Each bar shows the monthly in-sample Sharpe ratio of a tangency portfolio that is allowed to invest in the market portfolio and factors from all clusters except one. We use the simple enhanced portfolio optimization method from Pedersen et al. (2021), with a shrinkage parameter of w = 0.5. The analysis is done on US factors from 1972 to 2020.

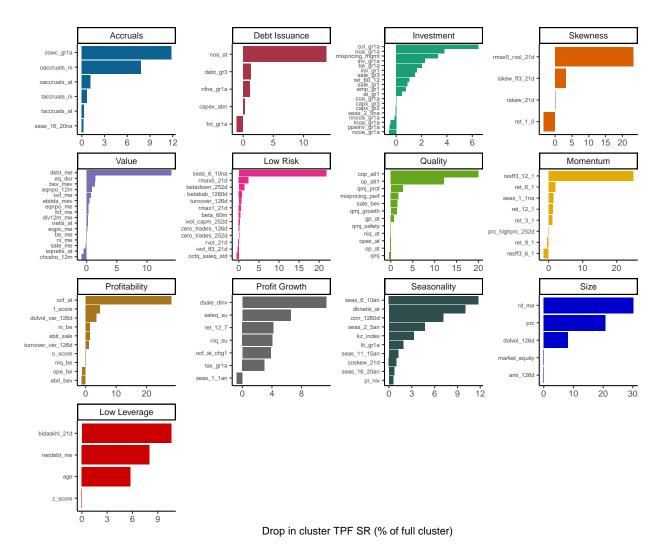


Figure H.5: Factor importance for cluster TPF

Note: Each bar shows the difference in the monthly in-sample Sharpe ratio of a tangency portfolio that invest in all factors within a cluster and a tangency portfolio that invest in all cluster factors except one. We show individual factors by their cluster. We use the simple enhanced portfolio optimization method from Pedersen et al. (2021), with a shrinkage parameter of w = 0.5. The analysis is done on US factors from 1972 to 2020.

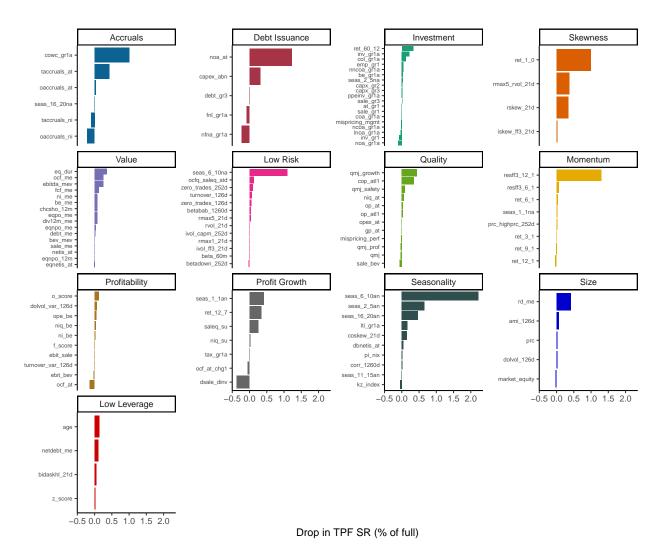


Figure H.6: Factor importance for full TPF

Note: Each bar shows the difference in the monthly in-sample Sharpe ratio of a tangency portfolio that invest in all factors and a tangency portfolio that invest in all factor except one. We show individual factors by their cluster. We use the simple enhanced portfolio optimization method from Pedersen et al. (2021), with a shrinkage parameter of w = 0.5. The analysis is done on US factors from 1972 to 2020.

I Cluster Construction

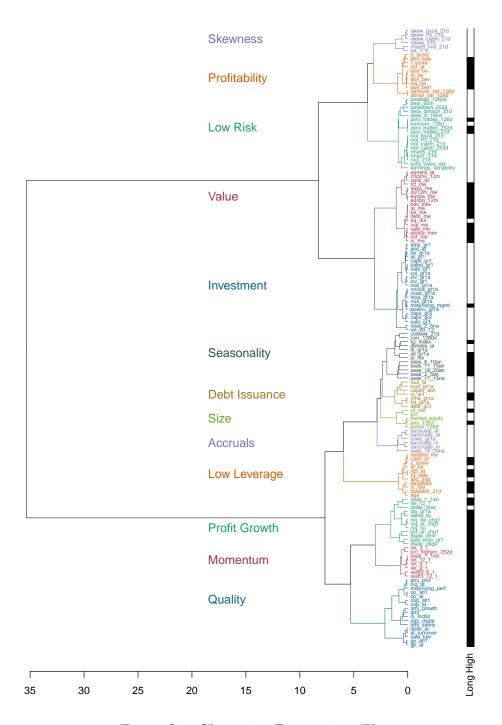


Figure I.1: Clustering Factors into Themes

Note: This figures shows a hierarchical clustering of all factors into 13 themes using the sample of US stocks from 1975-2020. Long high indicates whether the factor is long stocks with a high value of the underlying characteristic.

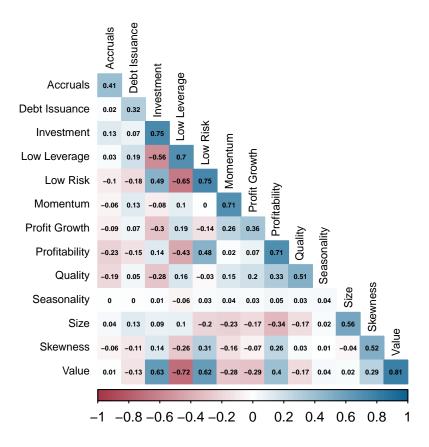


Figure I.2: Factor Theme Correlations

Note: This figure shows the average pairwise Pearson correlation between factors from different clusters (off diagonal elements) or between factors in the same cluster (diagonal elements), using data on US stocks during the 1975-2020 period.

J Details on Clusters, Factors, and Countries

Table J.1: Factor and Cluster Details

	Variable		Orig.		Orig.
Description	Name	Citation	Sample	Sign	Signif.
		Accruals			
Change in current operating work-	$cowc_gr1a$	Richardson et al. (2005)	1962-2001	-1	1
ing capital					
Operating accruals	$oaccruals_at$	Sloan (1996)	1962 - 1991	-1	1
Percent operating accruals	oaccruals_ni	Hafzalla Lundholm and Van Winkle	1989-2008	-1	1
		(2011)			
Years 16-20 lagged returns, nonan-	$seas_16_20na$	Heston and Sadka (2008)	1965 - 2002	-1	1
nual					

Total accruals Percent total accruals	taccruals_at taccruals_ni	Richardson et al. (2005) Hafzalla Lundholm and Van Winkle (2011)	1962-2001 1989-2008	-1 -1	1 1
	Т	Debt Issuance			
Abnormal corporate investment	capex_abn	Titman Wei and Xie (2004)	1973-1996	-1	1
Growth in book debt (3 years)	debt_gr3	Lyandres Sun and Zhang (2008)	1970-2005	-1	1
Change in financial liabilities	fnl_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Change in noncurrent operating li-	ncol_gr1a	Richardson et al. (2005)	1962-2001	-1	0
abilities					
Change in net financial assets	$nfna_gr1a$	Richardson et al. (2005)	1962 - 2001	1	1
Earnings persistence	ni_ar1	Francis et al. (2004)	1975-2001	1	0
Net operating assets	noa_at	Hirshleifer et al. (2004)	1964-2002	-1	1
		Investment			
Liquidity of book assets	aliq_at	Ortiz-Molina and Phillips (2014)	1984-2006	-1	0
Asset Growth	at_gr1	Cooper Gulen and Schill (2008)	1968-2003	-1	1
Change in common equity	be_gr1a	Richardson et al. (2005)	1962-2001	-1	1
CAPEX growth (1 year)	capx_gr1	Xie (2001)	1971-1992	-1	0
CAPEX growth (2 years)	capx_gr2	Anderson and Garcia-Feijoo (2006)	1976-1998	-1	1
CAPEX growth (3 years)	$capx_gr3$	Anderson and Garcia-Feijoo (2006)	1976-1998	-1	1
Change in current operating assets	coa_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Change in current operating liabil-	col_gr1a	Richardson et al. (2005)	1962-2001	-1	1
ities	_	D 1 7 1 1 1 (0011)	1007 0010	_	
Hiring rate	emp_gr1	Belo Lin and Bazdresch (2014)	1965-2010	-1	1
Inventory growth	inv_gr1	Belo and Lin (2011)	1965-2009	-1	1
Inventory change	inv_gr1a	Thomas and Zhang (2002)	1970-1997	-1	1
Change in long-term net operating assets	lnoa_gr1a	Fairfield Whisenant and Yohn (2003)	1964-1993	-1	1
Mispricing factor: Management		ntStambaugh and Yuan (2016)	1967-2013	1	1
Change in noncurrent operating assets	ncoa_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Change in net noncurrent operating assets	nncoa_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Change in net operating assets	noa_gr1a	Hirshleifer et al. (2004)	1964-2002	-1	1
Change PPE and Inventory	ppeinv_gr1a	Lyandres Sun and Zhang (2008)	1970 - 2005	-1	1
Long-term reversal	ret_60_12	De Bondt and Thaler (1985)	1926 - 1982	-1	1
Sales Growth (1 year)	$sale_gr1$	Lakonishok Shleifer and Vishny (1994)	1968-1989	-1	1
Sales Growth (3 years)	$sale_gr3$	Lakonishok Shleifer and Vishny (1994)	1968-1989	-1	1
Sales growth (1 quarter)	$saleq_gr1$	· ,	1967-2016	-1	0
Years 2-5 lagged returns, nonannual	$seas_2_5na$	Heston and Sadka (2008)	1965 - 2002	-1	1
	т	low Leverage			
Firm age	age	Jiang Lee and Zhang (2005)	1965-2001	-1	1
Liquidity of market assets	aliq_mat	Ortiz-Molina and Phillips (2014)	1984-2006	-1	0
Book leverage	at_be	Fama and French (1992)	1963-1990	-1	0
The high-low bid-ask spread	bidaskhl_21d	Corwin and Schultz (2012)	1927-2006	1	1
Cash-to-assets	cash_at	Palazzo (2012)	1972-2009	1	0
Net debt-to-price	netdebt_me	Penman Richardson and Tuna (2007)	1962-2001	-1	1
Earnings volatility	ni_ivol	Francis et al. (2004)	1975-2001	1	0

R&D-to-sales	rd_sale	Chan Lakonishok and Sougiannis (2001)	1975-1995	1	0
R&D capital-to-book assets	$rd5_at$	Li (2011)	1952-2004	1	0
Asset tangibility	tangibility	Hahn and Lee (2009)	1973-2001	1	0
Altman Z-score	z_score	Dichev (1998)	1981-1995	1	1
Titolikai Z goore	230010	Biolici (1000)	1001 1000	-	-
		Low Risk			
Market Beta	$beta_60m$	Fama and MacBeth (1973)	1935-1968	-1	1
Dimson beta	beta_dimson_21e	. ,	1955-1974	-1	0
Frazzini-Pedersen market beta		Frazzini and Pedersen (2014)	1926-2012	-1	1
Downside beta		Ang Chen and Xing (2006)	1963-2001	-1	1
Earnings variability		liFyancis et al. (2004)	1975-2001	-1	0
Idiosyncratic volatility from the	ivol_capm_21d	injunició et un (2001)	1967-2016	-1	0
CAPM (21 days)	1101_capiii_21a		1001 2010	-	O
Idiosyncratic volatility from the	ivol capm 252d	Ali Hwang and Trombley (2003)	1976-1997	-1	1
CAPM (252 days)	Ivoi_capiii_252d	All Hwang and Hollibley (2005)	1910-1991	-1	1
Idiosyncratic volatility from the	ivol_ff3_21d	Ang et al. (2006)	1963-2000	-1	1
Fama-French 3-factor model	1V01_113_21tt	Ang et al. (2000)	1905-2000	-1	1
	ivol_hxz4_21d		1067 2016	-1	0
Idiosyncratic volatility from the q-	IV01_IIXZ4_21Q		1967-2016	-1	U
factor model Cash flow volatility	a of a solo a std	H (2000)	1000 2004	1	1
· ·	ocfq_saleq_std	Huang (2009)	1980-2004	-1	1
Maximum daily return	rmax1_21d	Bali Cakici and Whitelaw (2011)	1962-2005	-1	1
Highest 5 days of return	$rmax5_21d$	Bali, Brown, Murray and Tang	1993-2012	-1	1
75	1.01.1	(2017)	1000 0000		
Return volatility	rvol_21d	Ang et al. (2006)	1963-2000	-1	1
Years 6-10 lagged returns, nonan-	$seas_6_10na$	Heston and Sadka (2008)	1965-2002	-1	1
nual		D	1000 1001	_	
Share turnover	turnover_126d	Datar Naik and Radcliffe (1998)	1963-1991	-1	1
Number of zero trades with	$zero_trades_21d$	Liu (2006)	1963-2003	1	0
turnover as tiebreaker (1 month)					
Number of zero trades with	zero_trades_126	d Liu (2006)	1963-2003	1	1
turnover as tiebreaker (6 months)		17. (22.2.2)	1000 0000	_	
Number of zero trades with	zero_trades_252d	d Liu (2006)	1963-2003	1	1
turnover as tiebreaker (12 months)					
	7	Momentum			
Current price to high price over last	_	dGeorge and Hwang (2004)	1963-2001	1	1
year	pre-mgnpre-202	accorge and 11 wang (2001)	1000 2001	1	
Residual momentum t-6 to t-1	$resff3_6_1$	Blitz Huij and Martens (2011)	1930-2009	1	1
Residual momentum t-12 to t-1	$resff3_12_1$	Blitz Huij and Martens (2011)	1930-2009	1	1
Price momentum t-3 to t-1	ret_3_1	Jegedeesh and Titman (1993)	1965-1989	1	1
Price momentum t-6 to t-1	ret_6_1	Jegadeesh and Titman (1993)	1965-1989	1	1
Price momentum t-9 to t-1	ret_9_1	Jegedeesh and Titman (1993)	1965-1989	1	1
Price momentum t-12 to t-1	ret_12_1	Jegedeesh and Titman (1993)	1965-1989	1	1
Year 1-lagged return, nonannual	seas_1_1na	Heston and Sadka (2008)	1965-2002	1	1
rear r-ragged revurn, nonamuar	3C43_1_1114	Tieston and Badka (2000)	1300-2002	1	1
	Pı	rofit Growth			
Change sales minus change Inven-	dsale_dinv —	Abarbanell and Bushee (1998)	1974-1988	1	1
tory	· · · · · · · · · · · · · · · · · · ·	(2000)			_
Change sales minus change receiv-	$dsale_drec$	Abarbanell and Bushee (1998)	1974-1988	-1	0
ables		(/			-
Change sales minus change SG&A	$dsale_dsga$	Abarbanell and Bushee (1998)	1974-1988	1	0
Change in quarterly return on as-	niq_at_chg1	(/	1972-2016	1	0
sets	- 5				

Change in quarterly return on equity	niq_be_chg1		1967-2016	1	0
Standardized earnings surprise	niq_su	Foster Olsen and Shevlin (1984)	1974-1981	1	1
Change in operating cash flow to as-	ocf_at_chg1	Bouchard, Krueger, Landier and	1990-2015	1	1
sets	8-	Thesmar (2019)			
Price momentum t-12 to t-7	ret_12_7	Novy-Marx (2012)	1925-2010	1	1
Labor force efficiency	$sale_emp_gr1$	Abarbanell and Bushee (1998)	1974-1988	1	0
Standardized Revenue surprise	saleq_su	Jegadeesh and Livnat (2006)	1987-2003	1	1
Year 1-lagged return, annual	seas_1_1an	Heston and Sadka (2008)	1965-2002	1	1
Tax expense surprise	tax_gr1a	Thomas and Zhang (2011)	1977-2006	1	1
Tax expense surprise	tax_grra	Thomas and Zhang (2011)	1311 2000	1	1
	Ī	Profitability			
Coefficient of variation for dollar	$dolvol_var_126d$	Chordia Subrahmanyam and An-	1966 - 1995	-1	1
trading volume		shuman (2001)			
Return on net operating assets	$ebit_bev$	Soliman (2008)	1984-2002	1	1
Profit margin	$ebit_sale$	Soliman (2008)	1984-2002	1	1
Pitroski F-score	f_score	Piotroski (2000)	1976-1996	1	1
Return on equity	ni_be	Haugen and Baker (1996)	1979-1993	1	1
Quarterly return on equity	niq_be	Hou Xue and Zhang (2015)	1972-2012	1	1
Ohlson O-score	o_score	Dichev (1998)	1981-1995	-1	1
Operating cash flow to assets	ocf_at	Bouchard, Krueger, Landier and	1990-2015	1	1
		Thesmar (2019)		-	-
Operating profits-to-book equity	ope_be	Fama and French (2015)	1963-2013	1	1
Operating profits-to-lagged book	ope_bel1		1967-2016	1	0
equity					
Coefficient of variation for share	turnover_var_12	66 Chordia Subrahmanyam and An-	1966-1995	-1	1
turnover		shuman (2001)			
***************************************		()			
		, ,			
	at tumpayan	Quality	1070 1002	1	0
Capital turnover	at_turnover	, ,	1979-1993	1	0
Capital turnover Cash-based operating profits-to-	at_turnover cop_at	Quality	1979-1993 1967-2016	1 1	0
Capital turnover Cash-based operating profits-to-book assets	cop_at	Quality Haugen and Baker (1996)	1967-2016	1	0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-		Quality			
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets	cop_at cop_atl1	Quality Haugen and Baker (1996) Ball et al. (2016)	1967-2016 1963-2014	1	0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change	cop_at	Quality Haugen and Baker (1996)	1967-2016	1	0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales	cop_atl1 dgp_dsale	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998)	1967-2016 1963-2014 1974-1988	1 1 1	0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets	cop_atl1 dgp_dsale gp_at	Quality Haugen and Baker (1996) Ball et al. (2016)	1967-2016 1963-2014 1974-1988 1963-2010	1 1 1	0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets	cop_atl1 dgp_dsale gp_at gp_atl1	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016	1 1 1 1 1	0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance	cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013	1 1 1 1 1 1	0 1 0 1 0 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters	cop_atl1 dgp_dsale gp_at gp_atl1	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016	1 1 1 1 1	0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases	cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992	1 1 1 1 1 1	0 1 0 1 0 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters	cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013	1 1 1 1 1 1	0 1 0 1 0 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005	1 1 1 1 1 1 1	0 1 0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013	1 1 1 1 1 1 1 1	0 1 0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005	1 1 1 1 1 1 1	0 1 0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014	1 1 1 1 1 1 1 1	0 1 0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets Operating leverage	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1 opex_at	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016) Novy-Marx (2011)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014 1963-2008	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0 1 0 1 0 1 0 1 1 1 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014	1 1 1 1 1 1 1 1	0 1 0 1 0 1 0
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets Operating leverage	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1 opex_at	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016) Novy-Marx (2011) Assness, Frazzini and Pedersen	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014 1963-2008	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0 1 0 1 0 1 0 1 1 1 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets Operating leverage Quality minus Junk: Composite	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1 opex_at qmj	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016) Novy-Marx (2011) Assness, Frazzini and Pedersen (2018)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014 1963-2008 1957-2016	1 1 1 1 1 1 1 1 1 1	0 1 0 1 0 1 1 1 1 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets Operating leverage Quality minus Junk: Composite	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1 opex_at qmj	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016) Novy-Marx (2011) Assness, Frazzini and Pedersen (2018) Assness, Frazzini and Pedersen	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014 1963-2008 1957-2016	1 1 1 1 1 1 1 1 1 1	0 1 0 1 0 1 1 1 1 1
Capital turnover Cash-based operating profits-to-book assets Cash-based operating profits-to-lagged book assets Change gross margin minus change sales Gross profits-to-assets Gross profits-to-lagged assets Mispricing factor: Performance Number of consecutive quarters with earnings increases Quarterly return on assets Operating profits-to-book assets Operating profits-to-lagged book assets Operating leverage Quality minus Junk: Composite Quality minus Junk: Growth	cop_at cop_atl1 dgp_dsale gp_at gp_atl1 mispricing_perf ni_inc8q niq_at op_at op_atl1 opex_at qmj qmj_growth	Quality Haugen and Baker (1996) Ball et al. (2016) Abarbanell and Bushee (1998) Novy-Marx (2013) Stambaugh and Yuan (2016) Barth Elliott and Finn (1999) Balakrishnan Bartov and Faurel (2010) Ball et al. (2016) Novy-Marx (2011) Assness, Frazzini and Pedersen (2018) Assness, Frazzini and Pedersen (2018)	1967-2016 1963-2014 1974-1988 1963-2010 1967-2016 1967-2013 1982-1992 1976-2005 1963-2013 1963-2014 1963-2008 1957-2016	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0 1 0 1 0 1 1 1 1 1

Quality minus Junk: Safety	$\rm qmj_safety$	Assness, Frazzini and Pedersen (2018)	1957-2016	1	1
Assets turnover	$sale_bev$	Soliman (2008)	1984-2002	1	1
		Seasonality			
Market correlation	corr_1260d	Assness, Frazzini, Gormsen, Pedersen (2020)	1925-2015	-1	1
Coskewness	$\cos kew_21d$	Harvey and Siddique (2000)	1963-1993	-1	1
Net debt issuance	$dbnetis_at$	Bradshaw Richardson and Sloan	1971-2000	-1	1
		(2006)			
Kaplan-Zingales index	kz_index	Lamont Polk and Saa-Requejo (2001)	1968-1995	1	1
Change in long-term investments	lti_gr1a	Richardson et al. (2005)	1962 - 2001	-1	1
Taxable income-to-book income	pi_nix	Lev and Nissim (2004)	1973-2000	1	1
Years 2-5 lagged returns, annual	$seas_25an$	Heston and Sadka (2008)	1965-2002	1	1
Years 6-10 lagged returns, annual	$seas_6_10an$	Heston and Sadka (2008)	1965-2002	1	1
Years 11-15 lagged returns, annual	$seas_11_15an$	Heston and Sadka (2008)	1965 - 2002	1	1
Years 11-15 lagged returns, nonannual	seas_11_15na	Heston and Sadka (2008)	1965-2002	-1	0
Years 16-20 lagged returns, annual	$seas_16_20an$	Heston and Sadka (2008)	1965-2002	1	1
Change in short-term investments	sti_gr1a	Richardson et al. (2005) Size	1962-2001	1	0
Amihud Measure	ami_126d	Amihud (2002)	1964 - 1997	1	1
Dollar trading volume	dolvol_126d	Brennan Chordia and Subrah- manyam (1998)	1966-1995	-1	1
Market Equity	market_equity	Banz (1981)	1926-1975	-1	1
Price per share	prc	Miller and Scholes (1982)	1940-1978	-1	1
R&D-to-market	rd_me	Chan Lakonishok and Sougiannis (2001)	1975-1995	1	1
		Skewness			
Idiosyncratic skewness from the CAPM	iskew_capm_21d		1967-2016	-1	0
Idiosyncratic skewness from the Fama-French 3-factor model	iskew_ff3_21d	Bali Engle and Murray (2016)	1925-2021	-1	1
Idiosyncratic skewness from the q-factor model	iskew_hxz4_21d		1967-2016	-1	0
Short-term reversal	ret_1_0	Jegadeesh (1990)	1929 - 1982	-1	1
Highest 5 days of return scaled by volatility	rmax5_rvol_21d	Assness, Frazzini, Gormsen, Pedersen (2020)	1925-2015	-1	1
Total skewness	$rskew_21d$	Bali Engle and Murray (2016)	1925-2021	-1	1
		Value			
Assets-to-market	at_me	Fama and French (1992)	1963-1990	1	0
Book-to-market equity	be_me	Rosenberg Reid and Lanstein	1973-1984	1	1
		(1985)	1001	-	-
Book-to-market enterprise value	bev_mev	Penman Richardson and Tuna (2007)	1962-2001	1	1
Net stock issues	$chcsho_12m$	Pontiff and Woodgate (2008)	1970-2003	-1	1
Debt-to-market	$debt_me$	Bhandari (1988)	1948-1979	1	1
Dividend yield	$div12m_me$	Litzenberger and Ramaswamy	1940-1980	1	1
•		(1979)			
		()			

Equity duration	eq_dur	Dechow Sloan and Soliman (2004)	1962 - 1998	-1	1
Net equity issuance	$eqnetis_at$	Bradshaw Richardson and Sloan	1971-2000	-1	1
		(2006)			
Equity net payout	$eqnpo_{-}12m$	Daniel and Titman (2006)	1968-2003	1	1
Net payout yield	eqnpo_me	Boudoukh et al. (2007)	1984-2003	1	1
Payout yield	eqpo_me	Boudoukh et al. (2007)	1984-2003	1	1
Free cash flow-to-price	fcf_me	Lakonishok Shleifer and Vishny	1963-1990	1	1
		(1994)			
Intrinsic value-to-market	$ival_me$	Frankel and Lee (1998)	1975-1993	1	0
Net total issuance	$netis_at$	Bradshaw Richardson and Sloan	1971-2000	-1	1
		(2006)			
Earnings-to-price	ni_me	Basu (1983)	1963-1979	1	1
Operating cash flow-to-market	ocf_me	Desai Rajgopal and Venkatachalam	1973-1997	1	1
		(2004)			
Sales-to-market	$sale_me$	Barbee Mukherji and Raines (1996)	1979-1991	1	1

Note: This table shows cluster names as underlined section headings and, for each cluster, a description of the factors included, the variable name used in the code, the original reference, the sample period used in the original reference, the sign of the factor ("1" means "long", "-1" means "short"), and whether the original reference found the factor to be significant ("1" means "yes", "0" means "no"). For example, the first value factor "at_me" goes long stocks with high values of assets-to-market and shorts those with low values (and would be done the reverse if the sign was "-1" instead of "1").

Table J.2: Alpha Across Regions

			U	S)evelope	ed ex. US		Eme	rging
	Factor	α_{OLS}	α_{EB}	$\frac{\epsilon}{\Pr(\alpha_{\text{EB}} < 0)}$	$\alpha_{ m OLS}$	α_{EB}	$\Pr(\alpha_{\text{EB}} < 0)$	α_{OLS}	α_{EB}	$\Pr(\alpha_{\text{EB}} < 0)$
1	aliq_mat*	-0.35	-0.31	1.00	-0.33	-0.27	1.00	-0.31	-0.28	1.00
2	$dsale_drec*$	-0.25	-0.22	1.00	-0.05	-0.11	0.86	-0.23	-0.18	0.95
3	bidaskhl_21d	-0.24	-0.25	1.00	-0.62	-0.42	1.00	-0.50	-0.38	1.00
4	ni_ivol*	-0.23	-0.18	0.99	-0.20	-0.13	0.90	0.03	-0.07	0.75
5	at_be^*	-0.16	-0.10	0.92	0.06	0.04	0.34	0.12	0.04	0.37
6	age	-0.15	-0.18	1.00	-0.64	-0.44	1.00	-0.59	-0.41	1.00
7	kz_index	-0.13	-0.12	0.93	-0.08	-0.08	0.79	-0.32	-0.15	0.93
8	$turnover_var_126d$	-0.13	-0.12	0.96	-0.02	-0.03	0.60	0.20	0.01	0.46
9	prc	-0.11	-0.02	0.60	0.02	0.06	0.26	0.07	0.07	0.23
10	sti_gr1a*	-0.09	-0.02	0.60	-0.01	0.03	0.37	0.17	0.08	0.21
11	dolvol_var_126d	-0.07	-0.07	0.85	-0.07	-0.03	0.63	0.20	0.02	0.43
12	$dsale_dsga^*$	-0.07	-0.02	0.58	0.20	0.13	0.11	0.33	0.15	0.09
13	ni_ar1*	-0.02	-0.07	0.81	0.04	0.03	0.39	-0.29	-0.06	0.71
14	$sale_emp_gr1*$	-0.01	-0.03	0.64	-0.24	-0.10	0.83	0.11	-0.00	0.51
15	$netdebt_me$	-0.01	0.03	0.32	0.11	0.11	0.13	0.20	0.12	0.13
16	z_score	-0.00	0.03	0.36	-0.02	0.03	0.36	0.20	0.10	0.17
17	$iskew_hxz4_21d*$	0.01	-0.08	0.80	-0.50	-0.18	0.94	-0.37	-0.16	0.90
18	rd_sale^*	0.01	0.06	0.22	0.22	0.18	0.03	0.25	0.15	0.08
19	market_equity	0.02	0.13	0.04	0.13	0.21	0.02	0.55	0.37	0.00
20	cash_at*	0.04	0.07	0.18	0.07	0.10	0.15	0.24	0.14	0.08
21	ami_126d	0.05	0.14	0.03	0.14	0.21	0.02	0.38	0.28	0.00
22	ncol_gr1a*	0.05	-0.01	0.57	-0.07	0.02	0.42	-0.08	0.02	0.41
23	debt_me	0.09	0.06	0.21	0.03	0.05	0.31	-0.06	-0.00	0.51
24	ni_inc8q*	0.10	0.13	0.07	0.38	0.25	0.02	0.26	0.18	0.07
25	tax_gr1a	0.10	0.09	0.13	0.06	0.10	0.17	0.30	0.16	0.06
26	saleq_gr1*	0.11	-0.03	0.66	0.03	0.04	0.37	-0.70	-0.16	0.91
$\frac{1}{27}$	ret_60_12	0.12	0.03	0.31	0.11	0.19	0.03	0.37	0.30	0.00
28	$rd5_at^*$	0.12	0.17	0.01	0.35	0.29	0.00	0.63	0.31	0.01
29	coskew_21d	0.12	0.12	0.05	0.28	0.19	0.02	-0.04	0.08	0.20
30	saleq_su	0.12	0.16	0.04	0.47	0.30	0.01	0.54	0.29	0.01
31	col_gr1a	0.13	0.01	0.46	0.00	0.07	0.23	-0.11	0.05	0.31
32	iskew_ff3_21d	0.13	0.08	0.18	-0.20	0.01	0.46	0.15	0.11	0.17
33	tangibility*	0.13	0.17	0.01	0.26	0.25	0.00	0.41	0.28	0.00
34	lti_gr1a	0.15	0.09	0.13	-0.01	0.04	0.35	-0.17	-0.01	0.52
35	pi_nix	0.16	0.14	0.05	0.06	0.11	0.14	0.09	0.12	0.13
36	bev_mev	0.17	0.16	0.02	0.28	0.25	0.00	0.27	0.22	0.02
37	gp_atl1*	0.18	0.20	0.01	0.22	0.24	0.01	0.53	0.31	0.00
38	at_me*	0.18	0.16	0.01	0.20	0.20	0.02	0.23	0.19	0.04
39	seas_16_20na	0.19	0.04	0.32	-0.13	0.02	0.44	-0.32	-0.02	0.57
40	zero_trades_21d*	0.19	0.16	0.01	0.21	0.18	0.04	0.40	0.26	0.01
41	ebit_sale	0.20	0.18	0.01	0.21	0.18	0.03	0.25	0.15	0.07
42	ret_3_1	0.21	0.11	0.06	0.26	0.15	0.06	0.08	0.08	0.21
43	be_me	0.23	0.22	0.00	0.32	0.29	0.00	0.32	0.27	0.01
44	op_atl1	0.23	0.23	0.00	0.25	0.25	0.01	0.43	0.27	0.00
45	at_turnover*	0.23	0.23	0.00	0.23	0.24	0.01	0.37	0.25	0.01
46	opex_at	0.24	0.22	0.00	0.22	0.22	0.01	0.23	0.18	0.04
47	ope_bel1*	0.24	0.23	0.00	0.30	0.22	0.00	0.43	0.26	0.00
48	earnings_variability*	0.24	0.16	0.02	0.09	0.07	0.24	-0.00	0.26	0.28
49	seas_1_1na	0.24 0.26	0.10	0.02	0.03	0.07	0.06	0.28	0.00	0.02
50	dolvol_126d	0.26	0.17 0.34	0.00	0.23 0.27	0.14 0.35	0.00	0.23	0.21 0.43	0.02
50 51	be_gr1a	0.26	0.34 0.13	0.05	0.27	0.35 0.15	0.06	-0.10	0.43 0.10	0.00
52	div12m_me	$0.26 \\ 0.27$	$0.13 \\ 0.27$	0.00	0.09 0.51	$0.13 \\ 0.46$	0.00	0.10	0.10 0.51	0.10
53	sale_me	0.27 0.28	0.27 0.26	0.00	0.31	0.40	0.00	0.71 0.42	0.31	0.00
აა	sate_ine	0.20	0.20	0.00	0.55	0.55	0.00	0.42	0.34	0.00

54	$ocfq_saleq_std$	0.28	0.25	0.00	0.38	0.30	0.00	0.69	0.39	0.00
55	niq_at	0.29	0.36	0.00	0.75	0.57	0.00	0.96	0.58	0.00
56	$sale_gr3$	0.29	0.16	0.02	0.09	0.19	0.03	0.15	0.23	0.02
57	$sale_gr1$	0.30	0.16	0.02	0.17	0.20	0.02	-0.19	0.08	0.22
58	ni_be	0.30	0.28	0.00	0.42	0.33	0.00	0.31	0.23	0.01
59	$ivol_capm_252d$	0.30	0.26	0.00	0.41	0.30	0.00	0.21	0.23	0.01
60	$seas_25na$	0.31	0.22	0.00	0.36	0.41	0.00	0.67	0.54	0.00
61	$ret_{-}6_{-}1$	0.31	0.22	0.00	0.33	0.23	0.01	0.38	0.29	0.00
62	$seas_11_15na^*$	0.31	0.22	0.00	-0.07	0.08	0.23	-0.26	0.05	0.34
63	o_score	0.31	0.29	0.00	0.38	0.33	0.00	0.45	0.31	0.00
64	beta_dimson_21d*	0.31	0.26	0.00	0.33	0.24	0.00	0.06	0.14	0.08
65	aliq_at*	0.31	0.17	0.01	0.04	0.14	0.08	-0.07	0.12	0.13
66	dgp_dsale^*	0.31	0.23	0.00	-0.11	0.02	0.44	-0.03	0.02	0.43
67	rd_me	0.32	0.39	0.00	0.36	0.39	0.00	0.39	0.39	0.00
68	corr_1260d	0.32	0.29	0.00	0.24	0.27	0.00	0.26	0.26	0.00
69	qmj_safety	0.33	0.34	0.00	0.32	0.36	0.00	0.81	0.51	0.00
70	emp_gr1	0.34	0.22	0.00	0.16	0.28	0.00	0.50	0.41	0.00
71	eq_dur	0.34	0.33	0.00	0.38	0.37	0.00	0.52	0.41	0.00
72	betadown_252d	0.35	0.31	0.00	0.48	0.36	0.00	0.25	0.27	0.00
73	prc_highprc_252d	0.35	0.31 0.26	0.00	0.38	0.30 0.27	0.00	0.40	0.32	0.00
74	turnover_126d	0.36	0.20	0.00	0.50	0.39	0.00	0.40	0.32	0.00
75	ret_1_0	0.36	0.32 0.29	0.00	0.30	0.39 0.28	0.00	0.07	0.39	0.00
76	gp_at	0.36	0.29 0.37	0.00	0.20 0.31	0.28 0.36	0.00	0.78	0.49	0.03
70 77	beta_60m		0.37	0.00			0.00		0.49 0.35	
78		0.37	0.32 0.20	0.00	0.38	$0.32 \\ 0.15$	0.00 0.07	0.43	$0.35 \\ 0.12$	$0.00 \\ 0.13$
	taccruals_at	0.37			0.06			-0.00		
79	zero_trades_126d	0.38	0.34	0.00	0.52	0.41	0.00	0.51	0.41	0.00
80	ival_me*	0.38	0.35	0.00	0.38	0.37	0.00	0.40	0.36	0.00
81	seas_2_5an	0.39	0.38	0.00	0.55	0.45	0.00	0.46	0.41	0.00
82	ope_be	0.39	0.36	0.00	0.45	0.39	0.00	0.49	0.36	0.00
83	sale_bev	0.40	0.39	0.00	0.32	0.35	0.00	0.59	0.41	0.00
84	niq_be	0.41	0.43	0.00	0.83	0.61	0.00	0.92	0.59	0.00
85	niq_at_chg1*	0.41	0.38	0.00	0.18	0.32	0.00	0.90	0.48	0.00
86	ret_9_1	0.41	0.32	0.00	0.42	0.32	0.00	0.57	0.44	0.00
87	taccruals_ni	0.42	0.22	0.00	0.04	0.12	0.11	-0.18	0.04	0.34
88	dbnetis_at	0.42	0.37	0.00	0.14	0.28	0.00	0.59	0.41	0.00
89	ebit_bev	0.42	0.39	0.00	0.33	0.35	0.00	0.62	0.41	0.00
90	$iskew_capm_21d*$	0.42	0.33	0.00	-0.04	0.16	0.05	0.21	0.24	0.01
91	eqpo_me	0.42	0.38	0.00	0.37	0.37	0.00	0.43	0.37	0.00
92	$seas_16_20an$	0.42	0.38	0.00	0.51	0.38	0.00	0.22	0.33	0.00
93	op_at	0.42	0.40	0.00	0.46	0.42	0.00	0.52	0.40	0.00
94	$betabab_1260d$	0.42	0.39	0.00	0.61	0.50	0.00	0.70	0.53	0.00
95	$seas_11an$	0.42	0.36	0.00	0.47	0.36	0.00	0.11	0.23	0.01
96	$ivol_capm_21d*$	0.42	0.38	0.00	0.53	0.43	0.00	0.45	0.40	0.00
97	ni_me	0.43	0.41	0.00	0.41	0.43	0.00	0.76	0.55	0.00
98	$seas_11_15an$	0.43	0.38	0.00	0.20	0.31	0.00	0.39	0.34	0.00
99	at_gr1	0.43	0.29	0.00	0.08	0.22	0.01	0.24	0.31	0.00
100	$zero_trades_252d$	0.44	0.40	0.00	0.57	0.45	0.00	0.54	0.45	0.00
101	$ivol_hxz4_21d*$	0.44	0.39	0.00	0.38	0.37	0.00	0.88	0.52	0.00
102	$ebitda_mev$	0.44	0.43	0.00	0.46	0.46	0.00	0.70	0.53	0.00
103	eqnpo $_12m$	0.45	0.44	0.00	0.64	0.58	0.00	0.72	0.58	0.00
104	$capx_gr3$	0.45	0.31	0.00	0.41	0.39	0.00	-0.02	0.25	0.01
105	niq_su	0.47	0.41	0.00	0.24	0.35	0.00	0.78	0.46	0.00
106	rvol_21d	0.47	0.42	0.00	0.52	0.42	0.00	0.33	0.35	0.00
107	ivol_ff3_21d	0.48	0.43	0.00	0.45	0.41	0.00	0.72	0.52	0.00
108	ocf_me	0.49	0.46	0.00	0.31	0.40	0.00	0.92	0.63	0.00
109	ret_12_7	0.49	0.44	0.00	0.54	0.45	0.00	0.41	0.39	0.00

110	,	0.40	0.05	0.00	0.0=	0.00	0.00	0.00	0.0=	0.01
110	capex_abn	0.49	0.35	0.00	0.27	0.32	0.00	0.06	0.27	0.01
111	niq_be_chg1*	0.50	0.44	0.00	0.20	0.35	0.00	0.87	0.50	0.00
112	chcsho_12m	0.50	0.46	0.00	0.42	0.41	0.00	0.28	0.33	0.00
113	$resff3_6_1$	0.51	0.39	0.00	0.56	0.43	0.00	0.47	0.41	0.00
114	eqnpo_me	0.51	0.47	0.00	0.35	0.40	0.00	0.62	0.49	0.00
115	coa_gr1a	0.51	0.37	0.00	0.17	0.30	0.00	0.26	0.35	0.00
116	qmj_growth	0.52	0.44	0.00	0.24	0.29	0.00	0.25	0.26	0.01
117	$eqnetis_at$	0.52	0.49	0.00	0.54	0.52	0.00	0.59	0.51	0.00
118	ret_12_1	0.52	0.42	0.00	0.47	0.37	0.00	0.47	0.41	0.00
119	$rskew_21d$	0.52	0.42	0.00	0.08	0.26	0.01	0.19	0.27	0.00
120	$netis_at$	0.53	0.50	0.00	0.53	0.52	0.00	0.68	0.55	0.00
121	$seas_6_10na$	0.53	0.47	0.00	0.65	0.50	0.00	0.36	0.40	0.00
122	$mispricing_perf$	0.55	0.52	0.00	0.57	0.51	0.00	0.53	0.46	0.00
123	f_score	0.56	0.51	0.00	0.51	0.47	0.00	0.57	0.45	0.00
124	$rmax1_21d$	0.56	0.50	0.00	0.59	0.48	0.00	0.38	0.40	0.00
125	ocf_at_chg1	0.56	0.49	0.00	0.48	0.45	0.00	0.46	0.43	0.00
126	$seas_6_10an$	0.57	0.54	0.00	0.99	0.65	0.00	0.33	0.48	0.00
127	fcf_me	0.58	0.56	0.00	0.50	0.55	0.00	1.05	0.73	0.00
128	$rmax5_21d$	0.58	0.51	0.00	0.63	0.51	0.00	0.31	0.38	0.00
129	$capx_gr2$	0.60	0.44	0.00	0.35	0.41	0.00	0.10	0.34	0.00
130	qmj_prof	0.60	0.55	0.00	0.48	0.48	0.00	0.59	0.48	0.00
131	qmj	0.60	0.56	0.00	0.55	0.52	0.00	0.62	0.50	0.00
132	capx_gr1*	0.64	0.47	0.00	0.32	0.41	0.00	0.15	0.37	0.00
133	$debt_gr3$	0.67	0.50	0.00	0.36	0.43	0.00	0.22	0.39	0.00
134	rmax5_rvol_21d	0.67	0.56	0.00	0.34	0.43	0.00	0.04	0.29	0.00
135	lnoa_gr1a	0.69	0.52	0.00	0.29	0.39	0.00	0.07	0.33	0.00
136	fnl_gr1a	0.71	0.54	0.00	0.25	0.40	0.00	0.45	0.48	0.00
137	ppeinv_gr1a	0.71	0.52	0.00	0.24	0.36	0.00	0.07	0.32	0.00
138	oaccruals_at	0.71	0.54	0.00	0.38	0.48	0.00	0.65	0.57	0.00
139	inv_gr1a	0.72	0.55	0.00	0.25	0.39	0.00	0.29	0.44	0.00
140	nfna_gr1a	0.73	0.56	0.00	0.20	0.40	0.00	0.56	0.53	0.00
141	cop_atl1	0.75	0.68	0.00	0.46	0.52	0.00	0.77	0.61	0.00
142	dsale_dinv	0.75	0.57	0.00	0.21	0.30	0.00	0.03	0.25	0.01
143	oaccruals_ni	0.76	0.55	0.00	0.15	0.35	0.00	0.57	0.51	0.00
144	ocf_at	0.77	0.71	0.00	0.72	0.65	0.00	0.68	0.58	0.00
145	mispricing_mgmt	0.78	0.63	0.00	0.58	0.64	0.00	0.66	0.68	0.00
146	ncoa_gr1a	0.80	0.61	0.00	0.33	0.45	0.00	0.29	0.47	0.00
147	inv_gr1	0.80	0.62	0.00	0.47	0.52	0.00	0.06	0.38	0.00
148	resff3_12_1	0.81	0.69	0.00	0.98	0.80	0.00	0.72	0.68	0.00
149	nncoa_gr1a	0.82	0.63	0.00	0.28	0.43	0.00	0.30	0.47	0.00
150	cowc_gr1a	0.85	0.64	0.00	0.40	0.43 0.51	0.00	0.57	0.57	0.00
151	noa_at	0.85	0.66	0.00	0.40	0.31 0.47	0.00	0.22	0.44	0.00
151 152	noa_gr1a	0.91	0.75	0.00	0.50	0.47	0.00	0.22 0.64	0.44 0.70	0.00
152 153	cop_at*	1.02	0.73	0.00	0.54 0.62	0.69	0.00	0.04 0.85	0.70 0.73	0.00
100	cop_at	1.02	0.91	0.00	0.02	0.09	0.00	0.60	0.75	0.00

Note: The table shows monthly alpha in percentages across three different regions. α_{OLS} is the intercept from an OLS regression of the factor return on the regional market return. α_{EB} is the factor-region specific posterior mean found via the empricial Bayes procedure applied jointly to all the factor-region specific factors. $\Pr(\alpha_{\text{EB}} < 0)$ is the probability that the alpha is negative based on the posterior distribution from the EB procedure. We count a factor as replicated if this probability is below 2.5%. The residual volatility of all strategies have been scaled to 10% annualized. A "*" indicates that the original paper did not propose the factors as a significant predictor of realized returns.

Table J.3: Country Information

	Cost	MOOT		Stooled		Total Mania / C	Modian MC
1	Country	MSCI	Start	Stocks	Mega Stocks	Total Market Cap	Median MC
1	USA	Developed	1926-01-31	4,356	449	4.28e + 07	796
2	CHN	Emerging	1991-02-28	4,007	102	1.07e + 07	816
3	JPN	Developed	1986-01-31	3,867	88	7.05e + 06	176
4	HKG	Developed	1986-01-31	2,352	61	5.33e+06	92
5	GBR	Developed	1985-12-31	1,650	36	3.14e+06	158
6	FRA	Developed	1986-01-31	693	36	2.94e+06	121
7	SAU	Emerging	2000-02-29	199	8	2.61e+06	460
8	DEU	Developed	1986-01-31	659	36	2.58e + 06	155
9	IND	Emerging	1988-09-30	3,527	26	2.57e + 06	10
10	KOR	Emerging	1986-02-28	2,258	21	2.09e+06	131
11	CAN	Developed	1982-03-31	718	35	2.08e+06	198
12	TWN	Emerging	1988-02-29	1,951	12	1.77e + 06	121
13	AUS	Developed	1985-11-30	1,702	19	1.68e+06	51
14	CHE	Developed	1986-01-31	233	22	1.66e+06	863
15	NLD	Developed	1986-01-31	119	17	1.11e+06	939
16	SWE	Developed	1986-01-31	688	16	1.00e+06	82
17	ITA	Developed	1986-01-31	359	11	7.68e+05	121
18	ESP	Developed	1986-01-31	182	12	7.02e + 05	239
19	RUS	Emerging	1995-08-31	186	11	6.48e + 05	184
20	DNK	Developed	1986-01-31	161	8	5.90e+05	184
21	BRA	Emerging	1988-05-31	220	6	5.90e+05	575
22	SGP	Developed	1986-01-31	562	7	5.31e+05	59 75
23	THA	Emerging	1986-07-31	762	5	5.30e+05	75
24	IDN	Emerging	1989-01-31	656	6	4.93e + 05	82
25	MYS	Emerging	1986-01-31	923	2	4.44e+05	55
26	ZAF	Emerging	1986-01-31	261	3	4.07e + 05	137
27	BEL	Developed	1986-01-31	131	4	3.94e + 05	431
28	NOR	Developed	1986-01-31	272	3	3.44e+05	230
29	MEX	Emerging	1986-02-28	117	3	3.39e+05	992
30	FIN	Developed	1986-01-31	152	6	3.15e+05	218
31	PHL	Emerging	1986-01-31	248	2	2.66e + 05	164
32	TUR	Emerging	1990-03-31	389	1	2.38e+05	119
33	ARE	Emerging	2001-06-30	104	4	2.29e+05	284
34	ISR	Developed	1994-12-31	415	1	2.23e+05	110
35	VNM	Frontier	2006-08-31	713	0	1.80e+05	18
36	POL	Emerging	1993-07-31	706	1	1.78e + 05	14
37	CHL	Emerging	1989-01-31	174	0	1.71e+05	221
38	QAT	Emerging	2001-12-31	47	2	1.65e + 05	971
39	IRL	Developed	1986-01-31	33	4	1.65e + 05	652
40	NZL	Developed	1986-01-31	122	0	1.38e + 05	196
41	AUT	Developed	1986-01-31	68	0	1.26e + 05	327
42	KWT	Frontier	2001-01-31	163	2	9.84e + 04	80
43	PER	Emerging	1990-01-31	103	0	8.95e + 04	81
44	COL	Emerging	1989-01-31	44	1	8.81e+04	404
45	PRT	Developed	1986-08-31	44	2	8.55e+04	97
46	MAR	Frontier	1995-09-30	71	0	6.51e+04	183
47	GRC	Emerging	1988-09-30	149	0	5.20e+04	33
48	PAK	Emerging	1992-09-30	411	0	4.97e + 04	19
49	ARG	Emerging	1988-09-30	68	1	4.95e+04	113
50	NGA	Frontier	1993-11-30	150	0	4.68e + 04	11
51	BGD	Frontier	2002-05-31	324	0	4.40e+04	30
52	EGY	Emerging	1996-12-31	204	0	3.87e + 04	46

53	HUN	Emerging	1993-06-30	33	0	2.70e + 04	54
54	CZE	Emerging	1995-01-31	14	0	2.67e + 04	282
55	ROU	Frontier	1997-11-30	76	0	2.55e + 04	29
56	BHR	Frontier	2001-03-31	26	0	2.14e + 04	243
57	KEN	Frontier	1993-11-30	50	0	2.09e+04	30
58	HRV	Frontier	1997-11-30	73	0	2.07e + 04	35
59	BGR	Standalone	1995-12-31	113	0	1.68e + 04	24
60	JOR	Frontier	1993-08-31	154	0	1.63e + 04	18
61	OMN	Frontier	1998-03-31	107	0	1.62e + 04	35
62	LKA	Frontier	1987-06-30	265	0	1.55e + 04	15
63	TTO	Standalone	1997-08-31	19	0	1.29e + 04	292
64	KAZ	Frontier	2009-06-30	12	0	1.21e + 04	394
65	ISL	Standalone	1995-12-31	22	0	1.20e + 04	329
66	$_{ m JAM}$	Standalone	1993-12-31	66	0	1.13e + 04	29
67	SVN	Frontier	1995-03-31	22	0	8.50e + 03	122
68	TUN	Frontier	1995-09-30	74	0	8.46e + 03	38
69	CIV	Frontier	2002-04-30	39	0	7.61e + 03	85
70	MUS	Frontier	1995-08-31	62	0	7.14e + 03	48
71	LUX	Not Rated	1986-01-31	8	0	7.14e + 03	393
72	LTU	Frontier	1995-10-31	28	0	5.51e + 03	61
73	MLT	Standalone	1995-08-31	22	0	5.05e + 03	124
74	LBN	Standalone	1997-11-30	8	0	4.12e+03	335
75	EST	Frontier	1996-01-31	19	0	3.48e + 03	69
76	TZA	Not Rated	2000-07-31	16	0	3.34e + 03	16
77	SRB	Frontier	2009-09-30	29	0	3.17e + 03	10
78	BWA	Standalone	1995-09-30	22	0	3.13e+03	91
79	SVK	Not Rated	1986-01-31	10	0	3.12e+03	99
80	CYP	Not Rated	1994-01-31	37	0	3.12e+03	21
81	PSE	Standalone	2008-07-31	27	0	2.97e + 03	59
82	$_{\mathrm{GHA}}$	Not Rated	1997-11-30	16	0	2.89e + 03	67
83	BMU	Not Rated	2007-08-31	8	0	2.51e+03	118
84	NAM	Not Rated	1996-06-30	8	0	2.18e + 03	329
85	MWI	Not Rated	2008-08-31	12	0	2.15e + 03	118
86	ECU	Not Rated	1999-04-30	2	0	1.85e + 03	927
87	LVA	Not Rated	1997-10-31	20	0	1.17e + 03	13
88	UGA	Not Rated	2011-10-31	9	0	1.15e + 03	97
89	ZMB	Not Rated	1996-03-31	10	0	5.27e + 02	26
90	UKR	Standalone	2008-02-29	4	0	3.28e + 02	52
91	GGY	Not Rated	2015-04-30	2	0	2.25e + 02	113
92	IRN	Not Rated	2002 - 05 - 31	0	0	0.00e+00	0
93	URY	Not Rated	1996-06-30	0	0	0.00e+00	0
	All			4.021700e + 04	1,092	1.01e + 08	

Note: The table shows summary statistics by the country where a security is listed. We include common stocks that are the primary security of the underlying firm, traded on a standard exchange, with non-missing return and market equity data. Country is the ISO code of the underlying exchange country. For further information, see https://en.wikipedia.org/wiki/List_of_ISO_3166_country_codes. MSCI shows the MSCI classification of each country as of January 7th 2021. For the most recent classification, see https://www.msci.com/market-classification. Start is the first date with a valid observation. In the next 4 columns, the data is shown as of December 31st 2020. Stocks is the number of stocks available. Mega stocks is the number of stocks with a market cap above the 80th percentile of NYSE stocks. Total Market Cap is the aggregate market cap in million USD. Median MC is the median market cap in million USD.

Data Documentation

K Global Factor Data Documentation

We end the Internet Appendix with a documentation of our global factor data and how to use it to replicate our results and for future research. We will continue to update this data and its documentation as seen on our websites. The online document also contains instructions on how to run the code, bug fixes, and so on.

K.1 Identifier Variables

Here we define important identifying variables for our empirical analysis. We assign stocks to countries by excntry. We assign stocks to size groups via size_grp. We only include stocks with 1 on all the the obs_main, exch_main, primary_sec and common indicators.

Table K.1: Identifier Variables

Name	Description
excntry	The country of the exchange where the security is traded. Usually expressed as an ISO currency code with
excitory	the exception of mul which indicates a multi country exchange ⁵⁴
	This groups each firm into one of five categories: Mega, Large, Small, Micro and Nano cap. The groups are
	non-overlapping and the breakpoints are based on the market equity of NYSE stocks. In particular, Mega
size_grp	caps are all stocks with market equity larger than the 80th percentile of NYSE stocks, Large caps are all
	remaining stocks larger than the 50th percentile, Small caps are larger than the 20th percentile, Micro caps
	are larger than the 1st percentile and Nano caps are the remaining stocks.
obs main	If there are more than one firm observations for one date, this identifies if the observation is considered as the
ODS_IIIaIII	'main' observation. If available, CRSP observations are considered as the 'main' observation.
	Indicator for main exchanges. If CRSP is the source, main exchanges are those with $crsp_exchcd$ 1, 2 and 3.
exch_main	If Compustat is the source, main exchanges are all comp_exchg except 0, 1, 2, 3, 4, 13, 15, 16, 17, 18, 19, 20,
	21, 127, 150, 157, 229, 263, 269, 281, 283, 290, 320, 326, 341, 342, 347, 348, 349, 352.
primary_sec	Primary security as identified by Compustat. A 'gvkey' can have up to three different primary securities ('iid)'
primary_sec	at a given time (US, CA, and international). All observations from CRSP has primary_sec=1.
common	Indicator for common stocks. If CRSP is the source, common is one if the SHRCD variable is 10, 11 or 12. If
Common	Compustat is the source, common is one if TPCI is '0'

K.2 Helper Functions

This section describes functions that we use to create variables. Many of the functions are used for variables with quarterly, monthly and daily frequencies, and these are specified by " $_zQ$ ", " $_zM$ " and " $_zD$ " respectively, where " $_z$ " is the number of quarters, months or days that the function is referencing. For example, COVAR_12M(X, Y) is the covariance of variables X and Y over the past 12 months.

Table K.2: Helper Functions

Function	Name	Description
Mean	\overline{X}_z	$\frac{1}{z} \sum_{n=0}^{z-1} X_{t-n}$
Variance	$VARC_z(X)$	$\frac{1}{z-1} \sum_{n=0}^{z-1} (X_{t-n} - \overline{X_{t}}_z)^2$
Covariance	$COVAR_z(X, Y)$	$\frac{1}{z-1} \sum_{n=0}^{z-1} (X_{t-n} - \overline{X_{t}}_z) (Y_{t-n} - \overline{Y_{t}}_z)$
Standard Deviation	$\sigma_z(X)$	$\sqrt{VARC.z(X)}$
Skewness	SKEW_z(X)	$\frac{1}{z \times \sigma_z(X)^3} \sum_{n=0}^{z-1} (X_{t-n} - \overline{X_{t_z}})^3$

⁵⁴Typically over the counter exchanges.

Function	Name	Description
Standardized Unexpected Realization	SUR_z(X)	$\frac{X_t - (X_{t-3} + \overline{(X_{t-3} - X_{t-15})}_z/4)}{\sigma_z(X_{t-3} - X_{t-15})}$
Change to Expectations	CHG_TO_EXP(X)	$\frac{X_t}{(X_{t-12} + X_{t-24})/2}$
Maximum	MAXn_z(X)	The maximum n values of given input.
Quality Minus Junk Helpers		
Earnings Volatility	_EVOL	$ROEQ_BE_STD \times 2$. If this is unavailable, we use ROE_BE_STD .
Rank of Variable	$_{ extstyle -}rVar$	Cross-sectional rank of Var within a country 55
Z transformation	ZV(rVar)	$\frac{_rVAR - _rVAR_z}{_t(_rVAR)}$

K.3 Accounting Characteristics

Datasets

- COMP.FUNDA
- COMP.FUNDQ
- COMP.G_FUNDA
- COMP.G_FUNDQ

General Information

- We create characteristics for annual and quarterly accounting data separately. We then take the most recent characteristics value from each dataset to create the final dataset.
- We assume that accounting variables are publically available 4 months after the end of the accounting period.
- In describing accounting variables, we use the Compustatitem names from the annual dataset. The equivalent item name in the quarterly dataset can be found by adding a 'q' or 'y' to the end of the annual item name. Specifically, 'q' indicates a value calculated over one quarter while 'y' refers to the cumulative value over the quarters with data available within a fiscal year.

Annualized Accounting Variables from Quarterly Data

- The value of a balance sheet item such as asset or book equity has the same meaning in the annual and the quarterly data. It is the value by the end of a fiscal period.
- The value of an income or cash flow statement item is different. In the annual data, it is calculated over one year. However, in the quarterly data, it is calculated over one quarter. To make quarterly income and cash flows items comparable to the corresponding annual item, we take the sum of the item over the last four quarters.

 $^{^{55}}OACCRUALS_AT,~BETABAB_1260d,~DEBT_AT$ and $_EVOL$ are sorted in descending order. All other variables are sorted in ascending order.

Accounting Variables

The abbreviation is used to refer to the accounting variable. A suffix of '*' indicates that we have altered the original Compustat item to increase the coverage or to create a variable that is a part of creating a characteristic in the final dataset. The characteristic name will reflect the accounting name except the '*' suffix. As an example, 'gp_at' is gross profit scaled by assets. In general, we will refer to Compustat variables using capital letters.

Table K.3: Accounting Variables

Name	Abbreviation	Construction		
	Income Statement			
Sales	sale*	We prefer SALE. If this is unavailable, we use REVT		
Cost of Goods Sold	\cos	Compustat item COGS		
Gross Profit	gp^*	We prefer to use GP. If this is unavailable we use sale*-COGS		
Selling, General and Administrative	xsga	Compustat item XSGA		
Expenses	Abga	•		
Advertising Expenses	xad	Compustat item XAD. Note that this is not available in Compustat Global		
Research and Development Expenses	xrd	Compustat item XRD. Note that this is not available in Compustat Global		
Staff Expenses	xlr	Compustat item XLR		
Special Items	$_{ m spi}$	Compustat item SPI		
Operating Expenses	opex*	We prefer to use XOPR. If this is unavailable, we use COGS+XSGA		
Operating Income Before Depreciation	ebitda*	We prefer to use EBITDA. If this is unavailable, we use OIBDP. If this is unavailable, we use SALE*-OPEX*. If this is unavailable, we use GP*-XSGA		
Depreciation and Amortization	dp	Compustat Item DP		
Operating Income After Depreciation	ebit*	We prefer to use EBIT. If this is unavailable, we use OIADP. If this is unavailable, we use EBITDA*-DP		
Interest Expenses	int	Compustat item XINT		
Operating Profit ala Ball et al (2015)	op*	We use EBITDA* + XRD . If XRD is unavailable, we set it to		
Operating 1 font ala Ban et al (2013)	ор	zero		
Operating Profit to Equity	ope*	We use EBITDA*-XINT. Note that we target the same variable as the numerator of the profitability characteristic used to create the Robust-minus weak factor in the fama-French 5 factor model (Fama and French, 2015)		
Earnings before Tax and Extraordinary Items	pi*	We prefer to use PI. If this is unavailable we use EBIT*-XINT+SPI+NOPI where we set SPI and NOPI to zero if missing		
Income Tax	tax	Compustat item TXT		
Extraordinary Items and Discontinued	e e de	We prefer to use XIDO. If this is unavailable, we use XI+DO where we set DO to zero if missing. The reason why we		
Operations	xido*	set missing DO to zero is because it is not available in COMP.G.FUNDQ		
Net Income	ni*	We prefer to use IB. If this is unavailable, we use NI-XIDO*. If this is unavailable, we prefer PI*-TXT-MII. If MII is unavailable, it is set to zero		
Net Income Including Extraordinary Items	nix*	We prefer NI. If this is not available, we prefer NI*+XIDO*. If XIDO* is unavailable, we set it to zero. If that is unavailable, we prefer NI*+XI+DO		
Firm Income	fi*	We use NIX*+XINT		
Dividends for Common Shareholds	dvc	Compustat Item DVC		
Total Dividends	div*	We prefer DVT. If this is not available, we use DV		
Income Before Extraordinary Items	ni_qtr*	We use IBQ		
Net Sales	$sale_qtr*$	We use SALEQ		
	Cash Fl	ow Statement		
Capital Expenditures	capx	Compustat item CAPX		
Capital Expenditures to Sales	capex_sale*	We use CAPX / SALE*		
		We use OCF*-CAPX. Note that the free cash flow is com-		
Free Cash Flow	fcf*	puted before financing activities and sale of assets is taken		
		into account		
		We use PRSTKC+PURTSHR Equity Buyback is mainly		
Equity Buyback	eqbb*	PRSTKC in NA and PURTSHR in GLOBAL. Either of PRSTKC or PURTSHR are allowed to be missing		
Equity Issuance	eqis*	Compustat item SSTK		

Name	Abbreviation	Construction
Equity Net Issuance	eqnetis*	We use EQIS*-EQBB*. Either EQIS* or EQBB* are allowed
1 0	•	to be missing
Net Equity Payout	eqpo*	We use DIV*+EQBB*
Equity Net Payout	eqnpo*	We use DIV*-EQNETIS*
Net Long-Term Debt Issuance	dltnetis*	We prefer to use DLTIS-DLTR where we only require that one of the items are non-missing. If this is unavailable, we use LTDCH. If this is unavailable we use the yearly change in long-term book debt DLTT
Net Short-Term Debt Issuance	dstnetis*	We prefer DLCCH. If this is unavailable, we use the yearly change in short-term book debt DLC
Net Debt Issuance	dbnetis*	We use DLTNETIS*+DSTNETIS* and only require one of the items to be non-missing We use EQNETIS*+DBNETIS*. Either EQNETIS* or
Net Issuance	netis*	DBNETIS* are allowed to be missing
Financial Cash Flow	fincf*	We prefer FINCF. If this is unavailable, we use NETIS*-DV+FIAO+TXBCOF. If FIAO or TXBCOF is missing, it is set to zero
	Balance	Sheet - Assets
Total Assets	at*	We prefer to use AT. If this is unavailable, then we use SEQ* $+$ DLTT $+$ LCT $+$ LO $+$ TXDITC. If LCT, LO, or TXDITC
Current Assets	ca*	are missing, then they are set to zero We prefer ACT. If this is unavailable, we use
		RECT+INVT+CHE+ACO
Account Receivables Cash and Short-Term Investment	rec cash	Compustat item RECT Compustat item CHE
Inventory	inv	Compustat item INVT
Non-Current Assets	nca*	We use AT* - CA*
Intangible Assets	intan	Compustat item INTAN
Investment and Advances	ivao	Compustat item IVAO
Property, Plans and Equipment Gross	ppeg	Compustat item PPEGT
Property, Plans and Equipment Net	ppen	Compustat item PPENT
	Balance S	heet - Liabilities
Total Liabilities	lt	Compustat item LT
Current Liabilities	cl*	We prefer LCT. If this is unavailable, we use AP+ DLC+ TXP+ LCO
Accounts Payable	ap	Compustat item AP
Short-Term Debt	debtst	Compustat item DLC
Income Tax Payable	txp	Compustat item TXP
Non-Current Liabilities Long-Term Debt	ncl* debtlt	We use LT-CL* Compustat item DLTT
Long-Term Debt	аеви	We prefer to use TXDITC. If this is unavailable, we use
Deferred Taxes and Investment Credit	txditc*	TXDB+ ITCB
	Balance S	heet - Financing
Preferred Stock	pstk*	We prefer to use PSTKRV. If this is unavailable, we use PSTKL. If this is unavailable, we use PSTK
Total Debt	$debt^*$	We use DLTT+ DLC. Either DLTT or DLC are allowed to me missing
Net Debt	netdebt*	We use DEBT*- CHE where we set CHE to zero if missing
Shareholders Equity		We prefer to use SEQ. If this is unavailable, we use
Shareholders Equity	seq^*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT
Book Equity	seq*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing
- 0	-	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if miss-
Book Equity	be* bev*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use
Book Equity	be* bev*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock
Book Equity Book Enterprise Value	be* bev* Balance S	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary
Book Equity Book Enterprise Value Net Working Capital	be* bev* Balance S	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL*
Book Equity Book Enterprise Value Net Working Capital Current Operating Assets Current Operating Liabilities Current Operating Working Capital	be* Balance S nwc* coa* col* cowc*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*-CHE We use CL*- DLC. If DLC is missing, it is set to zero We use COA*-COL*
Book Equity Book Enterprise Value Net Working Capital Current Operating Assets Current Operating Liabilities Current Operating Working Capital Non-Current Operating Assets	be* Balance S nwc* coa* col* cowc* ncoa*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*- CHE We use CL*- DLC. If DLC is missing, it is set to zero We use COA*-COL* We use AT* - CA*- IVAO
Book Equity Book Enterprise Value Net Working Capital Current Operating Assets Current Operating Liabilities Current Operating Working Capital Non-Current Operating Assets Non-Current Operating Liabilities	be* Balance S nwc* coa* col* cowc* ncoa* ncol*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*- CHE We use CA*- CHE We use COA*-COL* We use AT* - CA*- IVAO We use LT-CL*- DLTT
Book Equity Book Enterprise Value Net Working Capital Current Operating Assets Current Operating Liabilities Current Operating Working Capital Non-Current Operating Assets	be* Balance S nwc* coa* col* cowc* ncoa*	CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*- CHE We use CL*- DLC. If DLC is missing, it is set to zero We use COA*-COL* We use AT* - CA*- IVAO

Name	Abbreviation	Construction
Financial Liabilities	fnl*	We use DEBT*+PSTK*. If PSTK* is missing, it is set to
N. T.	c 4	zero
Net Financial Assets	nfna*	We use FNA*-FNL*
Operating Assets	oa*	We use COA*+NCOA*
Operating Liabilities	ol*	We use COL*+NCOL*
Net Operating Assets	noa*	We use OA*-OL*
Long-Term NOA	lnoa*	PPENT + INTAN + AO - LO + DP
Liquid Current Assets	caliq*	We prefer to use CA^* - INVT. If this is unavailable, we use $CHE + RECT$
Property Plant and Equipment Less Inventories	ppeinv*	PPEGT + INVT
Ortiz-Molina and Phillips Liquidity	aliq*	CHE + $0.75 \times \text{COA}^* + 0.5(\text{AT*} - \text{CA*} - \text{INTAN})$. If INTAN is missing, we set it to zero
'	Mar	ket Based
Market Equity	me	We use the market equity for the stock we deem to the primary security of the firm. Importantly, we do not align the market value with the end of the fiscal period. Instead, we update the
Market Enterprise Value	mev*	market value on a monthly basis and align it with the most recently available accounting characteristic We use ME_COMPANY + NETDEBT* × FX*
Market Enterprise Value Market Assets	mat*	We use $AT^* \times FX + BE^* \times FX + ME_COMPANY$
Market Assets		
Accruals		
Operating Accruals	oacc*	We prefer NI*-OANCF. If that is unavailable, we use the yearly change in COWC*+the yearly change in NNCOA*
Total Accruals	tacc*	We use OACC* + the yearly change in NFNA*
Operating Cash Flow	ocf*	We prefer to use OANCF. If this is unavailable, we use NI*-OACC*. If this is unavailable, we use NI* + DP - WCAPT. If WCAPT is missing, we use 0.
Quarterly Operating Cash Flow	ocf_qtr^*	We use OANCFQ. If this is unavailable, then we use IBQ + DPQ - WCAPTQ. If WCAPTQ is unavailable, we set it to
Cash Based Operating Profitability	cop*	We prefer EBITDA*+XRD-OACC*. If XRD is unavailable, we set it to zero
Other		
Employees in Thousands	emp	Compustat item EMP

Table K.4: Accounting Characteristics

Name	Abbreviation	Construction
${\bf Growth - Percentage}^{56}$		
Asset Growth 1yr	at_gr1	$\frac{AT^*_{t}}{AT^*_{t-12}} - 1$
Sales Growth 1yr	sale_gr1	$\frac{SALE^*_t}{SALE^*_{t-12}} - 1$
Sales Growth 3yr	sale_gr3	$\frac{SALE^*_t}{SALE^*_{t-36}} - 1$
Total Debt Growth 3yr	debt_gr3	$\frac{DEBT^*_{t}}{DEBT^*_{t-36}} - 1$
CAPX 1 year growth	capx_gr1	$\frac{CAPX_t}{CAPX_{t-12}} - 1$
CAPX 2 year growth	capx_gr2	$\frac{CAPX_t}{CAPX_{t-24}} - 1$
CAPX 3 year growth	capx_gr3	$\frac{CAPX_t}{CAPX_{t-36}} - 1$
Quarterly Sales Growth	saleq_gr1	$\frac{SALE_QTR^*_{t}}{SALE_QTR^*_{t-12}} - 1$
Inventory Change 1 yr	inv_gr1	$\frac{INV_t}{INV_{t-12}} - 1$

⁵⁶This refers to all variables with a suffix of "gr1" or "gr3". The variables are percentage growth in the accounting variables before the suffix. The number in the suffix refers to either 1 or 3 year growth. For all variables, we only take the percentage growth if the denominator is above zero.

Name	Abbreviation	Construction
Sales scaled by Employees Growth 1 yr	sale_emp_gr1	$\frac{SALE_EMP_t}{SALE_EMP_{t-12}} - 1$
Employee Growth 1 yr	$\mathrm{emp_gr1}$	$\frac{EMP_{t} - EMP_{t-12}}{0.5 \times EMP_{t+1} \cdot 5 \times EMP_{t-12}}$
G	Frowth - Changed S	caled by Total Assets
Inventory Change 1yr	inv_gr1a	$\frac{INV_t - INV_{t-12}}{AT^*_t}$
Investment and Advances Change 1yr	lti_gr1a	$\frac{LTI_t - LTI_{t-12}}{AT^*_t}$
Current Operating Assets Change 1yr	coa_gr1a	$\frac{COA^*_{t} - COA^*_{t-12}}{AT^*_{t}}$
Current Operating Liabilities Change 1yr	col_gr1a	$\frac{COL_{t}^{*}-COL_{t-12}^{*}}{AT_{t}^{*}}$
Non-Current Operating Assets Change 1yr	ncoa_gr1a	$\frac{NCOA^*_{t} - NCOA^*_{t-12}}{AT^*_{t}}$
Non-Current Operating Liabilities Change 1yr	ncol_gr1a	$\frac{NCOL^*_{t}-NCOL^*_{t-12}}{AT^*_{t}}$
Net Non-Current Operating Assets Change lyr	nncoa_gr1a	$\frac{NNCOA^*_{t} - NNCOA^*_{t-12}}{AT^*_{t}}$
Net Operating Assets Change 1yr	noa_gr1a	$\frac{NOA^*_{t}-NOA^*_{t-12}}{AT^*_{t}}$
Financial Liabilities Change 1yr	${ m fnl_gr1a}$	$\frac{FNL^*_{t} - FNL^*_{t-12}}{AT^*_{t}}$
Net Financial Assets Change 1yr	nfna_gr1a	$\frac{NFNA^*_t - NFNA^*_{t-12}}{AT^*_t}$
Effective Tax Rate Change 1yr	tax_gr1a	$\frac{TAX_t - TAX_{t-12}}{AT^*_t}$
Change in Property, Plant and Equipment Less Inventories scaled by lagged Assets	ppeinv_gr1a	$\frac{PPEINV_{t}^{*}-PPEINV_{t-12}^{*}}{AT_{t-12}^{*}}$
Change in Long-Term NOA scaled by average Assets	lnoa_gr1a	$\frac{LNOA^*_{t} - LNOA^*_{t-12}}{AT^*_{t} - AT^*_{t-12}}$
Book Equity Change 1 yr scaled by Assets	be_gr1a	$\frac{BE^*_t - BE^*_{t-12}}{AT^*_t}$
Change in Short-Term Investments scaled by Assets	sti_gr1a	$\frac{IVST_t - IVST_{t-12}}{AT^*_t}$
	Profit I	Margins
Operating Profit Margin after Depreciation	ebit_sale	$\frac{EBIT*_{t}}{SALE*_{t}}$
Return on Assets		
Gross Profit scaled by Assets	gp_at	$\frac{GP_t^*}{AT_t^*}$
Cash Based Operating Profitability scaled by Assets	cop_at	$\frac{COP^*_t}{AT^*_t}$
Quarterly Income scaled by AT	niq_at	$\frac{NI_QTR^*_t}{AT^*_{t-3}}$
Operating Cash Flow scaled by Assets	ocf_at	$\frac{OCF^*_t}{AT^*_t}$
Ball Operating Profit to Assets	op_at	$\frac{OP_t^*}{AT_t^*}$
Ball Operating Profit scaled by lagged Assets	op_atl1	$\frac{OP^*_t}{AT^*_{t-12}}$

Name	Abbreviation	Construction
Gross Profit scaled by lagged Assets	gp_atl1	$\frac{GP^*_t}{AT^*_{t-12}}$
Cash Based Operating Profitability scaled by lagged Assets	cop_atl1	$\frac{COP^*_t}{AT^*_{t-12}}$
	Return on 1	Book Equity
Operating Profit to Equity scaled by BE	ope_be	$\frac{OPE^*_t}{BE^*_t}$
Net Income scaled by BE	ni_be	$\frac{NI^*_t}{BE^*_t}$
Quarterly Income scaled by BE	niq_be	$\frac{NI_QTR^*_t}{BE^*_{t-3}}$
Operating Profit scaled by lagged Book Equity	ope_bel1	$\frac{OPE^*_{t}}{BE^*_{t-12}}$
	Return on In	vested Capital
Operating Profit after Depreciation scaled by BEV	ebit_bev	$\frac{EBIT*_t}{BEV*_t}$
	Issu	ance
Net Issuance scaled by Assets	netis_at	$\frac{NETIS^*_{\ t}}{AT^*_{\ t}}$
Equity Net Issuance scaled by Assets	eqnetis_at	$\frac{EQNETIS^*_t}{AT^*_t}$
Net Debt Issuance scaled by Assets	dbnetis_at	$\frac{DBNETIS^*_t}{AT^*_t}$
	Acc	ruals
Operating Accruals	oaccruals_at	$\frac{OACC^*_t}{AT^*_t}$
Percent Operating Accruals	oaccruals_ni	$\frac{OACC^*_t}{ NIX^*_t }$
Total Accruals	taccruals_at	$\frac{TACC^*_t}{AT^*_t}$
Percent Total Accruals	taccruals_ni	$\frac{TACC^*_t}{ NIX^*_t }$
Net Operating Asset to Total Assets	noa_at	$\frac{NOA^*_t}{AT^*_t}$
	Financial Sou	indness Ratios
Operating Leverage	opex_at	$\frac{OPEX_t^*}{AT_t^*}$
	Activity/Effi	ciency Ratios
Asset Turnover	at_turnover	$\frac{SALE_{t}^{*}}{(AT_{t}^{*}+AT_{t-12}^{*})/2}$
Miscellaneous		
Sales scaled by BEV	sale_bev	$\frac{SALE^*_t}{BEV^*_t}$
R&D scaled by Sales	rd_sale	$rac{XRD_t}{SALE^*_t}$
Balance Sheet Fundamental to Market Equity		
Book Equity scaled by Market Equity	be_me	$\frac{BE^*_t}{ME_t}$
Total Assets scaled by Market Equity	at_me	$\frac{AT^*_t}{ME_t}$
Total Debt scaled by ME	debt_me	$\frac{DEBT*_t}{ME_t}$

Name	Abbreviation	Construction
Net Debt scaled by ME	netdebt_me	$\frac{NETDEBT^*_t}{ME_t}$
Income Fundamentals to Market Equity		
Net Income scaled by ME	ni_me	$\frac{NI^*_t}{ME_t}$
Sales scaled by ME	sale_me	$\frac{SALE_t^*}{ME_t}$
Operating Cash Flow scaled by ME	ocf_me	$\frac{OCF^*_t}{ME_t}$
Free Cash Flow scaled by ME	fcf_me	$\frac{FCF^*_t}{ME_t}$
R&D scaled by ME	rd_me	$\frac{XRD_t}{ME_t}$
Balance	Sheet Fundamentals	s to Market Enterprise Value
Book Enterprise Value scaled by MEV	bev_mev	$\frac{BEV^*_t}{MEV^*_t}$
E	quity Payout/Issua	nce to Market Equity
Net Equity Payout scaled by ME	eqpo_me	$\frac{EQPO^*_t}{ME_t}$
Equity Net Payout scaled by ME	eqnpo_me	$\frac{EQNPO^*_t}{ME_t}$
Incon	ne Fundamentals to	Market Enterprise Value
Operating Profit before Depreciation scaled by MEV	ebitda_mev	$\frac{EBITDA_t^*}{MEV_t^*}$
	Income	Growth
Number of Consecutive Earnings Increases	ni_inc8q	Count number of earnings increases over past 8 quarters
Operating Cash Flow to Assets 1 yr Change	ocf_at_chg1	$OCF_AT_t - OCF_AT_{t-12}$
Change in Quarterly Income scaled by BE	niq_be_chg1	$NIQ_BE_t - NIQ_BE_{t-12}$
Change in Quarterly Income scaled by AT	niq_at_chg1	$NIQ_AT_t - NIQ_AT_{t-12}$
Change Sales minus Change Inventory	dsale_dinv	$CHG_TO_EXP(SALE^*_t) - CHG_TO_EXP(INV_t)$
Change Sales minus Change Receivables	$dsale_drec$	$CHG_TO_EXP(SALE*_t) - CHG_TO_EXP(REC_t)$
Change Gross Profit minus Change Sales	dgp_dsale	$CHG_TO_EXP(GP^*_t) - CHG_TO_EXP(SALE^*_t)$
Change Sales minus Change SG&A	dsale_dsga	$CHG_TO_EXP(SALE*_t) - CHG_TO_EXP(XSGA_t)$
Earnings Surprise	saleq_su	$SUR(SALE_QTR^*)$
Revenue Surprrise	niq_su	$SUR(NI_QTR^*)$
Other Variables		
Cash and Short Term Investments scaled by Assets	cash_at	$\frac{CASH_t}{AT^*_t}$
R&D Capital-to-Assets	rd5_at	$\frac{\sum_{n=0}^{4} (12 \bullet n) (XRD_{t-12*n})}{AT^*_{t}}$
Age	age	Age of the firms in months

Name	Abbreviation	Construction
Abnormal Corporate Investment	capex_abn	$\frac{{{\scriptscriptstyle CAPX_SALE}^*}_t}{{{\scriptscriptstyle (CAPX_SALE}^*}_{t-12} + {\scriptscriptstyle CAPX_SALE}^*}_{t-24} + {\scriptscriptstyle CAPX_SALE}^*}_{t-36})/3} - 1$
Earnings before Tax and Extraordinary Items to Net Income Including Extraordinary Items	pi_nix	$\frac{PI^*_t}{NIX^*_t}$
Book Leverage	at_be	$\frac{AT^*_t}{BE^*_t}$
Operating Cash Flow to Sales Quarterly Volatility	ocfq_saleq_std	$SDEV_16Q\left(\frac{OCF_QTR^*_t}{SALE_QTR^*_t}\right)\right)$
Liquidity scaled by lagged Assets	aliq_at	$\frac{ALIQ^*_t}{AT^*_{t-12}}$
Liquidity scaled by lagged Market Assets	aliq_mat	$\frac{ALIQ^*_t}{MAT^*_{t-12}}$
Tangibility	tangibility	$\frac{CASH_t + 0.715 \bullet REC_t + 0.547 \bullet INV_t + 0.535 \bullet PPEG_t}{AT^*_t}$
Equity Duration	eq_dur	Outlined in detail here
Piotroski F-Score	f_score	Outlined in detail here
Ohlson O-Score	o_score	Outlined in detail here
Altman Z-Score	z_score	Outlined in detail here
Kaplan-Zingales Index	kz_index	Outlined in detail here
Intrinsic value	intrinsic_value	Outlined in detail here
Intrinsic value-to-market	ival_me	$\frac{INTRINSIC_{\cdot}VALUE^*_{t}}{ME_{t}}$
Earnings Variability	earnings_variability	$\frac{\sigma_{60M} \left(NI_{t/AT_{t-12}}^{*}\right)}{\sigma_{60M} \left(OCF_{t/AT_{t-12}}^{*}\right)}$
1 yr lagged Net Income to Assets	ni_ar1	$\frac{NI^*_{t-12}}{AT^*_{t-12}}$
Net Income Idiosyncratic Volatility	ni_ivol	Outlined in detail here

K.4 Market Based Characteristics

Datasets

- CRSP.MSF
- CRSP.DSF
- COMP.SECD
- COMP.G_SECD
- \bullet COMP.SECM
- COMP.SECURITY
- COMP.G_SECURITY

Market Variables

A suffix of '*' indicates that we have altered or renamed the original item.

Table K.5: Market Variables

Name	Abbreviation	Construction
		Variables ⁵⁷
Share Adjustment Factor	adjfct*	We use CFACSHR
Shares	shares*	We use SHROUT/1000 so shares outstanding are in millions.
Price	prc*	We use PRC
Local Price	prc_local*	We use PRC*
Highest Daily Price/Ask	prc_high	We use ASKHI. If PRC* or AKSHI are negative, then PRC_HIGH is set to missing
Lowest Daily Price/Bid	prc_low	We use BIDLO. If PRC* or BIDLO are negative, then PRC_LOW is set to missing
Adjusted Proce	prc_adj*	We use PRC*×ADJFCT*
Market Equity	me*	We use PRC*×SHARES* so market equity is quoted in million USD.
Company Market Equity	me_company*	We sum ME* grouped by PERMNO and date
Dollar Volume	dolvol*	We use $VOL \times PRC^*$
Return	RET*	We use RET
Local Return	ret_local*	We use RET
		We use (RET*-T30RET)/21. If T30RET is unavailable, we
Excess Return	ret_exc*	use RF. If the return is a daily return rather than a monthly return, the RET - T30RET is divided by 1 rather than 21.
Excess Return t+1	ret_exc_lead1m*	Excess return (ret_exc*) in month t+1
Time Since Most Recent Return	ret_lag_dif*	We automatically set this to 1
Cumulative Return	ri*	This is the cumulative return estimated from RET*
Cumulative Return		We use
Monthly Dividend	div_tot*	(RET -RETX) \times lag(PRC*) \times (CFACSHR/lag(CFACSHR))
	Compust	tat Variables
Share Adjustment Factor	adjfct*	We use AJEXDI
Shares	shares*	We use CSHOC/1000000
		,
Price	prc*	We use PRC_LOCAL*×FX
Local Price	prc_local* me*	We use PRCCD
Market Equity		We use PRC*×SHARES*
Company Market Equity	me_company*	We use ME*
Dollar Volume	dolvol*	We use CSHTRD×PRC*
Return	RET*	We use RET_LOCAL*×FX
		We use (RET*-T30RET)/21. If T30RET is unavailable, we
Excess Return	ret_exc*	use RF. If the return is a daily return rather than a monthly return, the RET - T30RET is divided by 1 rather than 21.
Excess Return t+1	$ret_exc_lead1m^*$	Excess return (ret_exc*) in month t+1
Cumulative Return - Local	ri_local*	We use PRC_LOCAL*× TRFD/AJEXDI
Local Return	ret_local*	We use RLLOCAL*/lag(RLLOCAL*) - 1 We estimate the number of days since the previous return. If
Time Since Most Recent Return	ret_lag_dif*	the returns are monthly rather than daily, then the time is in months
Cumulative Return	ri*	RLLOCAL* × FX*
Monthly Dividend	div_tot*	We use DIV \times FX*. If DIV is missing, we set it to zero
Cash Dividend	div_cash*	We use DIVD × FX*. If DIVD is unavailable, we set it to zero
Special Cash Dividend	div_spc*	We use DIVSP \times FX*. If DIVSP is unavailable, we set it to zero
Bid-Ask Average Dummy	bidask*	When $PRCSTD = 4$ then 1, otherwise 0
		icing Factors
Excess Market Return	mktrf*	Country specific market return
		Country specific factor following Fama and French (1993) and
High Minus Low	hml*	using breakpoints from non-micro cap stocks within the country
Small Minus Big ala Fama-French	smb_ff*	Average of small portfolios minus average of large portfolios from hml*
Return on Equity	roe*	Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on return on equity and size rather than triple sorts with investment, due to the limited number of stocks in some international markets.

 $^{^{57}}$ lag is a lag function where lag(x) is the value of x from the previous time period

Name	Abbreviation	Construction
Investment	inv*	Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited number of stocks in some international markets
Small Minus Big ala Hou et al	smb_hxz*	Average of small portfolios minus average of large portfolios from roe* and inv*
Market Volatility for Each Stock	_mktvol_zd*	$\sigma_{zD}(MKTRF*_t)$ 58

Table K.6: Market Characteristics

Name	Abbreviation	Construction			
Market Based Size Measure					
Market Equity	market_equity	ME^*_t			
Equity Payout					
Dividend to Price - 12 Months	div12m_me	$\frac{\sum_{n=0}^{11} DIV_TOT^*_{t-n} \times SHARES^*_{t-n}}{ME^*_{t}}$			
Change in Shares - 12 Month	chcsho_12m	$\frac{SHARES^*_{t} \times ADJFCT^*_{t}}{SHARES^*_{t-12} \times ADJFCT^*_{t-12}} - 1$			
Net Equity Payout - 12 Month	eqnpo_12m	$\log\left(\frac{RI^*_t}{RI^*_{t-12}}\right) - \log\left(\frac{ME^*_t}{ME^*_{t-12}}\right)$			
Momentum/Reversal					
Short Term Reversal	ret_1_0	$\frac{RI_{t}^*}{RI_{t-1}^*} - 1$			
Momentum 1-3 Months	ret_3_1	$\left \frac{RI^*_{t-1}}{RI^*_{t-3}} - 1 \right $			
Momentum 1-6 Months	ret_6_1	$\left \frac{RI^*_{t-1}}{RI^*_{t-6}} - 1 \right $			
Momentum 1-9 Months	ret_9_1	$\left \frac{RI^*_{t-1}}{RI^*_{t-9}} - 1\right $			
Momentum 1-12 Months	ret_12_1	$\frac{RI^*_{t-1}}{RI^*_{t-12}} - 1$			
Momentum 7-12 Months	ret_12_7	$\left \frac{RI_{t-7}^*}{RI_{t-12}^*} - 1 \right $			
Momentum 12-60 Months	ret_60_12	$\frac{RI^*_{t-12}}{RI^*_{t-60}} - 1$			
Seasonality					
1 Year Annual Seasonality	seas_1_1an	Return in month t-12			
2 - 5 Year Annual Seasonality	seas_2_5an	Average return over annual lags from year t-2 to t-5			
6 - 10 Year Annual Seasonality	seas_6_10an	Average return over annual lags from year t-6 to t-10			
11 - 15 Year Annual Seasonality	seas_11_15an	Average return over annual lags from year t-11 to t-15			
16 - 20 Year Annual Seasonality	seas_16_20an	Average return over annual lags from year t-16 to t-20)			
1 Year Non-Annual Seasonality	seas_1_1na	Average return from month t-1 to t-11			
2 - 5 Year Non-Annual Seasonality	seas_2_5na	Average return over non-annual lags from year t-2 to t-5			
6 - 10 Year Non-Annual Seasonality	seas_6_10na	Average return over non-annual lags from year t-6 to t-10			
11 - 15 Year Non-Annual Seasonality	seas_11_15na	Average return over non-annual lags from year t-11 to t-15			

 $^{^{58}\}mathrm{Must}$ have enough non-missing values of stock to be estimated

Name	Abbreviation	Construction			
16 - 20 Year Non-Annual Seasonality	seas_16_20na	Average return over non-annual lags from year t-16 to t-20			
Combined Accounting and Market Based Characteristics					
Let e_t be defined as described here					
60 Month CAPM Beta Performance Based Mispricing	beta_60m $ \\ \mbox{mispricing_perf}^{59} $	$\frac{COVAR_60M(RET^*_{t}, MKTRF^*_{t})}{VARC_60M(MKTRF^*_{t})} \\ \frac{1}{4} \left(O_SCORE_t^{r01} + RET_12_1_t^{r01} + GP_AT_t^{r01} + NIQ_AT_t^{r01}\right)$			
Management Based Mispricing	mispricing_mgmt	$\frac{1}{6} \left(CHCSHO_12M_t^{r01} + EQNPO_12M_t^{r01} + \\ OACCRUALS_AT_t^{r01} + NOA_AT_t^{r01} + \\ AT_GR1_t^{r01} + PPEINV_GR1A_t^{r01} \right)$			
Residual Momentum - 6 Month	resff3_6_1	$-1 + \prod_{n=1}^{6} 1 + e_{t-n}$			
Residual Momentum - 12 Month	resff3_12_1	$-1 + \prod_{n=1}^{12} 1 + e_{t-n}$			
	Daily Ma	rket Data ⁶⁰			
	Let ϵ_t be defined	d as described here			
Return Volatility	rvol_zd	$\sigma_{zD}(RET_EXC^*_t)$			
Maximum Return	rmax1_zd	$MAX1_zD(RET^*_t)$			
Mean Maximum Return	rmax5_zd	$\frac{1}{5} \sum_{n=1}^{5} X_n, X_n \in MAX5_zD(RET^*)$			
Return Skewness	rskew_zd	$SKEW_zD(RET_EXC*_t)$			
Price-to-High	prc_highprc_zd	$\frac{PRC_ADJ^*_t}{MAX1.zD(PRC_ADJ^*_t)}$			
Amihud (2002) Measure	ami_zd	$\left(\frac{ RET^*_t }{DOLVOL^*_t}\right)_{zD} * 1000000$			
CAPM Beta	beta_zd	Described in detail here			
CAPM Idiosyncratic Vol.	ivol_capm_zd	Described in detail here			
CAPM Skewness	iskew_capm_zd	Described in detail here			
Coskewness	$coskew_zd^{61}$	$\frac{\overline{(\epsilon_{t} \times MKTRF_DM_{t}^{2})}_{zD}}{\sqrt{(\epsilon_{t}^{2})}_{zD} \times \overline{(MKTRF_DM_{t}^{2})}_{zD}}}$			
Fama and French Idiosyncratic Vol.	ivol_ff3_zd	Described in detail here			
Fama and French Skewness	iskew_ff3_zd	Described in detail here			
Hou, Xue and Zhang Idiosyncratic Vol.	ivol_hxz4_zd	Described in detail here			
Hou, Xue and Zhang Skewness	iskew_hxz4_zd	Described in detail here			
Dimson Beta	beta_dimson_zd	Created as described in Dimson (1979)			

⁵⁹A rank characteristic has the value of that characteristics rank with respect to other companies' same characteristic of the same month and country scaled [0, 1]. This is identified with a "r01" superscript.

⁶⁰Many of the variables in this section are estimated using rolling windows of data, and the variables are estimated using a variety of window lengths: 21, 126, 252 and 1260 days. In this section, I refer to the number of days as m as a proxy for any of the possible window lengths.

 $^{^{61}}MKTRF_DM_t = MKTRF^*_t - \overline{MKTRF^*_{tzD}}$

Name	Abbreviation	Construction			
Downside Beta	betadown_zd	Described in detail here			
Zero Trades	zero_trades_zd	Number of days with zero trades over period. In case of equal number of zero trading days, turnover_zd will decide on the rank following Liu (2006)			
Turnover	turnover_zd	$\left(\frac{TVOL_{t}^{*}}{SHARES_{t}^{*}*100000}\right)_{zD}$			
Turnover Volatility	turnover_var_zd	$\frac{\sigma_{zD}\left((TVOL^*_t/SHARES^*_t)*1000000\right)}{TURNOVER_zD_t}$			
Dollar Volume	dolvol_zd	$\overline{DOLVOL^*_{tzD}}$			
Dollar Volume Volatility	dolvol_var_zd	$\frac{\sigma_{zD}(DOLVOL^*_{t})}{DOLVOL_zD_t}$			
Correlation to Market	corr_zd	The correlation between $RET_EXC^*_3l = RET_EXC^*_t + RET_EXC^*_{t-1} + RET_EXC^*_{t-2}$ and $MKT_EXC_3l = MKTRF^*_t + MKTRF^*_{t-1} + MKTRF^*_{t-2}$			
Betting Against Beta	betabab_1260d	$\frac{CORR_1260d_t \times RVOL_252d_t}{_MKTVOL_252d^*_t}$			
Max Return to Volatility	rmax5_rvol_21d	$\frac{RMAX5_21d_t}{RVOL_252d_t}$			
21 Day Bid-Ask High-Low	bidaskhl_21d	High-low bid ask estimator created using code from Corwin and Schultz (2012)			
Quality Minus Junk					
		$ZV(ZV(GP_AT_t) + ZV(NI_BE_t) +$			
Quality Minus Junk - Profit	qmj_prof	$ZV(NI_AT_t) + ZV(OCF_AT_t) + ZV(GP_SALE^*_t) +$			
		$ZV(OACCRUALS_AT_t)$			
		$ZV\Big(ZV(GPOA_CH5_t) + ZV(ROE_CH5_t)$			
Quality Minus Junk - Growth	qmj_growth	$+ZV(ROA_CH5_t) + ZV(CFOA_CH5_t) +$			
		$ZV(GMAR_CH5_t)$			
Quality Minus Junk - Safety	qmj_safety	$ ZV \Big(ZV (BETABAB_1260d_t) + ZV (DEBT_AT_t) $			
		$+ZV(O_SCORE_t) + ZV(Z_SCORE_t) + ZV(_EVOL_t)$			
Quality Minus Junk	qmj	$(QMJ_PROF_t + QMJ_GROWTH_t + QMJ_SAFETY_t)/3$			

K.5 Detailed Characteristic Construction

This section includes detailed descriptions how we built characteristics that don't easily fit into the Accounting Characteristics or Market Characteristics tables.

• Equity Duration

- Define the following variables:
 - * horizon: number of months used to estimate helper variables
 - * r: constant used as assumed discount rate
 - $\ast\,$ roe_mean: constant used as the average ROE value
 - * roe_ar1: constant used as the expected growth rate of ROE
 - * g_mean: constant used as the average sales growth rate
 - * g_ar1: constant used as the expected growth rate of sales

- Create initial variables:

- * If the number of non-missing observations is less than or equal to 12 or the variables' respective denominators are less than or equal to 1 _roe0_t and _g0_t are set to missing.
- Forecast cash distributions

$$\begin{split} roe_c &= roe_mean \times (1 - roe_ar1) \\ g_c &= g_mean \times (1 - g_ar1) \\ _roe_t &= \sum_{i=1}^{horizon} roe_c + roe_ar1 \times _roe_{t-i} \\ _g_t &= \sum_{i=1}^{horizon} g_c + g_ar1 \times _g_{t-i} \\ _be_t &= \sum_{i=1}^{horizon} _be_{t-i} \times (1 + _g_t) \\ _cd_t &= \sum_{i=1}^{horizon} _be_t \times (_roe_t - _g_t) \end{split}$$

Create duration helper variables ⁶²

$$\begin{aligned} ed_constant &= horizon + \frac{1+r}{r} \\ ed_cw_w_t &= \sum_{i=1}^{horizon} ed_cd_w_{i-1} + i \times \frac{_.cd_t}{(1+r)^i} \\ ed_cd_t &= \sum_{i=1}^{horizon} ed_cd_{i-1} + \frac{_.cd_t}{(1+r)^i} \end{aligned}$$

– Characteristic: $eq_dur_t = \frac{ed_ed_w_t \times FX_t}{ME_COMPANY_t} + ed_constant \times \frac{ME_COMPANY_t - ed_cd_t \times FX_t}{ME_COMPANY_t}$

• Piotroski F-Score

 $^{^{62}}ed_cw_w$, ed_cd and ed_err are equal to 0 at i = 1. ed_cw_w and ed_cd recusrively build upon themselves over the length of the horizon, so $ed_cw_w_{i-1}$, for example, would be the previous iteration of ed_cw_w

- Create helper variables:

$$\begin{split} & -f_roa_t = \frac{NI^*_t}{AT^*_{t-12}} \\ & -f_croa_t = \frac{OCF^*_t}{AT^*_{t-12}} \\ & -f_droa_t = -f_roa_t - -f_roa_{t-12} \\ & -f_acc_t = -f_croa_t - -f_roa_t \\ & -f_lev = \frac{DLTT_t}{AT^*_t} - \frac{DLTT_{t-12}}{AT^*_{t-12}} \\ & -f_liq_t = \frac{CA^*_t}{CL^*_t} - \frac{CA^*_{t-12}}{CL^*_{t-12}} \\ & -f_eqis_t = EQIS^*_t \\ & -f_gm_t = \frac{GP^*_t}{SALE^*_t} - \frac{GP^*_{t-12}}{SALE^*_{t-12}} \\ & -f_aturn_t = \frac{SALE^*_t}{AT^*_{t-12}} - \frac{SALE^*_{t-12}}{AT^*_{t-24}} \end{split}$$

- * For all variables except $_f_acc$, $_f_aturn _f_eqis$, if the count of available observations is less than or equal to 12, then the variable is set to missing. If $_f_aturn$ has less than or equal to 24 non-missing observations, it is set to missing. If a variable has AT^*_t or AT^*_{t-12} as an input and $AT^*_t \le 0$ or $AT^*_{t-12} \le 0$, then it is set to missing. If $CL^*_t \le 0$ or $CL^*_{t-12} \le 0$ then $_f_liq_t$ is set to missing. If $SALE^*_t \le 0$ or $SALE^*_{t-12} \le 0$ then $_f_gm_t$ is set to missing.
- Characteristic 63

$$\begin{split} f_score_t = & -f_roa_{>0,t} + -f_croa_{>0,t} + -f_droa_{>0,t} + -f_acc_{>0,t} + \\ & -f_lev_{<0,t} + -f_liq_{>0,t} + -f_eqis_{=0,t} + -f_gm_{>0,t} + -f_aturn_{>0,t} \end{split}$$

- Ohlson O-Score
 - Create helper variables:

 $^{^{63}}$ A subscript of > 0, ex: $VAR_{t>0,t}$, is a dummy for if the variable is greater than zero, and it is defined similarly for $VAR_{t<0,t}$ or any other specification. Otherwise, not included as an input, Also, if any variables other than f-eqis_t are missing, then f-score_t is set to missing.

- * If $AT^*_t \leq 0$, then $_o_lat_t$, $_o_lev_t$, $_o_wc_t$, and $_o_roe_t$ are set to missing. If $CA^*_t \leq 0$ then $_o_cacl_t$ is set to missing. If $LT_t \leq 0$ then $_o_ffo_t$ is set to missing. If LT_t or AT^*_t are missing, then $_o_neg_eq_t$ is set to missing. If there are less than or equal to 12 observations or either of NIX^*_t and NIX^*_{t-12} are missing, then $_o_nich_t$ and $_o_neg_earn_t$ are set to missing.
- Characteristic:

$$o_score_t = -1.37 - 0.407 \times _o_lat_t + 6.03 \times _o_lev_t + 1.43 \times _o_wc_t + 0.076 \times _o_cacl_t - 1.72 \times _o_neg_eq_t - 2.37 \times _o_roe_t - 1.83 \times _o_ffo_t + 0.285 \times _o_neg_earn_t - 0.52 \times _o_nich_t$$

• Altman Z-Score

Create helper variables:

$$\begin{aligned} & \textit{z} \textit{_w} c_t = \frac{CA^*_t - CL^*_t}{AT^*_t} \\ & \textit{_z} \textit{_r} e_t = \frac{RE_t}{AT^*_t} \\ & \textit{_z} \textit{_e} b_t = \frac{EBITDA^*_t}{AT^*_t} \\ & \textit{_z} \textit{_s} a_t = \frac{SALE^*_t}{AT^*_t} \\ & \textit{_z} \textit{_m} e_t = \frac{ME \textit{_FISCAL}_t}{LT_t} \end{aligned}$$

- * If $AT^*_t \leq 0$ then any variable including AT^*_t , then it is set to missing. If $LT_t \leq 0$, then $-z_-me_t$ is set to missing.
- Characteristic:

$$z_score_t = 1.2 \times _z_wc_t + 1.4 \times _z_re_t + 3.3 \times _z_eb_t + 0.6 \times _z_me_t + 1.0 \times _z_sa_t$$

• Kaplan-Zingales Index

- Create helper variables:

- * If the number of non-missing observations is less than or equal to 12, then $_kz_cf_t$, $_kz_dv_t$ and $_kz_cs_t$ are set to zero. If $PPENT_{t-12} \le 0$ then $_kz_cf_t$, $_kz_dv_t$ and $_kz_cs_t$ are set to missing. If $AT^*_t \le 0$ then $_kz_dt$ is set to missing. If $(DEBT^*_t + SEQ^*_t) = 0$ then $_kz_db_t$ is set to missing.
- Characteristic:

$$kz_index = -1.002 \times _kz_cf_t + 0.283 \times _kz_d_t + 3.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t + 2.139 \times$$

• Intrinsic Value from Frankel and Lee

- Define r as a constant assumed discount rate
- Create helper variables:

* If $NIX^*_t \leq 0$ then

$$iv_po_t = \frac{DIV^*_t}{AT^*_t \times 0.06}$$

- * If the number of non-missing observations is less than or equal to 12 or $(BE^*_t + BE^*_{t-12}) \le 0$ then $_iv_roe_t$ is set to missing.
- Characteristics:

$$intrinsic_value_t = BE*_t + \frac{_iv_roe_t - r}{1 + r} \times BE*_t + \frac{_iv_roe_t - r}{(1 + r) \times r} \times _iv_be1_t$$

- * If $intrinsic_value_t \leq 0$ then it is set to missing.
- Net Income Idiosyncratic Volatility
 - Define the following variable ⁶⁴:

$$_ni_at_t = \frac{NI^*_t}{AT^*_t}$$

 A rolling regression of the following form is run for each company, with the time series split up into n groups:

$$_ni_at_t = \beta_0 + \beta_1 _ni_at_{t-12} + u_t$$

where edf_t = the error degrees of freedom of regression and $rmse_t$ = root mean square error of the regression.

Characteristic:

$$ni_ivol_t = \sqrt{\frac{rmse_t^2 \times edf_t}{edf_t + 1}}$$

- Beta, Idiosyncratic Volatility and Skewness of Asset Pricing Factor Regressions
 - This section describes the construction of beta_zd for the CAPM model, and the idiosyncratic volatility and skewness characteristics, which are estimated using three different factor models:
 - * CAPM (capm):

$$RET_{-}EXC^*_{t} = \beta_0 + \beta_1 MKTRF^*_{t} + \epsilon_t$$

* Fama-French 3 Factor Model (ff3):

$$RET_EXC^*_t = \beta_0 + \beta_1 MKTRF^*_t + \beta_2 HML^*_t + \beta_3 SMB_FF^*_t + e_t$$

⁶⁴If $AT^*_t \leq 0$, then $_ni_at_t$ is set to missing

* Hou, Xue and Zhang 4 Factor Model (hxz4):

$$RET_EXC^*_t = \beta_0 + \beta_1 MKTRF^*_t + \beta_2 SMB_HXZ^*_t + \beta_3 ROE^*_t + \beta_4 INV^*_t + \mu_t$$

Characteristics ⁶⁵:

$$beta_zd = \beta_1 \text{ from the CAPM model}$$

$$ivol_capm_zd_t = \sigma_{zD}(\epsilon_t)$$

$$ivol_ff3_zd_t = \sigma_{zD}(e_t)$$

$$ivol_hxz4_zd_t = \sigma_{zD}(\mu_t)$$

$$iskew_capm_zd_t = SKEW_zD(\epsilon_t)$$

$$iskew_ff3_zd_t = SKEW_zD(e_t)$$

$$iskew_hxz4_zd_t = SKEW_zD(\sigma_t)$$

• Downside Beta

- Define the following regression model run over z days:

$$RET_{-}EXC^*_{t} = \beta_0 + \beta_1 MKTRF^*_{t} + \epsilon_t$$

However, we restrict the data to when $MKTRF^*$ is negative.

- Characteristic:
 - * $betadown_zd = \beta_1$

K.6 FX Conversion Rate Construction

This section outlines how we create a daily dataset, beginning 01/01/1950 to now, of X currency - USD exchange rate using COMPUSTAT. This is run in the macro $compustat_fx()$ in the $project_macros.sas$ file.

- We use COMP.EXRT_DLY, which has daily conversion rates from GBP to other currencies 'X'.
- Every day available, we estimate the exchange rate fx_t as

$$fx_t = \frac{USD_{GBP,t}}{X_{GBP,t}}$$

where $X_{GBP,t}$ is the exchange rate of GBP to currency X on day t.

- In case there are gaps in information, we assume the exchange rate of the last observation until a new observation is available.
- fx_t is quoted as $\frac{X_t}{USD_t}$, so to go from X to USD, do $X_t \times fx_t$

 $^{^{65}}z$ indicates over how many days the model is run.

Global Factor Data Documentation

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1 Overview

• This documentation describes the Global Factor Data, and the associated code for constructing the data, based on (Jensen, Kelly, & Pedersen, 2023). The citation for use of this data and code is:

```
@article{JensenKellyPedersen2023,
  author = {Jensen, Theis Ingerslev and Kelly, Bryan and Pedersen, Lasse Heje},
  title = {Is There a Replication Crisis in Finance?},
  journal = {The Journal of Finance},
  volume = {78},
  number = {5},
  pages = {2465-2518},
  year = {2023}
}
```

- The Global Factor Data includes 406 characteristics and their associated factor portfolios. This is a superset of the 153 factors analyzed in Jensen, Kelly, and Pedersen (2023).
- This documentation is grouped into eight main sections: Identifier Variables, Industry Identifiers, Helper Functions, Accounting Characteristics, Market Based Characteristics, Detailed Characteristic Construction, FX Conversion Rate Construction and Factor Details and Citations.
 - Identifier Variables include firm identifying information, date, etc...
 - Each of the Characteristics sections includes at least three subsections: Datasets,
 Variables, and Characteristics.
 - Datasets refers to which datasets the items in variables are drawn from. For example, 'COMP.FUNDA' suggests we use variables from the FUNDA dataset provided by Compustat.
 - Variables refers to a table containing information about the variables drawn from the datasets previously identified. These tables include the name, abbreviation used throughout the section, and the construction of the variables. These variables are constructed in a way to maximize coverage and are not directly included in the final dataset.
 - Characteristics refers to a table of constructed characteristics made of the previously describes variables. These tables include the name, the abbreviation used in the published dataset, and the construction. These characteristics are in the final dataset.

1.1 How To Run the Code

• Access the code for this data set at https://github.com/bkelly-lab/ReplicationCrisis.

- This data is produced using the SAS Studio on Wharton Research Data Services (WRDS) servers. The github README file contains instruction on how to generate the data.
- Use the 'EOM' (end of month) variable as the date variable to join/merge datasets.

1.2 How To Use the Data

- The id column is the unique security \times source¹ identifier.
- The eom column shows the end of month, where the data is valid. In other words, it shows the information available by the end of a given month. As an example, the me value for a stocks with eom=20191231, will be the last available market equity before or at December 31st 2019. Therefore, when predicting the return column ret, characteristics should be lagged by one month (as ret shows the return in the current month identified by eom). Alternatively, you can predict next month's returns, stored in ret_exc_lead1m, without lagging the characteristics.
- The excntry column, identifies the country of the exchange where the security is traded.
- Suggested screens:
 - To restrict the sample to one observation per security \times month, use obs_main=1.
 - To restrict the sample to common stocks, use common=1.
 - To restrict the sample to prominent exchanges, use exch_main=1.
 - To restrict the sample to primary listing \times month, use primary_sec=1.

1.3 Versions, Bug Fixes, and Comments

- We will update the code and data regularly as CRSP and Compustat updates become available. We will also release periodic updates with bug fixes. Our GitHub repository: https://github.com/bkelly-lab/ReplicationCrisis/blob/master/GlobalFactors/CHANGELOG.md tracks the evolution in the code used to generate the data. Furthermore, Table 1 gives an overview of the most important changes.
- The code and data has been carefully vetted, but may contain bugs and certainly has room for improvement. We welcome any and all feedback regarding bugs or suggestions for improvements and extensions.
- Send correspondence to bryan.kelly@yale.edu with subject "Global Factor Data"

¹CRSP or Compustat.

Table 1: Log of Important Code and Methodology

Date	Changes				
03-05-2025	 Updated market returns macro to add a capped value option. Corrected error in o-score calculation 				
03-03-2023	• Added 'me' (market equity) and 'ret' (total return) and removed 'source_crsp' from daily return files.				
02-08-2022	• Fixed error in the construction of intrinsic_value. Previously, we failed to scale intrinsic_value by market equity as done in Frankel and Lee (1998). We call the new characteristic ival_me and keep intrinsic_value in the data set. The alpha of the new factor based on ival_me is significantly different from zero, while the factor based on intrinsic_value is insignificant.				
11-16-2021	 Changed return cutoffs to depend on all stocks, instead of only stocks from CRSP. Changed the 'source' (character) column to 'source_crsp' (integer), source_crsp is 1 if CRSP is the return data source. Changed the 'id' column from character to integer. For stocks from CRSP, the id is just their permno. For stocks from Compustat, the first digit is 1 if the stock is traded on a US exchange, 2 if it's traded on a Canadian exchange, and 3 otherwise. The next two digits are the IID from Compustat, and the remaining six digits are the gykey. Adapted the primary_sec column such that all observations from CRSP have primary_sec=1. Changed the treatment of zero return. Previously, we treated a zero return as a missing observation. Now, we have removed this screen, such that a zero return is treated like any other return. Changed the creation of characteristics based on daily stock market data. Previously, we winsorized daily returns, market equity, and dollar volume, before creating characteristics based on daily stock market data. Now, we have removed this winsorization, and daily characteristics are based on the raw data. Added the option to create daily factor return in the portfolios.R code. Added the option to create industry returns in the portfolios.R code. 				
08-27-2021	 Fixed a bug regarding how daily delisting returns from CRSP are incorporated. Added indfmt='FS' to the international accounting data. 				

Date	Changes
06-14-2021	• We changed the winsorization scheme. First, we removed the 0.01%/99.9% winsorization of market equity in all countries. Second, we removed the winsorization of returns from the CRSP database. For Compustat returns, we set returns above (below) the 99.9% (0.01%) of CRSP returns in the same month, to that level. In other words, we base our winsorization of Compustat data on CRSP data from the same month.
02-19-2021	 Previously we did not exclude securities that are only traded over the counter. In the new version of the data set, we include an indicator column "exch_main" to exclude non-standard exchanges. In the US, the main exchanges are AMEX, NASDAQ, and NYSE. Outside of the US, we exclude over the counter exchanges, stock connect exchanges in China, and cross-country exchanges such as BATS Chi-X Europe. The documentation includes a full list of the excluded exchanges. Included SIC, NAICS, and GICS industry codes.
02-15-2021	• Removed a bug that caused ivol_ff3_21d, iskew_ff3_21d, ivol_hxz4_21d, and iskew_hxz4_21d to require 17 (ff3) and 18 (hxz) observations for a valid estimate. Consistent with our original intent, we now require at least 15 observations for a valid estimate.
02-01-2021	 Fixed a small bug in the bidask_hl() macro. Lowered the requirement for the number of stocks needed when creating asset pricing factors (FF and HXZ). We previously required at least 5 stocks in a sub-portfolio (e.g., small stocks with high BM) for the observation to be valid. This led to missing observations in the 1950s for small stocks with low BM. We lowered this requirement to 3 stocks. Furthermore, when creating asset pricing factors, we changed the breakpoints to be based on NYSE stocks in the US instead of non-microcap stocks. Outside of the US, breakpoints are still based on non-microcap stocks.

Date	Changes
01-25-2021	 Changed residual momentum characteristics (resff3_12_1 & resff3_6_1) to be scaled with the standard deviation of residuals consistent with Blitz, Huij, and Mertens (2011). Fixed error in creating qmj_prof. The issue was that the oaccruals_at used the value instead of the z-score of ranks. This effectively meant that accruals didn't impact the profitability score. Fixed error for annual seasonality characteristics (factor names starting with seas_ and ending with _an). There was a bug in the screening procedure which meant that the characteristic for one stock could use information from an unrelated stock. Rounding issues when converting a .csv file to an excel file, caused the zero_trades_* variables to not have any decimals which made the turnover tie-breaker ineffective. Standardized unexpected earnings (niq_su) and sales (saleq_su) is computed as the actual value minus the expected value (standardized by the standard deviation of this change). Before, the expected value was computed as the mean yearly change over the last 8 quarters added to the last quarterly value. Now the expected value is the same mean yearly change, but added to the quarterly value 4 quarters ago consistent with Jegadeesh and Livnat (2006).

1.4 Terminology

- Annual data refers to accounting data from annual reports sourced from COMP.FUNDA and COMP.G_FUNDA.
- Quarterly data refers to accounting data from quarterly reports sourced from COMP.FUNDQ and COMP.G_FUNDQ.
- Final Dataset refers to "world_data.sas7bdat", the output dataset
- Fiscal period refers to the relevant period over which income and expenses have accrued.
- Accounting variables refers to accounting items such as assets, sales and net income.
- Market variables refers to market based items such as market equity and excess return.
- Characteristics refers to columns in the final dataset that reveals a characteristic about the security, For example asset growth, book to market equity, and net income to book equity.

2 Factor Portfolio Construction

- For each characteristic, we build the 1-month holding period factor return within each country as follows.
- In each country and month, we sort stocks into characteristic terciles (top/middle/bottom third) with breakpoints based on non-micro stocks in that country. Specifically, we start with all non-micro stocks in a country (i.e., larger than NYSE 20th percentile) and sort them into three groups of equal numbers of stocks based on the characteristic, say book-to-market. Then we distribute the micro-cap stocks into the three groups based on the same characteristic breakpoints. This process ensures that the non-micro stocks are distributed equally among across portfolios, creating more tradable portfolios.
- For each tercile, we compute its "capped value weight" return, meaning that we weight stocks by their market equity, winsorized at the NYSE 80th percentile. This construction ensures that tiny stocks have tiny weights and any one mega stock does not dominate a portfolio, seeking to create tradable, yet balanced, portfolios.
- The factor is then defined as the high-tercile return minus the low-tercile return, corresponding to the excess return of a long-short zero-net-investment strategy. The factor is long (short) the tercile identified by the original paper to have the highest (lowest) expected return.
- For a factor return to be non-missing, we require that it has at least 5 stocks in each of the long and short legs. We also require a minimum of 60 valid monthly observations for each country-specific factor for inclusion in our sample.
- We update characteristics with the most recent accounting data (which could be either annual or quarterly) starting four months after the end of the fiscal period.
- To compute a cluster (theme) return, we first sign factors according to the original reference, then we equal-weight the returns of factors within a specific cluster. The signing convention and cluster allocation follows (Jensen et al., 2023) and we show it in table 9.

3 Identifier Variables

This section covers all of the variables that give firm/date level identifiers and information. If a variable starts with 'comp' or 'crsp', then the following variable name is drawn from the specified dataset. For example, 'crsp_shrcd' is the 'shrcd' variable from CRSP.

Table 2: Identifier Variables

Name	Description
size_grp	This groups each firm into one of five categories: Mega, large, small, micro and nano cap. The groups are non-overlapping and the breakpoints are based on the market equity of NYSE stocks by the end of each month. In particular, Mega caps are stocks with a market cap above the 80th percentile of NYSE stocks, large caps are all remaining stocks above the 50th percentile, small caps are above the 20th percentile, micro caps above the 1st percentile and nano caps are the remaining stocks.

Name	Description
id	We generate a unique number for each security in our data set. For securities from CRSP, the id is just the corresponding permno. For stocks from Compustat, the first digits is 1 if the stocks is traded on a US exchange, 2 if it's traded on a Canadian exchange, and 3 otherwise. The next six digits are the gykey and the last two are the iid. ²
source_crsp	Identifies the source of the return data. A 1 (0), indicates that the source is CRSP (Compustat).
obs_main	For US stocks, we often have two observations for each security-month pair. One from Compustat, and one from CRSP. In cases with duplicates, the observation from CRSP has obs_main=1, and the observation from Compustat has obs_main=0. If there are more than one firm observations for one date, this identifies if the observation is considered as the 'main' observation. If available, CRSP observations are considered as the 'main' observation.
exch_main gvkey	Indicator for ordinary exchanges. If CRSP is the source, main exchanges are those with $crsp_exchcd$ 1, 2 and 3. If Compustat is the source, main exchanges are all comp_exchg except 0, 1, 2, 3, 4, 13, 15, 16, 17, 18, 19, 20, 21, 127, 150, 157, 229, 263, 269, 281, 283, 290, 320, 326, 341, 342, 347, 348, 349, 352. Permanent six-digit unique firm identifier from Compustat
iid	Permanent two-digit addition to 'gvkey' that identifies specific security of a firm from Compustat
primary_sec	Primary security as identified by Compustat. A 'gvkey' can have up to three different primary securities ('iid)' at a given time (US, CA, and international). All observations from CRSP has primary_sec=1. Permanent unique firm identifier from CRSP
permno	Permanent security identifier from CRSP
excntry curcd	The country of the exchange where the security is traded. Usually expressed as an ISO currency code with the exception of <i>mul</i> which indicates a multi country exchange ³ Currency of <i>prc_local</i> and the currency used to calculated <i>ret_local</i> .
fx	Ratio of curcd to USD at the date of observation
common	Indicator for common stocks. If CRSP is the source, common is one if the SHRCD variable is 10, 11 or 12. If Compustat is the source, common is one if TPCI is '0'
comp_tpci	Compustat issue type identifier
crsp_shrcd	CRSP share code
comp_exchg	Compustat stock exchange code
crsp_exchd	CRSP stock exchange code
date	Date of the last return observation during the month.
eom	The last day of the month in which the observation is made
adjfct	Share adjustment factor, using 'cfacshr' if the source is CRSP or 'ajexdi' if the source is Compustat

4 Industry Identification

This section describes the industry identifiers. First we contruct separate identifiers for CRSP and Compustat. Based on these datasets, we create one SIC, NAICS and GICS code for each firm based on Compustat data if available and otherwise CRSP. GVKEY is the company identifier for COMPUSTAT. PERMNO is the security identifier for CRSP. While we would prefer to use PERMCO, which is company level, different firms with different industry identifications can be listed under the same PERMCO. CRSP identifiers are available on a daily basis. For Compustat, we extract SIC and NAICS codes from annual accounting reports. Historical GICS codes are only available in Compustat. The Fama-French industry identifier is mapped from SIC codes using documentation provided by Ken French. We allow for using either 38 or 49 industry portfolio definitions, as defined here and here, respectively. By default, we use the 49 portfolio definition, but that can be adjusted in 'main.sas'.

²In Compustat, a security is identified by gvkey and iid. To map our id to Compustat, add 'C' or 'W' to the iid if the first digit is 2 or 3 respectively.

³Typically over the counter exchanges.

4.1 Datasets

- CRSP.DSENAMES
- COMP.FUNDA
- COMP.G_FUNDA
- COMP.CO_HGIC
- COMP.G_CO_HGIC

Table 3: Identifier Variables

Name	Description
sic	Firm SIC industry. We use Compustat data if available and otherwise use CRSP data.
naics	Firm NAICS industry. We use Compustat data if available and otherwise use CRSP data.
gics	Firm GICS industry. We use historical data from Compustat.
ff49	Classification of stocks into 49 industry groups based SIC codes and the methodology in Fama and French (1997) with the addition of a software industry.

5 Helper Functions

This section describes functions that we use to create variables. Many of the functions are used for variables with quarterly, monthly and daily frequencies, and these are specified by "_zQ", "_zM" and "_zD" respectively, where "z" is the number of quarters, months or days that the function is referencing. For example, COVAR_12M(X, Y) is the covariance of variables X and Y over the past 12 months.

Table 4: Helper Functions

Function	Name	Description	
Mean	\overline{X}_z	$\frac{1}{z} \sum_{n=0}^{z-1} X_{t-n}$	
Variance	VARC_z(X)	$\frac{1}{z-1} \sum_{n=0}^{z-1} (X_{t-n} - \overline{X_{t}}_z)^2$	
Covariance	$COVAR_z(X, Y)$	$\frac{1}{z-1} \sum_{n=0}^{z-1} (X_{t-n} - \overline{X_{t}}_z) (Y_{t-n} - \overline{Y_{t}}_z)$	
Standard Deviation	$\sigma_z(X)$	$\sqrt{VARC_{-z}(X)}$	
Skewness	$SKEW_z(X)$	$\frac{1}{z \times \sigma_z(X)^3} \sum_{n=0}^{z-1} (X_{t-n} - \overline{X_{tz}})^3$	
Standardized Unexpected Realization	$SUR_z(X)$	$\frac{X_t - (X_{t-3} + \overline{(X_{t-3} - X_{t-15})}_z/4)}{\sigma_z(X_{t-3} - X_{t-15})}$	
Change to Expectations	CHG_TO_EXP(X)	$\frac{X_t}{(X_{t-12} + X_{t-24})/2}$	
Maximum	$MAXn_z(X)$	The maximum n values of given input.	
Quality Minus Junk Helpers			
Earnings Volatility	_EVOL	$ROEQ_BE_STD \times 2$. If this is unavailable, we use ROE_BE_STD .	

Function	Name	Description
Rank of Variable	$_{ extstyle -}rVar$	Cross-sectional rank of Var within a $\operatorname{country}^4$
Z transformation	ZV(rVar)	$\frac{_{-rVAR}_{-rVAR_z}}{_{-t(_{-rVAR})}}$

6 Accounting Characteristics

6.1 Datasets

- COMP.FUNDA
- COMP.FUNDQ
- COMP.G_FUNDA
- COMP.G_FUNDQ

6.2 General Information

- We create characteristics for annual and quarterly accounting data separately. We then take the most recent characteristics value from each dataset to create the final dataset.
- We assume that accounting variables are publically available 4 months after the end of the accounting period.
- In describing accounting variables, we use the Compustat item names from the annual dataset. The equivalent item name in the quarterly dataset can be found by adding a 'q' or 'y' to the end of the annual item name. Specifically, 'q' indicates a value calculated over one quarter while 'y' refers to the cumulative value over the quarters with data available within a fiscal year.

6.3 Annualized Accounting Variables from Quarterly Data

- The value of a balance sheet item such as asset or book equity has the same meaning in the annual and the quarterly data. It is the value by the end of a fiscal period.
- The value of an income or cash flow statement item is different. In the annual data, it is calculated over one year. However, in the quarterly data, it is calculated over one quarter. To make quarterly income and cash flows items comparable to the corresponding annual item, we take the sum of the item over the last four quarters.

 $^{^4}OACCRUALS_AT$, $BETABAB_1260d$, $DEBT_AT$ and $_EVOL$ are sorted in descending order. All other variables are sorted in ascending order.

6.4 Accounting Variables

The abbreviation is used to refer to the accounting variable. A suffix of '*' indicates that we have altered the original Compustat item to increase the coverage or to create a variable that is a part of creating a characteristic in the final dataset. The characteristic name will reflect the accounting name except the '*' suffix. As an example, 'gp_at' is gross profit scaled by assets. In general, we will refer to Compustat variables using capital letters.

Table 5: Accounting Variables

Name	Abbreviation	Construction	
Income Statement			
Sales	sale*	We prefer SALE. If this is unavailable, we use REVT	
Cost of Goods Sold	cogs	Compustat item COGS	
Gross Profit	gp^*	We prefer to use GP. If this is unavailable we use sale*-COGS	
Selling, General and Administrative Expenses	xsga	Compustat item XSGA	
Advertising Expenses	xad	Compustat item XAD. Note that this is not available in Compustat Global	
Research and Development Expenses	xrd	Compustat item XRD. Note that this is not available in Compustat Global	
Staff Expenses	xlr	Compustat item XLR	
Special Items	spi	Compustat item SPI	
Operating Expenses	opex*	We prefer to use XOPR. If this is unavailable, we use COGS+XSGA	
Operating Income Before Depreciation	ebitda*	We prefer to use EBITDA. If this is unavailable, we use OIBDP. If this is unavailable, we use SALE*-OPEX*. If this is unavailable, we use GP*-XSGA	
Depreciation and Amortization	dp	Compustat Item DP	
Operating Income After Depreciation	ebit*	We prefer to use EBIT. If this is unavailable, we use OIADP. If this is unavailable, we use EBITDA*-DP	
Interest Expenses	int	Compustat item XINT	
*	.	We use EBITDA* + XRD. If XRD is unavailable, we set it to	
Operating Profit ala Ball et al (2015)	op*	zero	
Operating Profit to Equity	ope*	We use EBITDA*-XINT. Note that we target the same variable as the numerator of the profitability characteristic used to create the Robust-minus weak factor in the fama-French 5 factor model (Fama and French, 2015)	
Earnings before Tax and Extraordinary Items	pi*	We prefer to use PI. If this is unavailable we use EBIT*-XINT+SPI+NOPI where we set SPI and NOPI to zero if missing	
Income Tax	tax	Compustat item TXT	
Extraordinary Items and Discontinued Operations	xido*	We prefer to use XIDO. If this is unavailable, we use XI+DO where we set DO to zero if missing. The reason why we set missing DO to zero is because it is not available in COMP.G.FUNDQ	
Net Income	ni*	We prefer to use IB. If this is unavailable, we use NI-XIDO*. If this is unavailable, we prefer PI*-TXT-MII. If MII is unavailable, it is set to zero	
Net Income Including Extraordinary Items	nix*	We prefer NI. If this is not available, we prefer NI*+XIDO*. If XIDO* is unavailable, we set it to zero. If that is unavailable, we prefer NI*+XI+DO	
Firm Income	fi*	We use NIX*+XINT	
Dividends for Common Shareholds	dvc	Compustat Item DVC	
Total Dividends	div*	We prefer DVT. If this is not available, we use DV	
Income Before Extraordinary Items	ni_qtr^*	We use IBQ	
Net Sales	$sale_qtr*$	We use SALEQ	
	Cash Fl	ow Statement	
Capital Expenditures	capx	Compustat item CAPX	
Capital Expenditures to Sales	$capex_sale*$	We use CAPX / SALE*	
		We use OCF*-CAPX. Note that the free cash flow is com-	
Free Cash Flow	fcf*	puted before financing activities and sale of assets is taken	
		into account	

Name	Abbreviation	Construction
	110010.1001011	We use PRSTKC+PURTSHR Equity Buyback is mainly
Equity Buyback	eqbb*	PRSTKC in NA and PURTSHR in GLOBAL. Either of PRSTKC or PURTSHR are allowed to be missing
Equity Issuance	eqis*	Compustat item SSTK
Equity Net Issuance	eqnetis*	We use EQIS*-EQBB*. Either EQIS* or EQBB* are allowed to be missing
Net Equity Payout	eqpo*	We use DIV*+EQBB*
Equity Net Payout	eqnpo*	We use DIV*-EQNETIS*
		We prefer to use DLTIS-DLTR where we only require that
Net Long-Term Debt Issuance	dltnetis*	one of the items are non-missing. If this is unavailable, we use LTDCH. If this is unavailable we use the yearly change in long-term book debt DLTT
		We prefer DLCCH. If this is unavailable, we use the yearly
Net Short-Term Debt Issuance	dstnetis*	change in short-term book debt DLC
Net Debt Issuance	dbnetis*	We use DLTNETIS*+DSTNETIS* and only require one of the items to be non-missing
N T		We use EQNETIS*+DBNETIS* and require that both
Net Issuance	netis*	EQNETIS* and DBNETIS* are non-missing
		We prefer FINCF. If this is unavailable, we use NETIS*-
Financial Cash Flow	fincf*	DV+FIAO+TXBCOF. If FIAO or TXBCOF is missing, it
	_	is set to zero
1	Balance	Sheet - Assets
T + 1 A +	, %	We prefer to use AT. If this is unavailable, then we use SEQ*
Total Assets	at*	+ DLTT + LCT + LO + TXDITC. If LCT, LO, or TXDITC are missing, then they are set to zero
		We prefer ACT. If this is unavailable, we use
Current Assets	ca*	RECT+INVT+CHE+ACO
Account Receivables	rec	Compustat item RECT
Cash and Short-Term Investment	cash	Compustat item CHE
Inventory	inv	Compustat item INVT
Non-Current Assets	nca*	We use AT* - CA*
Intangible Assets	intan	Compustat item INTAN
Investment and Advances	ivao	Compustat item IVAO
Property, Plans and Equipment Gross	ppeg	Compustat item PPEGT
Property, Plans and Equipment Net	ppen Palamas C	Compustat item PPENT heet - Liabilities
Total Liabilities	lt	Compustat item LT
		We prefer LCT. If this is unavailable, we use AP+ DLC+
Current Liabilities	cl*	TXP+ LCO
Accounts Payable	ap	Compustat item AP
Short-Term Debt	debtst	Compustat item DLC
Income Tax Payable	$_{\mathrm{txp}}$	Compustat item TXP
Non-Current Liabilities	ncl*	We use LT-CL*
Long-Term Debt	debtlt	Compustat item DLTT
Deferred Taxes and Investment Credit	txditc*	We prefer to use TXDITC. If this is unavailable, we use
	Balance C	heet - Financing
	Dalance 5.	We prefer to use PSTKRV. If this is unavailable, we use
Preferred Stock	pstk*	PSTKL. If this is unavilable, we use PSTK
T . 1 D 1.	11.4	We use DLTT+ DLC. Either DLTT or DLC are allowed to
Total Debt	debt*	me missing
Net Debt	netdebt*	We use DEBT*- CHE where we set CHE to zero if missing We prefer to use SEQ. If this is unavailable, we use
Net Debt Shareholders Equity	netdebt* seq*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this
	seq^*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT
		We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC*
Shareholders Equity	seq^*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing
Shareholders Equity Book Equity	seq*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC*
Shareholders Equity	seq^*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE
Shareholders Equity Book Equity	seq* be* bev*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock
Shareholders Equity Book Equity Book Enterprise Value	seq* be* bev* Balance S	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary
Shareholders Equity Book Equity Book Enterprise Value Net Working Capital	seq* be* bev* Balance S nwc*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL*
Shareholders Equity Book Equity Book Enterprise Value Net Working Capital Current Operating Assets	seq* be* bev* Balance S nwc* coa*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*- CHE
Shareholders Equity Book Equity Book Enterprise Value Net Working Capital Current Operating Assets Current Operating Liabilities	seq* be* bev* Balance S nwc* coa* col*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*- CHE We use CL*- DLC. If DLC is missing, it is set to zero
Shareholders Equity Book Equity Book Enterprise Value Net Working Capital Current Operating Assets	seq* be* bev* Balance S nwc* coa*	We prefer to use SEQ. If this is unavailable, we use CEQ+PSTK* where we set PSTK* to zero if missing. If this is unavailable, we use AT- LT We use SEQ*+TXDITC*-PSTK* where we set TXDITC* and PSTK* to zero if missing We prefer to use ICAPT+DLC-CHE where DLC and CHE are set to zero if missing. If this is unavailable, we use SEQ*+NETDEBT*+ MIB where we set MIB to zero if missing. In the global data ICAPT is reduced by Treasury stock heet - Summary We use CA*-CL* We use CA*- CHE

Name	Abbreviation	Construction	
Non-Current Operating Liabilities	ncol*	We use LT-CL*- DLTT	
Net Non-Current Operating Assets	nncoa*	We use NCOA*-NCOL*	
Financial Assets	fna*	We use IVST+ IVAO. If either is missing, they are set to zero	
Financial Liabilities	fnl*	We use DEBT*+PSTK*. If PSTK* is missing, it is set to zero	
Net Financial Assets	nfna*	We use FNA*-FNL*	
Operating Assets	oa*	We use COA*+NCOA*	
Operating Liabilities	ol*	We use COL*+NCOL*	
Net Operating Assets	noa*	We use OA*-OL*	
Long-Term NOA	lnoa*	PPENT + INTAN + AO - LO + DP	
T: 11 G	1. *	We prefer to use CA* - INVT. If this is unavailable, we use	
Liquid Current Assets	caliq*	CHE + RECT	
Property Plant and Equipment Less Inventories	ppeinv*	PPEGT + INVT	
	1. sk	$CHE + 0.75 \times COA^* + 0.5(AT^* - CA^* - INTAN)$. If INTAN	
Ortiz-Molina and Phillips Liquidity	aliq*	is missing, we set it to zero	
	Mai	rket Based	
		We use the market equity for the stock we deem to the primary	
		security of the firm. Importantly, we do not align the market	
Market Equity	me	value with the end of the fiscal period. Instead, we update the	
		market value on a monthly basis and align it with the most	
		recently available accounting characteristic	
Market Enterprise Value	mev*	We use ME_COMPANY + NETDEBT* \times FX*	
Market Assets	mat*	We use $AT^* \times FX - BE^* \times FX + ME_COMPANY$	
	A	Accruals	
Operating Accruals	oacc*	We prefer NI*-OANCF. If that is unavailable, we use the	
1 0		yearly change in COWC*+the yearly change in NNCOA*	
Total Accruals	tacc*	We use OACC* + the yearly change in NFNA*	
		We prefer to use OANCF. If this is unavailable, we use NI*-	
Operating Cash Flow	ocf*	OACC*. If this is unavailable, we use $NI^* + DP - WCAPT$.	
		If WCAPT is missing, we use 0.	
Quarterly Operating Cash Flow	ocf_qtr^*	We use OANCFQ. If this is unavailable, then we use IBQ + DPQ - WCAPTQ. If WCAPTQ is unavailable, we set it to	
Cook Doord On water a Dooft of the	*	We prefer EBITDA*+XRD-OACC*. If XRD is unavailable,	
Cash Based Operating Profitability	cop^*	we set it to zero	
Other			
Employees in Thousands	emp	Compustat item EMP	

Table 6: Accounting Characteristics

Name	Abbreviation	Construction		
Accounting Based Size Measures				
Assets	assets	$AT*_t$		
Sales	sales	$SALE^*_t$		
Book Equity	book_equity	$BE*_t$		
Net Income	net_income	NI^*_t		
Enterprise Value	enterprise_value	MEV^*_t		
${\bf Growth - Percentage}^5$				
Asset Growth 1yr	at_gr1	$\frac{AT^*_t}{AT^*_{t-12}} - 1$		

⁵This refers to all variables with a suffix of "gr1" or "gr3". The variables are percentage growth in the accounting variables before the suffix. The number in the suffix refers to either 1 or 3 year growth. For all variables, we only take the percentage growth if the denominator is above zero.

Name	Abbreviation	Construction
Sales Growth 1yr	sale_gr1	$\frac{SALE^*_t}{SALE^*_{t-12}} - 1$
Current Asset Growth 1yr	ca_gr1	$\frac{CA_{t}^{*}}{CA_{t-12}^{*}} - 1$
Non-Current Asset Growth 1yr	nca_gr1	$\frac{NCA^*_t}{NCA^*_{t-12}} - 1$
Total Liabilities Growth 1yr	lt_gr1	$\frac{LT_t}{LT_{t-12}} - 1$
Current Liabilities Growth 1yr	cl_gr1	$\frac{CL^*_t}{CL^*_{t-12}} - 1$
Non-Current Liabilities Growth 1yr	ncl_gr1	$\frac{NCL_t^*}{NCL_{t-12}^*} - 1$
Book Equity Growth 1yr	be_gr1	$\frac{BE_t^*}{BE_{t-12}^*} - 1$
Preferred Stock Growth 1yr	pstk_gr1	$\frac{PSTK^*_t}{PSTK^*_{t-12}} - 1$
Total Debt Growth 1yr	debt_gr1	$\frac{DEBT^*_{t}}{DEBT^*_{t-12}} - 1$
Cost of Goods Sold Growth 1yr	cogs_gr1	$\frac{COGS_t}{COGS_{t-12}} - 1$
Selling, General, and Administrative Expenses Growth 1yr	sga_gr1	$\frac{XSGA_t}{XSGA_{t-12}} - 1$
Operating Expenses Growth 1yr	opex_gr1	$\frac{OPEX^*_t}{OPEX^*_{t-12}} - 1$
Asset Growth 3yr	at_gr3	$\frac{AT^*_{t}}{AT^*_{t-36}} - 1$
Sales Growth 3yr	sale_gr3	$\frac{SALE^*_t}{SALE^*_{t-36}} - 1$
Current Asset Growth 3yr	ca_gr3	$\frac{CA_{t}^{*}}{CA_{t-36}^{*}} - 1$
Non-Current Asset Growth 3yr	nca_gr3	$\frac{NCA_t^*}{NCA_{t-36}^*} - 1$
Total Liabilities Growth 3yr	lt_gr3	$\frac{LT_t}{LT_{t-36}} - 1$
Current Liabilities Growth 3yr	cl_gr3	$\frac{CL_t^*}{CL_{t-36}^*} - 1$
Non-Current Liabilities Growth 3yr	ncl_gr3	$\frac{NCL_{t}^*}{NCL_{t-36}^*} - 1$
Book Equity Growth 3yr	be_gr3	$\frac{BE_{t}^{*}}{BE_{t-36}^{*}} - 1$
Preferred Stock Growth 3yr	pstk_gr3	$\frac{PSTK^*_{t}}{PSTK^*_{t-36}} - 1$
Total Debt Growth 3yr	debt_gr3	$\frac{DEBT^*_{t}}{DEBT^*_{t-36}} - 1$
Cost of Goods Sold Growth 3yr	cogs_gr3	$\frac{COGS_t}{COGS_{t-36}} - 1$
Selling, General, and Administrative Expenses Growth 3yr	sga_gr3	$\frac{XSGA_t}{XSGA_{t-36}} - 1$
Operating Expenses Growth 3yr	opex_gr3	$\frac{OPEX^*_t}{OPEX^*_{t-36}} - 1$
Grov	wth - Changed Scale	ed by Total Assets
Gross Profit Change 1yr	gp_gr1a	$\frac{GP_t^*-GP_{t-12}^*}{AT_t^*}$
Operating Cash Flow Change 1yr	ocf_gr1a	$\frac{OCF^*_{t} - OCF^*_{t-12}}{AT^*_{t}}$
Cash and Short-Term Investments Change 1yr	cash_gr1a	$\frac{CASH_t - CASH_{t-12}}{AT^*_t}$
Inventory Change 1yr	inv_gr1a	$\frac{INV_t - INV_{t-12}}{AT^*_t}$
Receivables Change 1yr	rec_gr1a	$\frac{REC_t - REC_{t-12}}{AT^*_t}$

Name	Abbreviation	Construction
Property, Plans and Equiptment Gross Change 1yr	ppeg_gr1a	$\frac{PPEG_t - PPEG_{t-12}}{AT^*_t}$
Investment and Advances Change 1yr	lti_gr1a	$\frac{LTI_t - LTI_{t-12}}{AT^*_t}$
Intangible Assets Change 1yr	intan_gr1a	$\frac{INTAN_t - INTAN_{t-12}}{AT^*_t}$
Short-Term Debt Change 1yr	debtst_gr1a	$\frac{DEBTST_t - DEBTST_{t-12}}{AT^*_t}$
Accounts Payable Change 1yr	ap_gr1a	$\frac{AP_t - AP_{t-12}}{AT^*_t}$
Income Tax Payable Change 1yr	txp_gr1a	$\frac{TXP_t - TXP_{t-12}}{AT^*_t}$
Long-Term Debt Change 1yr	debtlt_gr1a	$\frac{DEBTLT_t - DEBTLT_{t-12}}{AT^*_t}$
Deferred Taxes and Investment Credit Change 1yr	txditc_gr1a	$\frac{TXDITC_{t}^{*}-TXDITC_{t-12}^{*}}{AT_{t}^{*}}$
Current Operating Assets Change 1yr	coa_gr1a	$\frac{COA^*_t - COA^*_{t-12}}{AT^*_t}$
Current Operating Liabilities Change 1yr	col_gr1a	$\frac{COL_{t}^{*}-COL_{t-12}^{*}}{AT_{t}^{*}}$
Current Operating Working Capital Change 1yr	cowc_gr1a	$\frac{COWC_{t}^{*}-COWC_{t-12}^{*}}{AT_{t}^{*}}$
Non-Current Operating Assets Change 1yr	ncoa_gr1a	$\frac{NCOA^*_{t} - NCOA^*_{t-12}}{AT^*_{t}}$
Non-Current Operating Liabilities Change 1yr	ncol_gr1a	$\frac{NCOL^*_{t}-NCOL^*_{t-12}}{AT^*_{t}}$
Net Non-Current Operating Assets Change 1yr	nncoa_gr1a	$\frac{NNCOA^*_{t} - NNCOA^*_{t-12}}{AT^*_{t}}$
Operating Assets Change 1yr	oa_gr1a	$\frac{OA_{t}^{*}-OA_{t-12}^{*}}{AT_{t}^{*}}$
Operating Liabilities Change 1yr	ol_gr1a	$\frac{OL^*_{t}-OL^*_{t-12}}{AT^*_{t}}$
Net Operating Assets Change 1yr	noa_gr1a	$\frac{NOA_{t}^{*}-NOA_{t-12}^{*}}{AT_{t}^{*}}$
Financial Assets Change 1yr	fna_gr1a	$\frac{FNA^*_t - FNA^*_{t-12}}{AT^*_t}$
Financial Liabilities Change 1yr	fnl_gr1a	$\frac{FNL_{t}^{*}-FNL_{t-12}^{*}}{AT_{t}^{*}}$
Net Financial Assets Change 1yr	nfna_gr1a	$\frac{NFNA^*_{t}-NFNA^*_{t-12}}{AT^*_{t}}$
Operating Profit before Depreciation Change 1yr	ebitda_gr1a	$\frac{EBITDA^*_t - EBITDA^*_{t-12}}{AT^*_t}$
Operating Profit after Depreciation Change 1yr	ebit_gr1a	$\frac{EBIT^*_t - EBIT^*_{t-12}}{AT^*_t}$
Operating Earnings to Equity Change 1yr	ope_gr1a	$\frac{OPE^*_{t} - OPE^*_{t-12}}{AT^*_{t}}$
Net Income Change 1yr	ni_gr1a	$\frac{NI_{t-NI_{t-12}}^*}{AT_{t}^*}$
Depreciation and Amortization Change 1yr	dp_gr1a	$\frac{DP_t - DP_{t-12}}{AT^*_t}$
Free Cash Flow Change 1yr	fcf_gr1a	$\frac{FCF_t^* - FCF_{t-12}^*}{AT_t^*}$
Net Working Capital Change 1yr	nwc_gr1a	$\frac{NWC^*_t - NWC^*_{t-12}}{AT^*_t}$
Net Income Including Extraordinary Items Change 1yr	nix_gr1a	$\frac{NIX_{t}^{*}-NIX_{t-12}^{*}}{AT_{t}^{*}}$
Equity Net Issuance Change 1yr	eqnetis_gr1a	$\frac{EQNETIS^*_t - EQNETIS^*_{t-12}}{AT^*_t}$

Name	Abbreviation	Construction
Net Long-Term Debt Issuance Change 1yr	dltnetis_gr1a	$\frac{DLTNETIS*_{t}-DLTNETIS*_{t-12}}{AT*_{t}}$
Net Short-Term Debt Issuance Change 1yr	dstnetis_gr1a	$\frac{DSTNETIS^*_{t} - DSTNETIS^*_{t-12}}{AT^*_{t}}$
Net Debt Issuance Change 1yr	dbnetis_gr1a	$\frac{DBNETIS^*_{t} - DBNETIS^*_{t-12}}{AT^*_{t}}$
Net Issuance Change 1yr	netis_gr1a	$\frac{NETIS_{t}^{*}-NETIS_{t-12}^{*}}{AT_{t}^{*}}$
Financial Cash Flow Change 1yr	fincf_gr1a	$\frac{FINCF*_{t}-FINCF*_{t-12}}{AT*_{t}}$
Equity Net Payout Change 1yr	eqnpo_gr1a	$\frac{EQNPO^*_{t} - EQNPO^*_{t-12}}{AT^*_{t}}$
Effective Tax Rate Change 1yr	tax_gr1a	$\frac{TAX_t - TAX_{t-12}}{AT^*_t}$
Dividend Payout Ratio Change 1yr	div_gr1a	$\frac{DIV^*_{t} - DIV^*_{t-12}}{AT^*_{t}}$
Equity Buyback Change 1yr	eqbb_gr1a	$\frac{EQBB^*_{t} - EQBB^*_{t-12}}{AT^*_{t}}$
Equity Issuance Change 1yr	eqis_gr1a	$\frac{EQIS^*_{t} - EQIS^*_{t-12}}{AT^*_{t}}$
Net Equity Payout Change 1yr	eqpo_gr1a	$\frac{EQPO^*_{t} - EQPO^*_{t-12}}{AT^*_{t}}$
Capital Expenditures Change 1yr	capx_gr1a	$\frac{CAPX_t - CAPX_{t-12}}{AT^*_t}$
Gross Profit Change 3yr	gp_gr3a	$\frac{GP^*_{t}-GP^*_{t-36}}{AT^*_{t}}$
Operating Cash Flow Change 3yr	ocf_gr3a	$\frac{OCF^*_{t} - OCF^*_{t-36}}{AT^*_{t}}$
Cash and Short-Term Investments Change 3yr	cash_gr3a	$\frac{CASH_t - CASH_{t-36}}{AT^*_t}$
Inventory Change 3yr	inv_gr3a	$\frac{INV_t - INV_{t-36}}{AT^*_t}$
Receivables Change 3yr	rec_gr3a	$\frac{REC_t - REC_{t-36}}{AT^*_t}$
Property, Plans and Equipment Gross Change 3yr	ppeg_gr3a	$\frac{PPEG_t - PPEG_{t-36}}{AT^*_t}$
Investment and Advances Change 3yr	lti_gr3a	$\frac{LTI_t - LTI_{t-36}}{AT_t^*}$
Intangible Assets Change 3yr	intan_gr3a	$\frac{INTAN_t - INTAN_{t-36}}{AT^*_t}$
Short-Term Debt Change 3yr	debst_gr3a	$\frac{DEBTST_t - DEBTST_{t-36}}{AT^*_t}$
Accounts Payable Change 3yr	ap_gr3a	$\frac{AP_t - AP_{t-36}}{AT^*_t}$
Income Tax Payable Change 3yr	txp_gr3a	$\frac{TXP_t - TXP_{t-36}}{AT^*_t}$
Long-Term Debt Change 3yr	debtlt_gr3a	$\frac{DEBTLT_t - DEBTLT_{t-36}}{AT^*_t}$
Deferred Taxes and Investment Credit Change 3yr	txditc_gr3a	$\frac{TXDITC^*_{t} - TXDITC^*_{t-36}}{AT^*_{t}}$
Current Operating Assets Change 3yr	coa_gr3a	$\frac{COA^*_t - COA^*_{t-36}}{AT^*_t}$
Current Operating Liabilities Change 3yr	col_gr3a	$\frac{COL_{t}^{*}-COL_{t-36}^{*}}{AT_{t}^{*}}$
Current Operating Working Capital Change 3yr	cowc_gr3a	$\frac{COWC^*_t - COWC^*_{t-36}}{AT^*_t}$
Non-Current Operating Assets Change 3yr	ncoa_gr3a	$\frac{NCOA^*_t - NCOA^*_{t-36}}{AT^*_t}$
Net Non-Current Operating Assets Change 3yr	nncoa_gr3a	$\frac{NNCOA^*_{t} - NNCOA^*_{t-36}}{AT^*_{t}}$
Operating Assets Change 3yr	oa_gr3a	$\frac{OA_{t}^{*}-OA_{t-36}^{*}}{AT_{t}^{*}}$

Name	Abbreviation	Construction	
Operating Liabilities Change 3yr	ol_gr3a	$\frac{OL^*_{t}-OL^*_{t-36}}{AT^*_{t}}$	
Net Operating Assets Change 3yr	noa_gr3a	$\frac{NOA^*_t - NOA^*_{t-36}}{AT^*_t}$	
Financial Assets Change 3yr	fna_gr3a	$\frac{FNA^*_t - FNA^*_{t-36}}{AT^*_t}$	
Financial Liabilities Change 3yr	fnl_gr3a	$\frac{FNL^*_{t} - FNL^*_{t-36}}{AT^*_{t}}$	
Net Financial Assets Change 3yr	nfna_gr3a	$\frac{NFNA^*_t - NFNA^*_{t-36}}{AT^*_t}$	
Operating Profit before Depreciation Change 3yr	ebitda_gr3a	$\frac{EBITDA^*_{t} - EBITDA^*_{t-36}}{AT^*_{t}}$	
Operating Profit after Depreciation Change 3yr	ebit_gr3a	$\frac{EBIT^*_{t} - EBIT^*_{t-36}}{AT^*_{t}}$	
Operating Earnings to Equity Change 3yr	ope_gr3a	$\frac{OPE^*_{t} - OPE^*_{t-36}}{AT^*_{t}}$	
Net Income Change 3yr	ni_gr3a	$\frac{NI^*_t - NI^*_{t-36}}{AT^*_t}$	
Depreciation and Amortization Change 3yr	dp_gr3a	$\frac{DP_t - DP_{t-36}}{AT^*_t}$	
Free Cash Flow Change 3yr	fcf_gr3a	$\frac{FCF^*_t - FCF^*_{t-36}}{AT^*_t}$	
Net Working Capital Change 3yr	nwc_gr3a	$\frac{NWC^*_t - NWC^*_{t-36}}{AT^*_t}$	
Inventory Change 1yr	inv_gr3a	$\frac{INV_t - INV_{t-36}}{AT^*_t}$	
Non-Current Operating Liabilities Change 3yr	ncol_gr3a	$\frac{NCOL^*_{t}-NCOL^*_{t-36}}{AT^*_{t}}$	
Net Income Including Extraordinary Items Change 3yr	nix_gr3a	$\frac{NIX_{t}^{*}-NIX_{t-36}^{*}}{AT_{t}^{*}}$	
Equity Net Issuance Change 3yr	eqnetis_gr3a	$\frac{EQNETIS_{t}^{*}-EQNETIS_{t-36}^{*}}{AT_{t}^{*}}$	
Net Long-Term Debt Issuance Change 3yr	dltnetis_gr3a	$\frac{DLTNETIS_{t}^{*}-DLTNETIS_{t-36}^{*}}{AT_{t}^{*}}$	
Net Short-Term Debt Issuance Change 3yr	dstnetis_gr3a	$\frac{DSTNETIS_{t}^{*}-DSTNETIS_{t-36}^{*}}{AT_{t}^{*}}$	
Net Debt Issuance Change 3yr	dbnetis_gr3a	$\frac{DBNETIS_{t}^{*}-DBNETIS_{t-36}^{*}}{AT_{t}^{*}}$	
Net Issuance Change 3yr	netis_gr3a	$\frac{NETIS_{t}^{*}-NETIS_{t-36}^{*}}{AT_{t}^{*}}$	
Financial Cash Flow Change 3yr	fincf_gr3a	$\frac{FINCF_{t}^{*}-FINCF_{t-36}^{*}}{AT_{t}^{*}}$	
Net Working Capital Change 3yr	nwc_gr3a	$\frac{NWC_{t}^{*}-NWC_{t-36}^{*}}{AT_{t}^{*}}$	
Equity Net Payout Change 3yr	eqnpo_gr3a	$\frac{EQNPO^*_{t} - EQNPO^*_{t-36}}{AT_{\cdot}t}$	
Effective Tax Rate Change 3yr	tax_gr3a	$\frac{TAX_t - TAX_{t-36}}{AT_{-t}}$	
Dividend Payout Ratio Change 3yr	div_gr3a	$\frac{DIV_{t}^{*}-DIV_{t-36}^{*}}{AT_{-t}}$	
Equity Buyback Change 3yr	eqbb_gr3a	$\frac{EQBB^*_t - EQBB^*_{t-36}}{AT_{\cdot}t}$	
Equity Issuance Change 3yr	eqis_gr3a	$\frac{EQIS_{t}^{*}-EQIS_{t-36}^{*}}{AT_{\cdot t}}$	
Net Equity Payout Change 3yr	eqpo_gr3a	$\frac{EQPO^*_{t} - EQPO^*_{t-36}}{AT_{-t}}$	
Capital Expenditures Change 3yr	capx_gr3a	$\frac{CAPX_t - CAPX_{t-36}}{AT_{-t}}$	
Investment			
Capital Expenditures scaled by Assets	capx_at	$\frac{CAPX_t}{AT^*_t}$	

Name	Abbreviation	Construction	
R&D scaled by Assets	rd_at	$\frac{XRD_t}{AT^*_t}$	
	Non-Recurrin	g Items	
Special Items scaled by Assets	spi_at	$\frac{SPI_t}{AT^*_t}$	
Extraordinary Items and Discontinued Operations scaled by Assets	xido_at	$\frac{XIDO^*_t}{AT^*_t}$	
Non-Recurring Items scaled by Assets	nri_at	$\frac{SPI_t + XIDO^*_t}{AT^*_t}$	
	Profit Mar	gins	
Gross Profit Margin	gp_sale	$\frac{GP^*_t}{SALE^*_t}$	
Operating Profit Margin before Depreciation	ebitda_sale	$\frac{EBITDA^*_t}{SALE^*_t}$	
Operating Profit Margin after Depreciation	ebit_sale	$\frac{EBIT*_t}{SALE*_t}$	
Pretax Profit Margin	pi_sale	$\frac{PI^*_t}{SALE^*_t}$	
Net Profit Margin before XI	ni_sale	$\frac{NI*_t}{SALE*_t}$	
Net Profit Margin	nix_sale	$\frac{NIX^*_t}{SALE^*_t}$	
Free Cash Flow Margin	fcf_sale	$\frac{FCF^*_t}{SALE^*_t}$	
Operating Cash Flow Margin	ocf_sale	$\frac{OCF^*_t}{SALE^*_t}$	
	Return on A	Assets	
Gross Profit scaled by Assets	gp_at	$\frac{GP*_t}{AT*_t}$	
Operating Profit before Depreciation scaled by Assets	ebitda_at	$\frac{EBITDA*_t}{AT*_t}$	
Operating Profit after Depreciation scaled by Assets	ebit_at	$\frac{EBIT^*_t}{AT^*_t}$	
Firm Income scaled by Assets	fi_at	$\frac{FI^*_t}{AT^*_t}$	
Cash Based Operating Profitability scaled by Assets	cop_at	$\frac{COP_{\ t}^*}{AT_{\ t}^*}$	
	Return on Boo	k Equity	
Operating Profit to Equity scaled by BE	ope_be	$\frac{OPE^*_t}{BE^*_t}$	
Net Income scaled by BE	ni_be	$\frac{NI_t^*}{BE_t^*}$	
Net Income Including Extraordinary Items scaled by BE	nix_be	$\frac{NIX_t^*}{BE_t^*}$	
Operating Cash Flow scaled by BE	ocf_be	$\frac{OCF^*_t}{BE^*_t}$	
Free Cash Flow scaled by BE	fcf_be	$\frac{FCF^*_t}{BE^*_t}$	
Return on Invested Capital			
Gross Profit scaled by BEV	gp_bev	$\frac{GP_t^*}{BEV_t^*}$	
Operating Profit before Depreciation scaled by BEV	ebitda_bev	$\frac{EBITDA^*_t}{BEV^*_t}$	

Name	Abbreviation	Construction	
Operating Profit after Depreciation scaled by BEV	ebit_bev	$\frac{EBIT^*_t}{BEV^*_t}$	
Firm Income scaled by BEV	fi_bev	$\frac{FI^*_t}{BEV^*_t}$	
Cash Based Operating Profitability scaled by BEV	cop_bev	$\frac{COP^*_t}{BEV^*_t}$	
	Return on Physic	cal Capital	
Gross Profit scaled by PPEN	gp_ppen	$\frac{GP^*_t}{PPEN_t}$	
Operating Profit before Depreciation scaled by PPEN	ebitda_ppen	$\frac{EBITDA^*_{\ t}}{PPEN_t}$	
Free Cash Flow scaled by PPEN	fcf_ppen	$\frac{FCF^*_t}{PPEN_t}$	
	Issuanc	ee	
Financial Cash Flow scaled by Assets	fincf_at	$\frac{FINCF_{t}^{*}}{AT_{t}^{*}}$	
Net Issuance scaled by Assets	netis_at	$\frac{NETIS^*_t}{AT^*_t}$	
Equity Net Issuance scaled by Assets	eqnetis_at	$\frac{EQNETIS^*_t}{AT^*_t}$	
Equity Issuance scaled by Assets	eqis_at	$\frac{EQIS_{t}^{*}}{AT_{t}^{*}}$	
Net Debt Issuance scaled by Assets	dbnetis_at	$\frac{DBNETIS^*_t}{AT^*_t}$	
Net Long-Term Debt Issuance scaled by Assets	dltnetis_at	$\frac{DLTNETIS_t^*}{AT_t^*}$	
Net Short-Term Debt Issuance scaled by Assets	dstnetis_at	$\frac{DSTNETIS^*_t}{AT^*_t}$	
	Equity Pag	yout	
Equity Net Payout scaled by Assets	eqnpo_at	$\frac{EQNPO^*_t}{AT^*_t}$	
Net Equity Payout scaled by Assets	eqbb_at	$\frac{EQBB*_t}{AT*_t}$	
Total Dividends scaled by Assets	div_at	$\frac{DIV_t^*}{AT_t^*}$	
	Accrua	ls	
Operating Accruals	oaccruals_at	$\frac{OACC^*_t}{AT^*_t}$	
Percent Operating Accruals	oaccruals_ni	$\frac{OACC*_t}{ NIX*_t }$	
Total Accruals	taccruals_at	$\frac{TACC^*_t}{AT^*_t}$	
Percent Total Accruals	taccruals_ni	$\frac{TACC^*_t}{ NIX^*_t }$	
Net Operating Asset to Total Assets	noa_at	$\frac{NOA_{t}^{*}}{AT_{t}^{*}}$	
Capitalization/Leverage Ratios			
Common Equity scaled by BEV	be_bev	$\frac{BE*_t}{BEV*_t}$	
Total Debt scaled by BEV	debt_bev	$\frac{DEBT^*_t}{BEV^*_t}$	
Cash and Short-Term Investments scaled by BEV	cash_bev	$\frac{CASH_t}{BEV_t^*}$	
Preferred Stock scaled by BEV	pstk_bev	$\frac{PSTK^*_t}{BEV^*_t}$	

Name	Abbreviation	Construction	
Long-Term Debt scaled by BEV	debtlt_bev	$rac{DEBTLT_t}{BEV^*_t}$	
Short-Term Debt scaled by BEV	debtst_bev	$\frac{DEBTST_t}{BEV*_t}$	
Total Debt scaled by MEV	debt_mev	$\frac{DEBT*_t}{MEV*_t}$	
Preferred Stock scaled by MEV	pstk_mev	$\frac{PSTK^*_{t}}{MEV^*_{t}}$	
Long-Term Debt scaled by MEV	debtlt_mev	$\frac{DEBTLT_t}{MEV^*_t}$	
Short-Term Debt scaled by MEV	debtst_mev	$\frac{DEBTST_t}{MEV^*_t}$	
	Financial Soundr	ness Ratios	
Interest scaled by Total Debt	int_debt	$\frac{INT_t}{DEBT*_t}$	
Interest scaled by Long-Term Debt	int_debtlt	$rac{INT_t}{DEBTLT_t}$	
Operating Profit before Depreciation scaled by Total Debt	ebitda_debt	$\frac{EBITDA^*_t}{DEBT^*_t}$	
Profit before D&A scaled by Current Liabilities	profit_cl	$\frac{EBITDA^*_t}{CL^*_t}$	
Operating Cash Flow scaled by Current Liabilities	ocf_cl	$\frac{OCF^*_{\ t}}{CL^*_{\ t}}$	
Operating Cash Flow scaled by Total Debt	ocf_debt	$\frac{OCF^*_t}{DEBT^*_t}$	
Cash Balance scaled by Total Liabilities	cash_lt	$rac{CASH_t}{LT_t}$	
Inventory scaled by Current Assets	inv_act	$\frac{INV_t}{ACT_t}$	
Receivables scaled by Current Assets	rec_act	$rac{REC_t}{ACT_t}$	
Short-Term Debt scaled by Total Debt	debtst_debt	$rac{DEBTST_t}{DEBT_t^*}$	
Current Liabilities scaled by Total Liabilities	cl_lt	$\frac{CL_{t}^{*}}{LT_{t}}$	
Long-Term Debt scaled by Total Debt	debtlt_debt	$rac{DEBTLT_t}{DEBT_t^*}$	
Operating Leverage	opex_at	$\frac{OPEX_{t}^{*}}{AT_{t}^{*}}$	
Free Cash Flow scaled by Operating Cash Flow	fcf_ocf	$\frac{FCF^*_t}{OCF^*_t}$	
Total Liabilities scaled by Total Tangible Assets	lt_ppen	$rac{LT_t}{PPEN_t}$	
Long-Term Debt to Book Equity	debtlt_be	$\frac{DEBTLT_t}{BE_t^*}$	
Working Capital scaled by Assets	nwc_at	$\frac{NWC^*_t}{AT^*_t}$	
Solvency Ratios			
Debt-to-Assets	debt_at	$\frac{DEBT^*_t}{AT^*_t}$	
Debt to Shareholders' Equity Ratio	debt_be	$\frac{DEBT^*_t}{BE^*_t}$	
Interest Coverage Ratio	ebit_int	$rac{EBIT*_{t}}{INT_{t}}$	
Liquidity Ratios			
Days Inventory Outstanding	inv_days	$\frac{\frac{INV_t + INV_{t-12}}{2}}{COGS_t} \times 365$	

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Quick Ratio $ \begin{array}{c} \text{Caliq_cl} & \begin{array}{c} \text{CL}^*_t \\ \text{CalIQ}^*_t \\ \text{Current Ratio} \end{array} \end{array} $
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Asset Turnover $at_turnover$
Asset Turnover $at_turnover$
Receivables Turnover rec_turnover $\frac{SALE^*_t}{(REC_t + REC_{t-12})/2}$ Account Payables Turnover ap_turnover $\frac{COGS_t + INV_t - INV_{t-12}}{(AP_t + AP_{t-12})/2}$ Miscellaneous Advertising scaled by Sales adv_sale $\frac{XAD_t}{SALE^*_t}$ Labor Expense scaled by Sales staff_sale $\frac{XLR_t}{SALE^*_t}$ Sales scaled by BEV sale_bev $\frac{SALE^*_t}{BEV^*_t}$
Labor Expense scaled by Sales staff_sale $\frac{XLR_t}{SALE^*_t}$ Sales scaled by BEV sale_bev $\frac{SALE^*_t}{BEV^*_t}$
Labor Expense scaled by Sales staff_sale $\frac{XLR_t}{SALE^*_t}$ Sales scaled by BEV sale_bev $\frac{SALE^*_t}{BEV^*_t}$
Sales scaled by BEV
R&D scaled by Sales rd_sale $\frac{XRD_t}{SALE^*_t}$
Sales scaled by Total Stockholders' Equity sale_be $\frac{SALE_t^*}{BE_t^*}$
Dividend Payout Ratio
Sales scaled by Working Capital sale_nwc $\frac{SALE^*_t}{NWC^*_t}$
Effective Tax Rate tax_pi tax_pi tax_t tax_t
Balance Sheet Fundamental to Market Equity
Book Equity scaled by Market Equity be_me $\frac{BE_t^*}{ME_t}$
Total Assets scaled by Market Equity at_me $\frac{AT^*_{t}}{ME_{t}}$
Cash and Short-Term Investments scaled by Market Equity $\frac{CASH_t}{ME_t}$
Income Fundamentals to Market Equity
Gross Profit scaled by ME gp_me $\frac{GP_t^*}{ME_t}$
Operating Profit before Depreciation scaled by ME ebitda_me $\frac{EBITDA^*_t}{ME_t}$
Operating Profit after Depreciation scaled by $\frac{EBIT_t^*}{ME_t}$
Operating Earnings to Equity scaled by ME $\frac{OPE_t^*}{ME_t}$
Net Income scaled by ME ni_me $\frac{NI^*_t}{ME_t}$
Sales scaled by ME sale_me $\frac{SALE^*_t}{ME_t}$

Name	Abbreviation	Construction	
Operating Cash Flow scaled by ME	ocf_me	$\frac{OCF^*_{t}}{ME_{t}}$	
Free Cash Flow scaled by ME	fcf_me	$\frac{FCF^*_{t}}{ME_{t}}$	
Net Income Including Extraordinary Items scaled by ME	nix_me	$\frac{NIX^*_t}{ME_t}$	
Cash Based Operating Profitability scaled by ME	cop_me	$\frac{COP^*_{t}}{ME_{t}}$	
R&D scaled by ME	rd_me	$\frac{XRD_t}{ME_t}$	
Balance She	et Fundamentals to	Market Enterprise Value	
Book Equity scaled by MEV	be_mev	$\frac{BE*_t}{MEV*_t}$	
Total Assets scaled by MEV	at_mev	$\frac{AT^*_t}{MEV^*_t}$	
Cash and Short-Term Investments scaled by MEV	cash_mev	$\frac{CASH_t}{MEV^*_t}$	
Book Enterprise Value scaled by MEV	bev_mev	$\frac{BEV^*_t}{MEV^*_t}$	
Property, Plans and Equipment Net scaled by MEV	ppen_mev	$\frac{PPEN_t}{MEV^*_t}$	
Equity Payout/Issuance to Market Equity			
Total Dividends scaled by ME	div_me	$\frac{DIV_{t}^{*}}{ME_{t}}$	
Equity Buyback scaled by ME	eqbb_me	$\frac{EQBB*_{t}}{ME_{t}}$	
Equity Issuance scaled by ME	eqis_me	$\frac{EQIS^*_t}{ME_t}$	
Net Equity Payout scaled by ME	eqpo_me	$\frac{EQPO^*_{t}}{ME_t}$	
Equity Net Payout scaled by ME	eqnpo_me	$\frac{EQNPO^*_t}{ME_t}$	
Equity Net Issuance scaled by ME	eqnetis_me	$\frac{EQNETIS^*_t}{ME_t}$	
Debt	Issuance to Marke	t Enterprise Value	
Net Long-Term Debt Issuance scaled by MEV	dltnetis_mev	$\frac{DLTNETIS_t^*}{MEV_t^*}$	
Net Short-Term Debt Issuance scaled by MEV	$dstnetis_mev$	$\frac{DSTNETIS^*_t}{MEV^*_t}$	
Net Debt Issuance scaled by MEV	dbnetis_mev	$\frac{DBNETIS^*_t}{MEV^*_t}$	
Firm Pay	out/Issuance to Ma	arket Enterprise Value	
Net Issuance scaled by MEV	netis_mev	$\frac{NETIS^*_t}{MEV^*_t}$	
Income Fundamentals to Market Enterprise Value			
Gross Profit scaled by MEV	gp_mev	$\frac{GP_t^*}{MEV_t^*}$	
Operating Profit before Depreciation scaled by MEV	ebitda_mev	$\frac{EBITDA_t^*}{MEV_t^*}$	
Operating Profit after Depreciation scaled by MEV	ebit_mev	$\frac{EBIT^*_t}{MEV^*_t}$	
Sales scaled by MEV	sale_mev	$\frac{SALE^*_t}{MEV^*_t}$	
Operating Cash Flow scaled by MEV	ocf_mev	$\frac{OCF^*_t}{MEV^*_t}$	

Name	Abbreviation	Construction
Free Cash Flow scaled by MEV	fcf_mev	$\frac{FCF^*_t}{MEV^*_t}$
Cash Based Operating Profitability scaled by MEV	cop_mev	$\frac{COP^*_t}{MEV^*_t}$
Financial Cash Flow Change scaled by MEV	fincf_mev	$\frac{FINCF_t^*}{MEV_t^*}$
	New Variables n	ot in HXZ
Net Income to Sales Quarterly Volatility	niq_saleq_std	$\sigma_{8Q}\left(rac{NI_QTR^*_t}{SALE_QTR^*_t} ight)$
Net Income scaled by Employees	ni_emp	$rac{NI_{}^{*}}{EMP_{t}}$
Sales scaled by Employees	sale_emp	$rac{SALE*_t}{EMP_t}$
Net Income scaled by Assets	ni_at	$\frac{NI_{t}^{*}}{AT_{t}^{*}}$
Operating Cash Flow scaled by Assets	ocf_at	$\frac{OCF^*_t}{AT^*_t}$
Operating Cash Flow to Assets 1 yr Change	ocf_at_chg1	$OCF_AT_t - OCF_AT_{t-12}$
Quarterly ROE Volatility	roeq_be_std	$\sigma_{16Q}\left(rac{NI_QTR^*_{t}}{BE^*_{t}} ight)$
ROE Volatility	roe_be_std	$\sigma_{60M}\left(rac{NI_{t}^{*}}{BE_{t}^{*}} ight)$
Gross Product to Assets 5 yr Change	gpoa_ch5	$\frac{GP_{t}^{*}}{AT_{t}^{*}} - \frac{GP_{t-60}^{*}}{AT_{t-60}^{*}}$
ROE 5 yr Change	roe_ch5	$\frac{NI_{t}^{*}}{BE_{t}^{*}} - \frac{NI_{t-60}^{*}}{BE_{t-60}^{*}}$
ROA 5 yr Change	roa_ch5	$\frac{NI_{t}^{*}}{AT_{t}^{*}} - \frac{NI_{t-60}^{*}}{AT_{t-60}^{*}}$
Operating Cash Flow to Assets 5 yr Change	cfoa_ch5	$\frac{OCF_{t}^{*}}{AT_{t}^{*}} - \frac{OCF_{t-60}^{*}}{AT_{t-60}^{*}}$
Gross Product to Sales 5 yr Change	gmar_ch5	$\frac{GP_{t}^{*}}{SALE_{t}^{*}} - \frac{GP_{t-60}^{*}}{SALE_{t-60}^{*}}$
	New Variables f	rom HXZ
Cash and Short Term Investments scaled by Assets	cash_at	$\frac{CASH_t}{AT^*_t}$
Number of Consecutive Earnings Increases	ni_inc8q	Count number of earnings increases over past 8 quarters
Change in Property, Plant and Equipment Less Inventories scaled by lagged Assets	ppeinv_gr1a	$\frac{PPEINV_{t}^{*}-PPEINV_{t-12}^{*}}{AT_{t-12}^{*}}$
Change in Long-Term NOA scaled by average Assets	lnoa_gr1a	$\frac{LNOA^*_{t}-LNOA^*_{t-12}}{AT^*_{t}-AT^*_{t-12}}$
CAPX 1 year growth	capx_gr1	$\frac{CAPX_t}{CAPX_{t-12}} - 1$
CAPX 2 year growth	capx_gr2	$\frac{CAPX_t}{CAPX_{t-24}} - 1$
CAPX 3 year growth	capx_gr3	$\frac{CAPX_t}{CAPX_{t-36}} - 1$
Change in Short-Term Investments scaled by Assets	sti_gr1a	$\frac{IVST_t - IVST_{t-12}}{AT^*_t}$
Quarterly Income scaled by BE	niq_be	$\frac{NL_{\cdot}QTR^{*}_{t}}{BE^{*}_{t-3}}$
Change in Quarterly Income scaled by BE	niq_be_chg1	$NIQ_BE_t - NIQ_BE_{t-12}$
Quarterly Income scaled by AT	niq_at	$\frac{NLQTR^*_t}{AT^*_{t-3}}$
Change in Quarterly Income scaled by AT	niq_at_chg1	$NIQ_AT_t - NIQ_AT_{t-12}$

Name	Abbreviation	Construction
Quarterly Sales Growth	saleq_gr1	$\frac{SALE_QTR^*_{t}}{SALE_QTR^*_{t-12}} - 1$
R&D Capital-to-Assets	rd5_at	$\frac{\sum_{n=0}^{4} (12 \times n)(XRD_{t-12*n})}{AT^*_{t}}$
Age	age	Age of the firms in months
Change Sales minus Change Inventory	dsale_dinv	$CHG_TO_EXP(SALE*_t) - CHG_TO_EXP(INV_t)$
Change Sales minus Change Receivables	dsale_drec	$CHG_TO_EXP(SALE*_t) - CHG_TO_EXP(REC_t)$
Change Gross Profit minus Change Sales	dgp_dsale	$CHG_TO_EXP(GP*_t) - CHG_TO_EXP(SALE*_t)$
Change Sales minus Change SG&A	dsale_dsga	$CHG_TO_EXP(SALE^*_t) - CHG_TO_EXP(XSGA_t)$
Earnings Surprise	saleq_su	$SUR(SALE_QTR^*)$
Revenue Surprrise	niq_su	$SUR(NI_QTR^*)$
Total Debt scaled by ME	debt_me	$\frac{DEBT^*_t}{ME_t}$
Net Debt scaled by ME	netdebt_me	$\frac{NETDEBT^*_t}{ME_t}$
Abnormal Corporate Investment	capex_abn	$\frac{{{CAPX_SALE}^*}_t}{{({CAPX_SALE}^*}_{t-12} + {CAPX_SALE}^*}_{t-24} + {CAPX_SALE}^*_{t-36})/3} - 1$
Inventory Change 1 yr	inv_gr1	$\frac{INV_t}{INV_{t-12}} - 1$
Book Equity Change 1 yr scaled by Assets	be_gr1a	$\frac{BE_{t}^{*}-BE_{t-12}^{*}}{AT_{t}^{*}}$
Ball Operating Profit to Assets	op_at	$\frac{OP_t^*}{AT_t^*}$
Earnings before Tax and Extraordinary Items to Net Income Including Extraordinary Items	pi_nix	$\frac{PI^*_t}{NIX^*_t}$
Ball Operating Profit scaled by lagged Assets	op_atl1	$\frac{OP^*_t}{AT^*_{t-12}}$
Operating Profit scaled by lagged Book Equity	ope_bel1	$\frac{OPE^*_t}{BE^*_{t-12}}$
Gross Profit scaled by lagged Assets	gp_atl1	$\frac{GP_{t}^{*}}{AT_{t-12}^{*}}$
Cash Based Operating Profitability scaled by lagged Assets	cop_atl1	$\frac{COP_t^*}{AT_{t-12}^*}$
Book Leverage	at_be	$\frac{AT^*_t}{BE^*_t}$
Operating Cash Flow to Sales Quarterly Volatility	ocfq_saleq_std	$\sigma_{16Q}\left(rac{OCF_QTR^*_t}{SALE_QTR^*_t} ight)$
Liquidity scaled by lagged Assets	aliq_at	$\frac{ALIQ^*_t}{AT^*_{t-12}}$
Liquidity scaled by lagged Market Assets	aliq_mat	$\frac{ALIQ^*_t}{MAT^*_{t-12}}$
Tangibility	tangibility	$\frac{CASH_t + 0.715 \times REC_t + 0.547 \times INV_t + 0.535 \times PPEG_t}{AT^*_t}$
Equity Duration	eq_dur	Outlined in detail here
Equity Dataston	f_score	Outlined in detail here
Piotroski F-Score		
Ohlson O-Score	o_score	Outlined in detail here

Name	Abbreviation	Construction
	z_score	Outlined in detail here
Altman Z-Score		
	kz_index	Outlined in detail here
Kaplan-Zingales Index		
	intrinsic_value	Outlined in detail here
Intrinsic Value		
Intrinsic value-to-market	ival_me	$\frac{INTRINSIC_{\cdot}VALUE*_{t}}{ME_{t}}$
Sales scaled by Employees Growth 1 yr	sale_emp_gr1	$\frac{SALE_EMP_t}{SALE_EMP_{t-12}} - 1$
Employee Growth 1 yr	emp_gr1	$\frac{EMP_t - EMP_{t-12}}{0.5 \times EMP_t + 0.5 \times EMP_{t-12}}$
Earnings Variability	earnings_variability	$\frac{\sigma_{60M} \left(NI_{t}^{*}/AT_{t-12}^{*} \right)}{\sigma_{60M} \left(OCF_{t}^{*}/AT_{t-12}^{*} \right)}$
1 yr lagged Net Income to Assets	ni_ar1	$\frac{cov((NI^*/AT^*)_t, (NI^*/AT^*)_{t-12})}{var((NI^*/AT^*)_{t-12})}$
	ni_ivol	Outlined in detail here
Net Income Idiosyncratic Volatility		

7 Market Based Characteristics

Datasets

- CRSP.MSF
- CRSP.DSF
- COMP.SECD
- COMP.G_SECD
- COMP.SECM
- COMP.SECURITY
- COMP.G_SECURITY

Market Variables

A suffix of '*' indicates that we have altered or renamed the original item.

Table 7: Market Variables

Name	Abbreviation	Construction		
CRSP Variables ⁶				

 $^{^{6}}$ lag is a lag function where lag(x) is the value of x from the previous time period

Name	Abbreviation	Construction			
Share Adjustment Factor	adjfct*	We use CFACSHR			
Shares	shares*	We use SHROUT/1000 so shares outstanding are in millions.			
Price	prc*	We use PRC			
Local Price	prc_local*	We use PRC*			
Highest Daily Price	prc_high	We use ASKHI. If PRC* or AKSHI are negative, the PRC_HIGH is set to missing			
Lowest Daily Price	prc_low	We use BIDLO. If PRC* or BIDLO are negative, then PRC_LOW is set to missing			
Market Equity	me*	We use PRC*×SHARES* so market equity is quoted in million USD.			
Company Market Equity Trading Volume	me_company* tvol*	We sum ME* grouped by PERMCO and date We use VOL			
Dollar Volume	dolvol*	We use TVOL*×PRC*			
Return	RET*	We use RET. In case of delisting, we calculate as (1+RET)*(1+DLRET)-1			
Local Return	ret_local*	We use RET. In case of delisting, we calculate as (1+RET)*(1+DLRET)-1			
Excess Return	ret_exc*	We use RET*-T30RET/21. If T30RET is unavailable, we use RF. If the return is a monthly return rather than a daily return, the T30RET is divided by 1 rather than 21.			
Excess Return t+1	ret_exc_lead1m*	Excess return (ret_exc*) in month t+1			
Time Since Most Recent Return	ret_lag_dif*	We automatically set this to 1			
Cumulative Return	ri*	This is the cumulative return estimated from RET*			
Monthly Dividend	div_tot*	We use			
		$(RET - RETX) \times lag(PRC^*) \times (CFACSHR/lag(CFACSHR))$			
		at Variables			
Share Adjustment Factor	adjfct*	We use AJEXDI			
Shares	shares*	We use CSHOC/1000000			
Price	prc*	We use PRC_LOCAL*×FX			
Local Price	prc_local* me*	We use PRCCD We use PRC*×SHARES*			
Market Equity Company Market Equity	me-company*	We use ME*			
Trading Volume	tvol*	We use CSHTRD			
Dollar Volume	dolvol*	We use TVOL*×PRC*			
Cumulative Return - Local	ri_local*	We use PRC_LOCAL*× TRFD/AJEXDI			
Camadon C 100 and - 100 an	1110001	We use RLLOCAL* / lag(RLLOCAL*) - 1. In case of delisting,			
Local Return	ret_local*	we use RLLOCAL*/lag(RLLOCAL*) - 1. In case of densting, we calculate as (RLLOCAL*/lag(RLLOCAL*) * (1+dlret ⁷) - 1)			
Cumulative Return	ri*	RLLOCAL* × FX*			
Return	RET*	We use RI*/lag(RI*) - 1. In case of delisting, we calculate as $(RI*/lag(RI*)*(1+dlret)-1)$			
		We use RET*-T30RET/21. If T30RET is unavailable, we			
Excess Return	ret_exc*	use RF. If the return is a monthly return rather than a daily return, the T30RET is divided by 1 rather than 21.			
Excess Return t+1	ret_exc_lead1m*	Excess return (ret_exc*) in month t+1 We estimate the number of days since the previous return. If			
Time Since Most Recent Return	ret_lag_dif*	the returns are monthly rather than daily, then the time is in months			
Monthly Dividend	div_tot*	We use DIV \times FX*. If DIV is missing, we set it to zero			
Cash Dividend	div_cash*	We use $\overline{\text{DIVD}} \times FX^*$. If $\overline{\text{DIVD}}$ is unavailable, we set it to zero			
Special Cash Dividend	div_spc*	We use DIVSP \times FX*. If DIVSP is unavailable, we set it to zero			
Bid-Ask Average Dummy	bidask*	When $PRCSTD = 4$ then 1, otherwise 0			
		icing Factors			
Excess Market Return	mktrf*	Country specific market return			
High Minus Low	hml*	Country specific factor following Fama and French (1993) and using breakpoints from non-micro cap stocks within the coun-			
Small Minus Big ala Fama-French	smb_ff*	try Average of small portfolios minus average of large portfolios from hml*			
Small Minus Big ala Fama-French	smb_ff*				

⁷dlret is set to -0.3 when dlsrni is '02' or '03' and set to 0 otherwise

Name	Abbreviation	Construction		
		Country specific factor following Hou, Xue and Zhang (2015)		
		and using breakpoints from non-micro cap stocks within the country. We use double sorts on return on equity and size rather than triple sorts with investment, due to the limited number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited		
Return on Equity	roe*	1 0		
		Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on return on equity and size rather than triple sorts with investment, due to the limited number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited number of stocks in some international markets Average of small portfolios minus average of large portfolios from roe* and inv*		
		country. We use double sorts on return on equity and size rather than triple sorts with investment, due to the limited number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited number of stocks in some international markets		
		number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited		
Investment				
	inv*	Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on return on equity and size rather than triple sorts with investment, due to the limited number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited number of stocks in some international markets Average of small portfolios minus average of large portfolios		
		rather than triple sorts with investment, due to the limited number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather than triple sorts with return on equity, due to the limited number of stocks in some international markets Average of small portfolios minus average of large portfolios		
		number of stocks in some international markets		
Small Minus Dig ale Hou et al	smb_hxz*	Average of small portfolios minus average of large portfolios		
Small Minus Big ala Hou et al	SIIID_IIXZ	and using breakpoints from non-micro cap stocks within the country. We use double sorts on return on equity and size ather than triple sorts with investment, due to the limited number of stocks in some international markets. Country specific factor following Hou, Xue and Zhang (2015) and using breakpoints from non-micro cap stocks within the country. We use double sorts on investment and size rather han triple sorts with return on equity, due to the limited number of stocks in some international markets average of small portfolios minus average of large portfolios rom roe* and inv*		
Market Volatility for Each Stock	_mktvol_zd*	$\sigma_{zD}(MKTRF^*_t)^{-8}$		

Table 8: Market Characteristics

Name	Abbreviation	Construction		
Market Based Size Measures				
Market Equity	market_equity	ME^*_t		
Total Dividend Paid to Market Equity				
Dividend to Price - 1 Month	div1m_me	$\frac{DIV_TOT^*_t \times SHARES^*_t}{ME^*_t}$		
Dividend to Price - 3 Months	div3m_me	$\frac{\sum_{n=0}^{2} DIV_TOT^*_{t-n} \times SHARES^*_{t-n}}{ME^*_{t}}$		
Dividend to Price - 6 Months	div6m_me	$\frac{\sum_{n=0}^{5} DIV_TOT^*_{t-n} \times SHARES^*_{t-n}}{ME^*_{t}}$		
Dividend to Price - 12 Months	div12m_me	$ \begin{array}{c} \stackrel{ME}{\sum_{n=0}^{2} DIV \cdot TOT^*_{t-n} \times SHARES^*_{t-n}} \\ \frac{\sum_{n=0}^{5} DIV \cdot TOT^*_{t-n} \times SHARES^*_{t-n}}{ME^*_{t}} \\ \frac{\sum_{n=0}^{1} DIV \cdot TOT^*_{t-n} \times SHARES^*_{t-n}}{ME^*_{t}} \end{array} $		
s	pecial Dividend P	Paid to Market Equity		
Special Dividend to Price - 1 Month	divspc1m_me	$\frac{DIV_SPC^*_t \times SHARES^*_t}{ME^*_t}$		
Special Dividend to Price - 12 Month	divspc12m_me	$\frac{\sum_{n=0}^{11} DIV_SPC^*_{t-n} \times SHARES^*_{t-n}}{ME^*_{t}}$		
	Change in Sha	ares Outstanding		
Change in Shares - 1 Month	chcsho_1m	$\frac{SHARES^*_{t} \times ADJFCT^*_{t}}{SHARES^*_{t-1} \times ADJFCT^*_{t-1}} - 1$		
Change in Shares - 3 Month	chcsho_3m	$\frac{SHARES^*_{t} \times ADJFCT^*_{t}}{SHARES^*_{t-3} \times ADJFCT^*_{t-3}} - 1$		
Change in Shares - 6 Month	chcsho_6m	$\frac{SHARES^*_{t} \times ADJFCT^*_{t}}{SHARES^*_{t-6} \times ADJFCT^*_{t-6}} - 1$		
Change in Shares - 12 Month	chcsho_12m	$\frac{SHARES^*_{t} \times ADJFCT^*_{t}}{SHARES^*_{t-12} \times ADJFCT^*_{t-12}} - 1$		
	Net Equity Payout			
Net Equity Payout - 1 Month	eqnpo_1m	$\log\left(\frac{RI^*_{t}}{RI^*_{t-1}}\right) - \log\left(\frac{ME^*_{t}}{ME^*_{t-1}}\right)$		
Net Equity Payout - 3 Month	eqnpo_3m	$\log\left(\frac{RI_{t}^{*}}{RI_{t-3}^{*}}\right) - \log\left(\frac{ME_{t}^{*}}{ME_{t-3}^{*}}\right)$		
Net Equity Payout - 6 Month	eqnpo_6m	$\log\left(\frac{RI^*_{t}}{RI^*_{t-6}}\right) - \log\left(\frac{ME^*_{t}}{ME^*_{t-6}}\right)$		
Net Equity Payout - 12 Month	eqnpo_12m	$log\left(\frac{RI^*_{t}}{RI^*_{t-12}}\right) - log\left(\frac{ME^*_{t}}{ME^*_{t-12}}\right)$		
	Momentu	ım/Reversal		

⁸Must have enough non-missing values of stock to be estimated

Name	Abbreviation	Construction	
Short Term Reversal	ret_1_0	$\frac{RI^*_t}{RI^*_{t-1}} - 1$	
Momentum 0-2 Months	ret_2_0	$\frac{RI_{t}^{*}}{RI_{t-2}^{*}} - 1$	
Momentum 0-3 Months	ret_3_0	$\frac{RI_{t}^{*}}{RI_{t-3}^{*}} - 1$	
Momentum 1-3 Months	ret_3_1	$\frac{RI^*_{t-1}}{RI^*_{t-2}} - 1$	
Momentum 0-6 Months	ret_6_0	$\frac{RI^*_{t}}{RI^*_{t-6}} - 1$	
Momentum 1-6 Months	ret_6_1	$\frac{RI^*_{t-1}}{RI^*_{t-6}} - 1$	
Momentum 0-9 Months	ret_9_0	$\frac{RI_{t}^{*}}{RI_{t-9}^{*}} - 1$	
Momentum 1-9 Months	ret_9_1	$\frac{RI^*_{t-1}}{RI^*_{t-9}} - 1$	
Momentum 0-12 Months	ret_12_0	$\frac{RI_{t}^{*}}{RI_{t-12}^{*}} - 1$	
Momentum 1-12 Months	ret_12_1	$\frac{R{I^*}_{t-1}}{R{I^*}_{t-12}} - 1$	
Momentum 7-12 Months	ret_12_7	$\frac{R{I^*}_{t-7}}{R{I^*}_{t-12}} - 1$	
Momentum 1-18 Months	ret_18_1	$\frac{R{I^*}_{t-1}}{R{I^*}_{t-18}} - 1$	
Momentum 1-24 Months	ret_24_1	$\frac{R{I^*}_{t-1}}{R{I^*}_{t-24}} - 1$	
Momentum 12-24 Months	ret_24_12	$\frac{RI^*_{t-12}}{RI^*_{t-24}} - 1$	
Momentum 1-36 Months	ret_36_1	$\frac{R{I^*}_{t-1}}{R{I^*}_{t-36}} - 1$	
Momentum 12-36 Months	ret_36_12	$\frac{RI^*_{t-12}}{RI^*_{t-36}} - 1$	
Momentum 1-48 Months	ret_48_1	$\frac{R{I^*}_{t-1}}{R{I^*}_{t-48}} - 1$	
Momentum 12-48 Months	ret_48_12	$\frac{RI^*_{t-12}}{RI^*_{t-48}} - 1$	
Momentum 1-60 Months	ret_60_1	$\frac{R{I^*}_{t-1}}{R{I^*}_{t-60}} - 1$	
Momentum 12-60 Months	ret_60_12	$\frac{RI^*_{t-12}}{RI^*_{t-60}} - 1$	
Momentum 36-60 Months	ret_60_36	$\frac{RI^*_{t-36}}{RI^*_{t-60}} - 1$	
	Seas	onality	
1 Year Annual Seasonality	seas_1_1an	Return in month t-12	
2 - 5 Year Annual Seasonality	seas_2_5an	Average return over annual lags from year t-2 to t-5	
6 - 10 Year Annual Seasonality	seas_6_10an	Average return over annual lags from year t-6 to t-10	
11 - 15 Year Annual Seasonality	seas_11_15an	Average return over annual lags from year t-11 to t-15	
16 - 20 Year Annual Seasonality	seas_16_20an	Average return over annual lags from year t-16 to t-20)	
1 Year Non-Annual Seasonality	seas_1_1na	Average return from month t-1 to t-11	
2 - 5 Year Non-Annual Seasonality	seas_2_5na	Average return over non-annual lags from year t-2 to t-5	
6 - 10 Year Non-Annual Seasonality	seas_6_10na	Average return over non-annual lags from year t-6 to t-10	
11 - 15 Year Non-Annual Seasonality	seas_11_15na	Average return over non-annual lags from year t-11 to t-15	
16 - 20 Year Non-Annual Seasonality	seas_16_20na	Average return over non-annual lags from year t-16 to t-20	

Name	Abbreviation	Construction	
Combined Accounting and Market Based Characteristics			
	Let e_t be define	d as described here	
60 Month CAPM Beta Performance Based Mispricing	beta_60m mispricing_perf ⁹	$\frac{COVAR_60M(RET^*_{t,MKTRF^*_{t}})}{VARC_60M(MKTRF^*_{t})} \\ \frac{1}{4} \left(O_SCORE_t^{r01} + RET_12_1_t^{r01} + GP_AT_t^{r01} + NIQ_AT_t^{r01}\right)$	
Management Based Mispricing	$mispricing_mgmt$	$\begin{split} &\frac{1}{6} \left(CHCSHO_12M_t^{r01} + EQNPO_12M_t^{r01} + \right. \\ &\left. OACCRUALS_AT_t^{r01} + NOA_AT_t^{r01} + \right. \\ &\left. AT_GR1_t^{r01} + PPEINV_GR1A_t^{r01} \right) \end{split}$	
Residual Momentum - 6 Month	$resff3_6_1$	$-1 + \prod_{n=1}^{6} 1 + e_{t-n}$	
Residual Momentum - 12 Month	resff3_12_1	$-1 + \prod_{n=1}^{12} 1 + e_{t-n}$	
	Daily Ma	rket Data ¹⁰	
	Let ϵ_t be defined	d as described here	
Return Volatility	rvol_zd	$\sigma_{zD}(RET_EXC^*_t)$	
Maximum Return	rmax1_zd	$MAX1_zD(RET*_t)$	
Mean Maximum Return	rmax5_zd	$\frac{1}{5} \sum_{n=1}^{5} X_n, X_n \in MAX5_zD(RET^*)$	
Return Skewness	rskew_zd	$SKEW_zD(RET_EXC*_t)$	
Price-to-High	prc_highprc_zd	$\frac{PRC_ADJ^*_t}{MAX1_zD(PRC_ADJ^*_t)}$	
Amihud (2002) Measure	ami_zd	$\left(\frac{ RET^*_t }{DOLVOL^*_t}\right)_{z,D} * 1000000$	
CAPM Beta	beta_zd	Described in detail here	
CAPM Idiosyncratic Vol.	ivol_capm_zd	Described in detail here	
CAPM Skewness	iskew_capm_zd	Described in detail here	
Coskewness	$coskew_zd^{11}$	$\frac{\overline{\left(\epsilon_{t} \times MKTRF_DM_{t}^{2}\right)_{zD}}}{\sqrt{\left(\epsilon_{t}^{2}\right)_{zD} \times \overline{\left(MKTRF_DM_{t}^{2}\right)_{zD}}}}$	
Fama and French Idiosyncratic Vol.	ivol_ff3_zd	Described in detail here	
Fama and French Skewness	iskew_ff3_zd	Described in detail here	
Hou, Xue and Zhang Idiosyncratic Vol.	ivol_hxz4_zd	Described in detail here	
Hou, Xue and Zhang Skewness	iskew_hxz4_zd	Described in detail here	
Dimson Beta	beta_dimson_zd	Created as described in Dimson (1979)	
Downside Beta	betadown_zd	Described in detail here	

⁹A rank characteristic has the value of that characteristics rank with respect to other companies' same characteristic of the same month and country scaled [0, 1]. This is identified with a "r01" superscript.

 $^{^{10}}$ Many of the variables in this section are estimated using rolling windows of data, and the variables are estimated using a variety of window lengths: 21, 126, 252 and 1260 days. In this section, I refer to the number of days as m as a proxy for any of the possible window lengths.

 $^{^{11}}MKTRF_DM_t = MKTRF*_t - \overline{MKTRF*_{tzD}}$

Name	Abbreviation	Construction			
Zero Trades	zero_trades_zd	Number of days with zero trades over period. In case of equ number of zero trading days, turnover_zd will decide on t rank following Liu (2006)			
Turnover	turnover_zd				
Turnover Volatility	turnover_var_zd	$TURNOVER_zD_t$			
Dollar Volume	dolvol_zd	$\overline{DOLVOL^*_{tzD}}$			
Dollar Volume Volatility	dolvol_var_zd	$\frac{\sigma_{zD}(DOLVOL^*_t)}{DOLVOL_zD_t}$			
Correlation to Market	corr_zd	The correlation between $RET_EXC^*_3l = RET_EXC^*_t + RET_EXC^*_{t-1} + RET_EXC^*_{t-2}$ and $MKT_EXC_3l = MKTRF^*_t + MKTRF^*_{t-1} + MKTRF^*_{t-2}$			
Betting Against Beta	betabab_1260d	$\frac{CORR_1260d_t \times RVOL_252d_t}{_MKTVOL_252d^*_t}$			
Max Return to Volatility	rmax5_rvol_21d	$\frac{RMAX5_21d_t}{RVOL_252d_t}$			
21 Day Bid-Ask High-Low	bidaskhl_21d	High-low bid ask estimator created using code from Corwin and Schultz (2012)			
21 Day Return Volatility High-Low	rvolhl_21d	High-low return volatility estimator created using code from Corwin and Schultz (2012)			
	Quality 1	Minus Junk			
		$ZV(ZV(GP_AT_t) + ZV(NI_BE_t) +$			
Quality Minus Junk - Profit	qmj_prof	$ZV(NI_AT_t) + ZV(OCF_AT_t) + ZV(GP_SALE^*_t) +$			
		$ZV(OACCRUALS_AT_t)$			
		$ZV(ZV(GPOA_CH5_t) + ZV(ROE_CH5_t)$			
Quality Minus Junk - Growth	qmj_growth	$+ZV(ROA_CH5_t) + ZV(CFOA_CH5_t) +$			
		$ZV(GMAR_CH5_t)\Big)$			
Quality Minus Junk - Safety	qmj_safety	$ZV\Big(ZV(BETABAB_1260d_t) + ZV(DEBT_AT_t)$			
		$+ZV(O_SCORE_t) + ZV(Z_SCORE_t) + ZV(_EVOL_t)$			
Quality Minus Junk	qmj	$\frac{QMJ_PROF_t + QMJ_GROWTH_t + QMJ_SAFETY_t}{3}$			

8 Detailed Characteristic Construction

This section includes detailed descriptions how we built characteristics that don't easily fit into the Accounting Characteristics or Market Characteristics tables.

• Equity Duration

- Define the following variables:
 - * horizon: number of months used to estimate helper variables
 - * r: constant used as assumed discount rate
 - * roe_mean: constant used as the average ROE value

- * roe_ar1: constant used as the expected growth rate of ROE
- * g_mean: constant used as the average sales growth rate
- * g_ar1: constant used as the expected growth rate of sales
- Create initial variables:

- * If the number of non-missing observations is less than or equal to 12 or the variables' respective denominators are less than or equal to 1 $_roe0_t$ and $_g0_t$ are set to missing.
- Forecast cash distributions

$$roe_c = roe_mean \times (1 - roe_ar1)$$

$$g_c = g_mean \times (1 - g_ar1)$$

$$_roe_t = \sum_{i=1}^{horizon} roe_c + roe_ar1 \times _roe_{t-i}$$

$$_g_t = \sum_{i=1}^{horizon} g_c + g_ar1 \times _g_{t-i}$$

$$_be_t = \sum_{i=1}^{horizon} _be_{t-i} \times (1 + _g_t)$$

$$_cd_t = \sum_{i=1}^{horizon} _be_t \times (_roe_t - _g_t)$$

- Create duration helper variables ¹²

$$ed_constant = horizon + \frac{1+r}{r}$$

$$ed_cw_w_t = \sum_{i=1}^{horizon} ed_cd_w_{i-1} + i \times \frac{__cd_t}{(1+r)^i}$$

$$ed_cd_t = \sum_{i=1}^{horizon} ed_cd_{i-1} + \frac{__cd_t}{(1+r)^i}$$

- Characteristic:

$$eq_dur_t = \frac{ed_ed_w_t \times FX_t}{ME_COMPANY_t} + ed_constant \times \frac{ME_COMPANY_t - ed_cd_t \times FX_t}{ME_COMPANY_t}$$

 $^{^{12}}ed_cw_w$, ed_cd and ed_err are equal to 0 at i = 1. ed_cw_w and ed_cd recurrively build upon themselves over the length of the horizon, so $ed_cw_w_{i-1}$, for example, would be the previous iteration of ed_cw_w

• Piotroski F-Score

- Create helper variables:

$$\begin{split} -f_roa_t &= \frac{NI^*_t}{AT^*_{t-12}} \\ -f_croa_t &= \frac{OCF^*_t}{AT^*_{t-12}} \\ -f_droa_t &= -f_roa_t - -f_roa_{t-12} \\ -f_acc_t &= -f_croa_t - -f_roa_t \\ -f_lev &= \frac{DLTT_t}{AT^*_t} - \frac{DLTT_{t-12}}{AT^*_{t-12}} \\ -f_liq_t &= \frac{CA^*_t}{CL^*_t} - \frac{CA^*_{t-12}}{CL^*_{t-12}} \\ -f_eqis_t &= EQIS^*_t \\ -f_gm_t &= \frac{GP^*_t}{SALE^*_t} - \frac{GP^*_{t-12}}{SALE^*_{t-12}} \\ -f_aturn_t &= \frac{SALE^*_t}{AT^*_{t-12}} - \frac{SALE^*_{t-12}}{AT^*_{t-24}} \end{split}$$

- * For all variables except $_f_acc$, $_f_aturn$ $_f_eqis$, if the count of available observations is less than or equal to 12, then the variable is set to missing. If $_f_aturn$ has less than or equal to 24 non-missing observations, it is set to missing. If a variable has AT^*_t or AT^*_{t-12} as an input and $AT^*_t \leq 0$ or $AT^*_{t-12} \leq 0$, then it is set to missing. If $CL^*_t \leq 0$ or $CL^*_{t-12} \leq 0$ then $_f_liq_t$ is set to missing. If $SALE^*_t \leq 0$ or $SALE^*_{t-12} \leq 0$ then $_f_gm_t$ is set to missing.
- Characteristic¹³

$$f_score_t = _f_roa_{>0,t} + _f_croa_{>0,t} + _f_droa_{>0,t} + _f_acc_{>0,t} + \\ _f_lev_{<0,t} + _f_liq_{>0,t} + _f_eqis_{=0,t} + _f_gm_{>0,t} + _f_aturn_{>0,t}$$

• Ohlson O-Score

 $^{^{13}}$ A subscript of > 0, ex: $VAR_{t>0,t}$, is a dummy for if the variable is greater than zero, and it is defined similarly for $VAR_{t<0,t}$ or any other specification. Otherwise, not included as an input, Also, if any variables other than f-eqis $_t$ are missing, then f-score $_t$ is set to missing.

- Create helper variables:

- * If $AT^*_t \leq 0$, then $_o_lat_t$, $_o_lev_t$, $_o_wc_t$, and $_o_roe_t$ are set to missing. If $CA^*_t \leq 0$ then $_o_cacl_t$ is set to missing. If $LT_T \leq 0$ then $_o_ffo_t$ is set to missing. If LT_t or AT^*_t are missing, then $_o_neg_eq_t$ is set to missing. If there are less than or equal to 12 observations or either of NIX^*_t and NIX^*_{t-12} are missing, then $_o_nich_t$ and $_o_neg_earn_t$ are set to missing.
- Characteristic:

$$o_score_t = -1.37 - 0.407 \times _o_lat_t + 6.03 \times _o_lev_t + 1.43 \times _o_wc_t + 0.076 \times _o_cacl_t - 1.72 \times _o_neg_eq_t - 2.37 \times _o_roe_t - 1.83 \times _o_ffo_t + 0.285 \times _o_neg_earn_t - 0.52 \times _o_nich_t$$

• Altman Z-Score

- Create helper variables:

$$z_{-}wc_{t} = \frac{CA^{*}_{t} - CL^{*}_{t}}{AT^{*}_{t}}$$

$$z_{-}re_{t} = \frac{RE_{t}}{AT^{*}_{t}}$$

$$z_{-}eb_{t} = \frac{EBITDA^{*}_{t}}{AT^{*}_{t}}$$

$$z_{-}sa_{t} = \frac{SALE^{*}_{t}}{AT^{*}_{t}}$$

$$z_{-}me_{t} = \frac{ME_FISCAL_{t}}{LT_{t}}$$

- * If $AT^*_t \leq 0$ then any variable including AT^*_t , then it is set to missing. If $LT_t \leq 0$, then z_me_t is set to missing.
- Characteristic:

$$z_score_t = 1.2 \times _z_wc_t + 1.4 \times _z_re_t + 3.3 \times _z_eb_t + 0.6 \times _z_me_t + 1.0 \times _z_sa_t$$

- Kaplan-Zingales Index
 - Create helper variables:

- * If the number of non-missing observations is less than or equal to 12, then $_kz_cf_t$, $_kz_dv_t$ and $_kz_cs_t$ are set to zero. If $PPENT_{t-12} \le 0$ then $_kz_cf_t$, $_kz_dv_t$ and $_kz_cs_t$ are set to missing. If $AT^*_t \le 0$ then $_kz_q_t$ is set to missing. If $(DEBT^*_t + SEQ^*_t) = 0$ then $_kz_db_t$ is set to missing.
- Characteristic:

 $kz_index = -1.002 \times _kz_cf_t + 0.283 \times _kz_q_t + 3.139 \times _kz_db_t - 39.368 \times _kz_dv_t - 1.315 \times _kz_cs_t$

- Intrinsic Value from Frankel and Lee
 - Define r as a constant assumed discount rate
 - Create helper variables:

* If $NIX^*_t \leq 0$ then

$$iv_{-}po_{t} = \frac{DIV^{*}_{t}}{AT^{*}_{t} \times 0.06}$$

* If the number of non-missing observations is less than or equal to 12 or $(BE^*_t + BE^*_{t-12}) \leq 0$ then $_iv_roe_t$ is set to missing.

- Characteristics:

$$intrinsic_value_t = BE*_t + \frac{_iv_roe_t - r}{1 + r} \times BE*_t + \frac{_iv_roe_t - r}{(1 + r) \times r} \times _iv_be1_t$$

- * If $intrinsic_value_t \leq 0$ then it is set to missing.
- Net Income Idiosyncratic Volatility
 - Define the following variable ¹⁴:

$$_{-}ni_{-}at_{t} = \frac{NI^{*}_{t}}{AT^{*}_{t}}$$

 A rolling regression of the following form is run for each company, with the time series split up into n groups:

$$_ni_at_t = \beta_0 + \beta_1 _ni_at_{t-12} + u_t$$

where edf_t = the error degrees of freedom of regression and $rmse_t$ = root mean square error of the regression.

- Characteristic:

$$ni_ivol_t = \sqrt{\frac{rmse_t^2 \times edf_t}{edf_t + 1}}$$

- Beta, Idiosyncratic Volatility and Skewness of Asset Pricing Factor Regressions
 - This section describes the construction of beta_zd for the CAPM model, and the idiosyncratic volatility and skewness characteristics, which are estimated using three different factor models:
 - * CAPM (capm):

$$RET_{-}EXC^*_{t} = \beta_0 + \beta_1 MKTRF^*_{t} + \epsilon_t$$

* Fama-French 3 Factor Model (ff3):

$$RET_{-}EXC^*_{t} = \beta_0 + \beta_1 MKTRF^*_{t} + \beta_2 HML^*_{t} + \beta_3 SMB_{-}FF^*_{t} + e_t$$

* Hou, Xue and Zhang 4 Factor Model (hxz4):

$$RET_{-}EXC^*_{t} = \beta_0 + \beta_1 MKTRF^*_{t} + \beta_2 SMB_{-}HXZ^*_{t} + \beta_3 ROE^*_{t} + \beta_4 INV^*_{t} + \mu_t$$

¹⁴If $AT^*_t \leq 0$, then $_ni_at_t$ is set to missing

- Characteristics ¹⁵:

$$beta_zd = \beta_1 \text{ from the CAPM model}$$

$$ivol_capm_zd_t = \sigma_{zD}(\epsilon_t)$$

$$ivol_ff3_zd_t = \sigma_{zD}(e_t)$$

$$ivol_hxz4_zd_t = \sigma_{zD}(\mu_t)$$

$$iskew_capm_zd_t = SKEW_zD(\epsilon_t)$$

$$iskew_ff3_zd_t = SKEW_zD(e_t)$$

$$iskew_hxz4_zd_t = SKEW_zD(\sigma_t)$$

• Downside Beta

- Define the following regression model run over z days:

$$RET_{-}EXC^*_{t} = \beta_0 + \beta_1 MKTRF^*_{t} + \epsilon_t$$

However, we restrict the data to when $MKTRF^*$ is negative.

- Characteristic:
 - * $betadown_zd = \beta_1$

9 FX Conversion Rate Construction

This section outlines how we create a daily dataset, beginning 01/01/1950 to now, of X currency - USD exchange rate using COMPUSTAT. This is run in the macro $compustat_f x()$ in the $project_macros.sas$ file.

- We use COMP.EXRT_DLY, which has daily conversion rates from GBP to other currencies 'X'.
- Every day available, we estimate the exchange rate fx_t as

$$fx_t = \frac{USD_{GBP,t}}{X_{GBP,t}}$$

where $X_{GBP,t}$ is the exchange rate of GBP to currency X on day t.

- In case there are gaps in information, we assume the exchange rate of the last observation until a new observation is available.
- fx_t is quoted as $\frac{X_t}{USD_t}$, so to go from X to USD, do $X_t \times fx_t$

 $^{^{15}}z$ indicates over how many days the model is run.

10 Factor Details and Citations

Table 9: Factor and Cluster Details

	Variable		Orig.		Orig.
Description	Name	Citation	Sample	Sign	Signif.
		Accruals			
Change in current operating work-	cowc_gr1a	Richardson, Sloan, Soliman, and	1962-2001	-1	1
ing capital	o o	Tuna (2005)			
Operating accruals	$oaccruals_at$	Sloan (1996)	1962-1991	-1	1
Percent operating accruals	oaccruals_ni	Hafzalla, Lundholm, and Matthew	1989-2008	-1	1
		Van Winkle (2011)			
Years 16-20 lagged returns, nonan-	$seas_16_20na$	Heston and Sadka (2008)	1965-2002	1	1
nual					
Total accruals	$taccruals_at$	Richardson et al. (2005)	1962-2001	-1	1
Percent total accruals	taccruals_ni	Hafzalla et al. (2011)	1989-2008	-1	1
		Debt Issuance			
Abnormal corporate investment	$capex_abn$	Titman, Wei, and Xie (2004)	1973-1996	-1	1
Growth in book debt (3 years)	$debt_gr3$	Lyandres, Sun, and Zhang (2008)	1970 - 2005	-1	1
Change in financial liabilities	fnl_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Change in noncurrent operating li-	$ncol_gr1a$	Richardson et al. (2005)	1962-2001	-1	0
abilities					
Change in net financial assets	$nfna_gr1a$	Richardson et al. (2005)	1962-2001	1	1
Earnings persistence	ni_ar1	Francis, LaFond, Olsson, and	1975-2001	1	0
		Schipper (2004)			
Net operating assets	noa_at	Hirshleifer, Hou, Teoh, and Zhang (2004)	1964-2002	-1	1
		Investment			
Liquidity of book assets	aliq_at	Ortiz-Molina and Phillips (2014)	1984-2006	-1	0
Asset Growth	at_gr1	Cooper, Gulen, and Schill (2008)	1968-2003	-1	1
Change in common equity	be_gr1a	Richardson et al. (2005)	1962-2001	-1	1
CAPEX growth (1 year)	capx_gr1	Xie (2001)	1971-1992	-1	0
CAPEX growth (2 years)	capx_gr2	Anderson and Garcia-Feijoo (2006)	1976-1998	-1	1
CAPEX growth (3 years)	capx_gr3	Anderson and Garcia-Feijoo (2006)	1976-1998	-1	1
Change in current operating assets	coa_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Change in current operating liabil-	col_gr1a	Richardson et al. (2005)	1962-2001	-1	1
ities	0	(2000)		-	-
Hiring rate	emp_gr1	Belo, Lin, and Bazdresch (2014)	1965-2010	-1	1
Inventory growth	inv_gr1	Belo and Lin (2012)	1965-2009	-1	1
Inventory change	inv_gr1a	J. K. Thomas and Zhang (2002)	1970-1997	-1	1
Change in long-term net operating	lnoa_gr1a	Fairfield, Whisenant, and Yohn	1964-1993	-1	1
assets	G	(2003)			
Mispricing factor: Management	mispricing_mg	mtStambaugh and Yuan (2017)	1967-2013	1	1
Change in noncurrent operating as-	ncoa_gr1a	Richardson et al. (2005)	1962-2001	-1	1
sets	<u> </u>				
Change in net noncurrent operating	nncoa_gr1a	Richardson et al. (2005)	1962-2001	-1	1
assets	_	, ,			
Change in net operating assets	noa_gr1a	Hirshleifer et al. (2004)	1964-2002	-1	1
Change PPE and Inventory	ppeinv_gr1a	Lyandres et al. (2008)	1970-2005	-1	1
endinger i i i dina inventory					

Sales Growth (1 year)	$sale_gr1$	Lakonishok, Shleifer, and Vishny (1994)	1968-1989	-1	1
Sales Growth (3 years)	$sale_gr3$	Lakonishok et al. (1994)	1968-1989	-1	1
Sales growth (1 quarter)	saleq_gr1	(=)	1967-2016	-1	0
Years 2-5 lagged returns, nonannual	seas_2_5na	Heston and Sadka (2008)	1965-2002	-1	1
,		, ,			
		ow Leverage	1005 0001	_	
Firm age	age	Jiang, Lee, and Zhang (2005)	1965-2001	-1	1
Liquidity of market assets	aliq_mat	Ortiz-Molina and Phillips (2014)	1984-2006	-1	0
Book leverage	at_be	Fama and French (1992)	1963-1990	-1	0
The high-low bid-ask spread	bidaskhl_21d	Corwin and Schultz (2012)	1927-2006	1	1
Cash-to-assets	cash_at	Palazzo (2012)	1972-2009	1	0
Net debt-to-price	netdebt_me	Penman, Richardson, and Tuna (2007)	1962-2001	-1	1
Earnings volatility	ni_ivol	Francis et al. (2004)	1975 - 2001	1	0
R&D-to-sales	rd_sale	Chan, Lakonishok, and Sougiannis (2001)	1975-1995	1	0
R&D capital-to-book assets	$rd5_at$	Li (2011)	1952-2004	1	0
Asset tangibility	tangibility	Hahn and Lee (2009)	1973-2001	1	0
Altman Z-score	z_score	Dichev (1998)	1981-1995	1	1
Tribinar 2 score	ZEGOTC	Dienev (1990)	1001 1000	1	_
		Low Risk			
Market Beta	$beta_60m$	Fama and MacBeth (1973)	1935-1968	-1	1
Dimson beta	beta_dimson_21	d Dimson (1979)	1955 - 1974	-1	0
Frazzini-Pedersen market beta	$betabab_1260d$	Frazzini and Pedersen (2014)	1926 - 2012	-1	1
Downside beta	$betadown_252d$	Ang, Chen, and Xing (2006)	1963-2001	-1	1
Earnings variability	earnings_variabi	liFyancis et al. (2004)	1975 - 2001	-1	0
Idiosyncratic volatility from the CAPM (21 days)	ivol_capm_21d		1967-2016	-1	0
Idiosyncratic volatility from the CAPM (252 days)	$ivol_capm_252d$	Ali, Hwang, and Trombley (2003)	1976-1997	-1	1
Idiosyncratic volatility from the Fama-French 3-factor model	$ivol_ff3_21d$	Ang, Hodrick, Xing, and Zhang (2006)	1963-2000	-1	1
Idiosyncratic volatility from the q-	$ivol_hxz4_21d$	(2000)	1967-2016	-1	0
factor model	C 1 1	II (2000)	1000 0004	1	-1
Cash flow volatility	ocfq_saleq_std	Huang (2009)	1980-2004	-1	1
Maximum daily return	rmax1_21d	Bali, Cakici, and Whitelaw (2011)	1962-2005	-1	1
Highest 5 days of return	rmax5_21d	Bali, Brown, and Tang (2017)	1993-2012	-1	1
Return volatility	rvol_21d	Ang, Hodrick, et al. (2006)	1963-2000	-1	1
Years 6-10 lagged returns, nonannual	seas_6_10na	Heston and Sadka (2008)	1965-2002	-1	1
Share turnover	$turnover_126d$	Datar, Naik, and Radcliffe (1998)	1963-1991	-1	1
Number of zero trades with	$zero_trades_21d$	Liu (2006)	1963-2003	1	0
turnover as tiebreaker (1 month)					
Number of zero trades with	zero_trades_126	d Liu (2006)	1963-2003	1	1
turnover as tiebreaker (6 months)					
Number of zero trades with turnover as tiebreaker (12 months)	zero_trades_2526	d Liu (2006)	1963-2003	1	1
	7	Momentum_			
Current price to high price over last		dGeorge and Hwang (2004)	1963-2001	1	1
year	pre-manpre-202	accorde and Hwang (2004)	1000-2001	1	1
Residual momentum t-6 to t-1	resff3_6_1	Blitz, Huij, and Martens (2011)	1930-2009	1	1
Residual momentum t-12 to t-1	resff3_12_1	Blitz et al. (2011)	1930-2009	1	1
		·- ·- (-·- /		-	_

Price momentum t-3 to t-1	ret_3_1	Jegadeesh and Titman (1993)	1965-1989	1	1
Price momentum t-6 to t-1	ret_6_1	Jegadeesh and Titman (1993)	1965-1989	1	1
Price momentum t-9 to t-1	ret_9_1	Jegadeesh and Titman (1993)	1965-1989	1	1
Price momentum t-12 to t-1	$ret_{-}12_{-}1$	Jegadeesh and Titman (1993)	1965-1989	1	1
Year 1-lagged return, nonannual	seas_1_1na	Heston and Sadka (2008)	1965-2002	1	1
	<u>P</u> :	rofit Growth			
Change sales minus change Inventory	$dsale_dinv$	Abarbanell and Bushee (1998)	1974-1988	1	1
Change sales minus change receivables	$dsale_drec$	Abarbanell and Bushee (1998)	1974-1988	-1	0
Change sales minus change SG&A	$dsale_dsga$	Abarbanell and Bushee (1998)	1974-1988	1	0
Change in quarterly return on assets	niq_at_chg1		1972-2016	1	0
Change in quarterly return on equity	niq_be_chg1		1967-2016	1	0
Standardized earnings surprise	niq_su	Foster, Olsen, and Shevlin (1984)	1974-1981	1	1
Change in operating cash flow to as-	ocf_at_chg1	Bouchaud, Krueger, Landier, and	1990-2015	1	1
sets	001-00-01181	Thesmar (2019)	1000 2010	-	-
Price momentum t-12 to t-7	ret_12_7	Novy-Marx (2012)	1925-2010	1	1
Labor force efficiency	$sale_emp_gr1$	Abarbanell and Bushee (1998)	1974-1988	1	0
Standardized Revenue surprise	saleq_su	Jegadeesh and Livnat (2006)	1987-2003	1	1
Year 1-lagged return, annual	seas_1_1an	Heston and Sadka (2008)	1965-2002	1	1
Tax expense surprise	tax_gr1a	J. Thomas and Zhang (2011)	1977 - 2006	1	1
		Profitability			
Coefficient of variation for dollar	dolvol_var_126d	Chordia, Subrahmanyam, and An-	1966-1995	-1	1
trading volume		shuman (2001)			
Return on net operating assets	ebit_bev	Soliman (2008)	1984-2002	1	1
Profit margin	ebit_sale	Soliman (2008)	1984-2002	1	1
Pitroski F-score	f_score	Piotroski (2000)	1976-1996	1	1
Return on equity	ni_be	Haugen and Baker (1996)	1979-1993	1	1
Quarterly return on equity Ohlson O-score	niq_be	Hou, Xue, and Zhang (2015) Dichev (1998)	1972-2012	1	1 1
Operating cash flow to assets	o_score ocf_at	Bouchaud et al. (2019)	1981-1995 1990-2015	-1 1	1
Operating cash now to assets Operating profits-to-book equity	ope_be	Fama and French (2015)	1963-2013	1	1
Operating profits-to-lagged book	ope_bel1	rama and French (2019)	1967-2016	1	0
equity	оредост		1307-2010	1	U
Coefficient of variation for share	turnover_var_12	66 Chordia et al. (2001)	1966-1995	-1	1
turnover					
		Quality			
Capital turnover	at_turnover	Haugen and Baker (1996)	1979-1993	1	0
Cash-based operating profits-to-	cop_at	iiaugen und Baker (1000)	1967-2016	1	0
book assets					-
Cash-based operating profits-to-	cop_atl1	Ball, Gerakos, Linnainmaa, and	1963-2014	1	1
lagged book assets	•	Nikolaev (2016)			
Change gross margin minus change sales	dgp_dsale	Abarbanell and Bushee (1998)	1974-1988	1	0
Gross profits-to-assets	gp_at	Novy-Marx (2013)	1963-2010	1	1
Gross profits-to-lagged assets	gp_atl1	• •	1967-2016	1	0
Mispricing factor: Performance	mispricing_perf	Stambaugh and Yuan (2017)	1967-2013	1	1
Number of consecutive quarters	ni_inc8q	Barth, Elliott, and Finn (1999)	1982-1992	1	0
with earnings increases					

Quarterly return on assets	niq_at	Balakrishnan, Bartov, and Faurel (2010)	1976-2005	1	1
Operating profits-to-book assets	op_at	(2010)	1963-2013	1	1
Operating profits-to-lagged book assets	op_atl1			1	1
Operating leverage	opex_at	Novy-Marx (2011)	1963-2008	1	1
Quality minus Junk: Composite	qmj	C. S. Asness, Frazzini, and Pedersen (2019)	1957-2016	1	1
Quality minus Junk: Growth	qmj_growth	C. S. Asness et al. (2019)	1957-2016	1	1
Quality minus Junk: Profitability	qmj_prof	C. S. Asness et al. (2019)	1957 - 2016	1	1
Quality minus Junk: Safety	qmj_safety	C. S. Asness et al. (2019)	1957 - 2016	1	1
Assets turnover	${\rm sale_bev}$	Soliman (2008)	1984-2002	1	1
	,	Seasonality			
Market correlation	corr_1260d	C. Asness, Frazzini, Gormsen, and	1925-2015	-1	1
1101101 0011010101	0011_11 _ 0004	Pedersen (2020)	1020 2010	-	-
Coskewness	$\cos kew_21d$	Harvey and Siddique (2000)	1963-1993	-1	1
Net debt issuance	$dbnetis_at$	Bradshaw, Richardson, and Sloan	1971-2000	-1	1
		(2006)			
Kaplan-Zingales index	kz_index	Lamont, Polk, and Saaá-Requejo (2001)	1968-1995	1	1
Change in long-term investments	lti_gr1a	Richardson et al. (2005)	1962-2001	-1	1
Taxable income-to-book income	pi_nix	Lev and Nissim (2004)	1973 - 2000	1	1
Years 2-5 lagged returns, annual	$seas_25an$	Heston and Sadka (2008)	1965 - 2002	1	1
Years 6-10 lagged returns, annual	$seas_6_10an$	Heston and Sadka (2008)	1965 - 2002	1	1
Years 11-15 lagged returns, annual	$seas_11_15an$	Heston and Sadka (2008)	1965 - 2002	1	1
Years 11-15 lagged returns, nonannual	seas_11_15na	Heston and Sadka (2008)	1965-2002	-1	0
Years 16-20 lagged returns, annual	$seas_16_20an$	Heston and Sadka (2008)	1965 - 2002	-1	1
Change in short-term investments	sti_gr1a	Richardson et al. (2005)	1962-2001	1	0
		Size			
Amihud Measure	ami_126d	Amihud (2002)	1964-1997	1	1
Dollar trading volume	dolvol_126d	Brennan, Chordia, and Subrah-	1966-1995	-1	1
-		manyam (1998)			
Market Equity	$market_equity$	Banz (1981)	1926-1975	-1	1
Price per share	prc	Miller and Scholes (1982)	1940-1978	-1	1
R&D-to-market	rd_me	Chan et al. (2001)	1975-1995	1	1
	Short	-Term Reversal			
Idiosyncratic skewness from the CAPM	iskew_capm_21d		1967-2016	-1	0
Idiosyncratic skewness from the Fama-French 3-factor model	iskew_ff3_21d	Bali, Engle, and Murray (2016)	1925-2021	-1	1
Idiosyncratic skewness from the q-factor model	iskew_hxz4_21d		1967-2016	-1	0
Short-term reversal	ret_1_0	Jegadeesh (1990)	1929-1982	-1	1
Highest 5 days of return scaled by		C. Asness et al. (2020)	1925-2015	-1	1
volatility Total skewness	rskew_21d	Bali et al. (2016)	1925-2021	-1	1
TOTAL DISCALIONS	10110 W _2 1U	Dail 00 al. (2010)	1020-2021	1	1
		Value			
Assets-to-market	at_me	Fama and French (1992)	1963-1990	1	0

Book-to-market equity	be_me	Rosenberg, Reid, and Lanstein	1973-1984	1	1
		(1985)			
Book-to-market enterprise value	bev_mev	Penman et al. (2007)	1962-2001	1	1
Net stock issues	$chcsho_{-}12m$	Pontiff and Woodgate (2008)	1970 - 2003	-1	1
Debt-to-market	$debt_me$	Bhandari (1988)	1948 - 1979	1	1
Dividend yield	$div12m_me$	Litzenberger and Ramaswamy	1940-1980	1	1
		(1979)			
Ebitda-to-market enterprise value	$ebitda_mev$	Loughran and Wellman (2011)	1963-2009	1	1
Equity duration	eq_dur	Dechow, Sloan, and Soliman (2004)	1962-1998	-1	1
Net equity issuance	$eqnetis_at$	Bradshaw et al. (2006)	1971 - 2000	-1	1
Equity net payout	$eqnpo_12m$	Daniel and Titman (2006)	1968-2003	1	1
Net payout yield	$eqnpo_me$	Boudoukh, Michaely, Richardson,	1984-2003	1	1
		and Roberts (2007)			
Payout yield	eqpo_me	Boudoukh et al. (2007)	1984-2003	1	1
Free cash flow-to-price	fcf_me	Lakonishok et al. (1994)	1963-1990	1	1
Intrinsic value-to-market	$ival_me$	Frankel and Lee (1998)	1975 - 1993	1	0
Net total issuance	$netis_at$	Bradshaw et al. (2006)	1971 - 2000	-1	1
Earnings-to-price	ni_me	Basu (1983)	1963 - 1979	1	1
Operating cash flow-to-market	ocf_me	Desai, Rajgopal, and Venkatacha-	1973 - 1997	1	1
		lam (2004)			
Sales-to-market	$sale_me$	Barbee Jr, Mukherji, and Raines	1979 - 1991	1	1
		(1996)			

Other Factors

	Otr
Assets	assets
Sales	sales
Book Equity	book_equity
Net Income	$\operatorname{net_income}$
Enterprise Value	$enterprise_value$
Current Asset Growth 1yr	ca_gr1
Non-Current Asset Growth 1yr	nca_gr1
Total Liabilities Growth 1yr	lt_gr1
Current Liabilities Growth 1yr	cl_gr1
Non-Current Liabilities Growth 1yr	ncl_gr1
Book Equity Growth 1yr	be_gr1
Preferred Stock Growth 1 yr	$pstk_gr1$
Total Debt Growth 1yr	$debt_gr1$
Cost of Goods Sold Growth 1yr	$cogs_gr1$
Selling, General, and Administra-	sga_gr1
tive Expenses Growth 1yr	
Operating Expenses Growth 1yr	$opex_gr1$
Asset Growth 3yr	at_gr3
Current Asset Growth 3yr	ca_gr3
Non-Current Asset Growth 3yr	nca_gr3
Total Liabilities Growth 3yr	lt_gr3
Current Liabilities Growth 3yr	cl_gr3
Non-Current Liabilities Growth 3yr	ncl_gr3
Book Equity Growth 3yr	be_gr3
Preferred Stock Growth 3yr	$pstk_gr3$
Cost of Goods Sold Growth 3yr	$cogs_gr3$
Selling, General, and Administra-	sga_gr3
tive Expenses Growth 3yr	
Operating Expenses Growth 3yr	$opex_gr3$
Gross Profit Change 1yr	gp_gr1a

Operating Cash Flow Change 1yr	ocf_gr1a
Cash and Short-Term Investments	cash_gr1a
Change 1yr	
Receivables Change 1yr	rec_gr1a
Property, Plans and Equipment	ppeg_gr1a
Gross Change 1yr	
Intangible Assets Change 1yr	intan_gr1a
Short-Term Debt Change 1yr	debtst_gr1a
Accounts Payable Change 1yr	ap_gr1a
Income Tax Payable Change 1yr	txp_gr1a
Long-Term Debt Change 1yr	debtlt_gr1a
Deferred Taxes and Investment	txditc_gr1a
Credit Change 1yr	
Non-Current Operating Liabilities	ncol_gr1a
Change 1yr	
Operating Assets Change 1yr	oa_gr1a
Operating Liabilities Change 1yr	ol_gr1a
Financial Assets Change 1yr	fna_gr1a
Operating Profit before Deprecia-	ebitda_gr1a
tion Change 1yr	ebitda_gi1a
Operating Profit after Depreciation	obit orlo
Change 1yr	ebit_gr1a
	one male
Operating Earnings to Equity	ope_gr1a
Change 1yr	1 -
Net Income Change 1yr Depreciation and Amortization	ni_gr1a
Depreciation and Amortization	dp_gr1a
	1 0
Change 1yr	
Change 1yr Free Cash Flow Change 1yr	fcf_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr	fcf_gr1a nwc_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordi-	fcf_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr	fcf_gr1a nwc_gr1a nix_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance	fcf_gr1a nwc_gr1a nix_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance Change 1yr	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance Change 1yr	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a dltnetis_gr1a
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Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance Change 1yr Net Short-Term Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Issuance Change 1yr Financial Cash Flow Change 1yr Equity Net Payout Change 1yr Equity Net Payout Ratio Change 1yr Equity Buyback Change 1yr Equity Issuance Change 1yr Net Equity Payout Change 1yr Capital Expenditures Change 1yr Gross Profit Change 3yr Operating Cash Flow Change 3yr Cash and Short-Term Investments	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a dltnetis_gr1a dstnetis_gr1a dbnetis_gr1a netis_gr1a eqnpo_gr1a eqnpo_gr1a eqbb_gr1a eqis_gr1a eqpo_gr1a eqpo_gr1a capx_gr1a gp_gr3a ocf_gr3a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance Change 1yr Net Short-Term Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Issuance Change 1yr Financial Cash Flow Change 1yr Equity Net Payout Change 1yr Equity Net Payout Change 1yr Equity Buyback Change 1yr Equity Issuance Change 1yr Requity Issuance Change 1yr Capital Expenditures Change 1yr Gross Profit Change 3yr Operating Cash Flow Change 3yr Cash and Short-Term Investments Change 3yr	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a dltnetis_gr1a dstnetis_gr1a dbnetis_gr1a netis_gr1a fincf_gr1a eqnpo_gr1a div_gr1a eqbb_gr1a eqis_gr1a eqpo_gr1a capx_gr1a gp_gr3a ocf_gr3a cash_gr3a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance Change 1yr Net Short-Term Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Issuance Change 1yr Financial Cash Flow Change 1yr Equity Net Payout Change 1yr Equity Net Payout Ratio Change 1yr Equity Buyback Change 1yr Equity Issuance Change 1yr Requity Issuance Change 1yr Capital Expenditures Change 1yr Gross Profit Change 3yr Operating Cash Flow Change 3yr Cash and Short-Term Investments Change 3yr Inventory Change 3yr	fcf_gr1a nwc_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a dltnetis_gr1a dstnetis_gr1a dbnetis_gr1a fincf_gr1a eqnpo_gr1a eqnpo_gr1a eqbb_gr1a eqis_gr1a eqpo_gr1a capx_gr1a gp_gr3a ocf_gr3a cash_gr3a inv_gr3a rec_gr3a
Change 1yr Free Cash Flow Change 1yr Net Working Capital Change 1yr Net Income Including Extraordinary Items Change 1yr Equity Net Issuance Change 1yr Net Long-Term Debt Issuance Change 1yr Net Short-Term Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Debt Issuance Change 1yr Net Issuance Change 1yr Financial Cash Flow Change 1yr Equity Net Payout Change 1yr Equity Net Payout Change 1yr Equity Buyback Change 1yr Equity Issuance Change 1yr Equity Issuance Change 1yr Capital Expenditures Change 1yr Gross Profit Change 3yr Operating Cash Flow Change 3yr Cash and Short-Term Investments Change 3yr Inventory Change 3yr Receivables Change 3yr	fcf_gr1a nwc_gr1a nix_gr1a eqnetis_gr1a dltnetis_gr1a dstnetis_gr1a dbnetis_gr1a netis_gr1a fincf_gr1a eqnpo_gr1a div_gr1a eqbb_gr1a eqis_gr1a eqpo_gr1a capx_gr1a gp_gr3a ocf_gr3a cash_gr3a inv_gr3a

Investment and Advances Change	lti_gr3a
3yr	
Intangible Assets Change 3yr	$intan_gr3a$
Short-Term Debt Change 3yr	$debtst_gr3a$
Accounts Payable Change 3yr	ap_gr3a
Income Tax Payable Change 3yr	txp_gr3a
Long-Term Debt Change 3yr	debtlt_gr3a
Deferred Taxes and Investment	txditc_gr3a
Credit Change 3yr	txuitc_groa
- ·	
Current Operating Assets Change	coa_gr3a
3yr	1 0
Current Operating Liabilities	col_gr3a
Change 3yr	
Current Operating Working Capi-	$cowc_gr3a$
tal Change 3yr	
Non-Current Operating Assets	$ncoa_gr3a$
Change 3yr	
Net Non-Current Operating Assets	$nncoa_gr3a$
Change 3yr	
Operating Assets Change 3yr	oa_gr3a
Operating Liabilities Change 3yr	ol_gr3a
Net Operating Assets Change 3yr	noa_gr3a
Financial Assets Change 3yr	fna_gr3a
Financial Liabilities Change 3yr	fnl_gr3a
Net Financial Assets Change 3yr	nfna_gr3a
Operating Profit before Deprecia-	ebitda_gr3a
	ebitda_gr5a
tion Change 3yr	ahit mu?a
Operating Profit after Depreciation	ebit_gr3a
Change 3yr	
Operating Earnings to Equity	ope_gr3a
Change 3yr	
Net Income Change 3yr	ni_gr3a
Depreciation and Amortization	dp_gr3a
Change 3yr	
Free Cash Flow Change 3yr	fcf_gr3a
Net Working Capital Change 3yr	nwc_gr3a
Inventory Change 1yr	inv_gr3a
Non-Current Operating Liabilities	$ncol_gr3a$
Change 3yr	
Net Income Including Extraordi-	nix_gr3a
nary Items Change 3yr	
Equity Net Issuance Change 3yr	eqnetis_gr3a
Net Long-Term Debt Issuance	dltnetis_gr3a
Change 3yr	411110110-8104
Net Short-Term Debt Issuance	dstnetis_gr3a
Change 3yr	dstrictis_groa
Net Debt Issuance Change 3yr	dbnotic gr3a
	dbnetis_gr3a
Net Issuance Change 3yr	netis_gr3a
Financial Cash Flow Change 3yr	fincf_gr3a
Net Working Capital Change 3yr	nwc_gr3a
Equity Net Payout Change 3yr	eqnpo_gr3a
Effective Tax Rate Change 3yr	tax_gr3a
Dividend Payout Ratio Change 3yr	div_gr3a
Equity Buyback Change 3yr	$eqbb_gr3a$

Equity Issuance Change 3yr	eqis_gr3a
Net Equity Payout Change 3yr	eqpo_gr3a
Capital Expenditures Change 3yr	capx_gr3a
Capital Expenditures scaled by As-	capx_at
sets	
R&D scaled by Assets	rd_at
Special Items scaled by Assets	spi_at
Extraordinary Items and Discontin-	xido_at
	xido_at
ued Operations scaled by Assets	. ,
Non-Recurring Items scaled by As-	nri_at
sets	
Gross Profit Margin	gp_sale
Operating Profit Margin before De-	$ebitda_sale$
preciation	
Pretax Profit Margin	pi_sale
Net Profit Margin before extraordi-	ni_sale
nary income	
Net Profit Margin	nix_sale
Free Cash Flow Margin	fcf_sale
Operating Cash Flow Margin	ocf_sale
Operating Cash Flow Margin Operating Profit before Deprecia-	ebitda_at
tion scaled by Assets	ebitda_at
	-1-:4 -4
Operating Profit after Depreciation	ebit_at
scaled by Assets	a .
Firm Income scaled by Assets	fi_at
Net Income Including Extraordi-	nix_be
nary Items scaled by BE	
Operating Cash Flow scaled by BE	ocf_be
Free Cash Flow scaled by BE	fcf_be
Gross Profit scaled by BEV	gp_bev
Operating Profit before Deprecia-	$ebitda_bev$
tion scaled by BEV	
Firm Income scaled by BEV	fi_bev
Cash Based Operating Profitability	cop_bev
scaled by BEV	cop_cc.
Gross Profit scaled by PPEN	on ppon
Operating Profit before Deprecia-	gp_ppen
	ebitda_ppen
tion scaled by PPEN	СС
Free Cash Flow scaled by PPEN	fcf_ppen
Financial Cash Flow scaled by As-	$fincf_at$
sets	
Equity Issuance scaled by Assets	eqis_at
Net Long-Term Debt Issuance	$dltnetis_at$
scaled by Assets	
Net Short-Term Debt Issuance	$dstnet is_at$
scaled by Assets	
Equity Net Payout scaled by Assets	eqnpo_at
Net Equity Payout scaled by Assets	eqbb_at
Total Dividends scaled by Assets	div_at
Common Equity scaled by BEV	be_bev
Total Debt scaled by BEV	debt_bev
Cash and Short-Term Investments	cash_bev
	Casii_DeV
scaled by BEV	
Preferred Stock scaled by BEV	$pstk_bev$

Long-Term Debt scaled by BEV Short-Term Debt scaled by BEV Total Debt scaled by MEV Preferred Stock scaled by MEV Long-Term Debt scaled by MEV Short-Term Debt scaled by MEV Interest scaled by Total Debt Interest scaled by Long-Term Debt Operating Profit before Depreciation scaled by Total Debt Profit before D&A scaled by Cur-	debtlt_bev debtst_bev debt_mev pstk_mev debtlt_mev debtst_mev int_debt int_debtlt ebitda_debt
rent Liabilities Operating Cash Flow scaled by Current Liabilities	ocf_cl
Operating Cash Flow scaled by Total Debt	
Cash Balance scaled by Total Liabilities	cash_lt
Inventory scaled by Current Assets Receivables scaled by Current Assets	inv_act rec_act
Short-Term Debt scaled by Total Debt	
Current Liabilities scaled by Total Liabilities	cl_lt
Long-Term Debt scaled by Total Debt	
Free Cash Flow scaled by Operating Cash Flow	fcf_ocf
Total Liabilities scaled by Total Tangible Assets	lt_{-ppen}
Long-Term Debt to Book Equity	debtlt_be
Working Capital scaled by Assets	nwc_at
Debt-to-Assets	debt_at
Debt to Shareholders' Equity Ratio	debt_be ebit_int
Interest Coverage Ratio	
Days Inventory Outstanding Days Sales Outstanding	inv_days rec_days
Days Accounts Payable Outstand-	ap_days
ing	
Cash Conversion Cycle	cash_conversion
Cash Ratio	cash_cl
Quick Ratio	caliq_cl
Current Ratio	ca_cl
Inventory Turnover	$inv_turnover$
Receivables Turnover	$rec_turnover$
Account Payables Turnover	ap_turnover
Advertising scaled by Sales	adv_sale
Labor Expense scaled by Sales	staff_sale
Sales scaled by Total Stockholders'	sale_be
Equity Dividend Payout Ratio	div_ni
Dividend Payout Ratio Sales scaled by Working Capital	sale_nwc
Effective Tax Rate	tax_pi

Intrinsic Value	intrinsic_value
Cash and Short-Term Investments	cash_me
scaled by Market Equity	0001121110
Gross Profit scaled by ME	gp_me
Operating Profit before Deprecia-	ebitda_me
tion scaled by ME	
Operating Profit after Depreciation	ebit_me
scaled by ME	
Operating Earnings to Equity	ope_me
scaled by ME	
Net Income Including Extraordi-	nix_me
nary Items scaled by ME	
Cash Based Operating Profitability	cop_me
scaled by ME	
Book Equity scaled by MEV	be_mev
Total Assets scaled by MEV	at_mev
Cash and Short-Term Investments scaled by MEV	cash_mev
Property, Plans and Equipment	nnon morr
Net scaled by MEV	ppen_mev
Total Dividends scaled by ME	div_me
Equity Buyback scaled by ME	eqbb_me
Equity Issuance scaled by ME	eqis_me
Equity Net Issuance scaled by ME	eqnetis_me
Net Long-Term Debt Issuance	1
scaled by MEV	
Net Short-Term Debt Issuance	$dstnetis_mev$
scaled by MEV	
Net Debt Issuance scaled by MEV	$dbnetis_mev$
Net Issuance scaled by MEV	$netis_mev$
Gross Profit scaled by MEV	gp_mev
Operating Profit after Depreciation	$ebit_mev$
scaled by MEV	
Sales scaled by MEV	sale_mev
Operating Cash Flow scaled by	ocf_mev
MEV	c c
Free Cash Flow scaled by MEV	fcf_mev
Cash Based Operating Profitability scaled by MEV	cop_mev
Financial Cash Flow Change scaled	fincf_mev
by MEV	mici_mev
Net Income to Sales Quarterly	niq_saleq_std
Volatility	mq_sareq_sea
Net Income scaled by Employees	ni_emp
Sales scaled by Employees	sale_emp
Net Income scaled by Assets	ni_at
Quarterly ROE Volatility	$roeq_be_std$
ROE Volatility	roe_be_std
Gross Product to Assets 5 yr	$gpoa_ch5$
Change	
ROE 5 yr Change	roe_ch5
ROA 5 yr Change	roa_ch5
Operating Cash Flow to Assets 5 yr	cfoa_ch5
Change	

Gross Product to Sales 5 yr Change	gmar_ch5	
Dividend to Price - 1 Month	div1m_me	
Dividend to Price - 3 Months	div3m_me	
Dividend to Price - 6 Months	div6m_me	
Special Dividend to Price - 1 Month	divspc1m_me	
Special Dividend to Price - 12	divspc12m_me	
Month	divsperzin_ine	
Change in Shares - 1 Month	chcsho_1m	
Change in Shares - 3 Month	chcsho_3m	
Change in Shares - 6 Month	chcsho_6m	
Net Equity Payout - 1 Month	eqnpo_1m	
Net Equity Payout - 3 Month	eqnpo_3m	
Net Equity Payout - 6 Month	eqnpo_6m	
Momentum 0-2 Months	ret_2_0	
Momentum 0-3 Months	ret_3_0	
Momentum 0-6 Months	ret_6_0	
Momentum 0-9 Months	ret_9_0	
Momentum 0-12 Months	ret_12_0	
Momentum 1-18 Months	ret_18_1	
Momentum 1-24 Months	ret_24_1	
Momentum 12-24 Months	ret_24_12	
Momentum 1-36 Months	ret_36_1	
Momentum 12-36 Months	ret_36_12	
Momentum 1-48 Months	ret_48_1	
Momentum 12-48 Months	ret_48_12	
Momentum 1-60 Months	ret_60_1	
Momentum 36-60 Months	ret_60_36	
Market beta (21 days)	$beta_21d$	
Market beta (252 days)	$beta_252d$	
Return volatility (252 days)	$rvol_252d$	
Idiosyncratic volatility from the	$ivol_capm_60m$	
CAPM (60 months)		
The high-low return volatility	rvolhl_21d	Corwin and Schultz (2012)

Note: This table shows cluster names as underlined section headings and, for each cluster, a description of the factors included, the variable name used in the code, the original reference, the sample period used in the original reference, the sign of the factor ("1" means "long", "-1" means "short"), and whether the original reference found the factor to be significant ("1" means "yes", "0" means "no"). For example, the first value factor "at_me" goes long stocks with high values of assets-to-market and shorts those with low values (and would be done the reverse if the sign was "-1" instead of "1").

11 Miscellaneous

Table 10: Country Code Key and MSCI Categorization

Country	EXCNTRY-Country Code	MSCI Categorization
Argentina	ARG	standalone
Australia	AUS	developed
Austria	AUT	developed
Bahrain	BHR	frontier
Bangladesh	BGD	frontier
Belgium	BEL	developed
Bermuda	BMU	not rated
Botswana	BWA	standalone
Brazil	BRA	emerging
Bulgaria	BGR	standalone
Canada	CAN	developed
Chile	CHL	emerging
China	CHN	emerging
Colombia	COL	emerging
Croatia	HRV	frontier
Cyprus	CYP	not rated
Czech Republic	CZE	emerging
Denmark	DNK	developed
Ecuador	ECU	not rated
Egypt	EGY	emerging
Estonia	EST	frontier
Finland	FIN	developed
France	FRA	developed
Germany	DEU	developed
Ghana	GHA	not rated
Greece	GRC	emerging
Guernsey	GGY	not rated
Hong Kong	HKG	developed
Hungary	HUN	emerging
Iceland	ISL	frontier
India	IND	emerging
Indonesia	IDN	emerging
Iran, Islamic Republic of	IRN	not rated
Ireland	IRL	developed
Israel	ISR	developed
Italy	ITA	developed
Jamaica	JAM	standalone
Japan	JPN	developed
Jordan	JOR	frontier
Kazakhstan	KAZ	frontier
Kenya	KEN	frontier
Korea, Republic of	KOR	emerging
Kuwait	KWT	emerging
Latvia	LVA	frontier
Lebanon	LBN	standalone
L	·	

Country	EXCNTRY-Country Code	MSCI Categorization
Lithuania	LTU	frontier
Luxembourg	LUX	not rated
Malawi	MWI	not rated
Malaysia	MYS	emerging
Malta	MLT	standalone
Mauritius	MUS	frontier
Mexico	MEX	emerging
Morocco	MAR	frontier
Namibia	NAM	not rated
Netherlands	NLD	developed
New Zealand	NZL	developed
Nigeria	NGA	standalone
Norway	NOR	developed
Oman	OMN	frontier
Pakistan	PAK	frontier
Palestinian Territory, Occupied	PSE	standalone
Peru	PER	emerging
Philippines	PHL	emerging
Poland	POL	emerging
Portugal	PRT	developed
Qatar	QAT	emerging
Romania	ROU	frontier
Russian Federation	RUS	not rated
Saudi Arabia	SAU	emerging
Senegal	SEN	frontier
Serbia	SRB	frontier
Singapore	SGP	developed
Slovakia	SVK	not rated
Slovenia	SVN	frontier
South Africa	ZAF	emerging
Spain	ESP	developed
Sri Lanka	LKA	frontier
Sweden	SWE	developed
Switzerland	CHE	developed
Taiwan, Province of China	TWN	emerging
Tanzania, United Republic of	TZA	not rated
Thailand	THA	emerging
Trinidad and Tobago	TTO	standalone
Tunisia	TUN	frontier
Turkey	TUR	emerging
Uganda	UGA	not rated
Ukraine	UKR	standalone
United Arab Emirates	ARE	emerging
United Kingdom	GBR	developed
United States	USA	developed
Uruguay	URY	not rated
Venezuela, Bolivarian Republic of	VEN	not rated
Viet Nam	VNM	frontier
Zambia	ZMB	not rated

Country	EXCNTRY-Country Code	MSCI Categorization
Zimbabwe	ZWE	standalone

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