# In-Recitation Quiz (Cover Pset8)

Name:	Signature:
NetID:	RUID:

### **Quiz Instructions:**

- Indicate your answer in the box provided. Answers indicated elsewhere will not be graded and receive a **zero** grade, irrespective of the correctness.
- CREDIT is only given for CORRECT answers and NO PARTIAL CREDIT.
- Simplify your answer as much as possible.

### Problem 2.3.1 Grade:

Consider a binary code with 5 bits (0 or 1) in each code word. An example of a code word is 01010. In each code word, a bit is a zero with probability 0.8, independent of any other bit.

- 1. What is the probability of the code word 00111?
- 2. What is the probability that a code word contains exactly three ones?

# Problem 1.6.9 Grade:

In an experiment with *equiprobable outcomes*, the sample space is S = 1, 2, 3, 4 and  $P[s] = \frac{1}{4}$  for all  $s \in S$ . Find three events in S that are pairwise independent but are not independent.

#### Problem 2.3.3 Grade:

Suppose each day that you drive to work a traffic light that you encounter is either green with probability 7/16, red with probability 7/16, or yellow with probability 1/8, independent of the status of the light on any other day. If over the course of five days, G, Y, and R denote the number of times the light is found to be greed, yellow, or red, respectively. What is the probability that P[G=2,Y=1,R=2]? Also, what is the probability P[G=R]?

## Problem 2.2.3 Grade:

Your Starburst candy has 12 pieces, three pieces of each of four flavors: berry, lemon, orange, and cherry, arranged in a random order in the pack. You draw the first three pieces from the pack.

- 1. What is the probability they are all the same flavor?
- 2. What is the probability they are all different flavors?

ECE 14:332:226

**Problem 3.5.19** 

Grade:

Let  $X^{[n]}$  be the  $\mathsf{Binom}(n,p)$  discrete random variable with n trails and success rate p of each trail. That says  $X^{[n-1]}$  would be  $\mathsf{Binom}(n-1,p)$ . Prove that  $\mathbb{E}\big[X^{[n]}\big]=np$ . Hint:

- 1. Show that  $x\binom{n}{x} = n\binom{n-1}{x-1}$
- 2. Write down the PMF of Binom(n, p)
- 3. Use the Definition of  $\mathbb{E}\big[X^{[n]}\big]$
- 4. Use the property of PMF  $\sum_{x=0}^{n} P_{X^{[n]}}(x) = \sum_{x-1=0}^{n-1} P_{X^{[n-1]}}(x-1) = 1$

Problem 3.7.1

Grade:

Starting on day n=1, you buy one lottery ticket each day. Each ticket costs 1 dollar and is independently a winner that can be cashed for 5 dollars with probability 0.1; otherwise the ticket is worthless. Let  $X_n$  equal your **net profit** after **n** days. What is  $\mathbb{E}[X_n]$ ?

- 1. What is the PMF ( $\mathbb{P}(X)$ ) and the Expectation ( $\mathbb{E}[X]$ ) of **one day's** net profit?
- 2. What is the relationship between  $\mathbb{E}[X]$  and  $\mathbb{E}[X_n]$ ?

Problem 3.8.5

Grade:

Let X have the PMF

$$P_X(x) = \binom{4}{x} \left(\frac{1}{2}\right)^4.$$

Find  $\mathbb{P}(\mu_x - \sigma_x \leq X \leq \mu_X + \sigma_X)$ .

Hint (Hint is not question. Answering hint does not yield credit):

1. Which probability distribution does X follow?

Answers: