Strictness and Laziness

Laziness can be used to improve the efficiency and modularity of functional programs

Topics to Cover

- Strictness vs non-strictness
- Lazy lists
- Separating program description from evaluation

How to solve this problem?

Imagine if you had a deck of cards and you were asked to remove the odd-numbered cards and flip over all the queens.

Ideally, you'd make **a single pass** through the deck, looking for queens and odd numbered cards **at the same time**.

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Program trace for List

```
List(1,2,3,4).map(_ + 10).filter(_ % 2 == 0).map(_ * 3)

⇒'List(11,12,13,14).filter(_ % 2 == 0).map(_ * 3)

⇒'List(12,14).map(_ * 3)

=>'List(36,42)|

Wouldn't it be nice if we could somehow fuse sequences of transformations like this into a single pass and avoid creating temporary data structures?
```

Strict and Non-strict Functions

- A strict function always evaluates its arguments.
 - Strict functions are the norm in most programming languages including Scala.
- A non-strict function may choose <u>not</u> to evaluate one or more of its arguments.

Non-Strictness in Scala

Short-circuiting Boolean functions **&&** and **||** are non-strict. Another example of non-strictness is the **if-expression** in Scala:

```
val result = if a > b then f(a) else g(b)
```

[if-function is **strict in its condition parameter**, since it'll always evaluate the condition to determine which branch to take, and **non-strict in the two branches** for the true and false cases, since it'll only evaluate one or the other based on the condition.]

Thunk in FP

 A zero-argument anonymous function f: () => A that acts as an unevaluated form of argument expression to support the effect of call-by-name.

```
def if2[A](cond: Boolean, onTrue: () => A, onFalse: () => A): A =
   if cond then onTrue() else onFalse()

if2(a < 22,
     () => println("a"),
     () => println("b")
)
```

Call By Value vs. Call By Name

Call by Value

- Calculates all of the arguments before the call and then passes the resulting values to the function.
- Strict evaluation square(41.0 + 1.0) => square(42.0) square(sys.error("failure")) => Boom!

Call by Name

- The function receives the unevaluated argument expression and evaluate it if necessary.
- Lazy evaluation

By-Name Parameters in Scala

By-Name Parameters in Scala

An argument that's passed unevaluated to a function will be evaluated **once for each reference** in the function body.

Scala won't (by default) cache the result of evaluating an argument:

```
scala> def maybeTwice(b: Boolean, i: => Int) = if (b) i+i else 0
maybeTwice: (b: Boolean, i: => Int)Int

scala> val x = maybeTwice(true, { println("hi"); 1+41 })
hi
hi
x: Int = 84
```

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maybeTwice: (b: Boolean, i: => Int)Int

scala> val x = maybeTwice(true, { println("hi"); 1 + 41 })
hi
hi
x: Int = 84
```

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Lazy Val

Adding the **lazy** keyword to a **val** declaration will **delay** evaluation until it's first referenced. It will also **cache** the result to prevent repeated evaluation.

Formal definition of strictness

- If the evaluation of an expression runs forever or throws an error instead of returning a definite value, we say that the expression doesn't terminate, or that it evaluates to *bottom*.
- A function f is **strict** if the expression f(x) evaluates to bottom for all x that evaluate to bottom.

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LazyList

```
enum LazyList[+A]:
   case Empty
   case Cons(h: () => A, t: () => LazyList[A])
```

A nonempty stream consists of a head and a tail, which are both non-strict. Due to technical limitations, these are thunks that must be explicitly forced, rather than by-name parameters.

```
sealed trait Stream[+A]
case object Empty extends Stream[Nothing]
case class Cons[+A](h: () => A, t: () => Stream[A]) extends Stream[A]
```

LazyList Companion Object

```
object LazyList:
  // Smart constructors: cons and empty
  def cons[A](hd: => A, tl: => LazyList[A]): LazyList[A] =
    lazy val head = hd // memoize 
                                                     We cache the head
    lazv val tail = tl
                                                     and tail as lazy
    Cons(() => head, () => tail)
                                                     values to avoid
                                                     repeated evaluation.
  def empty[A]: LazyList[A] = Empty
  def apply[A](as: A*): LazyList[A] =
                                                     A convenient variable-argument
                                                     method for constructing a
    if as.isEmpty then empty
                                                     Stream from multiple elements.
    else cons(as.head, apply(as.tail*)) <</pre>
```

```
def headOption: Option[A] = this match
  case Empty => None
  case Cons(h, _) => Some(h())
Explicit forcing of the
  h thunk using h()
```

• This ability of LazyList to evaluate only the portion actually demanded (we don't evaluate the tail of the Cons) is useful.

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Memoizing & Avoiding Recomputation

• Smart constructors

- · Ensures some additional invariant or
- Provides a slightly different signature than the "real" constructors used for pattern matching.
- By convention, smart constructors typically lowercase the first letter of the corresponding data constructor.

```
def cons[A](hd: => A, tl: => LazyList[A]): LazyList[A] = {
    lazy val head = hd
    lazy val tail = tl
    Cons(() => head, () => tail)
}
cons smart constructor takes care
of memoizing the by-name
arguments for the head and tail of
the Cons.
```

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Avoiding Recomputation

 If we use Cons directly, this code will actually compute expensive(x) twice.

```
val x = Cons(() => expensive(y), tl)
val h1 = x.headOption
val h2 = x.headOption
```

```
def headOption: Option[A] = this match
  case Empty => None
  case Cons(h, _) => Some(h())
```

The empty smart constructor just returns Empty, but annotates
 Empty as a LazyList[A].

```
def empty[A]: LazyList[A] = Empty
```

 Scala takes care of wrapping the arguments to cons in thunks, so the as.head and apply(as.tail*) expressions won't be evaluated until we force the LazyList.

```
def apply[A](as: A*): LazyList[A] = {
  if (as.isEmpty) then Empty
  else cons(as.head, apply(as.tail*))
}
Beware that `as` itself is strict!
```

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Implement a helper Function and some useful functions to inspect the LazyList

```
// Convert LazyList to List
def toList: List[A]
// Take the first n elements of a LazyList
def take(n: Int): LazyList[A]
// Skip the first n elements of a LazyList
def drop(n: Int): LazyList[A]
// Take the first elms of a LazyList that match the given predicate
def takeWhile(p: A => Boolean): LazyList[A]
// Skip the first elms of a LazyList that match the given predicate
def dropWhile(p: A => Boolean): LazyList[A]
```

Separating Program Description from Evaluation

Separation of concerns: to separate the description of computations from actually running them.

Laziness lets us separate the description of an expression from the evaluation of that expression.

→ Can describe a "larger" expression, and then evaluate only a portion of it.

```
def exists(p: A => Boolean): Boolean = this match
  case Cons(h, t) => p(h()) || t().exists(p)
  case _ => false
```

Remember also that the tail of the lazy list is a lazy val. So not only does the traversal terminate early, the tail of the lazy list is never evaluated at all!

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Lazy foldRight for LazyLists

```
If f doesn't
              def foldRight[B](z: \Rightarrow B)(f: (A, \Rightarrow B) \Rightarrow B): B =
                                                                                  The arrow => in front
evaluate its
                                                                                  of the argument type B
                 this match
second
                                                                                  means that the
                   case Cons(h, t) => f(h(), t().foldRight(z)(f))
argument,
                                                                                  function f takes its
the recursion
                   case Empty => z
                                                                                  second argument by
                                                                                  name and may choose
never occurs.
                                                                                  not to evaluate it.
```

We can see this by using **foldRight** to implement exists:

```
def exists(p: A => Boolean): Boolean =
  foldRight(false)((a, b) => p(a) | b)
```

Exercises

• [Exercise 5.4] Implement forAll, which checks that all elements in the LazyList match a given predicate. Your implementation should terminate the traversal as soon as it encounters a nonmatching value.

```
def forAll(p: A => Boolean): Boolean = ???
```

- [Exercise 5.5] Use foldRight to implement takeWhile.
- [Exercise 5.6] Implement headOption using foldRight.
- [Exercise 5.7] Implement map, filter, append, and flatMap using foldRight. The append method should be non-strict in its argument.

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Program Trace for LazyList

```
Apply map
             LazyList(1,2,3,4).map(_+ 10).filter(_- % 2 == 0).toList
                                                                                              to the first
  Apply
                                                                                              element.
  filter to
             cons(11, LazyList(2,3,4).map(_ + 10)).filter(_ % 2 == 0).toList
  the first
                                                                                          Apply map to
  element.
             LazyList(2,3,4).map(_ + 10).filter(_ % 2 == 0).toList
                                                                                          the second
                                                                                          element.
             cons(12, LazyList(3,4).map(_ + 10)).filter(_ % 2 == 0).toList
Apply
             12 :: LazyList(3,4).map(_ + 10).filter(_ % 2 == 0).toList
filter to
                                                                                           Apply
the second
             12 :: cons(13, LazyList(4).map(_ + 10)).filter(_ % 2 ==
                                                                                           filter to
element.
                                                                                           the fourth
Produce the
             0).toList
                                                                                           element and
first element of
                                                                                           produce the
the result.
             12 :: LazyList(4).map( + 10).filter( % 2 == 0).toList
                                                                                           final element
                                                                                           of the result.
             12 :: cons(14, LazyList().map( + 10)).filter( % 2 == 0).toList
             12 :: 14 :: LazyLis' 	
                                             map and filter have no more work to do,
                                             and the empty stream becomes the empty list.
             12 :: 14 :: List()
```

What We Observed - Incremental nature of lazy list transformations

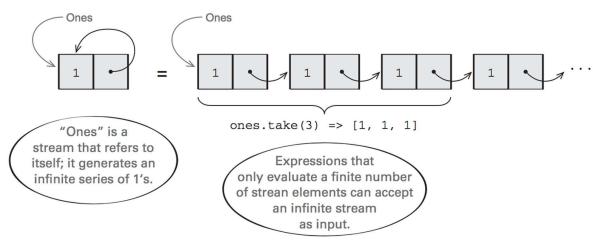
- The thing to notice in this trace is how the filter and map transformations are interleaved.
- Note that we don't fully instantiate the intermediate lazy list that results from the map.
- Since intermediate lazy lists aren't instantiated, it's easy to reuse existing operations in novel ways without having to worry about needless processing.

```
def find(p: A => Boolean): Option[A] =
  filter(p).headOption
```

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Infinite LazyLists

val ones: LazyList[Int] = LazyList.cons(1, ones)



Many functions can be evaluated using finite resources even if their inputs generate infinite sequences.

```
val ones: LazyList[Int] = LazyList.cons(1, ones)
```

Although ones is infinite, the functions we've written so far only inspect the portion of the stream needed to generate the demanded output. For example:

```
scala> ones.take(5).toList
res0: List[Int] = List(1, 1, 1, 1, 1)
scala> ones.exists(_ % 2 != 0)
res1: Boolean = true
```

Try playing with a few other examples:

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Exercises

• [Exercise 5.8] Generalize ones slightly to the function continually, which returns an infinite LazyList of a given value.

```
def continually[A](a: A): LazyList[A]
```

• [Exercise 5.9] Write a function that generates an infinite lazy list of integers, starting from n, then n + 1, n + 2, and so on.

```
def from(n: Int): LazyList[Int]
```

• [Exercise 5.10] Write a function fibs that generates the infinite lazy list of Fibonacci numbers: 0, 1, 1, 2, 3, 5, 8, and so on.

[Exercise 5.11] Unfold: Corecursive Function

- A *corecursive function* produces data and need not terminate so long as they remain productive.
- The unfold is a very general LazyList-building function.
- unfold takes an initial state, and a function for producing both the next state and the next value.

```
def unfold[A,S](state: S)(f: S => Option[(A,S)]): LazyList[A]
```

Option is used to indicate when the LazyList should be terminated,
if at all.

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More Exercises

- [Exercise 5.12] Write fibs, from, continually, and ones in terms of unfold.
- [Exercise 5.13] Use unfold to implement map, take, takeWhile, zipWith (as in chapter 3), and zipAll. The zipAll function should continue the traversal as long as either lazy list has more elements—it uses Option to indicate whether each lazy list has been exhausted.

```
def zipAll[B](that: LazyList[B]): LazyList[(Option[A], Option[B])]
```

Visit "hasSequence" again

• Implement has Sequence in terms of starts with and tails:

```
def hasSubsequence[A](l: LazyList[A]): Boolean =
    tails.exists(_.startsWith(l))

def startsWith[A](prefix: LazyList[A]): Boolean = ???

def tails: LazyList[LazyList[A]] = ???

// LazyList(1, 2, 3).tails = LazyList(LazyList(1, 2, 3), LazyList(2, 3), LazyList(3), LazyList())
```

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