

# ***Pattern Recognition & Machine Learning***

## **Lab-4 :- “Boosting & Bayes Classification”**

### **Objectives**

Following were the portion-wise objectives of the whole Lab-4 :-

1. Take Decision Tree as base-learner/ weak learner and prepare AdaBoost Classifier Models with different numbers of Trees. Compare their performance in respect to Iris Dataset and perform other relevant tasks too.
2. With the help of Iris Dataset again, perform Naive Bayes Classification, use Logarithmic Discriminant Function to compute accuracy and calculate Bayes Risk associated with the Classification Process. Perform other relevant tasks too.
3. Plot different Graphs for different Probabilities and Visualise the insights of Bayes Classification through Prior, Likelihood, Evidence and calculate Posterior Probabilities for 3 different Datasets, with different number of features and classes accordingly.

### **Datasets**

The following were the Datasets, used to fulfill the requirements of Lab-4 :-

1. Iris Dataset :- [dataset](#) (50 Samples of 3 different Iris Species (Total 150 Samples))
2. Car Dataset :- [DATASET 1](#) (If Cost > 550, Label 1 otherwise Label 0)
3. “C1 and C2” Dataset :- [c1](#) and [c2](#)

# Dependencies

Following were the Dependencies in order to fulfill the requirements of Lab-4 :-

1. Numpy
2. Pandas
3. Sklearn
4. Seaborn
5. Matplotlib
6. Scipy

## Preprocessing Methods

In the Scenario of Iris Dataset :-

1. Ordinal Encoder was used, which assigns the float value of a Categorical String-Type Label, according to its relative Alphabetical Order. Resultant Encodings were {"Iris-Setosa" : 0.0 , "Iris-Versicolor" : 1.0 , "Iris-Virginica" : 2.0}
2. For Visualisation and Posterior Probability Calculation purposes, the Continuous Features were given Quantile Ranges with their corresponding labels and converted to Discrete Values using pd.cut, as follows :-

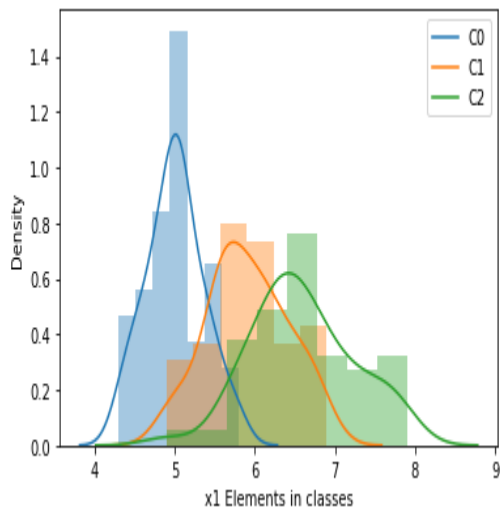
| Labels | Sepal Length (cm) | Sepal Width (cm) | Petal Length (cm) | Petal Width (cm) |
|--------|-------------------|------------------|-------------------|------------------|
| 1      | [4.3,4.9)         | [2.0,2.4)        | [1.0,1.983)       | [0.1,0.5)        |
| 2      | [4.9,5.5)         | [2.4,2.8)        | [1.983,2.967)     | [0.5,0.9)        |
| 3      | [5.5,6.1)         | [2.8,3.2)        | [2.967,3.95)      | [0.9,1.3)        |
| 4      | [6.1,6.7)         | [3.2,3.6)        | [3.95,4.933)      | [1.3,1.7)        |
| 5      | [6.7,7.3)         | [3.6,4.0)        | [4.933,5.917)     | [1.7,2.1)        |
| 6      | [7.3,7.904)       | [4.0,4.402)      | [5.917,6.906)     | [2.1,2.502)      |

Note :-

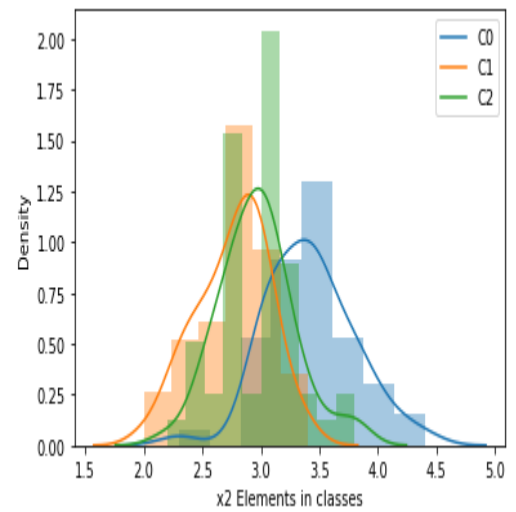
Ordinal Encoder was from "Sklearn" Dependency , whereas Cut from "Pandas" Dependency.

3. Class-Wise Continuous Histogram Plots for each Feature, were as follows :-

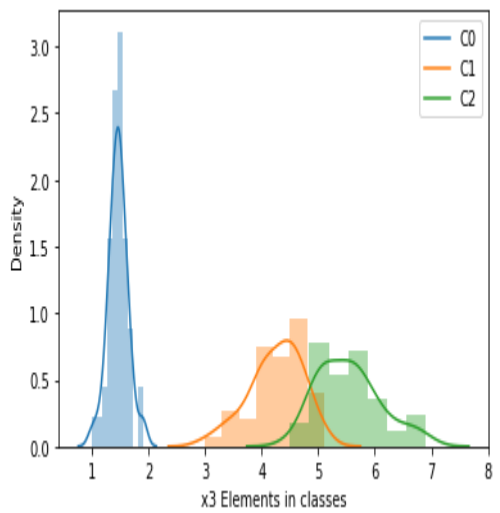
X1 Feature Histogram Plot



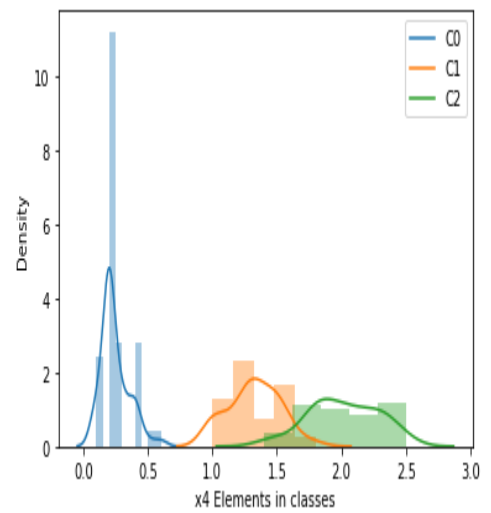
X2 Feature Histogram Plot



X3 Feature Histogram Plot

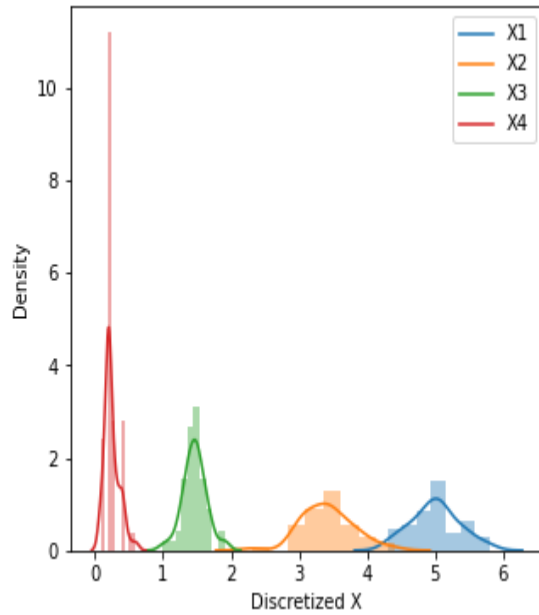


X4 Feature Histogram Plot

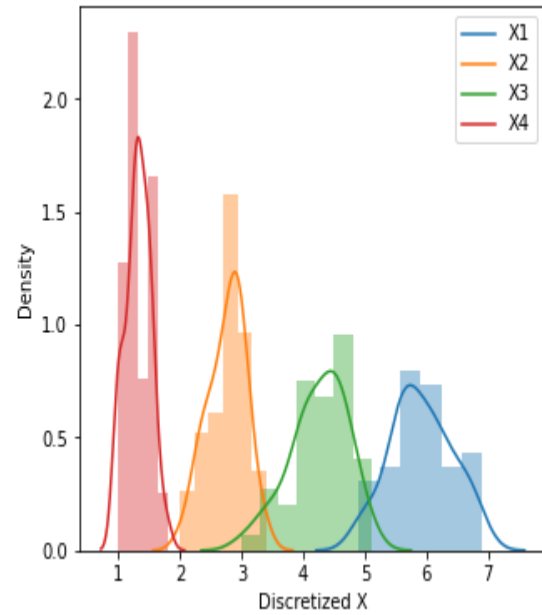


4. Feature-Wise Continuous Histogram Plots for each class, were as follows :-

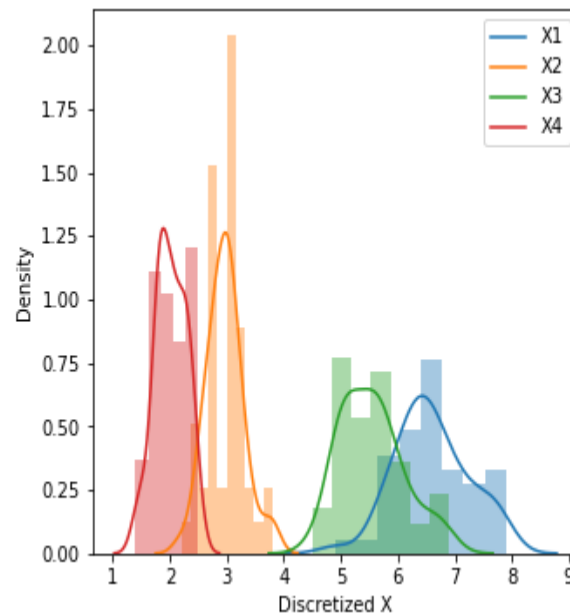
Class-0 Histogram Plot



Class-1 Histogram Plot

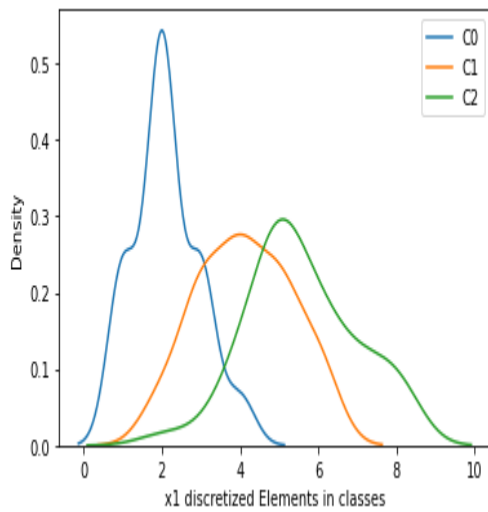


Class-2 Histogram Plot

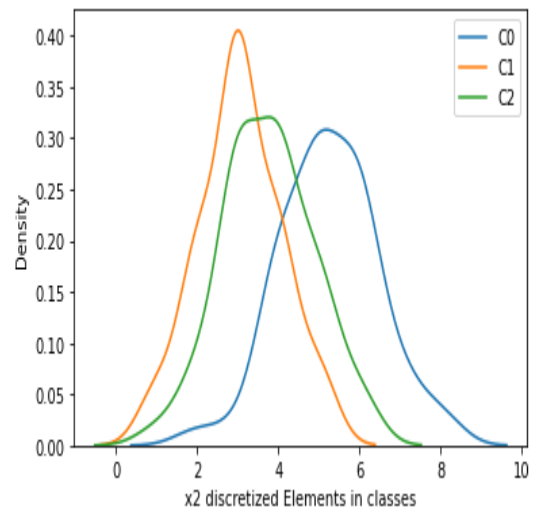


5. Class-Wise Discrete Histogram Plots for each Feature, were as follows :-

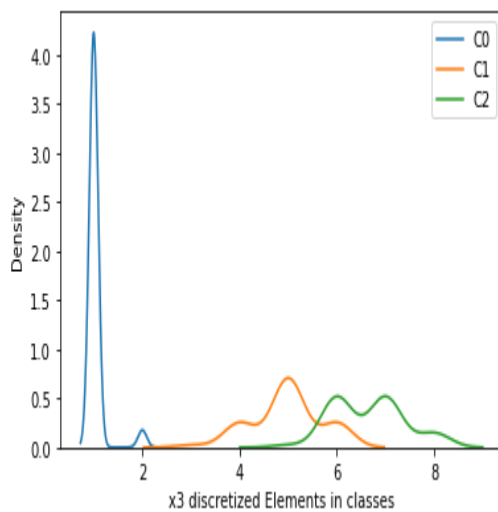
X1 Feature Histogram Plot



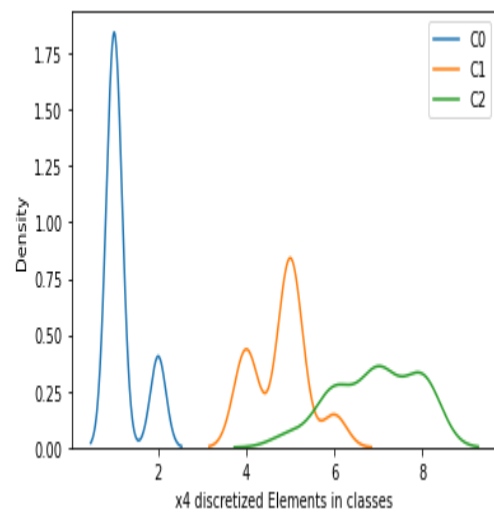
X2 Feature Histogram Plot



X3 Feature Histogram Plot



X4 Feature Histogram Plot



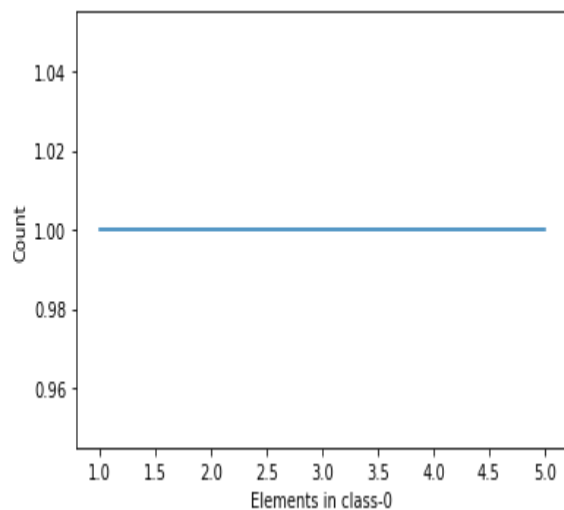
In the Scenario of Car Dataset :-

1. If Cost > 550, label was assigned as 1, otherwise 0.
2. Unique Discrete Values of Height were found out alongside their counts, as follows :-

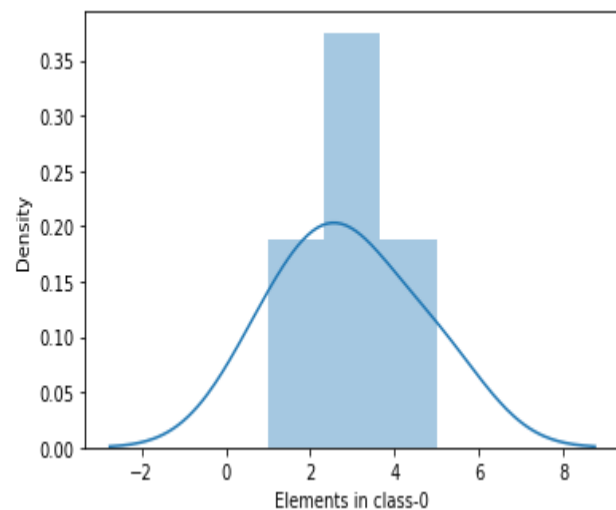
| Height | Class "0" Count | Class "1" Count |
|--------|-----------------|-----------------|
| 1      | 1               | 5               |
| 1.5    | 0               | 5               |
| 2      | 0               | 4               |
| 2.5    | 1               | 2               |
| 3      | 1               | 6               |
| 4      | 0               | 1               |
| 5      | 1               | 0               |

3. Count and Density Visualisation Plots for Class-0 and Class-1 were as follows :-

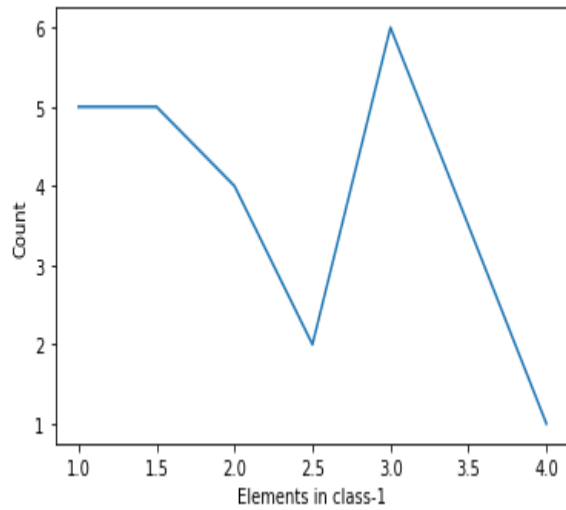
Count Plot for Class-0



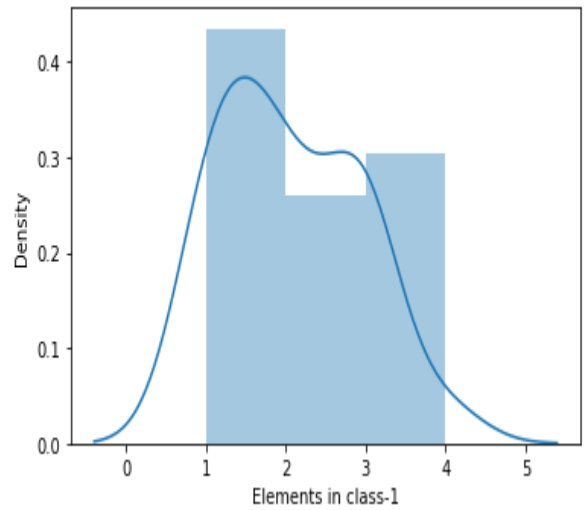
Density Plot for Class-0



Count Plot for Class-1



Density Plot for Class-1



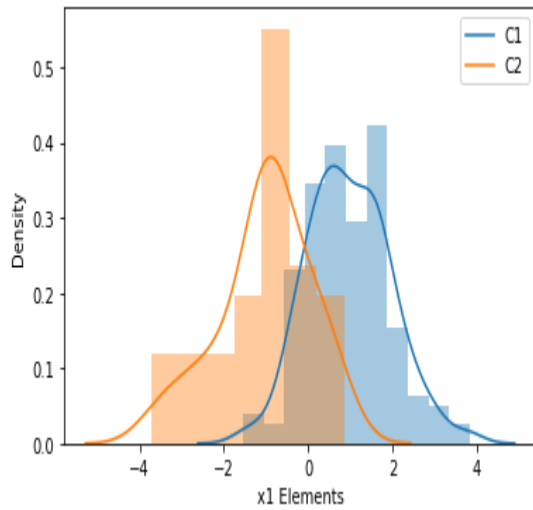
In the Scenario of “c1 and c2” Dataset :-

1. Different Datasets were already provided with their corresponding Feature Values, according to c1 and c2 classes.

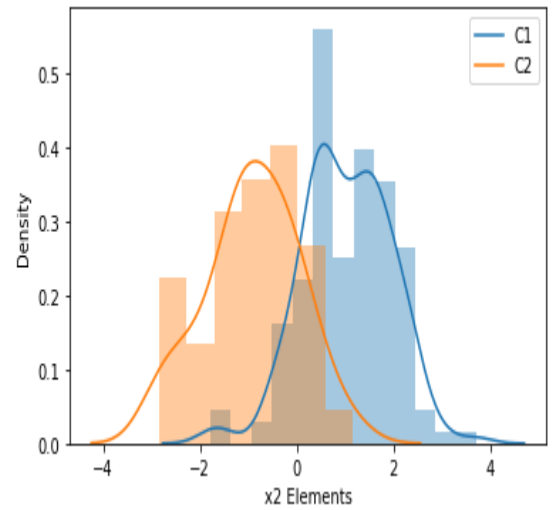
| Label | X1 Feature Range | X2 Feature Range |
|-------|------------------|------------------|
| 1     | [-3.702,-2.76)   | [-2.846,-2.026)  |
| 2     | [-2.76,-1.818)   | [-2.026,-1.205)  |
| 3     | [-1.818,-0.876)  | [-1.205,-0.384)  |
| 4     | [-0.876,0.0659)  | [-0.384,0.437)   |
| 5     | [0.0659,1.008)   | [0.437,1.258)    |
| 6     | [1.008,1.95)     | [1.258,2.079)    |
| 7     | [1.95,2.892)     | [2.079,2.899)    |
| 8     | [2.892,3.842)    | [2.899,3.727)    |

2. Class-Wise Continuous Histogram Plots for x1 and x2 elements, were as follows :-

Histogram Plot wrt. X1 elements

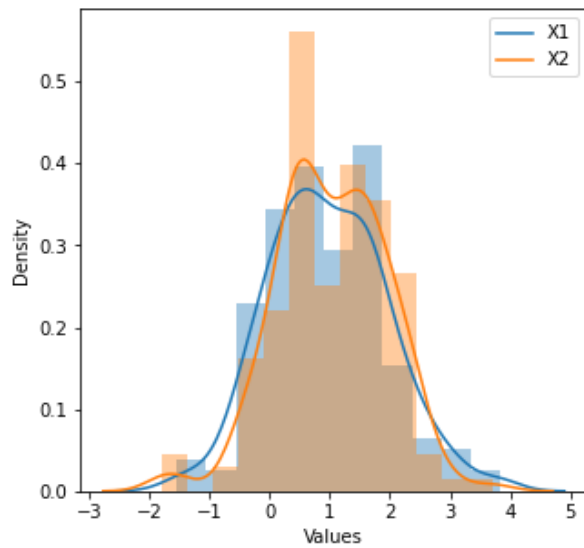


Histogram Plot wrt. X2 elements

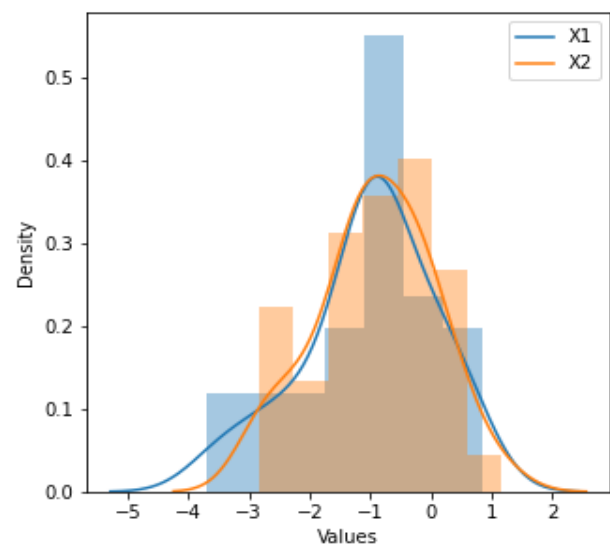


3. Feature-Wise Continuous Histogram Plots for c1 and c2 classes, were as follows :-

Histogram Plot wrt. C1 classes

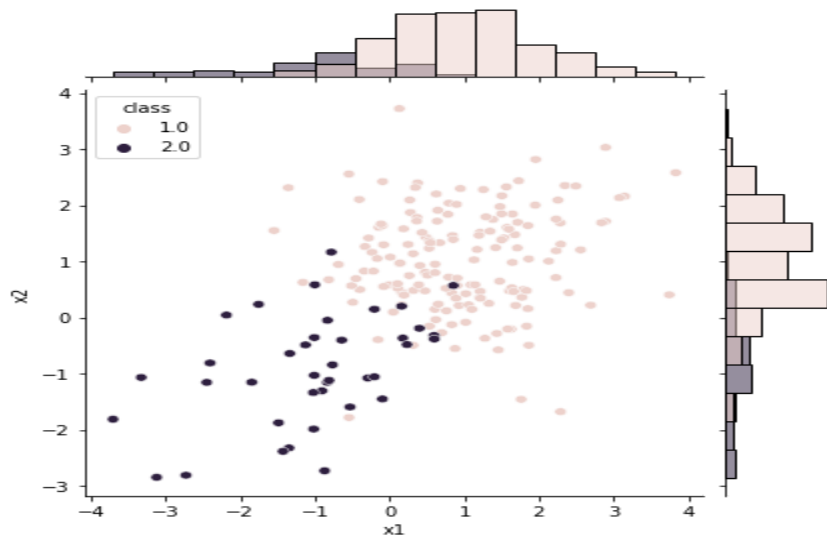


Histogram Plot wrt. C2 classes

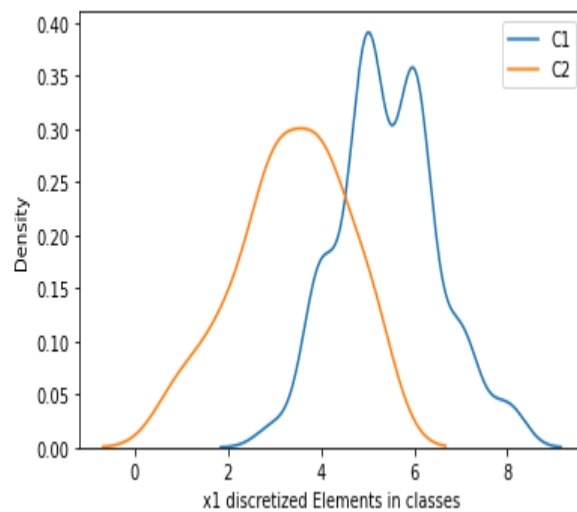
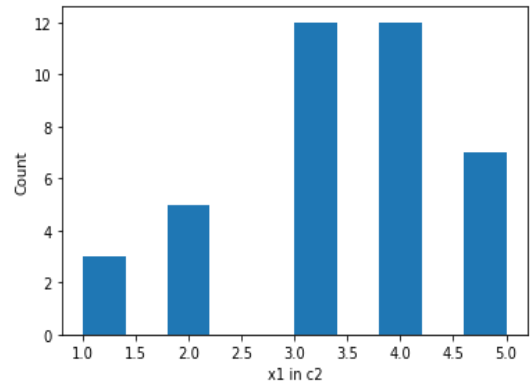
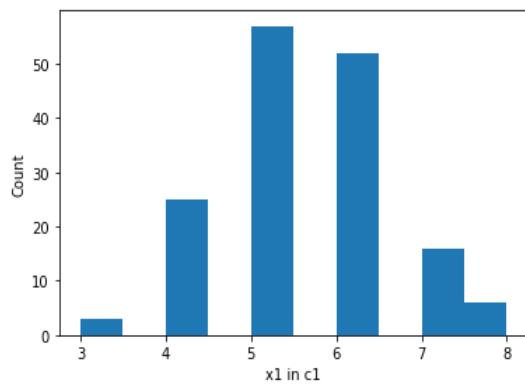


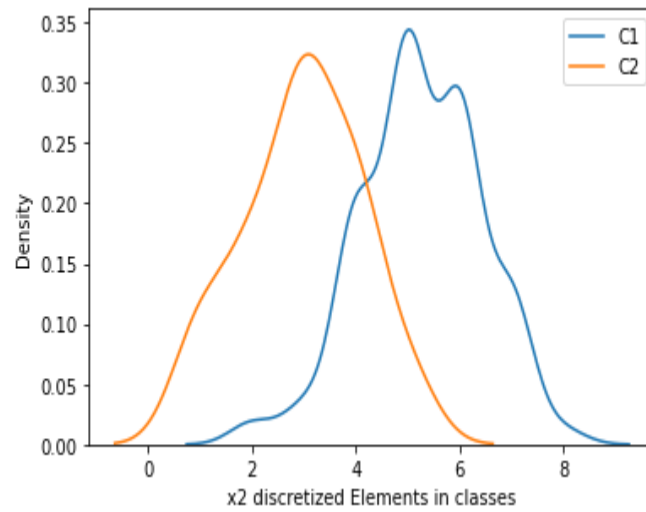
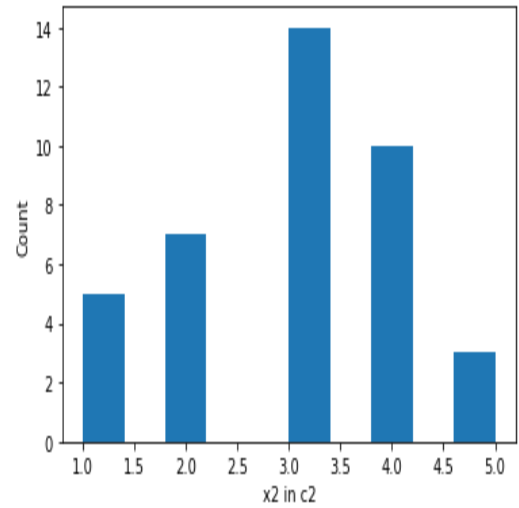
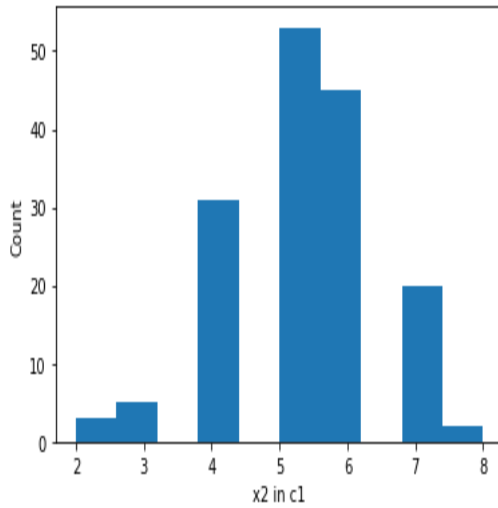


4. Joint Scatter and Histogram Plot for “C1 and C2 Dataset”, was as follows :-



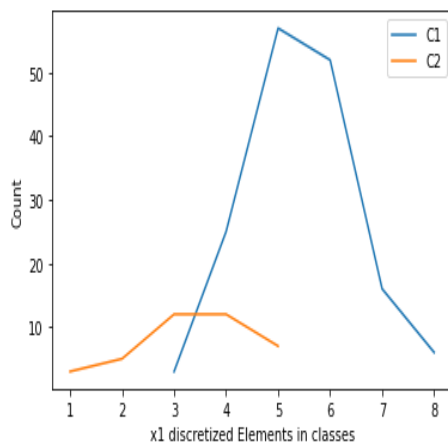
5. Discrete Histogram Plots and Line Plots for Class-wise Feature distribution, were as follows :-



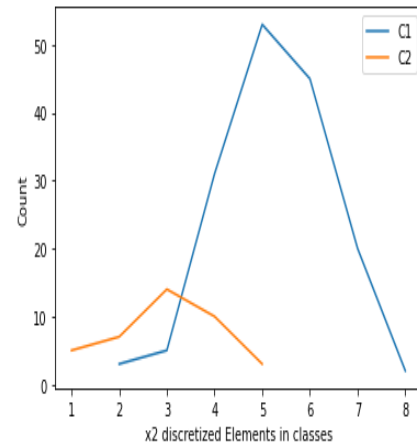


6. Class-Wise Line Plots for Unique Discrete Labels of each Feature, were as follows :-

Class-Wise X1 Line Plot



Class-Wise X2 Line Plot

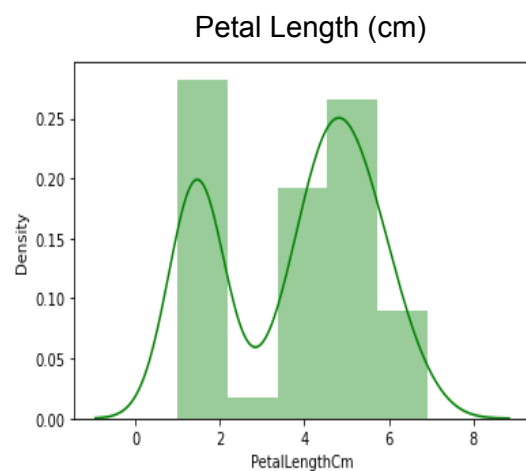
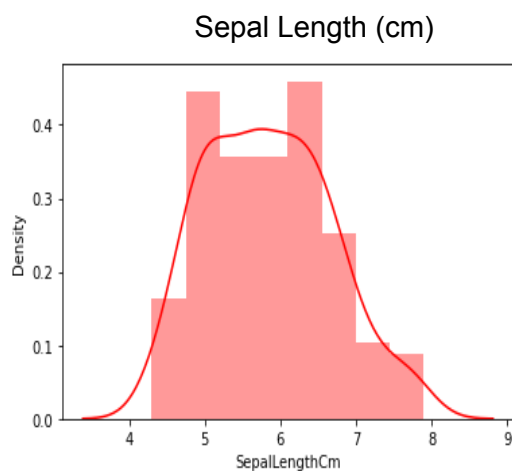
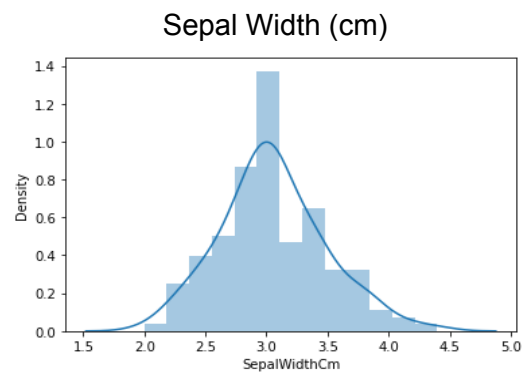
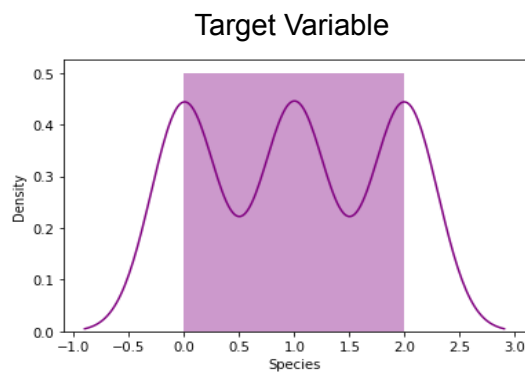


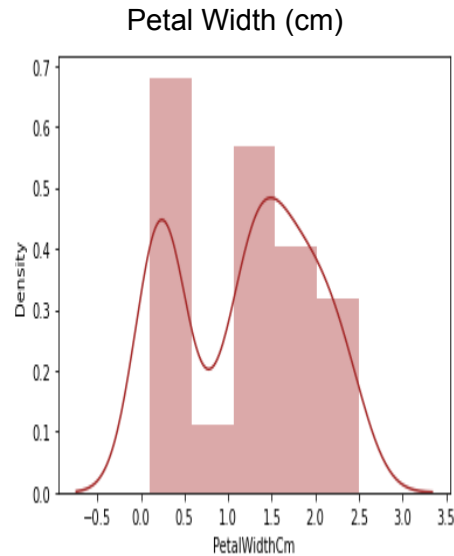
# *Boosting with Decision Tree*

## Procedures

1. Visualize the Target Variable and distribution of each sample for each Feature amongst 4 features.
2. Choose Decision Tree as Weak Learner, tune its parameter and train the boosting classification model, using it.
3. Prepare AdaBoost Model with Decision Tree as Weak Learner, vary its parameters and compare their performance.

## Visualisations





## Stratified K-Fold Split

Unlike the classic method of Train\_Test\_Split where we divide the Training and Test portions according to mentioned split ratio and random state parameter, Stratified K-Fold Split allows the user to prevent Biasness of Multi-Class Dataset, as it constitute one more parameter, i.e number of different Folds/Combinations for train-test splits. The Model/Estimator having this type of Training-Test Split, have more varieties/options to try randomized input, which will lead to lesser Biasness towards a particular Input Class, amongst other classes.

## Decision Tree as Weak Learner

After using Stratified K-Fold Split, the Training Data portion was used for Decision Tree with Max Depth = 2. Following, were some details, obtained from Weak Learner, as follows :-

1. Cross-Validation Scores - [0.91667 , 0.95833 , 0.95833 , 0.95833 , 0.91667]
2. Mean Score - 0.94166
3. Standard Deviation of Scores - 0.02041
4. Variance of Scores - 0.00041
5. Test Accuracy - 96.66667 %

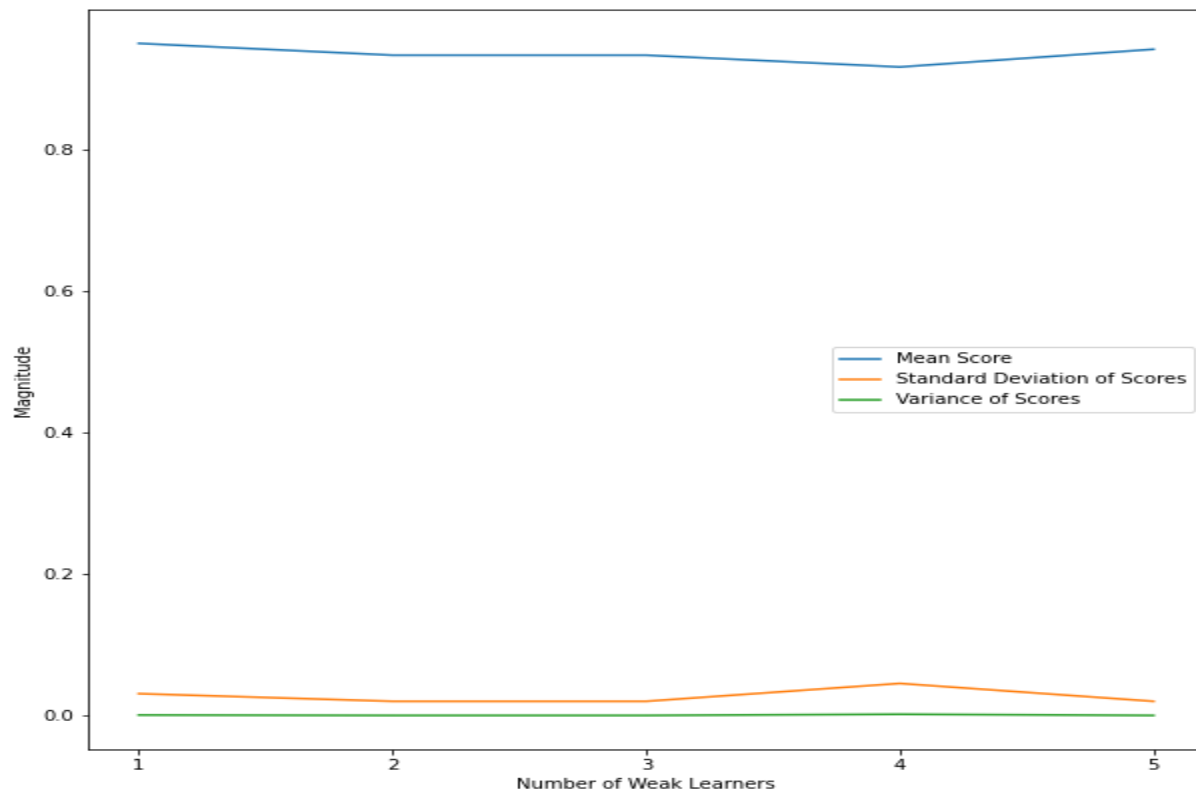
# AdaBoost with Varying Number of Trees

Adaboost with Number of Trees (Weak Learners) from 1 to 5, were made and details were drawn out as follows :-

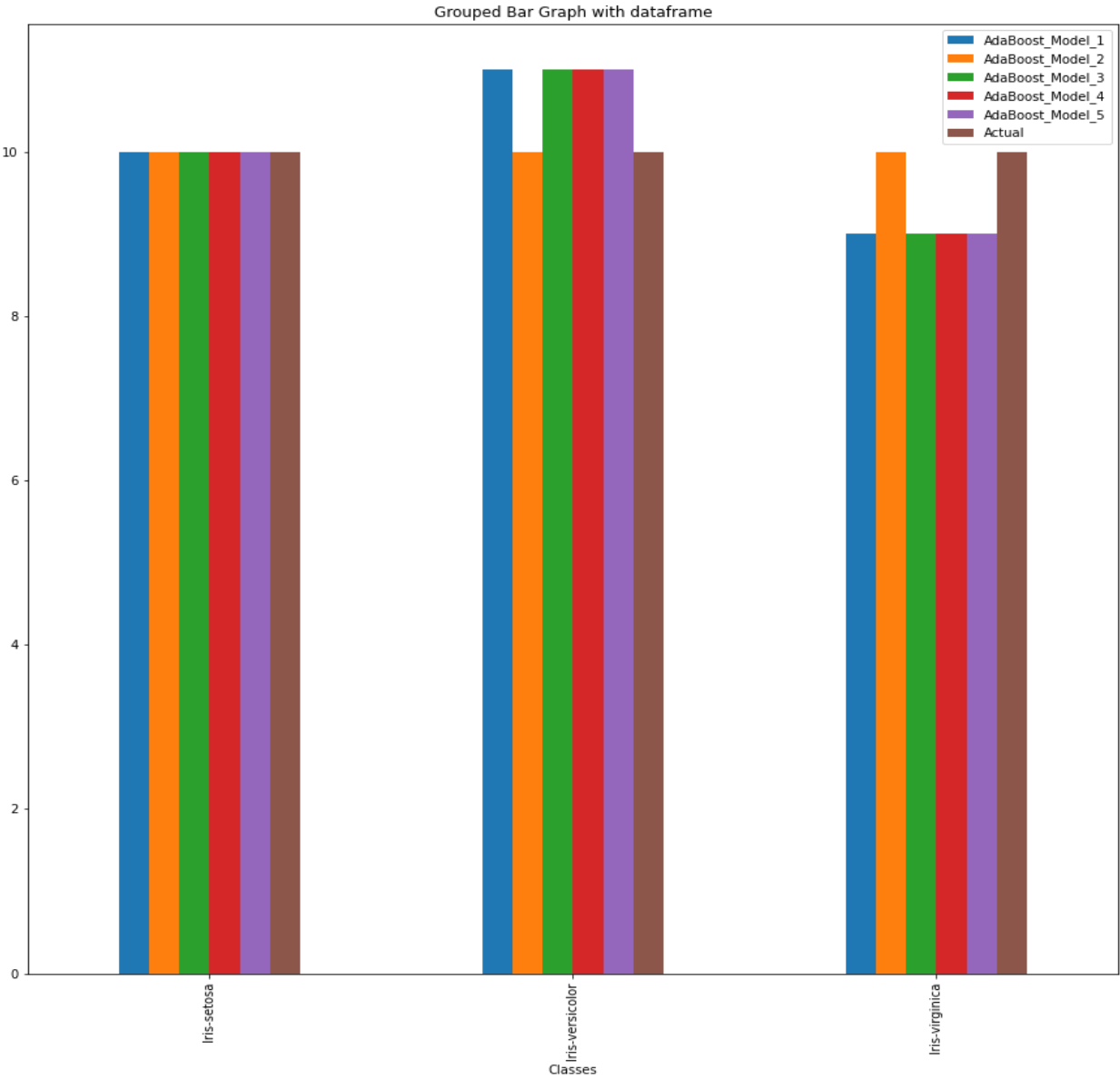
| No.of Trees | Mean CV Scores | Std. of CV Scores | Var. of CV Scores | Test Accuracy |
|-------------|----------------|-------------------|-------------------|---------------|
| 1           | 0.95           | 0.0311            | 0.0009            | 96.667%       |
| 2           | 0.9333         | 0.0204            | 0.0004            | 100%          |
| 3           | 0.9333         | 0.0204            | 0.0004            | 96.667%       |
| 4           | 0.9166         | 0.0456            | 0.0002            | 96.667%       |
| 5           | 0.9416         | 0.0204            | 0.0004            | 96.667%       |

To make things more simple, some of the useful plots , were as follows :-

Line Plot for Cross-Validation Score Analysis of each Adaboost Model



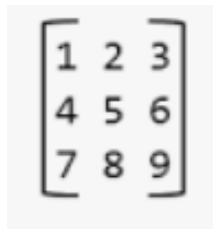
Class-Wise Grouped Bar Plots for Prediction analysis of each model, in respect to Actual



# *Bayes Classification*

## **Procedures**

1. Estimate the accuracy of different Naive Bayes algorithms, use 5-fold cross validation on the data set and plot the ROC AUC curve for different values of parameters.
2. Use a linear discriminant function to calculate the accuracy on the classification task with 80% training and 20% testing data split.
3. Calculate the Bayes risk, corresponding to each Naive Bayes Algorithm.



Given:  $\lambda =$

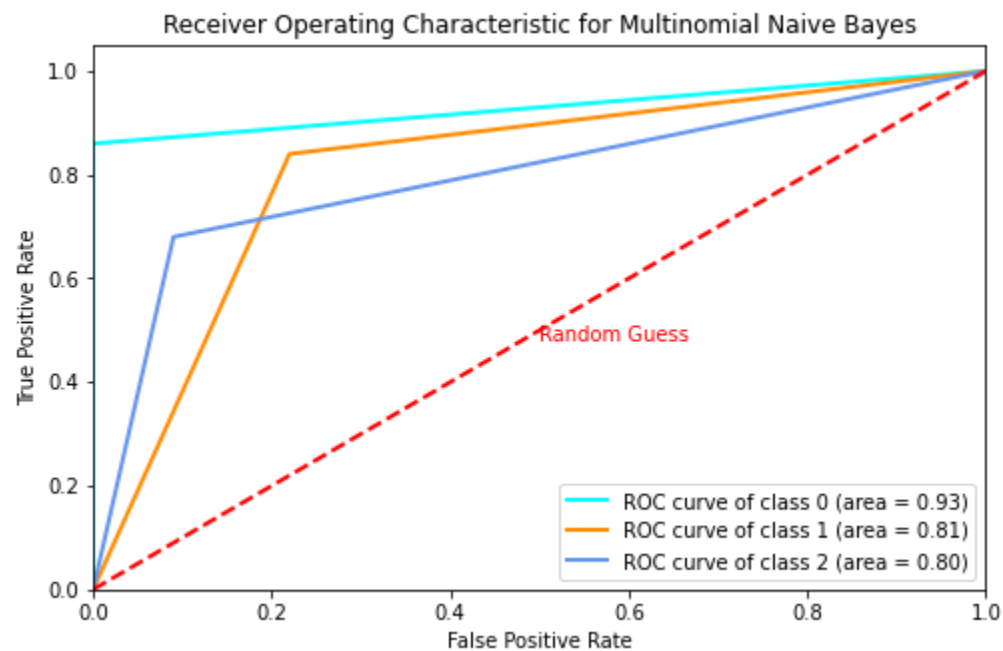
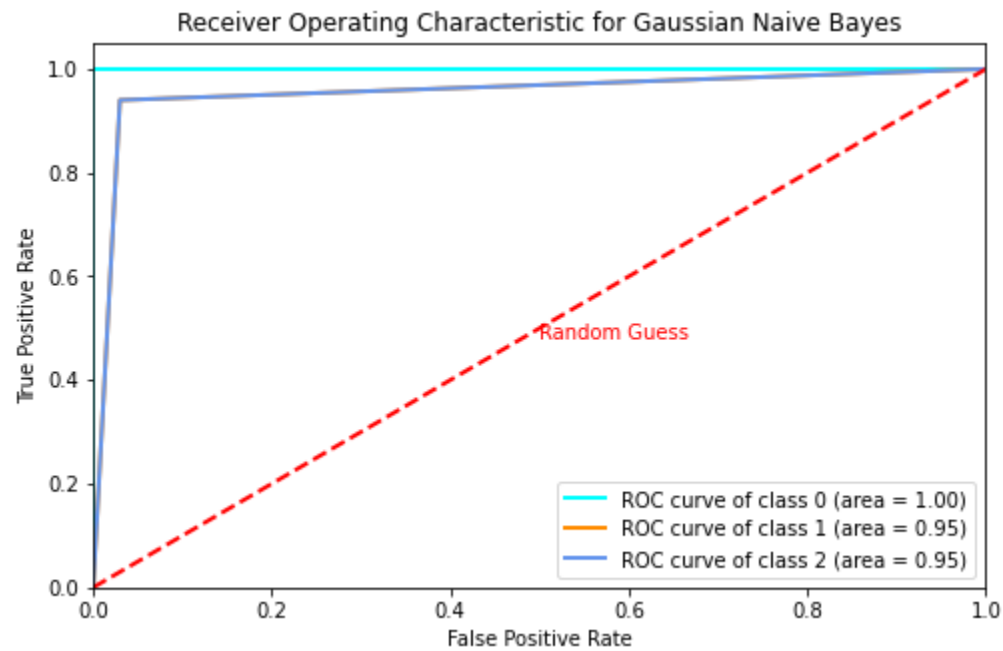
## **Different Naive Bayes Algorithms**

4 Different kinds of Naive Bayes Algorithms were used, as following :-

1. Gaussian Naive Bayes
2. Multinomial Naive Bayes
3. Complement Naive Bayes
4. Bernoulli Naive Bayes

Also, for accuracy check on Classification Task, Logarithmic Discriminant Function was used with 8:2 split ratio for training-test data points.

ROC-AUC Curves for Multinomial and Gaussian Naive Bayes Models, were as follows :-

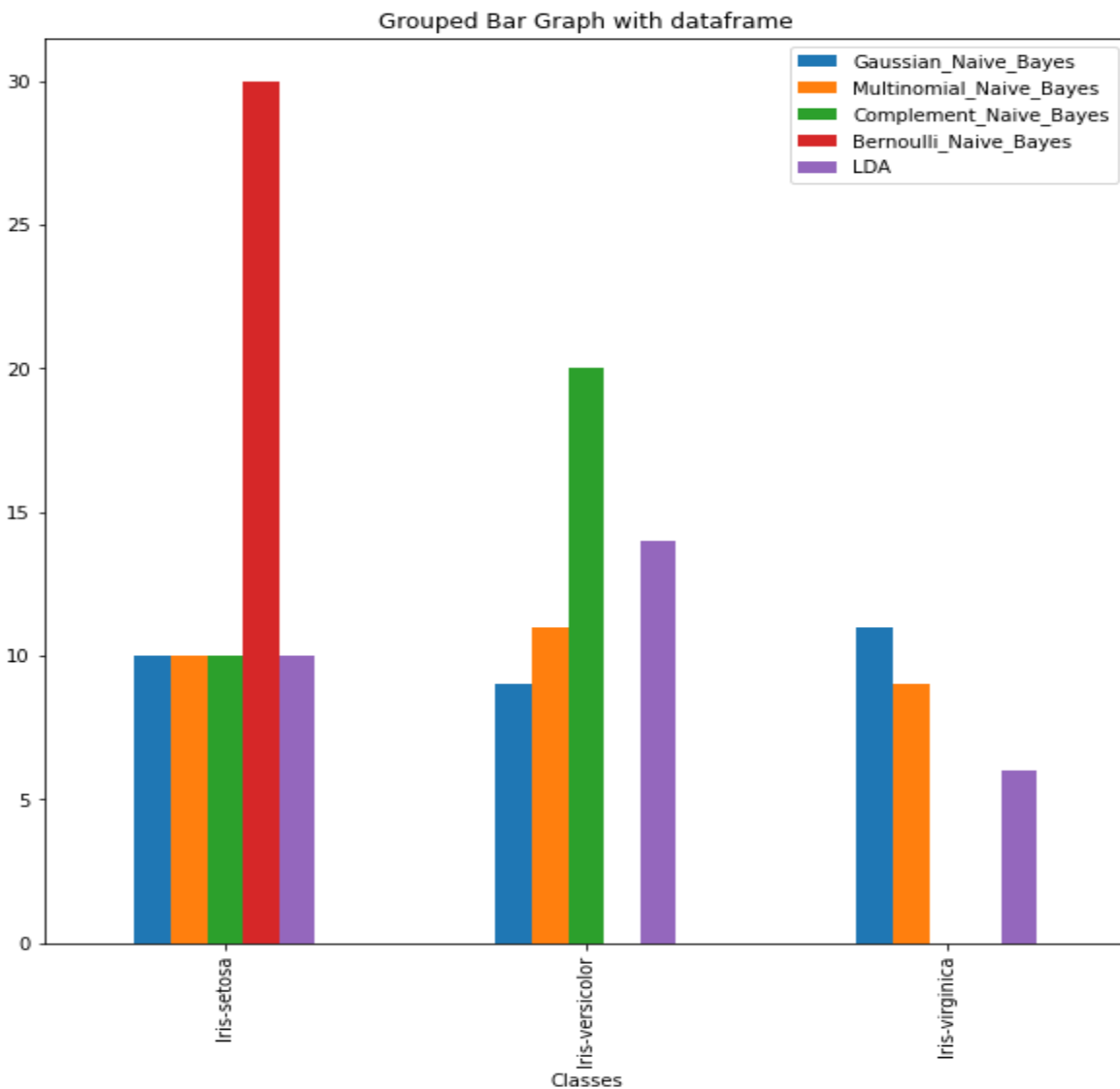


Some of the Details regarding these Algorithms were drawn, as follows :-



| Naive_Bayes Model | Mean CV score | Std. of CV scores | Var. of CV scores | Test Accuracy |
|-------------------|---------------|-------------------|-------------------|---------------|
| Gaussian          | 0.95          | 0.0485            | 0.0023            | 96.667%       |
| Multinomial       | 0.95833       | 0.0456            | 0.0020            | 96.667%       |
| Complement        | 0.66667       | 0                 | 0                 | 66.667%       |
| Bernoulli         | 0.33334       | 0                 | 0                 | 33.334%       |
| LDA               | 0.96668       | 0.0311            | 0.0009            | 100%          |

Grouped Bar Plots for Predictions according to Classes and Models , were as follows :-



# Bayes Risk

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

Given:  $\lambda =$

Bayes Risk for a particular Discrete Point  $\mathbf{x}$  is as follows :-

$$R(\alpha_i|\mathbf{x}) = \sum_{j=1}^c \lambda(\alpha_i|\omega_j) P(\omega_j|\mathbf{x})$$

In this Lab-4, Train-Test Split ratio was 8:2, which led to 30 Dataset Samples in Test Portion. Just for Comparison, another Lambda Matrix was taken from Zero-One Loss Method, where Diagonal Elements becomes 0 and other elements remain 1. Total Bayes Risk Values for Whole Test Samples, were drawn as follows :-

| Naive_Bayes Models | Zero-One Loss Method | Custom Lambda Matrix |
|--------------------|----------------------|----------------------|
| Gaussian           | 59.9999              | 451.6251             |
| Multinomial        | 59.9999              | 457.7253             |
| Complement         | 60.0000              | 448.4974             |
| Bernoulli          | 60                   | 450                  |
| LDA                | 60                   | 438.0873             |

# Bayes Visualisations

Formula for calculating Posterior Probabilities, as follows :-

$$\text{posterior} = \frac{\text{likelihood} \times \text{prior}}{\text{evidence}}.$$

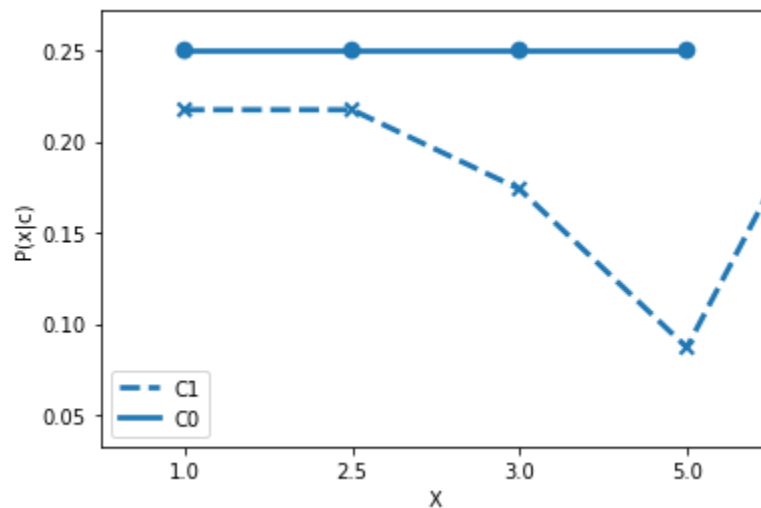
Where :-

Likelihood is  $P(X | \omega_i)$ , Prior is  $P(\omega_i)$  and Evidence is as follows :-

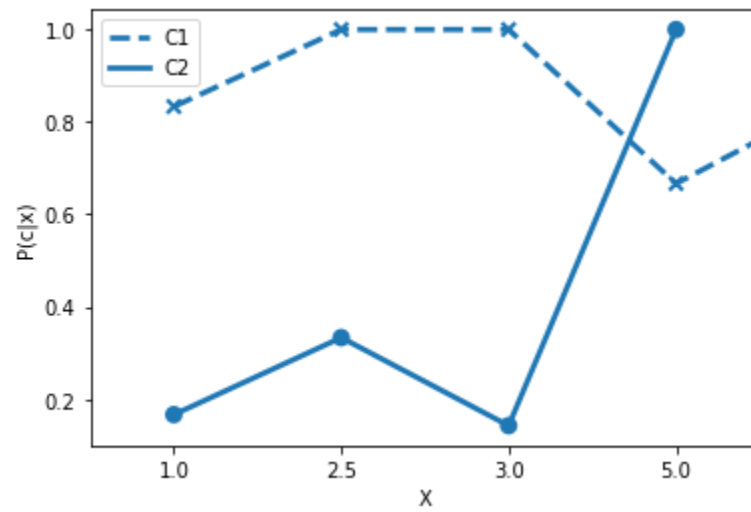
$$p(\mathbf{x}) = \sum_{j=1}^c p(\mathbf{x}|\omega_j)P(\omega_j).$$

In the scenario of Car-Dataset :-

## 1. Likelihood Plot -

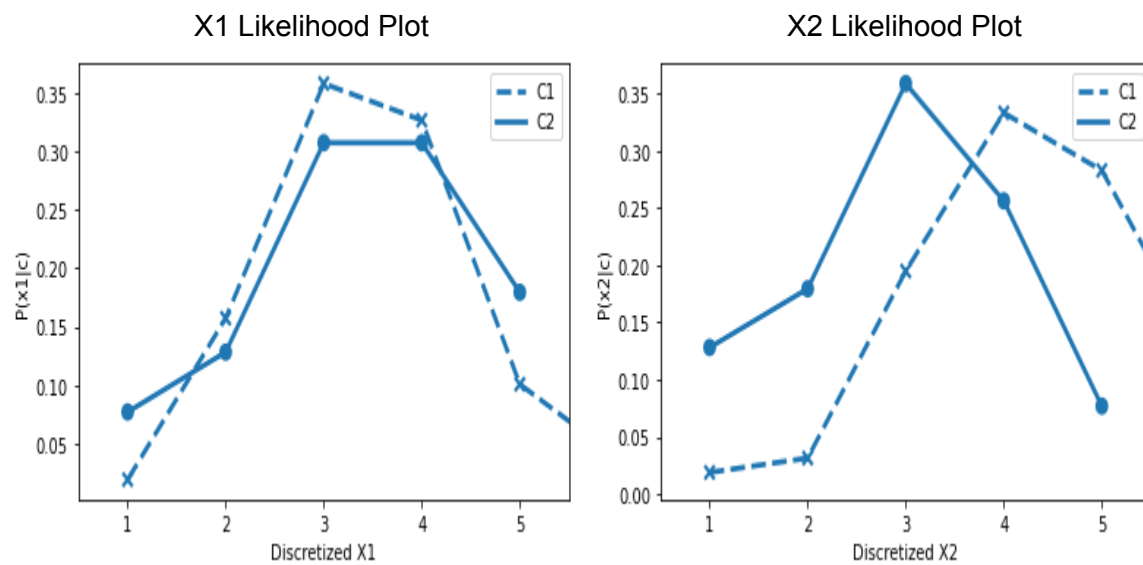


## 2. Posterior Plot -

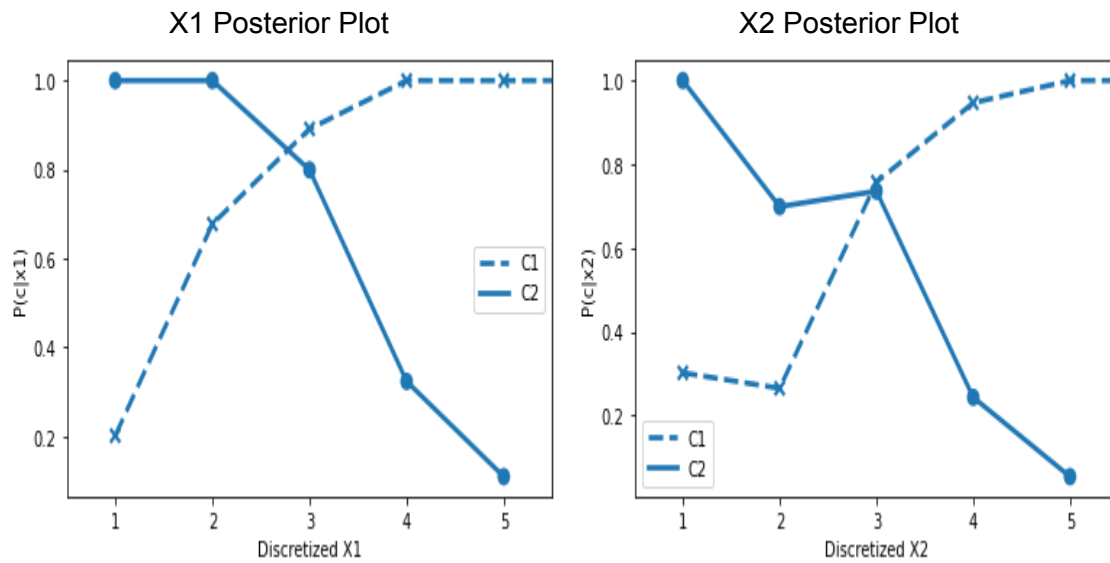


In the Scenario of “C1 and C2” Dataset :-

## 1. Likelihood Plots -

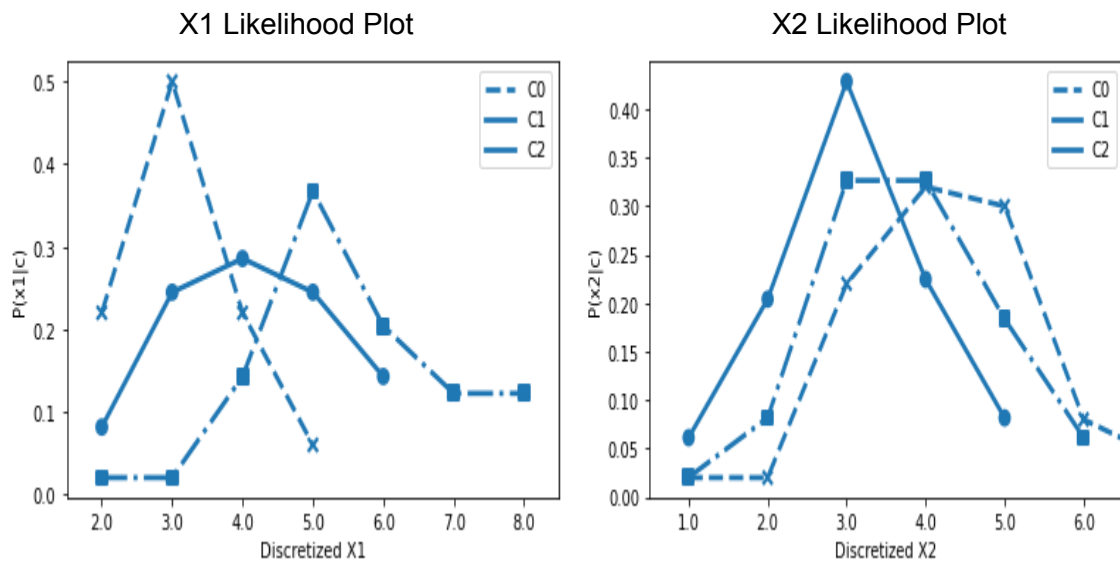


## 2. Posterior Plots -

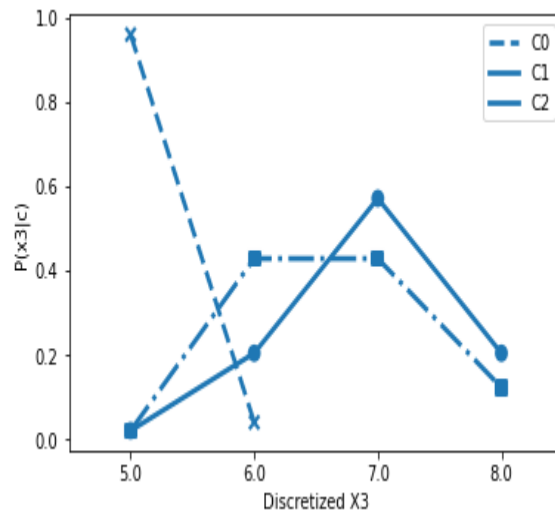


In the Scenario of "Iris" Dataset :-

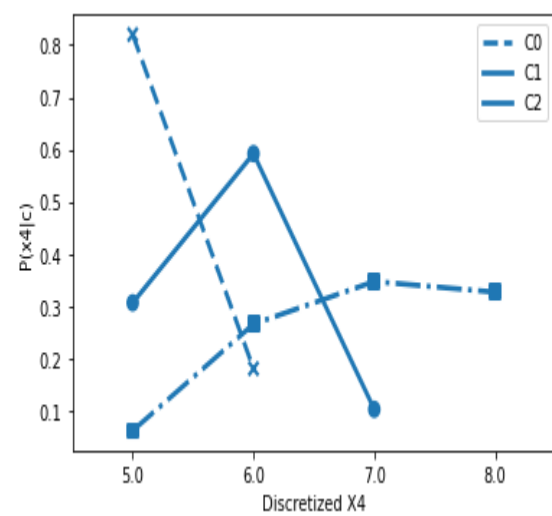
### 1. Likelihood Plots :-



X3 Likelihood Plot

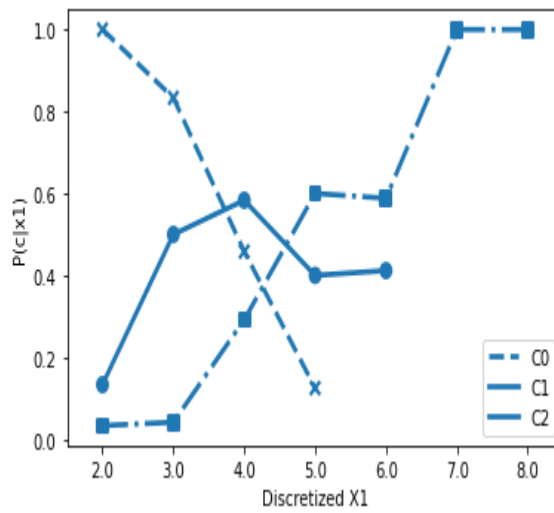


X4 Likelihood Plot

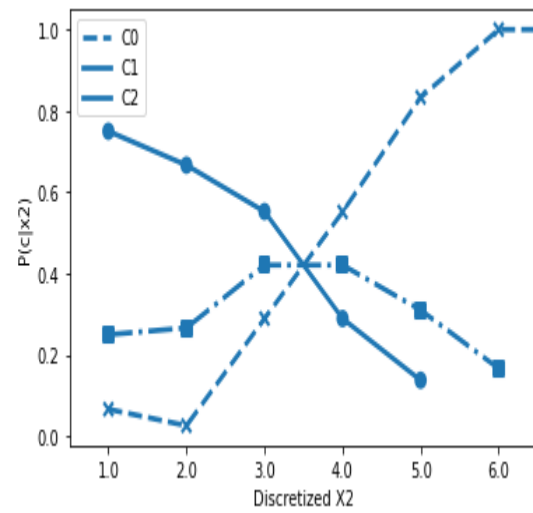


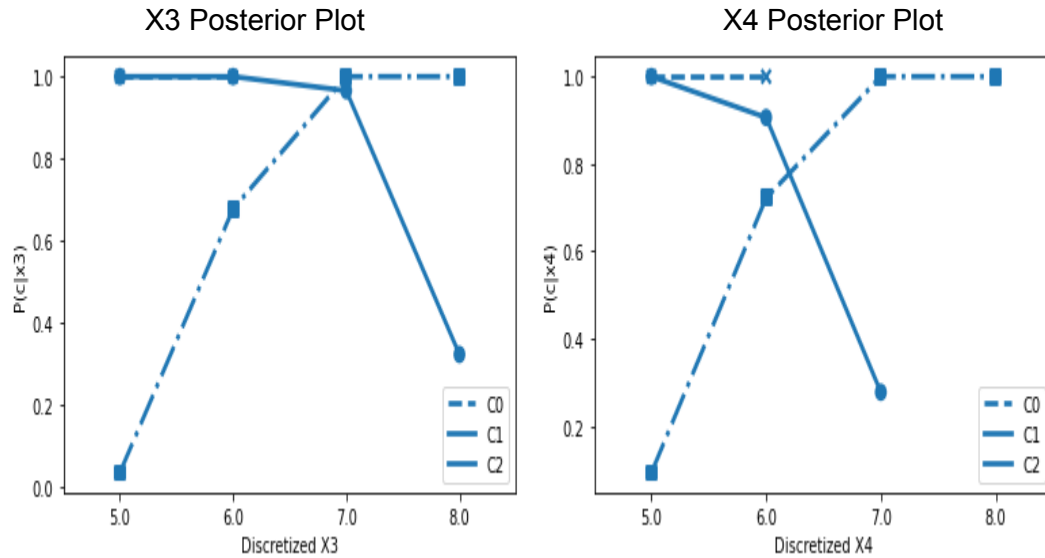
## 2. Posterior Plots :-

X1 Posterior Plot



X2 Posterior Plot





## Conclusion

1. In Order to deal with Continuous Dataset for Naive Bayesian Algorithms, convert them to Discrete Bins and assign Labels altogether.
2. Although Decision Tree with Max\_Depth = 2 was a weak learner, it gave an accuracy of 96.67% on Iris Dataset.
3. Bayesian Risk of Whole Test Dataset for given lambda matrix was maximum for Multinomial Naive Bayes and least for LDA Model.
4. Amongst Naive Bayesian Models, Bernoulli Naive Bayes Model performed worst for Iris Dataset, with 33.34% accuracy. The Reason might be because its purpose is in Binary Classification only, not in Multi-Class Classification.