Reference Manual

Release 9.6

The Sage Development Team

CONTENTS

1	User	Interfaces	3		
2	Grap	hics	5		
3	Math	nematics	7		
	3.1	Parents and Categories	7		
	3.2	Basic Rings and Fields	7		
	3.3	Linear Algebra			
	3.4	Calculus and Analysis	8		
	3.5	Probability and Statistics	8		
	3.6	Mathematical Structures	8		
	3.7	Discrete Mathematics	8		
	3.8	Geometry, Topology, and Homological Algebra	9		
	3.9	Number Fields, Function Fields, and Valuations	9		
	3.10	Number Theory	9		
	3.11	Algebraic and Arithmetic Geometry	10		
	3.12	Miscellaneous			
4	Prog	ramming	11		
	4.1	Facilities	11		
	4.2	Interfaces	11		
5	Gene	ral Information	13		
6	6 Indices and Tables				

Here you find documentation for all of Sage's features, illustrated with lots of examples. A thematic index follows.

This documentation is licensed under the Creative Commons Attribution-Share Alike 3.0 License.

CONTENTS 1

2 CONTENTS

ONE

USER INTERFACES

- Command Line Interface
- Jupyter Notebook Interface

TWO

GRAPHICS

- 2D Graphics
- 3D Graphics

THREE

MATHEMATICS

3.1 Parents and Categories

- Parents and Elements
- Coercion
- Categories

3.2 Basic Rings and Fields

- Integers and Rational Numbers
- Real and Complex Numbers
- Commutative Polynomials
- Power Series and Laurent Series
- Finite Rings and Fields
- p-adic Numbers
- Noncommutative Polynomials
- Quaternion Algebras

3.3 Linear Algebra

- Matrices and Spaces of Matrices
- · Vectors and Modules
- Tensors on Free Modules of Finite Rank

3.4 Calculus and Analysis

- Symbolic Calculus
- Mathematical Constants
- Elementary and Special Functions
- Asymptotic Expansions
- Numerical Optimization

3.5 Probability and Statistics

- Probability
- Statistics
- Quantitative Finance

3.6 Mathematical Structures

- Sets
- Monoids
- Groups
- Semirings
- Rings
- Algebras

3.7 Discrete Mathematics

- Combinatorics
- Graph Theory
- Quivers
- Matroid Theory
- Discrete Dynamics
- · Coding Theory
- Cryptography
- · Game Theory
- Symbolic Logic
- SAT solvers

3.8 Geometry, Topology, and Homological Algebra

- Euclidean Spaces and Vector Calculus
- · Combinatorial and Discrete Geometry
- Cell Complexes, Simplicial Complexes, and Simplicial Sets
- · Manifolds and Differential Geometry
- Hyperbolic Geometry
- Parametrized Surfaces
- · Knot Theory
- · Chain Complexes and their Homology

3.9 Number Fields, Function Fields, and Valuations

- · Number Fields
- · Function Fields
- Discrete Valuations

3.10 Number Theory

- Diophantine approximation
- · Quadratic Forms
- L-Functions
- Arithmetic Subgroups of $SL_2(\mathbf{Z})$
- General Hecke Algebras and Hecke Modules
- · Modular Symbols
- · Modular Forms
- · Quasimodular Forms
- Modular Forms for Hecke Triangle Groups
- Modular Abelian Varieties
- Miscellaneous Modular-Form-Related Modules

3.11 Algebraic and Arithmetic Geometry

- Schemes
- Plane and Space Curves
- Elliptic and Hyperelliptic Curves

3.12 Miscellaneous

- Databases
- Games

FOUR

PROGRAMMING

4.1 Facilities

- Data Structures
- Utilities
- Test Framework
- Parallel Computing

4.2 Interfaces

- Interpreter Interfaces
- C/C++ Library Interfaces
- Python Technicalities

FIVE

GENERAL INFORMATION

- External Packages
- Bibliographic References
- History and License

SIX

INDICES AND TABLES

- genindex
- modindex
- search