

# CS6120: Lecture 12

## Web Search

## Machine Translation

Kenneth Church

<https://kwchurch.github.io/>

# Your Projects

- Oral:
  - 20-40 minutes
- Written
  - 5-20 pages
  - lots of references
- Say everything three times
  - Winston: How to Speak
  - <https://www.youtube.com/watch?v=Unzc731iCUY>
- Examples:
  - <https://aclanthology.org/2022.acl-long.60>
  - [http://34.204.188.58/cgi-bin/similar?embedding=s2\\_recommendations&limit=20&search=An+Information-theoretic+Approach+to+Prompt+Engineering+Without+Ground+Truth+Labels](http://34.204.188.58/cgi-bin/similar?embedding=s2_recommendations&limit=20&search=An+Information-theoretic+Approach+to+Prompt+Engineering+Without+Ground+Truth+Labels)
  - <https://aclanthology.org/events/acl-2022/>



# Web Search & Information Retrieval

## Information Retrieval

- Textbook
  - <https://www-nlp.stanford.edu/IR-book/>
- Term-by-doc matrix:  $M$ 
  - Similarity of terms:  $M M^T$
  - Similarity of doc:  $M^T M$
- Index: Inverted file (postings)
  - Rows of  $M$
- Solitaire → Multiplayer Game
  - Solitaire: users lose to library (casino)
  - Multiplayer Game: Ecosystems
    - Readers, writers, advertisers, market makers

## Web Search

- Left rail (algo) vs. right rail (ads)
  - Instant Answers
- Crawl: wget
  - Seed URLs → sample of ``everything''
  - Deep web
  - WayBack Machine
    - <https://web.archive.org/>
- User logs: queries, clicks
  - Larger than crawls
    - Healthy ecosystem → more readers than writers
  - Behavioral signals
    - (super-important feedback)

# Web Crawling

<https://nlp.stanford.edu/IR-book/pdf/20crawl.pdf>

- Expensive: Limited to a few large companies
- Prioritize URLs by coverage of
  - Popular pages (estimates of demand)
  - Freshness (estimates of when the content is likely to differ from what is in cache)
- How large is the web? [Spider traps!](#)
  - (Near duplicate pages & Approximate nearest neighbors)
  - Calendar pages are not spider traps, but...
  - Ads, view counters
    - <https://www.wysiwygwebbuilder.com/phpcounter.html>
    - <https://www.geeksforgeeks.org/comparator-function-of-qsort-in-c/>
- Politeness (robots.txt): denial of service attacks
- Bragging Rights
  - Our Index is bigger than yours → Race Conditions
- How do you get seeds?
  - Toolbar, Gmail, Chrome, phones, Social Media, DNS ([Domain Name System](#))
  - Security/privacy holes & DNS



# Types of Answers

- Left Rail: 10 blue links
  - algo search
  - learning to rank: [https://en.wikipedia.org/wiki/Learning\\_to\\_rank](https://en.wikipedia.org/wiki/Learning_to_rank)
- Right Rail: ads
  - auction: [https://en.wikipedia.org/wiki/Sponsored\\_search\\_auction](https://en.wikipedia.org/wiki/Sponsored_search_auction)
- Instant Answers
  - Internal groups compete for types of queries

# Instant Answers

Google 1+1

Images Videos Perspectives Shopping News Maps Books Flights Finance All filters Tools

See results about 1+1 Song by Sia

1 + 1 = 2

Rad | Deg x! ( ) % AC  
Inv sin ln 7 8 9 ÷  
π cos log 4 5 6 ×  
e tan √ 1 2 3 −  
Ans EXP x<sup>y</sup> 0 . = +

Feedback

YouTube · BeyoncéVEVO 8.6M+ views · 12 years ago Beyoncé - 1+1 (Audio) - YouTube

Music video by Beyoncé performing 1+1. (C) 2011 Sony Music Entertainment.

4:34

Wikipedia https://en.wikipedia.org › wiki › 1+1\_(song)

1+1 (song)

"1+1" is a song recorded by American recording artist Beyoncé for her fourth studio album, 4 (2011). It was released by Columbia Records in the United ...

Genius https://genius.com › Beyonce-1-1-lyrics

Beyoncé – 1+1 Lyrics

Aug 8, 2022 — [Post-Chorus 1] When my days look low. Pull me in close and don't let me go, make love to me. So when the world's at war, let our love heal ...

1+1 Song by Beyoncé

Beyoncé - 1+1 (Video) - YouTube https://www.youtube.com › watch

Listen

Spotify YouTube iHeart Deezer

Album: 4 Artist: Beyoncé Released: 2011 Genres: R&B/Soul, Pop

People also search for

Beyoncé, Beyoncé - 1+1 (Video), Beyoncé - 1+1 (Song), Beyoncé - 1+1 (Lyrics)

# Instant Answers 10 Blue Links

Snippet

Opium War

Images Videos News Shopping Maps Books Flights Finance All filters ▾ Tools

Opium Wars : Overview Outcome Purpose



The first Opium War (1839–42) was fought between China and Great Britain, and the second Opium War (1856–60), also known as the Arrow War or the Anglo-French War in China, was fought by Great Britain and France against China. Qing dynasty. Read more about the Qing dynasty.

Nov 6, 2023

Britannica https://www.britannica.com › ... › International Relations

Opium Wars | Definition, Summary, Facts, & Causes - Britannica

About featured snippets · Feedback

U.S. Department of State (.gov) https://history.state.gov › milestones › china-1

The Opening to China Part I: the First Opium War, ...

The Opium War and these treaties were emblematic of an era in which Western powers tried to gain unfettered access to Chinese products and markets for European ...

U.S. Department of State (.gov) https://history.state.gov › milestones › china-2

The Opening to China Part II: The Second Opium War, ...

Following the First Opium War in the 1840s, the Western powers concluded a series of treaties with China in an effort to open its lucrative markets to Western ...

Wikipedia https://en.wikipedia.org › wiki › First\_Opium\_War

First Opium War

The First Opium War also known as the Anglo-Chinese War, was a series of military engagements fought between the British Empire and the Qing dynasty of ...

Result: British Victory: Treaty of Nanking; Esta... Location: China and South China Sea

Date: 4 September 1839 – 29 August 1842; (2... Territorial changes: Hong Kong Island cede...

Opium · The Opium War (film) · Treaty of Nanking · Nerbudda incident

About

The Opium Wars were two conflicts waged between China and Western powers during the mid-19th century. The First Opium War was fought from 1839 to 1842 between China and Britain. Wikipedia

Location: China, Guangzhou, Guangdong Province

Start date: 1839

End date: 1860

Feedback

# Ads

Google TV

Filter by

- Smart TV
- Under 32 inches
- 32 – 43 inches
- 43 – 55 inches
- 55 – 75 inches
- Over 75 inches
- On sale
- 4K
- Roku
- Under \$350
- LED

Sponsored :

| Image | Product                           | Price      | Rating      | Description     |
|-------|-----------------------------------|------------|-------------|-----------------|
|       | LG - 48" Class A2 Series...       | \$599.99   | ★★★★★ (7k+) | Best Buy        |
|       | Samsung 55" Class The...          | \$1,499.99 | ★★★★★ (9k+) | Samsung         |
|       | Samsung 65" Class OLED...         | \$1,599.99 | ★★★★★ (9k+) | Samsung         |
|       | Sony - 65" Class BRAVI...         | \$1,899.99 | ★★★★★ (2k+) | Best Buy        |
|       | LG C3 Series 77-Inch Clas...      | \$2,496.99 | ★★★★★ (2k+) | Amazon.com      |
|       | Gold Series 32" (Vizio) / 1 Ye... | \$899.00   | ★★★★★ (2k+) | MirageVision... |
|       | LG 50" Class 4K UHD Sm...         | \$299.99   | ★★★★★ (350) | Target          |
|       | Samsung 55" Class The...          | \$1,699.99 | ★★★★★ (20)  | Samsung         |

Screen Size

- Under 32 inches
- 32 – 43 inches
- 43 – 55 inches
- 55 – 75 inches
- Over 75 inches

HDTV Format

- 4K
- 1080p
- 8K
- 720p

Price

Brand

Features

Display Type

Supported Streaming Services

Screen Form

Color

Stores

Walmart

https://www.walmart.com › tv-home-theater

TV & Video - Walmart.com

Shop TVs and Video equipment at Walmart.com and browse Smart TVs, big screen TVs and streaming devices like Roku. Save money. Live better.

4.5 ★ seller rating (846) · \$9.95 same-day delivery over \$35 · Free 90-day returns

TV Mounts & Accessories · TV Antennas, HDTV Antennas...

Best Buy

https://www.bestbuy.com › TV & Home Theater

TVs: Televisions & HDTVs

Shop Best Buy for the latest TVs, including deals on LED, 4K, OLED & curved flat screen TVs from top-rated brands.

4.7 ★ seller rating (422) · 3–5 day delivery · Free 15-day returns

TVs Under \$500 · Flat-screen TV · Smart TVs · 65-Inch TVs

# Evaluation

- Extract sample of queries from query logs
- Scrape 10 blue links from release candidates
  - (and competition)
  - (over time)
- Send Queries and candidate URLs to human judges
  - score 1-5 (plus perhaps offensive)
  - perfect, excellent, good, fair, poor, offensive/illegal/irresponsible
- Score scrapes with NDCG
- Learning to Rank
- Track scores over time
  - and hopefully get better and better over time
- Issues
  - Judges prefer Google Brand
    - Even when the links are the same
  - Learning to rank → Cheating
    - Watermarking
  - Now that Google is a monopoly
    - Little incentive to improve
    - Web search may be degrading
      - (creating opportunity for chat bots)
  - SEOs (Search Engine Optimization)

# Ad Auction

<https://moz.com/blog/understanding-google-ads-auction>

- Bid
- Quality
  - Estimate of CTR (clicks)
- Market maker (Google)
  - Maximizing benefit to
    - Readers
    - Writers
    - Advertisers
- Economic Optimization
  - Different from learning to rank

|              | Max CPC Bid | x | Quality Score | = | Ad Rank | Ad Position |
|--------------|-------------|---|---------------|---|---------|-------------|
| Advertiser 1 | \$3.00      |   | 8             |   | 24      | 1           |
| Advertiser 2 | \$4.00      |   | 5             |   | 20      | 2           |
| Advertiser 3 | \$6.00      |   | 2             |   | 12      | 3           |
| Advertiser 4 | \$8.00      |   | 1             |   | 8       | 4           |



Search Wikipedia

**Search**

# Vickrey auction

14 languages ▾

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From Wikipedia, the free encyclopedia

A **Vickrey auction** or **sealed-bid second-price auction (SBSPA)** is a type of sealed-bid auction. Bidders submit written bids without knowing the bid of the other people in the auction. The highest bidder wins but the price paid is the second-highest bid. This type of auction is strategically similar to an English auction and gives bidders an incentive to bid their true value. The auction was first described academically by Columbia University professor William Vickrey in 1961<sup>[1]</sup> though it had been used by stamp collectors since 1893.<sup>[2]</sup> In 1797 Johann Wolfgang von Goethe sold a manuscript using a sealed-bid, second-price auction.<sup>[3]</sup>

Vickrey's original paper mainly considered auctions where only a single, indivisible good is being sold. The terms *Vickrey auction* and *second-price sealed-bid auction* are, in this case only, equivalent and used interchangeably. In the case of multiple identical goods, the bidders submit inverse demand curves and pay the opportunity cost.<sup>[4]</sup>

Vickrey auctions are much studied in economic literature but uncommon in practice. Generalized variants of the Vickrey auction for multiunit auctions exist, such as the generalized second-price auction used in Google's and Yahoo!'s online advertisement programmes<sup>[5][6]</sup> (not incentive compatible) and the Vickrey–Clarke–Groves auction (incentive compatible).

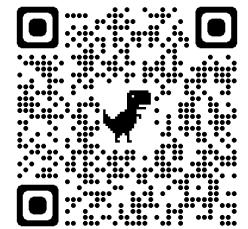
 Part of a series on  
**Auctions**

**Types**

[All-pay \(Chinese\)](#) · [Amsterdam](#) · [Anglo-Dutch](#) ·  
[Barter double](#) · [Best/not best](#) · [Brazilian](#) ·  
[Calcutta](#) · [Candle](#) · [Click-box bidding](#) ·  
[Combinatorial](#) · [Common value](#) ·  
[Deferred-acceptance](#) · [Discriminatory price](#) ·  
[Double](#) · [Dutch](#) · [English](#) · [Forward](#) · [French](#) ·  
[Generalized first-price](#) ·  
[Generalized second-price](#) · [Japanese](#) ·  
[Knapsack](#) · [Multi-attribute](#) · [Multiunit](#)

# Priors: $\Pr(\text{URL})$ Query-independent

- Page Rank
  - Prior:  $\Pr(\text{URL})$
  - Eigenvalue
  - Random Surfer Model
  - <https://en.wikipedia.org/wiki/PageRank>
- [ProNE: Fast and Scalable Network Representation Learning](#)
- [https://en.wikipedia.org/wiki/Graph\\_neural\\_network](#)
- $\text{URL} \rightarrow \text{Noisy Channel} \rightarrow Q$ 
  - $\Pr(\text{URL}) = \text{ARGMAX}_U \Pr(U) \Pr(Q|U)$
- Prior:  $\Pr(\text{URL})$
- Channel:  $\Pr(Q|\text{URL})$



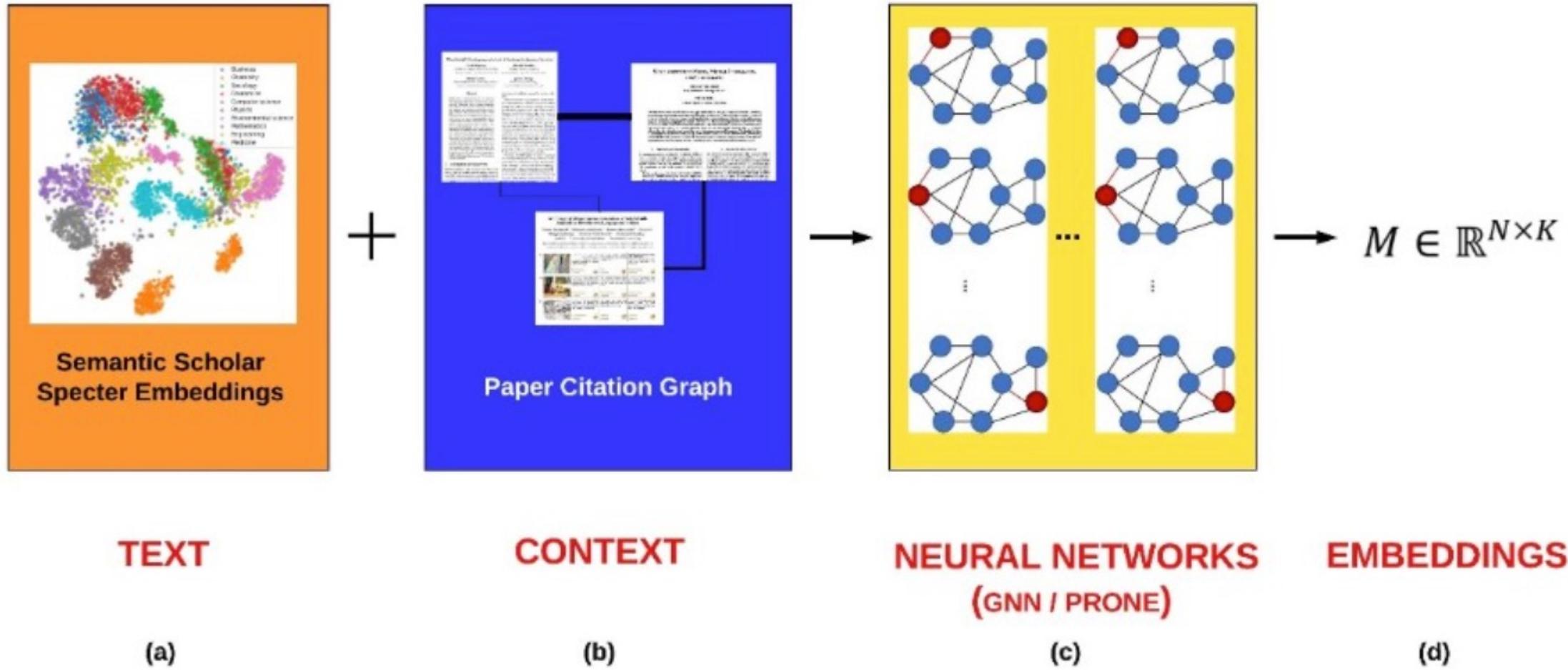
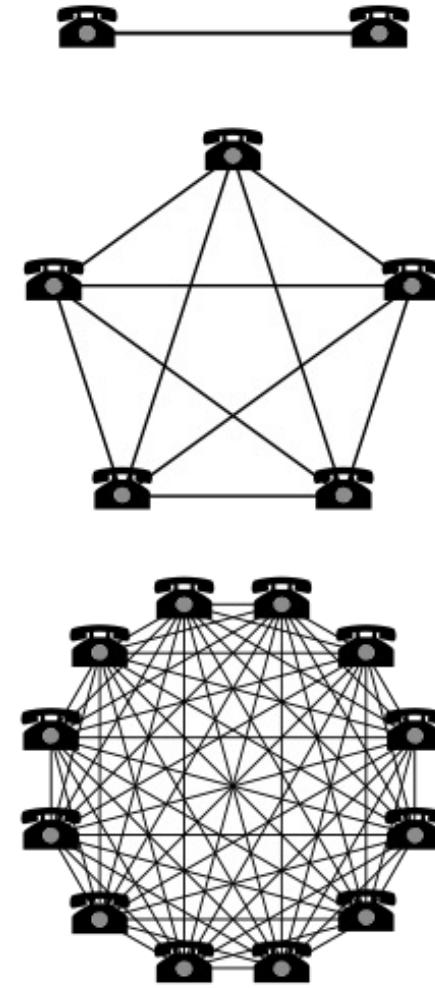


Figure 1: Embeddings are typically based on text (titles and abstracts). We will create multiple embeddings based on combinations of text and context (citations).



# Metcalf's Law (Network Effects)

- History: 3Com was selling small networks
  - $3 = 1 \text{ printer} + 2 \text{ computers}$
  - Metcalfe argued they should sell bigger networks
    - (and more 3Com products)
    - because of economies of scale
- Economy of Scale:
  - Benefits scale faster than costs
    - Benefits:  $\sim n^2$
    - Costs:  $\sim n$
  - Law has been good for AT&T, Google, Social Media
  - Hypo: also good for Academic Search
    - Consequently, we should experiment with large graphs



# Linear Algebra & Term-by-Document Matrices

- Singular Value Decomposition (SVD)
- Principal Component Analysis (PCA)
- Dimension Reduction
- Rotations
- Approximate Nearest Neighbors (ANN)

# Nearly Everything To Vectors (Embeddings) (VectorDB)

- “Everything”
  - Words (Terms): word2vec
  - Documents (Text Strings):
    - doc2vec, BERT, Specter
  - Graphs (GNNs)
    - Example: citation graph
  - Semantics (“Meaning”)
  - All the world’s languages
  - Audio (Speech, Music)
  - Pictures and Videos
- Embeddings
  - Similarity  $\approx$  Cosine
  - Similar documents
    - Word Overlap
    - Nearby in citation graph
    - Similar topics, venues, authors
  - Latent (Hidden) Dimensions
- Computational Convenience
  - Dimension Reduction
  - Rotations
  - Approximate Nearest Neighbors

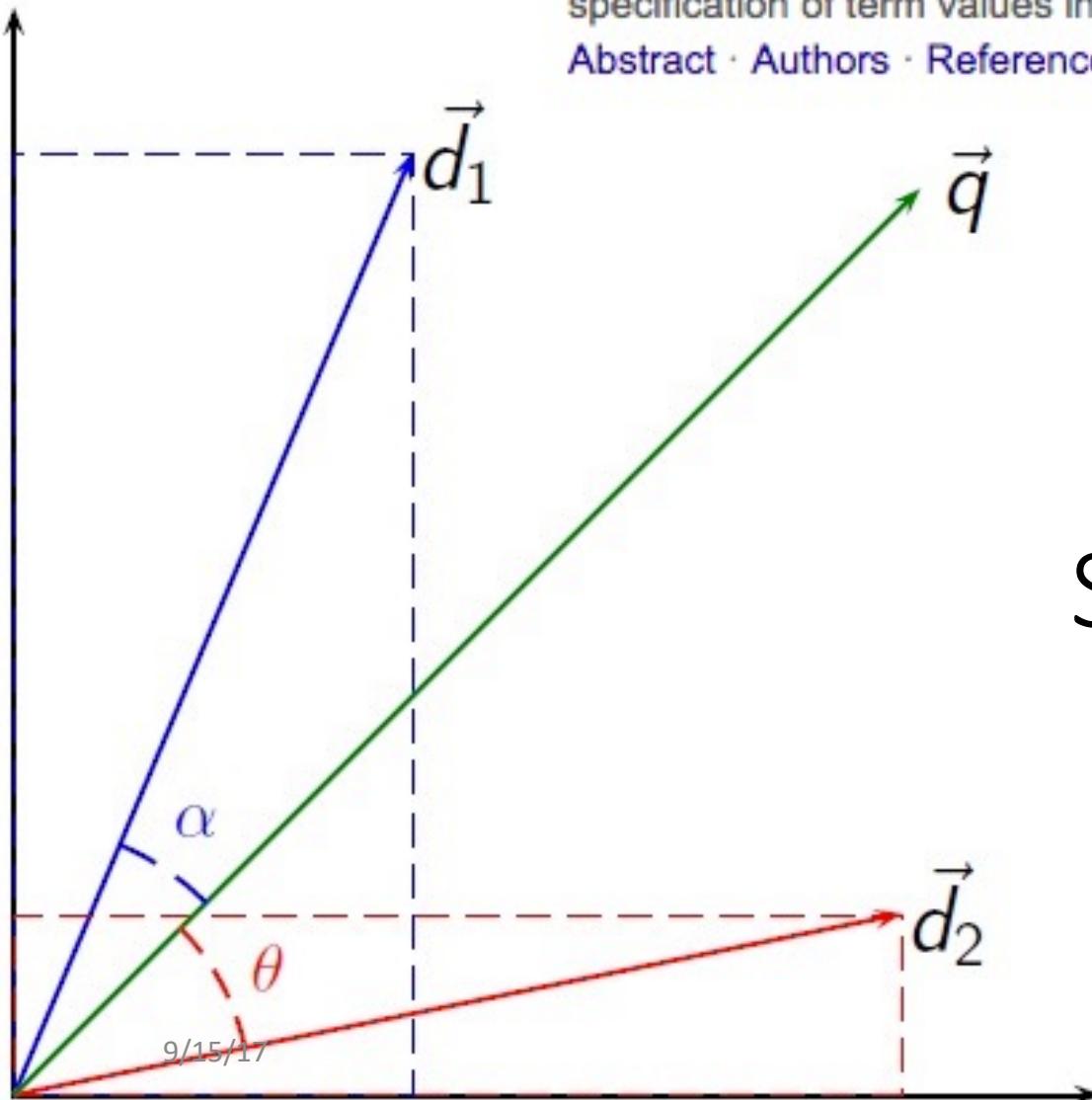
## A vector space model for automatic indexing - ACM Digital Library

[dl.acm.org/citation.cfm?id=361220](https://dl.acm.org/citation.cfm?id=361220) ▾

by G Salton - 1975 - Cited by 7464 - Related articles

A vector space model for automatic indexing, Published by ACM .... Salton, G., and Yang, C.S. On the specification of term values in automatic indexing.

[Abstract](#) · [Authors](#) · [References](#) · [Cited By](#)



# Salton's Vector Space Model

# Word2vec (Embeddings)

- $M \in \mathbb{R}^{V \times K}$  (tall-skinny matrix)
  - $V$ : vocabulary size ( $\approx 500k$ )
  - $K$ : hidden dimensions ( $\approx 300$ )
- $MM^T = \cos(w_i, w_j) \propto PMI(w_i, w_j)$ 
  - Similarity of all pairs of words in  $V$
  - It might be infeasible to materialize  $MM^T$ 
    - But there are approximations (ANNs)
    - that find many/most of the large values
- Better for capturing collocations
  - Collocations:  $w_i$  &  $w_j$  appear near one another (more than chance)
- Less appropriate for other notions of similarity
  - Both synonyms and antonyms appear near one another
  - (But they don't mean the same thing)



# The Bag of Words Representation

I love this movie! It's sweet, but with satirical humor. The dialogue is great and the adventure scenes are fun... It manages to be whimsical and romantic while laughing at the conventions of the fairy tale genre. I would recommend it to just about anyone. I've seen it several times, and I'm always happy to see it again whenever I have a friend who hasn't seen it yet!



# Information Retrieval (IR) notation

## Term Weighting: $\text{tf} * \text{IDF}$

- t: term
- d: document
- D: # of documents in library
- Interpretation:
  - Entropy:  $H = -\log(P)$
  - where  $P = \Pr(t \in d)^{\text{count}(t,d)}$
- $\text{tf}(t,d)$ : term frequency
  - # of times that t appears in d
- $\text{df}(t)$ : document frequency
  - # of documents that contain t
  - (at least once)
- $\text{IDF}(t)$ : inverse doc frequency
  - $\text{IDF}(t) = -\log_2 \frac{\text{df}(t)}{D}$
- $\text{tf} * \text{IDF}$  weighting
  - Assumes (too much) indep

# Bellcore Example

- Example of term by document matrix
  - A document  $\approx$  a bag of words
  - A word  $\approx$  a bag of documents
    - *You shall know a word by the company it keeps*
- Example of SVD for dimension reduction
  - Suggestion: reducing dimensions  $\rightarrow$  better separation of classes of interest
- Motivate latent dimensions
  - as a method to embed both terms and documents
  - into a common (unified) vector space

# Bellcore's Example: Bag of Words + SVD

[http://wordvec.colorado.edu/papers/Deerwester\\_1990.pdf](http://wordvec.colorado.edu/papers/Deerwester_1990.pdf)

- c1 Human machine *interface* for Lab ABC *computer* applications
  - c2 A *survey* of *user* opinion of computer *system response time*
  - c3 The EPS *user interface* management *system*
  - c4 *System* and *human system* engineering testing of EPS
  - c5 Relation of *user-perceived response time* to error measurement
- 
- m1 The generation of random, binary, unordered *trees*
  - m2 The intersection *graph* of paths in *trees*
  - m3 *Graph minors* IV: Widths of *trees* and well-quasi-ordering
  - m4 *Graph minors*: A *survey*

# Term by Documents Matrix

|    |   |
|----|---|
| c1 | Human machine interface for Lab ABC computer applications     |
| c2 | A survey of user opinion of computer system response time     |
| c3 | The EPS user interface management system                      |
| c4 | System and human system engineering testing of EPS            |
| c5 | Relation of user-perceived response time to error measurement |
| m1 | The generation of random, binary, unordered trees             |
| m2 | The intersection graph of paths in trees                      |
| m3 | Graph minors IV: Widths of trees and well-quasi-ordering      |
| m4 | Graph minors: A survey  |

| c1 | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |           |
|----|----|----|----|----|----|----|----|----|-----------|
| 1  |    |    | 1  |    |    |    |    |    | human     |
| 1  |    | 1  |    |    |    |    |    |    | interface |
| 1  | 1  |    |    |    |    |    |    |    | computer  |
|    |    | 1  | 1  | 1  |    |    |    |    | user      |
|    |    | 1  | 1  | 2  |    |    |    |    | system    |
|    |    | 1  |    | 1  |    |    |    |    | response  |
|    |    | 1  |    | 1  |    |    |    |    | time      |
|    |    | 1  |    | 1  |    |    |    |    | EPS       |
|    |    |    | 1  | 1  |    |    |    |    | survey    |
|    |    |    |    | 1  |    |    |    |    | trees     |
|    |    |    |    |    | 1  | 1  | 1  | 1  | graph     |
|    |    |    |    |    |    | 1  | 1  | 1  | minors    |

# Term by Document Matrix

| c1 | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |           |
|----|----|----|----|----|----|----|----|----|-----------|
| 1  |    |    | 1  |    |    |    |    |    | human     |
| 1  |    | 1  |    |    |    |    |    |    | interface |
| 1  | 1  |    |    |    |    |    |    |    | computer  |
|    | 1  | 1  |    | 1  |    |    |    |    | user      |
| 1  | 1  | 2  |    |    |    |    |    |    | system    |
| 1  |    |    |    | 1  |    |    |    |    | response  |
| 1  |    |    |    | 1  |    |    |    |    | time      |
|    |    | 1  | 1  |    |    |    |    |    | EPS       |
|    |    |    |    | 1  |    |    |    | 1  | survey    |
|    |    |    |    |    | 1  | 1  | 1  |    | trees     |
|    |    |    |    |    |    | 1  | 1  | 1  | graph     |
|    |    |    |    |    |    |    | 1  | 1  | minors    |

# Singular Value Decomposition (SVD)

- $M \approx U D V^T$
- $D$  is diagonal
  - Eigenvalues
  - Sorted from largest to smallest
- $U$  and  $V$  are Eigenvectors
  - Orthogonal and unit length
    - $U^T U = I$
    - $V^T V = I$
- $\cos(M, M) = MM^T$ 
  - $UDV^T(UDV^T)^T$
  - $UDV^T(VD^T U^T)$
  - $UD^2 U^T$
- $M \rightarrow UD$ 
  - Plus dimension reduction
  - Replace smaller Eigenvalues with 0

# Dimension Reduction

- Standard Recipe
  - Set smaller Eigenvalues to 0
- Interpretation
  - L2 optimality (least squares)
- Recall that Eigenvalues are sorted from largest to smallest
- Motivation for dimension reduction
  - Computational resources:
    - Space
      - Specter:  $M \in \mathbb{R}^{N \times K}$
      - N is 200M documents
      - K is 768 (BERT hidden layer)
      - $MM^T \in \mathbb{R}^{N \times N}$  (**very** large)
    - Time
  - Statistical convenience:
    - Smoothing (soft thesaurus)
    - Replace zeros with small values
  - Computational convenience:
    - Approximate nearest neighbors
    - <https://pypi.org/project/annoy/>

# SVD and PCA

## SVD (Singular Value Decomposition)

- $M \approx U D V^T$
- $D$ : Eigenvalues
- $U$ : Eigenvectors
- $M$  need not be square
  - (just non-singular)

## PCA (Principal Component Analysis)

- $Q \propto X^T X = W \Lambda W^T$
- $Q$  is square by construction
  - $\Lambda$ : Eigenvalues
  - $W$ : Covariances
    - Diagonal of  $W$  are variances

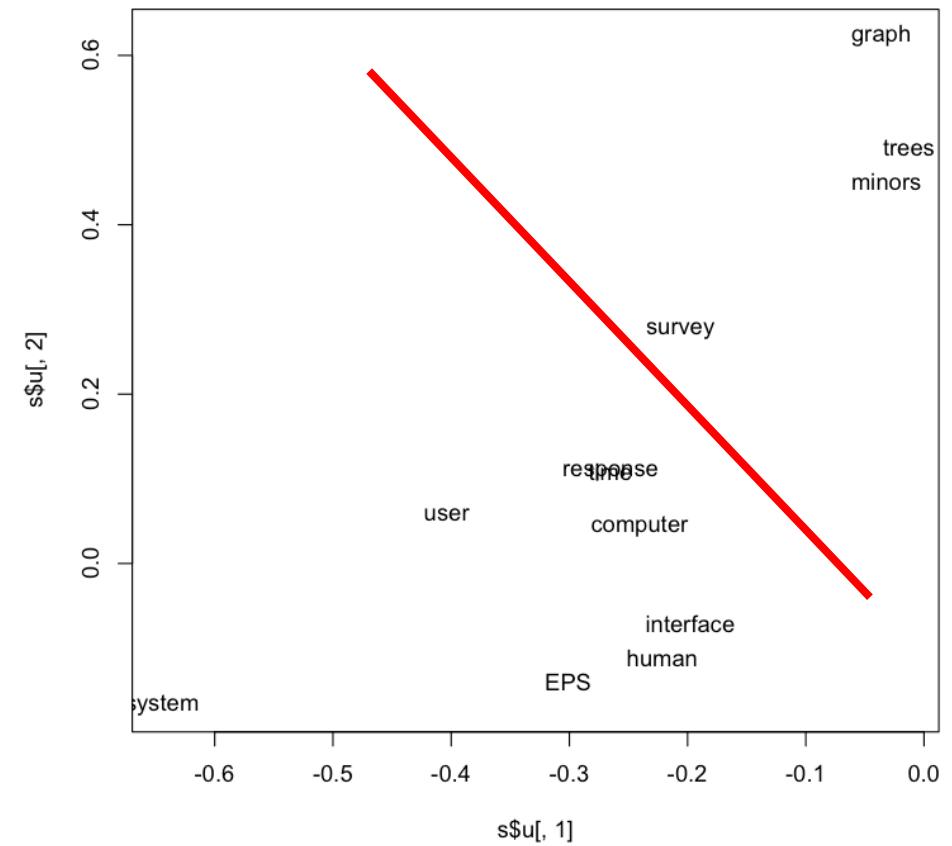
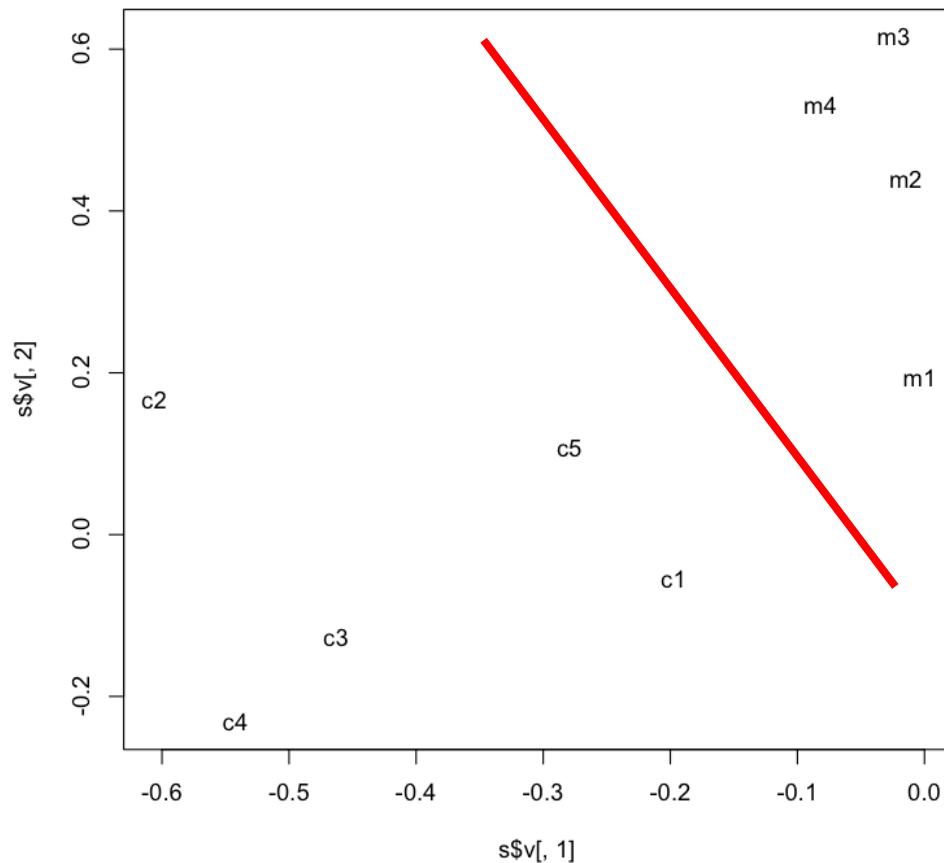
# Dimension Reduction in R

$$bellcore \approx U D V^T$$

```
bellcore =  
  
structure(.Data = c(1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,  
 1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 1, 0, 1, 1, 0, 0, 1, 0, 0, 0,  
 0, 1, 0, 0, 0, 2, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 0,  
 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0,  
 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0,  
 0, 0, 0, 0, 0, 1, 0, 1, 1),  
.Dim = c(12, 9),  
.Dimnames = list(c("human", "interface", "computer",  
 "user", "system", "response", "time", "EPS",  
 "survey", "trees", "graph", "minors"),  
 c("c1", "c2", "c3", "c4", "c5", "m1", "m2", "m3",  
 "m4")))
```

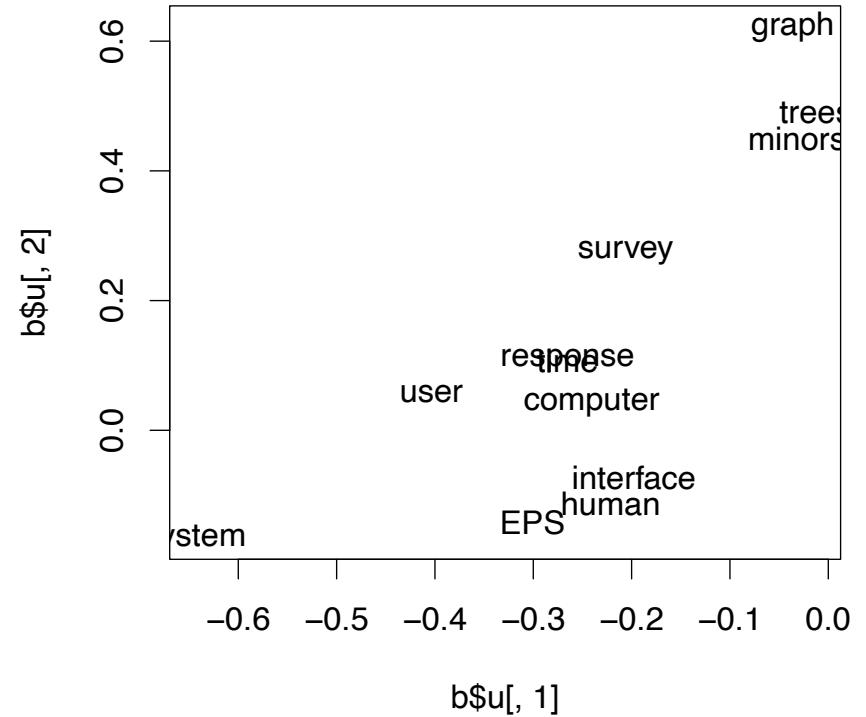
```
b = svd(bellcore)  
b2 = b$u[,1:2] %*% diag(b$d[1:2]) %*%  
 t(b$v[,1:2])  
dimnames(b2) = dimnames(bellcore)  
par(mfrow=c(2,2))  
plot(hclust(as.dist(-cor(bellcore))))  
plot(hclust(as.dist(-cor(t(bellcore)))))  
plot(hclust(as.dist(-cor(b2))))  
plot(hclust(as.dist(-cor(t(b2)))))
```

# SVD maps terms & docs into internal dimensions



$$bellcore \approx U D V^T$$

| c1 | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |           |
|----|----|----|----|----|----|----|----|----|-----------|
| 1  |    |    | 1  |    |    |    |    |    | human     |
| 1  |    | 1  |    |    |    |    |    |    | interface |
| 1  | 1  |    |    |    |    |    |    |    | computer  |
|    | 1  | 1  |    | 1  |    |    |    |    | user      |
|    | 1  | 1  | 2  |    |    |    |    |    | system    |
| 1  |    |    | 1  |    |    |    |    |    | response  |
| 1  |    |    | 1  |    |    |    |    |    | time      |
|    | 1  | 1  |    |    |    |    |    |    | EPS       |
| 1  |    |    |    | 1  | 1  |    |    |    | survey    |
|    |    |    | 1  | 1  | 1  |    |    |    | trees     |
|    |    |    |    | 1  | 1  | 1  |    |    | graph     |
|    |    |    |    |    | 1  | 1  |    |    | minors    |



```

b = svd(bellcore)

b2 = b$u[,1:2] %*% diag(b$d[1:2]) %*% t(b$v[,1:2])

dimnames(b2) = dimnames(bellcore)

par(mfrow=c(2,2))

plot(hclust(as.dist(-cor(bellcore)))))

plot(hclust(as.dist(-cor(t(bellcore))))))

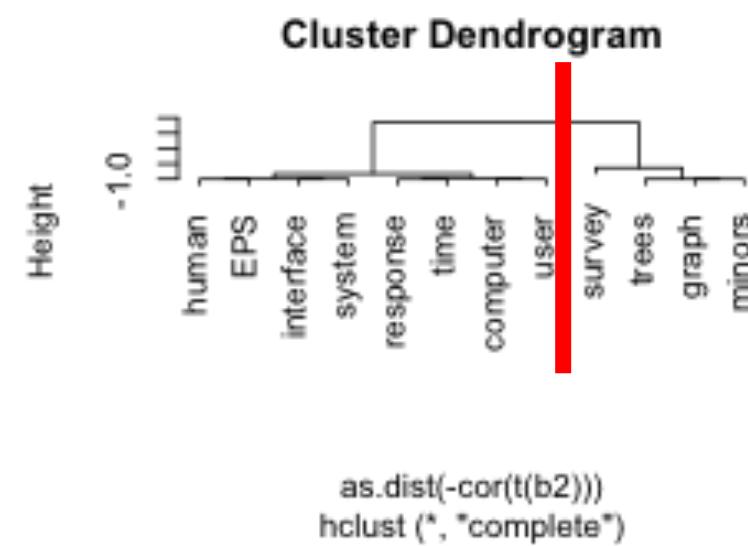
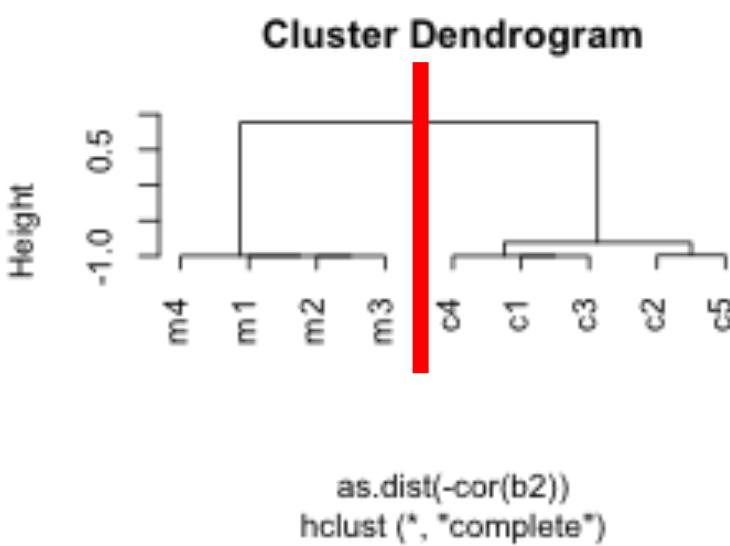
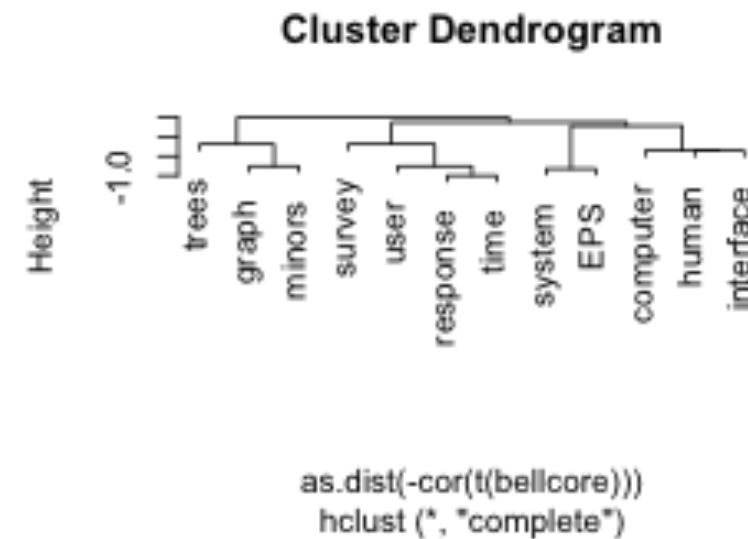
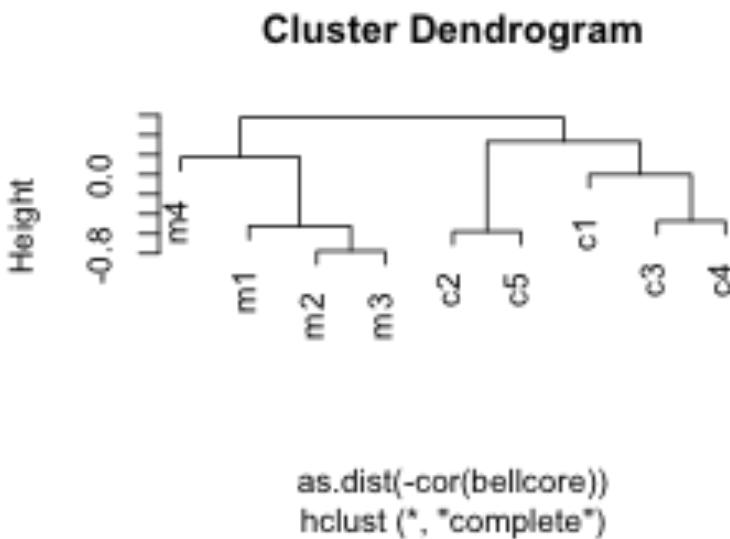
plot(hclust(as.dist(-cor(b2)))))

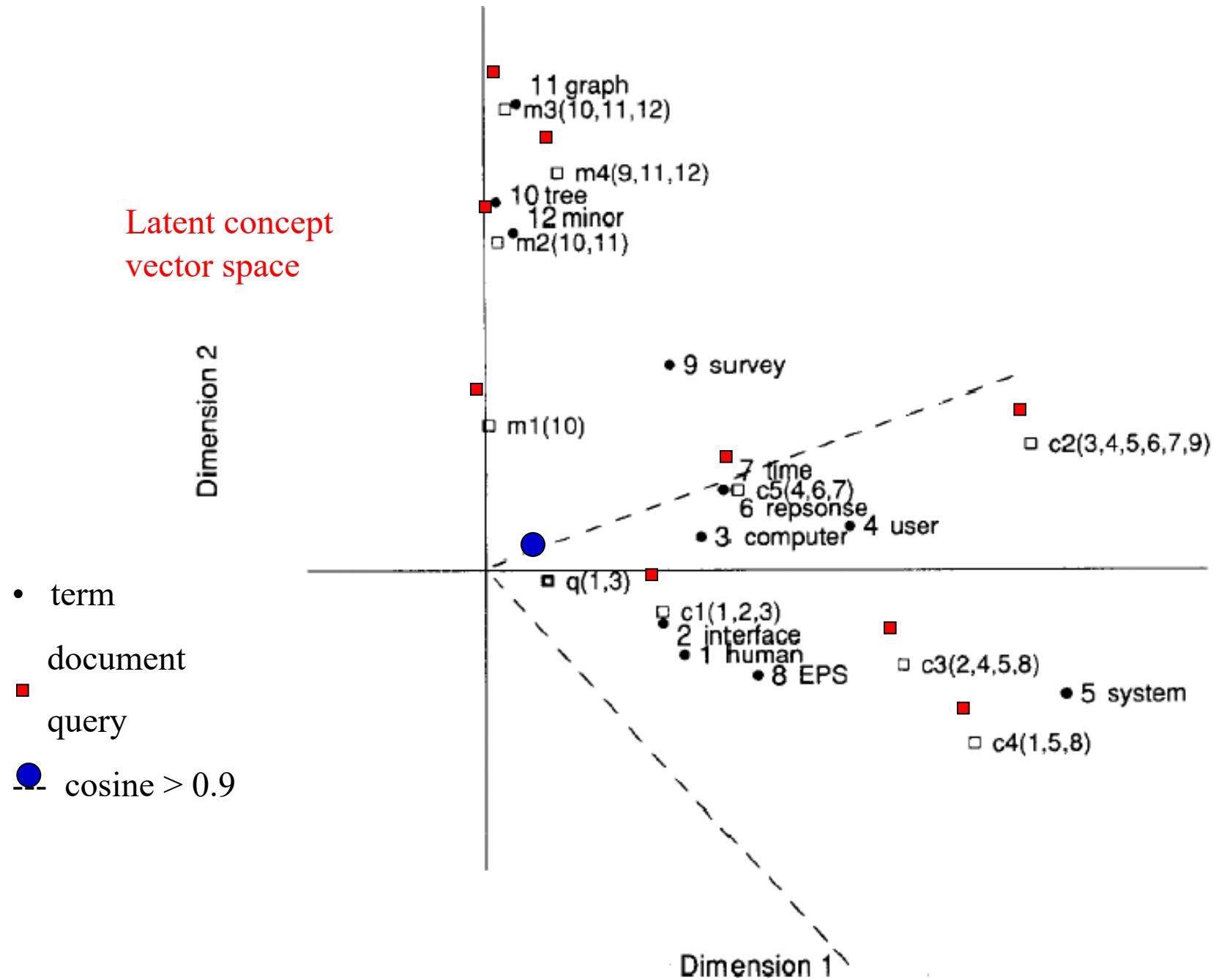
plot(hclust(as.dist(-cor(t(b2))))))

```

## Term by Document Matrix

| c1 | c2 | c3 | c4 | c5 | m1     | m2     | m3 | m4 |           |
|----|----|----|----|----|--------|--------|----|----|-----------|
| 1  |    |    | 1  |    |        |        |    |    | human     |
| 1  |    | 1  |    |    |        |        |    |    | interface |
| 1  | 1  |    |    |    |        |        |    |    | computer  |
|    | 1  | 1  |    | 1  |        |        |    |    | user      |
|    | 1  | 1  | 2  |    |        |        |    |    | system    |
| 1  |    |    | 1  |    |        |        |    |    | response  |
| 1  |    |    | 1  |    |        |        |    |    | time      |
|    | 1  | 1  |    |    |        |        |    |    | EPS       |
|    |    |    | 1  | 1  |        |        |    |    |           |
|    |    |    |    |    | survey |        |    |    |           |
|    |    |    |    |    | 1      | trees  |    |    |           |
|    |    |    |    |    |        | graph  |    |    |           |
|    |    |    |    |    |        | minors |    |    |           |





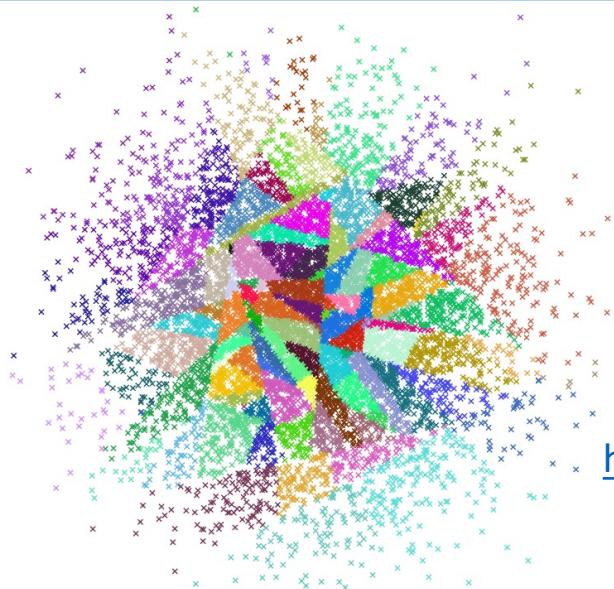
# Approximate Nearest Neighbors (ANN)

- Indexing time:
  - Input: Embedding  $M \in \mathbb{R}^{N \times K}$
  - Output: Indexes
- Query time:
  - Input:
    - Embedding, Indexes, query
  - Query:  $q \in \mathbb{R}^K$
  - Output: candidates,  $c \in \mathbb{R}^K$ 
    - where  $c$  is near  $q$
    - sorted by  $\text{sim}(q, c)$

```
from gensim.similarities.annoy import AnnoyIndexer

# 100 trees are being used in this example
annoy_index = AnnoyIndexer(model, 100)
# Derive the vector for the word "science" in our model
vector = wv["science"]
# The instance of AnnoyIndexer we just created is passed
approximate_neighbors = wv.most_similar([vector], topn=11, indexer=annoy_index)
# Neatly print the approximate_neighbors and their corresponding cosine similarity values
print("Approximate Neighbors")
for neighbor in approximate_neighbors:
    print(neighbor)
```

[https://radimrehurek.com/gensim/auto\\_examples/tutorials/run\\_annoy.html](https://radimrehurek.com/gensim/auto_examples/tutorials/run_annoy.html)



<https://pypi.org/project/annoy/>

# Machine Translation

- <https://web.stanford.edu/~jurafsky/slp3/13.pdf>

