

Graunt, Halley, and US 1993 Life Table

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Source of Data

Age	Graunt	1993
0	100	100
6	64	99
16	40	99
26	25	98
36	16	97
46	10	95
56	6	92
66	3	84
76	1	70

Data Input

- Graunt's Life Table

```
graunt <- data.frame(x = c(0, seq(6, 76, by = 10)),
                      xPo_g = c(100, 64, 40, 25, 16, 10, 6, 3, 1))
```

More data

- US 1993 life table for the same age group

```
us93 <- data.frame(x = graunt$x,
                     xPo_us = c(100, 99, 99, 98, 97, 95, 92, 84, 70))
```

Data Extraction

There are many ways to extract part of `us93` data frame.

```
us93["xPo_us"]
```

```
##   xPo_us
## 1   100
## 2    99
## 3    99
## 4    98
## 5    97
## 6    95
## 7    92
## 8    84
## 9    70
```

```
us93["xPo_us"][[1]]
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93["xPo_us"]$xPo_us
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93["xPo_us"]$xPo
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93[2]
```

```
##   xPo_us
## 1   100
## 2    99
## 3    99
## 4    98
## 5    97
## 6    95
## 7    92
## 8    84
## 9    70
```

```
us93[2][[1]]
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93[2]$xPo_us
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93[, "xPo_us"]
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93[, 2]
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93$xPo_us
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

```
us93$xPo
```

```
## [1] 100 99 99 98 97 95 92 84 70
```

Into one single data frame

Combine two data frames into one single data frame, compare the results.

```
(graunt_us <- data.frame(graunt, xPo_us = us93$xPo))
```

x	xPo_g	xPo_us
0	100	100
6	64	99
16	40	99
26	25	98
36	16	97
46	10	95
56	6	92
66	3	84
76	1	70

```
(graunt_us_2 <- data.frame(graunt, us93[2]))
```

x	xPo_g	xPo_us
0	100	100
6	64	99
16	40	99
26	25	98
36	16	97
46	10	95
56	6	92
66	3	84
76	1	70

```
(graunt_us_2 <- data.frame(graunt, us93[, 2]))
```

x	xPo_g	us93...2
0	100	100
6	64	99
16	40	99
26	25	98
36	16	97
46	10	95
56	6	92
66	3	84
76	1	70

Life Expectancy

The basic principle is that the area under the survival function is the life expectancy.

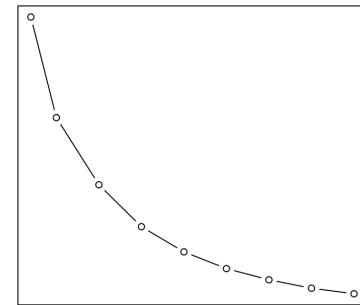
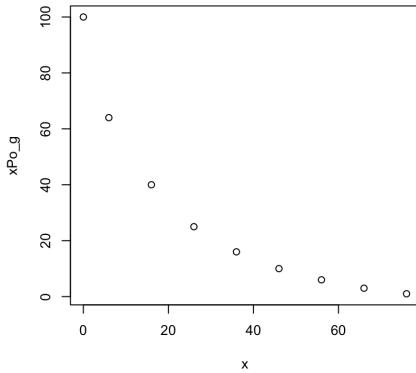
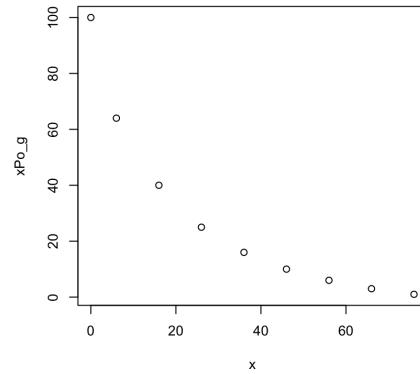
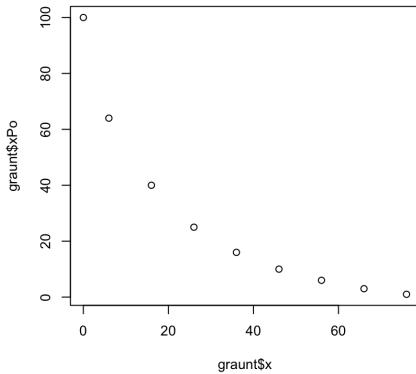
$X \geq 0, X \sim F(x) \Rightarrow X \equiv F^{-1}(U), U \sim U(0, 1)$, therefore,

$$E(X) = E\{F^{-1}(U)\} = \int_0^1 F^{-1}(u)du = \int_0^\infty 1 - F(x)dx = \int_0^\infty S(x)dx$$

Step by step approach to draw survival function plot

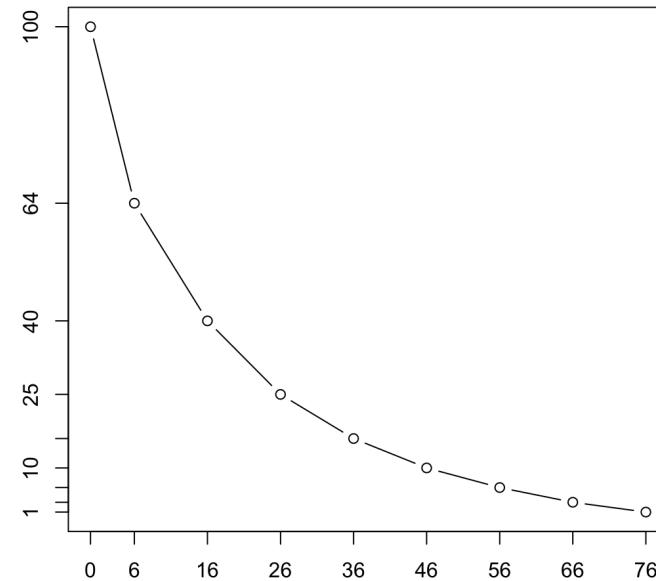
1. Basic plot with points and lines, compare the following threes methods

```
par(mfrow = c(2, 2))
plot(graunt$x, graunt$xPo)
plot(xPo_g ~ x, data = graunt)
plot(graunt)
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
```



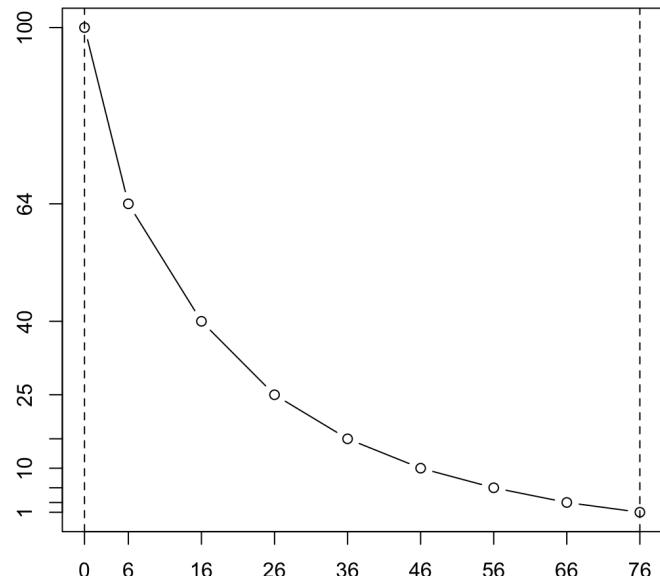
2. Denote the ages and observed survival rates on the axes

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g)
```



3. Denote the age 0 and 76 by dotted lines

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
```



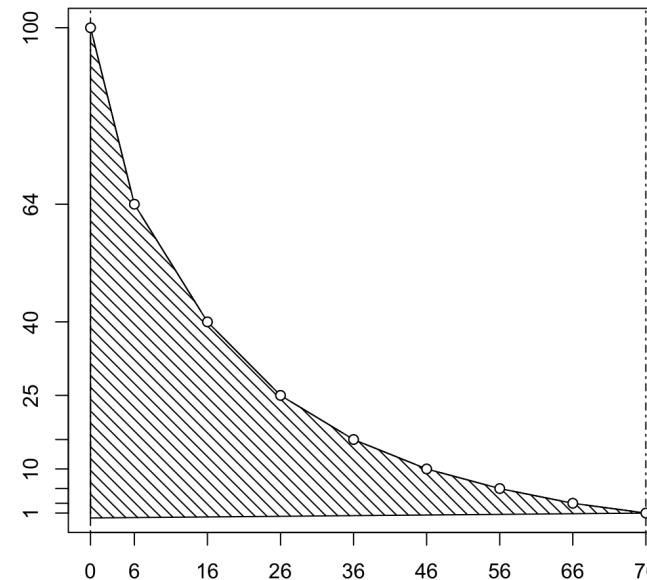
Setting up coordinates for polygon() (Clockwise)

```
graunt_x <- c(graunt$x, 0)
graunt_y <- c(graunt$xPo_g, 0)
graunt_poly <- data.frame(x = graunt_x, y = graunt_y)
```

4. Shading

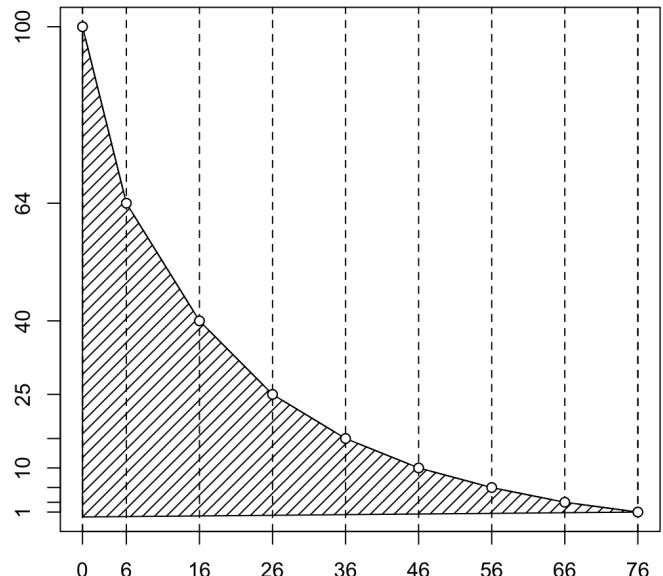
Note the effect of the last line of code.

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 4)
polygon(graunt_poly, density = 15, angle = 135)
points(graunt, pch = 21, col = "black", bg = "white")
```



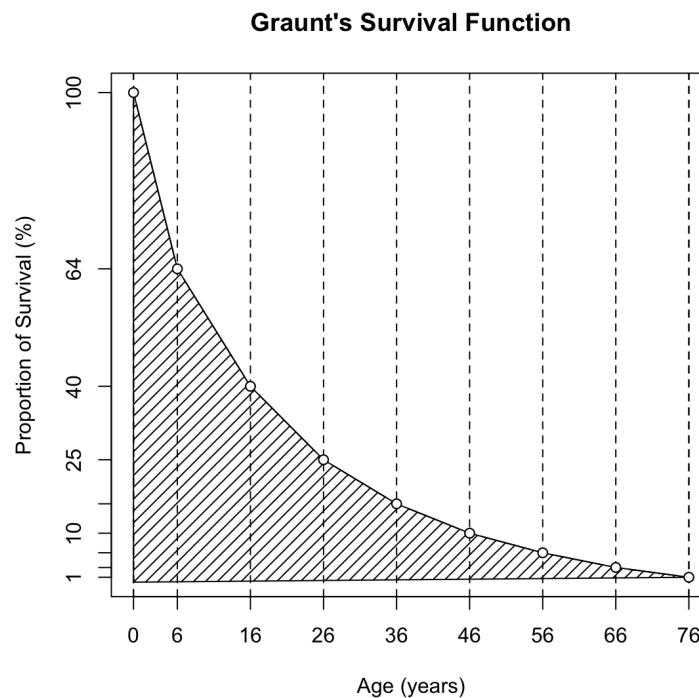
5. Grids

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
polygon(graunt_poly, density = 15)
abline(v = graunt$x, lty = 2)
points(graunt, pch = 21, col = "black", bg = "white")
```



6. Title, x-axis label, and y-axis label

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
polygon(graunt_poly, density = 15)
abline(v = graunt$x, lty = 2)
points(graunt, pch = 21, col = "black", bg = "white")
main_title <- "Graunt's Survival Function"
x_lab <- "Age (years)"
y_lab <- "Proportion of Survival (%)"
title(main = main_title, xlab = x_lab, ylab = y_lab)
```



Area under the curve

The area under the curve can be approximated by the sum of the areas of trapezoids, therefore the area is $\sum_{i=1}^{n-1} (x_{i+1} - x_i) \times \frac{1}{2}(y_i + y_{i+1})$.

- `diff()`, `head()`, and `tail()` can be used to write a function to compute the area easily.

```
area.R <- function(x, y) {
  sum(diff(x) * (head(y, -1) + tail(y, -1))/2)
}
area.R(graunt$x, graunt$xPo_g)/100
```

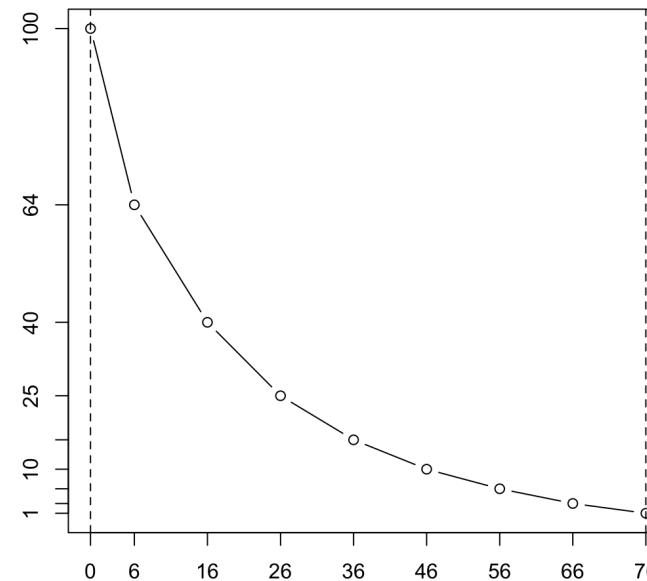
```
## [1] 18.17
```

Comparison with US 1993 life table

The shaded area between the survival function of Graunt and that of US 1993 represents the difference of life expectancies.

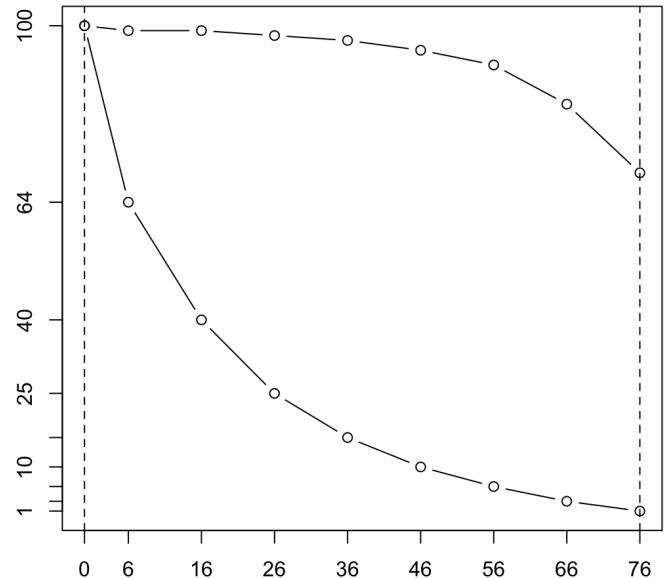
1. Draw Graunt's first with axes, lower and upper limits. Check what happens if you place `abline(...)` right after `plot(...)`.

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
```



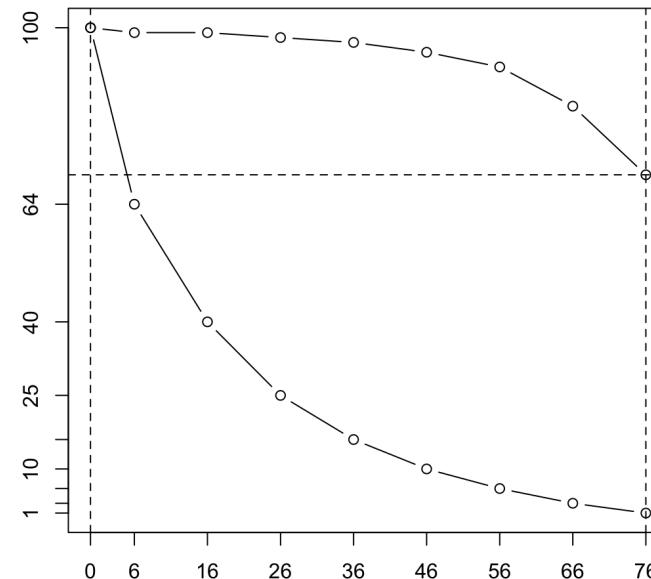
2. Add US 1993 survival function

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
lines(us93, type = "b")
```



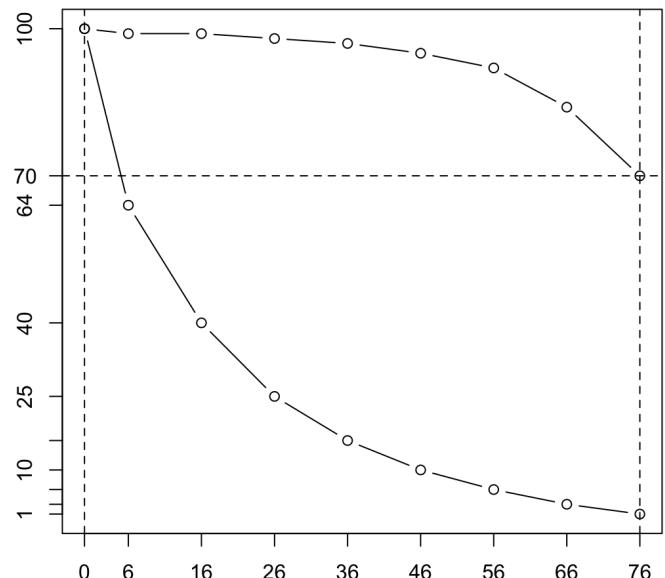
3. Actually, US 1993 life table is truncated at the age 76. Specify that point.

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
lines(us93, type = "b")
abline(h = 70, lty = 2)
```



4. Using las = 1 to specify 70%.

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
lines(us93, type = "b")
abline(h = 70, lty = 2)
axis(side = 2, at = 70, labels = 70, las = 1)
```



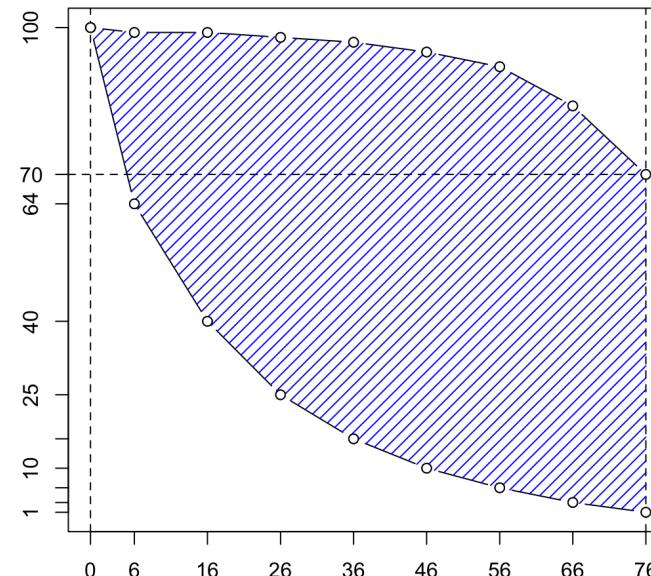
Setting coordinates for polygon()

```
us_graunt_x <- c(us93$x, rev(graunt$x))
us_graunt_y <- c(us93$xPo_us, rev(graunt$xPo_g))
us_graunt <- data.frame(x = us_graunt_x, y = us_graunt_y)
```

5. Shading

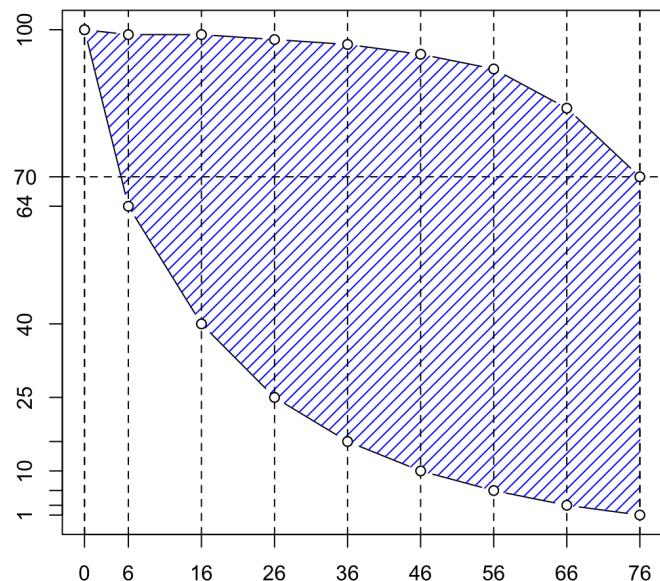
What is the effect of border = NA, the last line of code?

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
lines(us93, type = "b")
abline(h = 70, lty = 2)
axis(side = 2, at = 70, labels = 70, las = 1)
polygon(us_graunt, density = 15, col = "blue", border = NA)
points(us_graunt, pch = 21, col = "black", bg = "white")
```



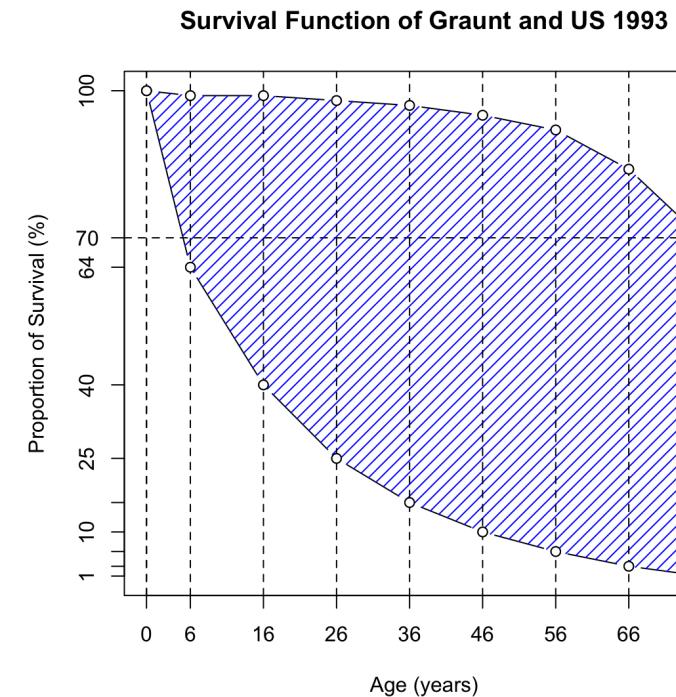
6. Grids

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
lines(us93, type = "b")
abline(h = 70, lty = 2)
axis(side = 2, at = 70, labels = 70, las = 1)
polygon(us_graunt, density = 15, col = "blue", border = NA)
abline(v = graunt$x, lty = 2)
points(us_graunt, pch = 21, col = "black", bg = "white")
```



7. Title, x-axis and y-axis labels

```
plot(graunt, ann = FALSE, xaxt = "n", yaxt = "n", type = "b")
axis(side = 1, at = graunt$x, labels = graunt$x)
axis(side = 2, at = graunt$xPo, labels = graunt$xPo_g)
abline(v = c(0, 76), lty = 2)
lines(us93, type = "b")
abline(h = 70, lty = 2)
axis(side = 2, at = 70, labels = 70, las = 1)
polygon(us_graunt, density = 15, col = "blue", border = NA)
abline(v = graunt$x, lty = 2)
points(us_graunt, pch = 21, col = "black", bg = "white")
main_title_g_us <- "Survival Function of Graunt and US 1993"
title(main = main_title_g_us, xlab = x_lab, ylab = y_lab)
```



```
# dev.copy(device = png, file = "../pics/graunt_us93.png")
```

Life expectancy

The area under the US 1993 survival function is

```
area.R(us93$x, us93$xPo_us)/100
```

```
## [1] 70.92
```

The area of shaded region is

```
area.R(us93$x, us93$xPo_us)/100 - area.R(graunt$x, graunt$xPo_g)/100
```

```
## [1] 52.75
```

Comparison with Halley's life table

Halley's life table

```
age <- 0:84
lx <- c(1238, 1000, 855, 798, 760, 732, 710, 692, 680, 670, 661, 653, 646, 640, 634,
628, 622, 616, 610, 604, 598, 592, 586, 579, 573, 567, 560, 553, 546, 539, 531, 523,
515, 507, 499, 490, 481, 472, 463, 454, 445, 436, 427, 417, 407, 397, 387, 377, 367,
357, 346, 335, 324, 313, 302, 292, 282, 272, 262, 252, 242, 232, 222, 212, 202, 192,
182, 172, 162, 152, 142, 131, 120, 109, 98, 88, 78, 68, 58, 50, 41, 34, 28, 23, 20)
length(lx)
```

```
## [1] 85
```

```
halley <- data.frame(age, lx)
halley$xPo <- round(halley$lx / lx[1] * 100, digits = 1)
head(halley)
```

```
##   age   lx   xPo
## 1   0 1238 100.0
## 2   1 1000  80.8
## 3   2   855  69.1
## 4   3   798  64.5
## 5   4   760  61.4
## 6   5   732  59.1
```

```
tail(halley)
```

```
##   age   lx   xPo
## 80  79 50  4.0
## 81  80 41  3.3
## 82  81 34  2.7
## 83  82 28  2.3
## 84  83 23  1.9
## 85  84 20  1.6
```

```
halley_lx <- halley[-3]
halley <- halley[-2]
head(halley)
```

```
##   age   xPo
## 1   0 100.0
## 2   1  80.8
## 3   2  69.1
## 4   3  64.5
## 5   4  61.4
## 6   5  59.1
```

```
tail(halley)
```

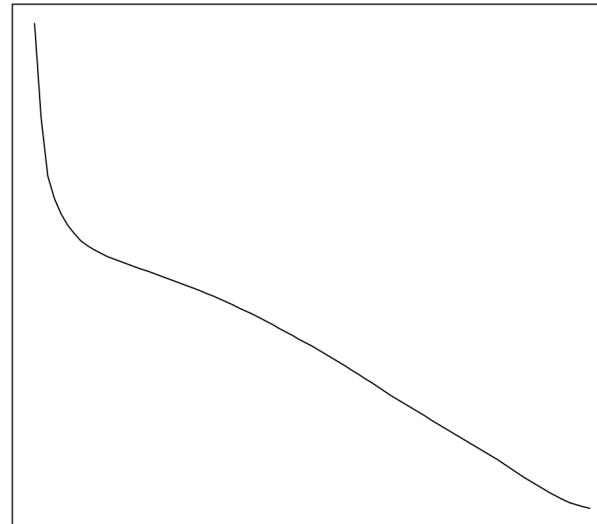
```
##     age xPo
## 80    79 4.0
## 81    80 3.3
## 82    81 2.7
## 83    82 2.3
## 84    83 1.9
## 85    84 1.6
```

R base graphics

To make the comparison easy, plot the points at the same age group of Graunt's, 0, 6, 16, 26, 36, 46, 56, 66, 76. Step by step approach

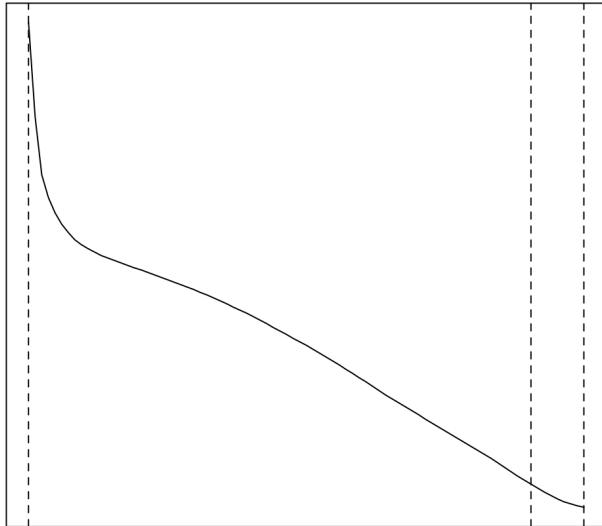
1. Halley's survival function first

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
```



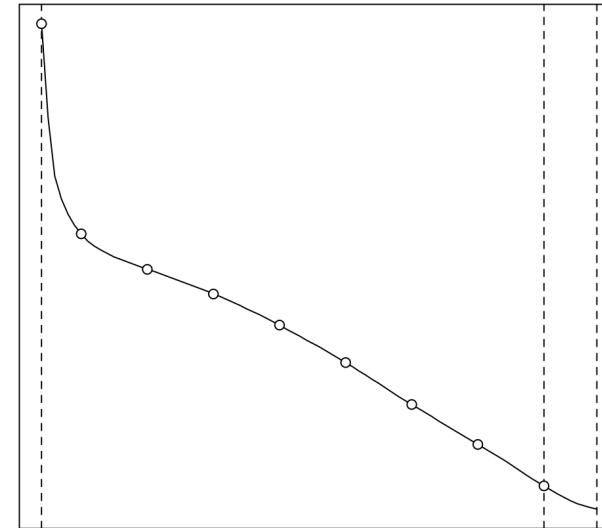
2. Denote the age at 0, 76, and 84 by vertical dotted lines

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
```



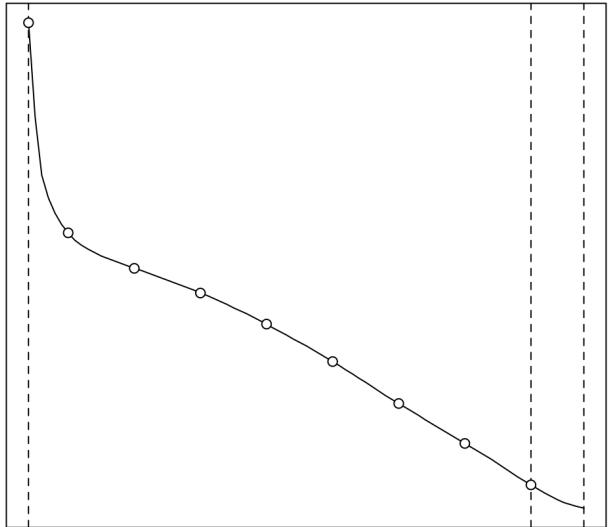
3. Mark the points at 0, 6, 16, 26, 36, 46, 56, 66, 76 on Halley's survival function.

```
age_graunt <- age %in% graunt$x
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(xPo[age_graunt] ~ age[age_graunt], data = halley, pch = 21, col = "black", bg = "white")
```



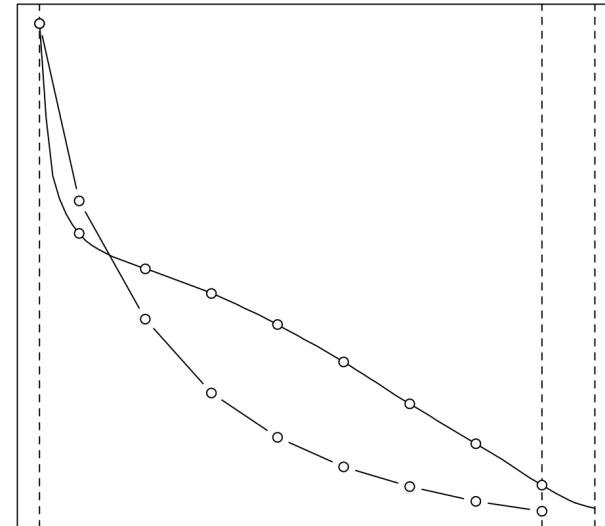
Using subset()

```
halley_graunt <- subset(halley, age_graunt)
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
```



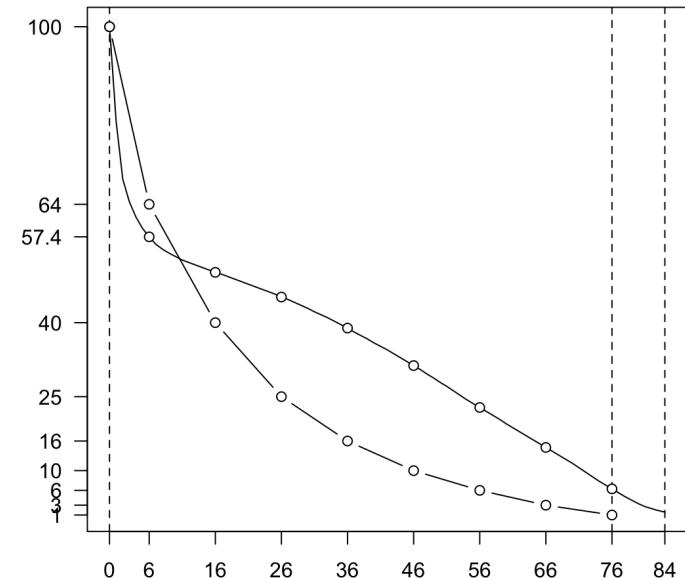
4. Add Graunt's survival function

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
```



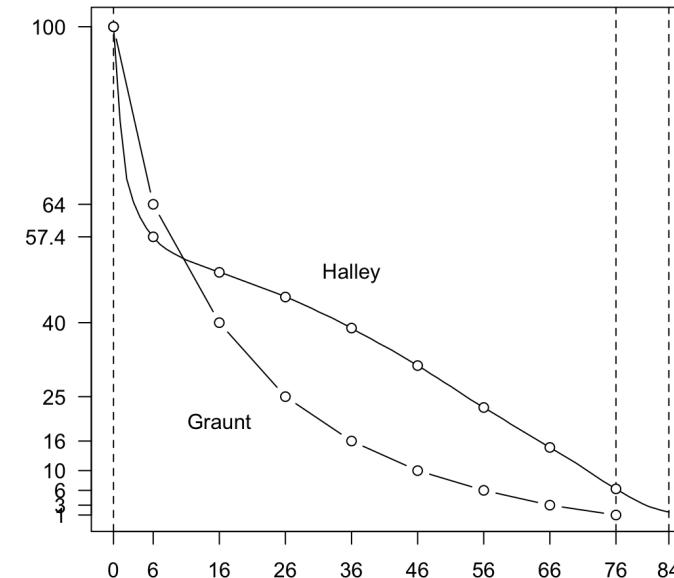
5. x-axis label and y-axis label with `las = 1`. Add Halley's proportion of survival at `age = 6`.

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(graunt$x, 84), labels = c(graunt$x, 84))
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g, las = 1)
xPo_halley_age_6 <- halley$xPo[age == 6]
axis(side = 2, at = xPo_halley_age_6, labels = xPo_halley_age_6, las = 1)
```



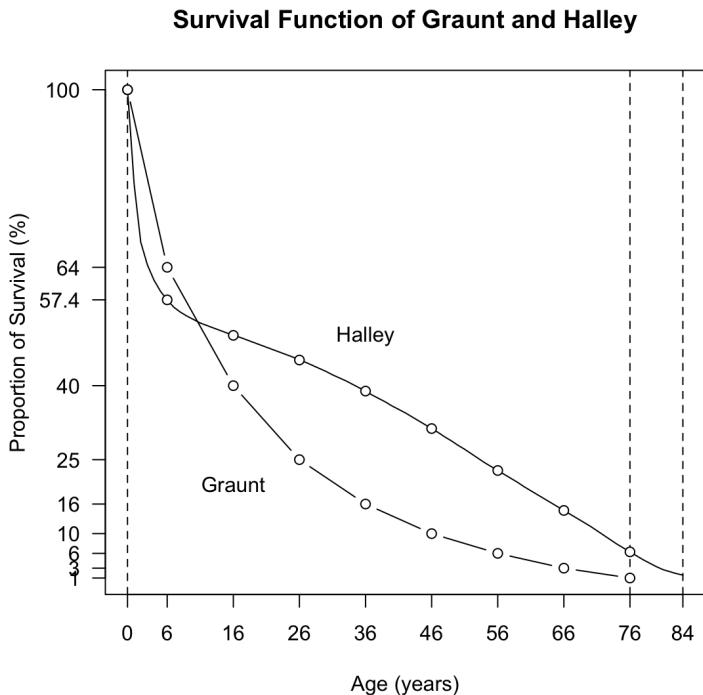
6. Specify the developers at proper coordinates with `text()`

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(graunt$x, 84), labels = c(graunt$x, 84))
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g, las = 1)
axis(side = 2, at = xPo_halley_age_6, labels = xPo_halley_age_6, las = 1)
text(x = c(16, 36), y = c(20, 50), label = c("Graunt", "Halley"))
```



7. Main title, x-axis label, and y-axis label

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(grault, pch = 21, col = "black", bg = "white")
lines(grault, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(grault$x, 84), labels = c(grault$x, 84))
axis(side = 2, at = grault$xPo_g, labels = grault$xPo_g, las = 1)
axis(side = 2, at = xPo_halley_age_6, labels = xPo_halley_age_6, las = 1)
text(x = c(16, 36), y = c(20, 50), label = c("Graunt", "Halley"))
main_title_2 <- "Survival Function of Graunt and Halley"
title(main = main_title_2, xlab = x_lab, ylab = y_lab)
```



Polygon

Setting the coordinates for `polygon()`. The intersection is found at $x = 10.8$, $y = 52.8$ with `locator(1)` and couple of trial and errors.

- Upper region

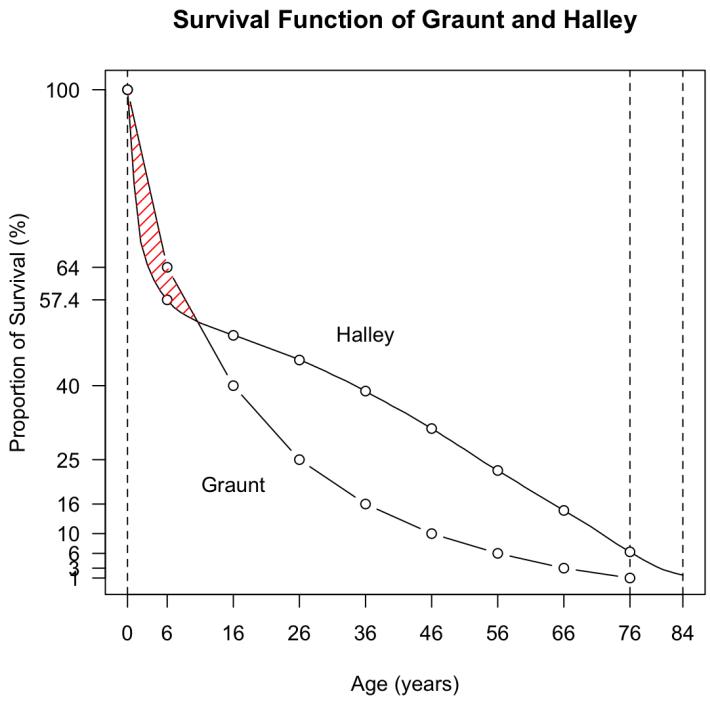
```
poly_1_x <- c(grault$x[1:2], 10.8, halley$age[11:1])
poly_2_x <- c(grault$xPo_g[1:2], 52.8, halley$xPo[11:1])
poly_upper <- data.frame(x = poly_1_x, y = poly_2_x)
```

- Lower region

```
poly_2_x <- c(10.8, halley$age[12:85], grault$x[9:3])
poly_2_y <- c(52.8, halley$xPo[12:85], grault$xPo_g[9:3])
poly_lower <- data.frame(x = poly_2_x, y = poly_2_y)
```

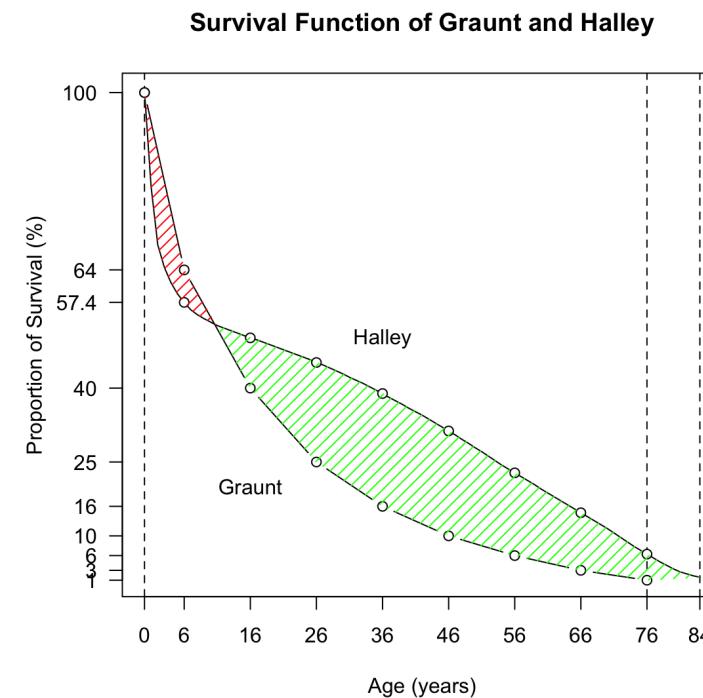
8. Shading upper region first

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(graunt$x, 84), labels = c(graunt$x, 84))
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g, las = 1)
axis(side = 2, at = xPo_halley_age_6, labels = xPo_halley_age_6, las = 1)
text(x = c(16, 36), y = c(20, 50), label = c("Graunt", "Halley"))
title(main = main_title_2, xlab = x_lab, ylab = y_lab)
polygon(poly_upper, angle = 45, density = 15, col = "red", border = NA)
```



9. Shading lower region next

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(graunt$x, 84), labels = c(graunt$x, 84))
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g, las = 1)
axis(side = 2, at = xPo_halley_age_6, labels = xPo_halley_age_6, las = 1)
text(x = c(16, 36), y = c(20, 50), label = c("Graunt", "Halley"))
title(main = main_title_2, xlab = x_lab, ylab = y_lab)
polygon(poly_upper, angle = 45, density = 15, col = "red", border = NA)
polygon(poly_lower, angle = 45, density = 15, col = "green", border = NA)
```



10. Fill the points. Extra points at the 84.

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(graunt_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(graunt$x, 84), labels = c(graunt$x, 84))
axis(side = 2, at = graunt$xPo_g, labels = graunt$xPo_g, las = 1)
axis(side = 2, at = xPo_halley_age_6, labels = xPo_halley_age_6, las = 1)
text(x = c(16, 36), y = c(20, 50), label = c("Graunt", "Halley"))
title(main = main_title_2, xlab = x_lab, ylab = y_lab)
polygon(poly_upper, angle = 45, density = 15, col = "red", border = NA)
polygon(poly_lower, angle = 45, density = 15, col = "green", border = NA)
points(graunt, pch = 21, col = "black", bg = "white")
points(halley_graunt, pch = 21, col = "black", bg = "white")
points(x = 84, y = halley$xPo[85], pch = 21, col = "black", bg = "white")
```

Life expectancy

Compute the difference of life expectancies

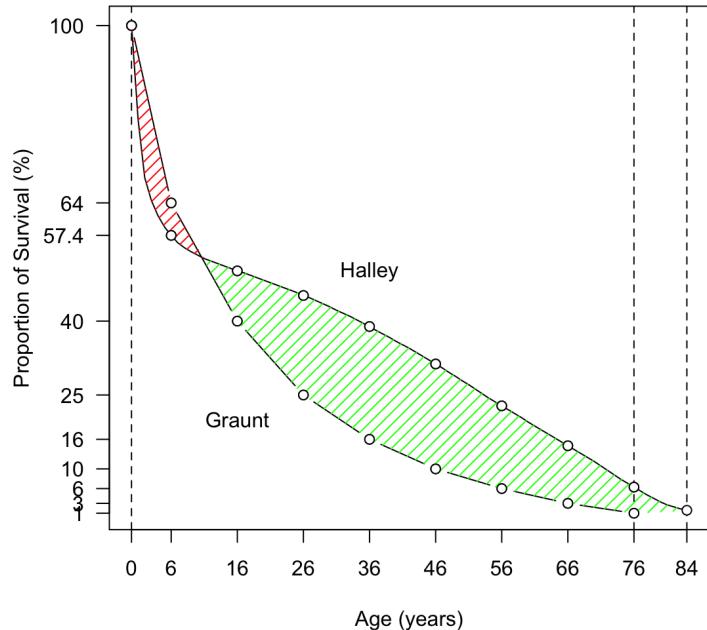
```
(life_exp_halley <- area.R(halley$age, halley$xPo)/100)
```

```
## [1] 27.872
```

```
(life_exp_graunt <- area.R(graunt$x, graunt$xPo_g)/100)
```

```
## [1] 18.17
```

Survival Function of Graunt and Halley



```
# dev.copy(device = png, file = "../pics/graunt_halley_png")
```

Graunt, Halley, and US 1993

Polygon with R Base Plot

Coordinates

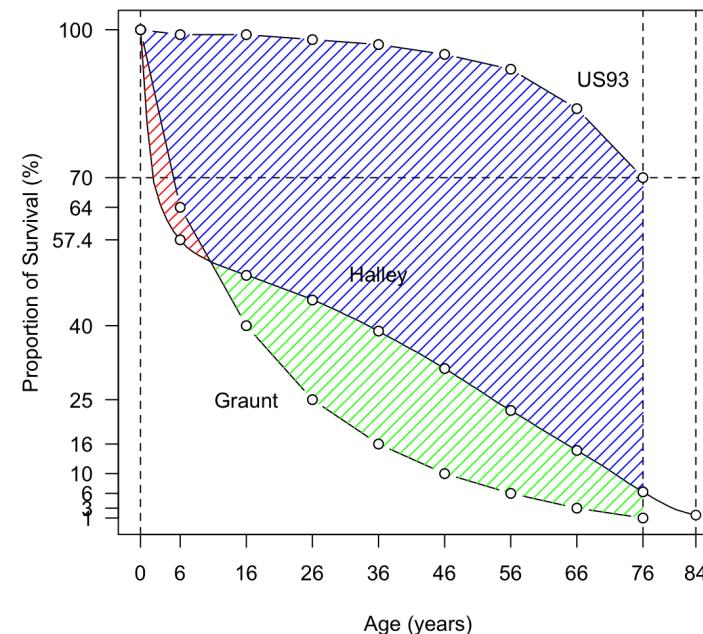
In order to make the graphs truncated at the age 76, restrict the age of Halley up to 76.

```
graunt_2 <- graunt
halley_2 <- halley
us93_2 <- us93
names(graunt_2) <- c("x", "Graunt")
names(halley_2) <- c("x", "Halley")
names(us93_2) <- c("x", "US93")
poly_lower_76 <- subset(poly_lower, poly_lower$x <= 76)
poly_3_x <- c(us93_2$x, halley_2$x[85:12], 10.8, graunt_2$x[2:1])
poly_3_y <- c(us93_2$US93, halley_2$Halley[85:12], 52.8, graunt_2$Graunt[2:1])
poly_us <- data.frame(x = poly_3_x, y = poly_3_y)
poly_us_76 <- subset(poly_us, poly_us$x <= 76)
```

Straight to Polygon

```
plot(halley, ann = FALSE, xaxt = "n", yaxt = "n", type = "l")
abline(v = c(0, 76, 84), lty = 2)
points(halley_graunt, pch = 21, col = "black", bg = "white")
lines(graunt, type = "b", pch = 21, col = "black", bg = "white")
lines(us93, type = "b", pch = 21, col = "black", bg = "white")
axis(side = 1, at = c(graunt$x, 84), labels = c(graunt$x, 84))
axis(side = 2, at = c(graunt$xPo_g, xPo_halley_age_6), labels = c(graunt$xPo_g, xPo_halley_age_6), las = 1)
abline(h = 70, lty = 2)
axis(side = 2, at = 70, labels = 70, las = 1)
main_title_3 <- "Survival Function Plots"
title(main = main_title_3, xlab = x_lab, ylab = y_lab)
polygon(poly_upper, angle = 45, density = 15, col = "red", border = NA)
polygon(poly_lower_76, angle = 45, density = 15, col = "green", border = NA)
polygon(poly_us_76, angle = 45, density = 15, col = "blue", border = NA)
points(graunt, pch = 21, col = "black", bg = "white")
points(halley_graunt, pch = 21, col = "black", bg = "white")
points(us93_2, pch = 21, col = "black", bg = "white")
points(x = 84, y = halley$xPo[85], pch = 21, col = "black", bg = "white")
text(x = c(16, 36, 70), y = c(25, 50, 90), label = c("Graunt", "Halley", "US93"))
```

Survival Function Plots



```
# dev.copy(device = png, file = ".../pics/graunt_halley_us93_poly.png")
```

ggplot

```
library(ggplot2)
```

Data Reshape

Attach `reshape2` package to change wide format to long format

```
library(reshape2)
```

How `melt()` works

```
graunt_us_melt <- melt(graunt_us,
                        id.vars = "x",
                        measure.vars = c("xPo_g", "xPo_us"),
                        value.name = "xPo",
                        variable.name = "times")
graunt_us_melt
```

```
##      x  times xPo
## 1    0 xPo_g 100
## 2    6 xPo_g  64
## 3   16 xPo_g  40
## 4   26 xPo_g  25
## 5   36 xPo_g  16
## 6   46 xPo_g  10
## 7   56 xPo_g   6
## 8   66 xPo_g   3
## 9   76 xPo_g   1
## 10  0 xPo_us 100
## 11  6 xPo_us  99
## 12 16 xPo_us  99
## 13 26 xPo_us  98
## 14 36 xPo_us  97
## 15 46 xPo_us  95
## 16 56 xPo_us  92
## 17 66 xPo_us  84
## 18 76 xPo_us  70
```

```
str(graunt_us_melt)
```

```
## 'data.frame': 18 obs. of 3 variables:
## $ x     : num  0 6 16 26 36 46 56 66 76 0 ...
## $ times: Factor w/ 2 levels "xPo_g","xPo_us": 1 1 1 1 1 1 1 1 1 2 ...
## $ xPo  : num  100 64 40 25 16 10 6 3 1 100 ...
```

- Change factor levels of `times`

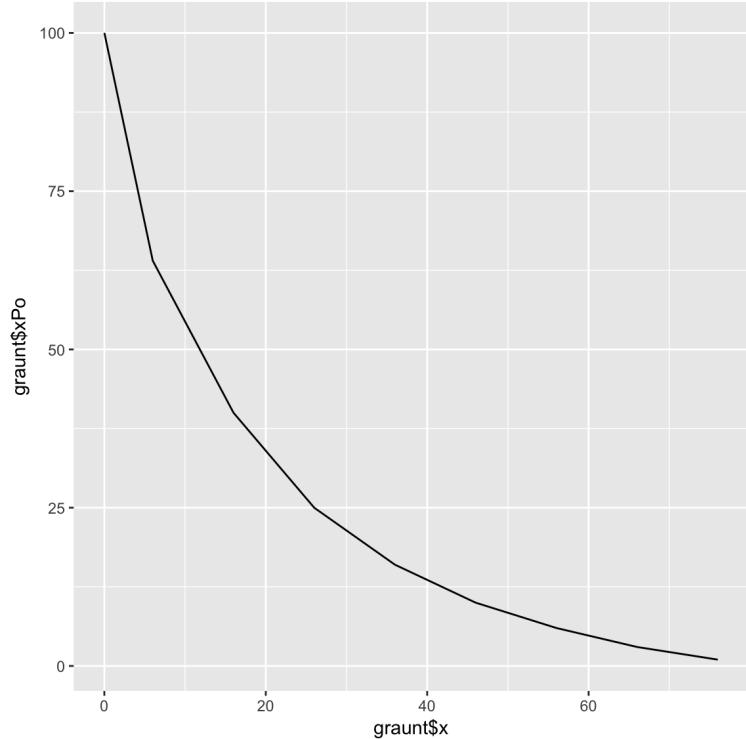
```
levels(graunt_us_melt$times) <- c("Graunt", "US1993")
graunt_us_melt
```

```
##      x  times xPo
## 1    0 Graunt 100
## 2    6 Graunt  64
## 3   16 Graunt  40
## 4   26 Graunt  25
## 5   36 Graunt  16
## 6   46 Graunt  10
## 7   56 Graunt   6
## 8   66 Graunt   3
## 9   76 Graunt   1
## 10  0 US1993 100
## 11  6 US1993  99
## 12 16 US1993  99
## 13 26 US1993  98
## 14 36 US1993  97
## 15 46 US1993  95
## 16 56 US1993  92
## 17 66 US1993  84
## 18 76 US1993  70
```

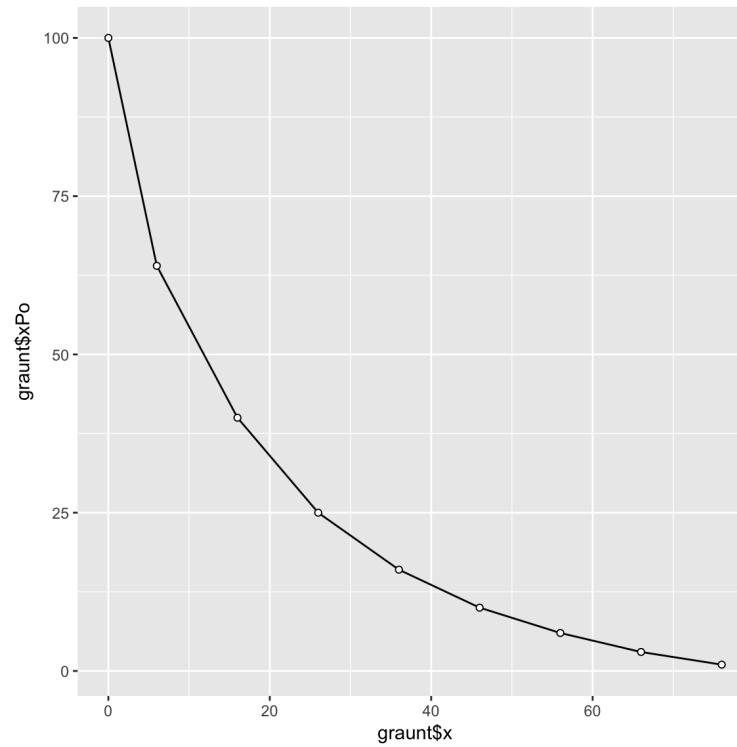
Graunt

Structure of ggplot

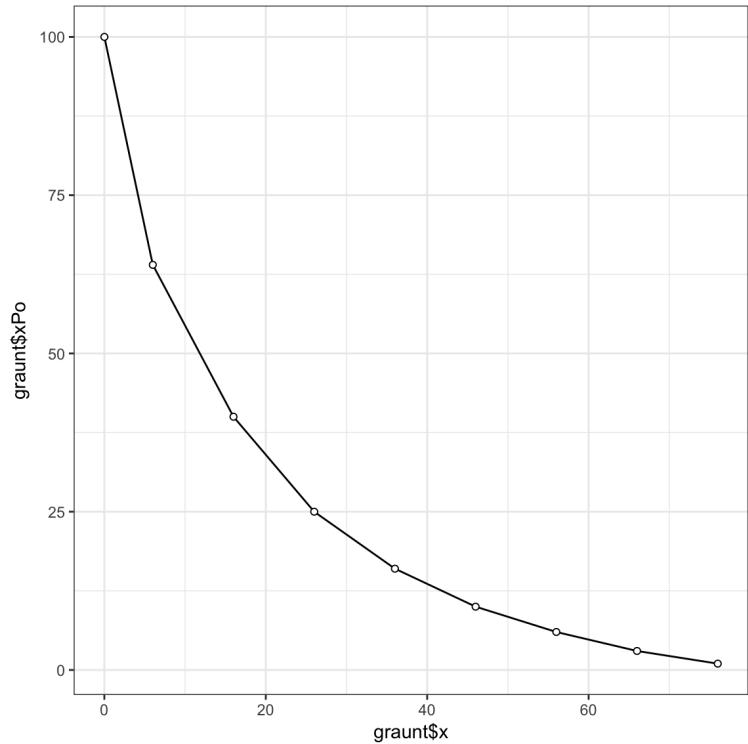
```
(g1 <- ggplot() +  
  geom_line(data = graunt,  
            mapping = aes(x = graunt$x, y = graunt$xPo)))
```



```
(g2 <- g1 +  
  geom_point(data = graunt,  
             mapping = aes(x = graunt$x, y = graunt$xPo),  
             shape = 21, fill = "white"))
```

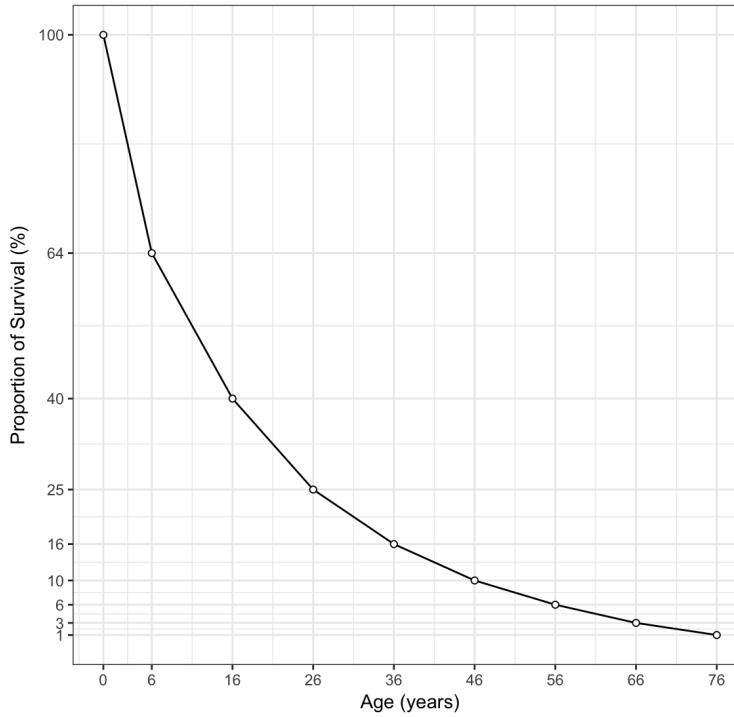


```
(g3 <- g2 +  
  theme_bw())
```

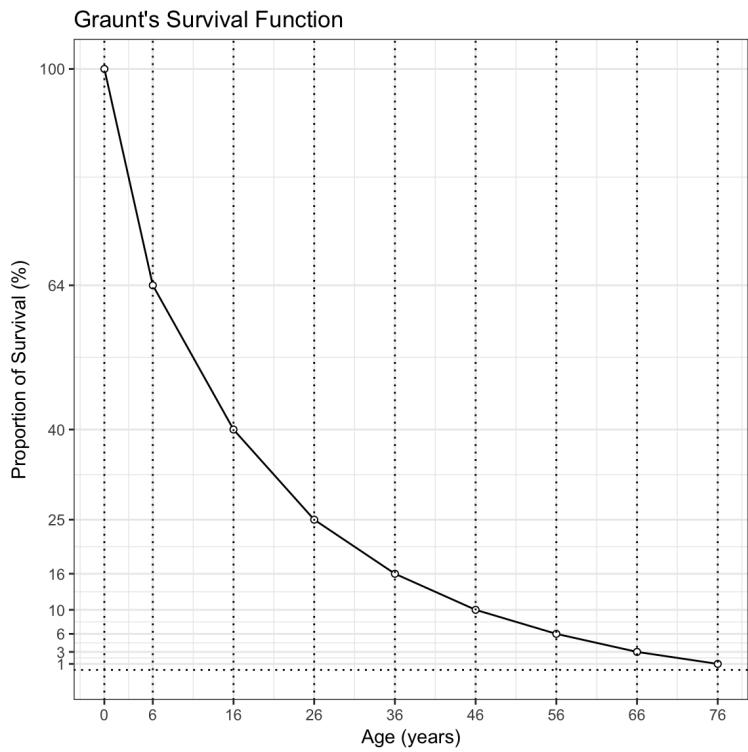


```
(g4 <- g3 +  
  xlab(x_lab) +  
  ylab(y_lab) +  
  ggtitle(main_title) +  
  scale_x_continuous(breaks = graunt$x) +  
  scale_y_continuous(breaks = graunt$xPo_g))
```

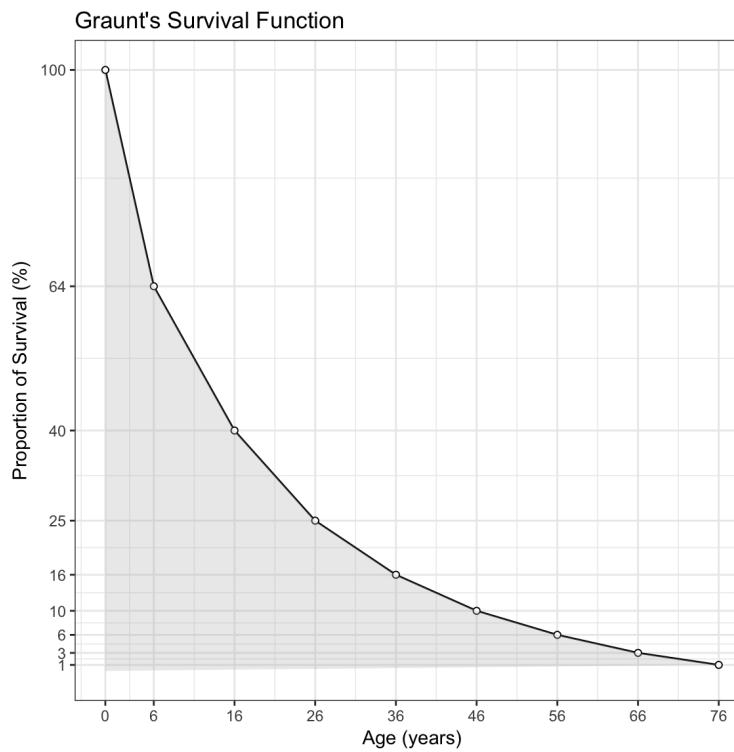
Graunt's Survival Function



```
(g5 <- g4 +
  geom_vline(xintercept = graunt$x, linetype = "dotted") +
  geom_hline(yintercept = 0, linetype = "dotted"))
```



```
(pg4 <- g4 +
  geom_polygon(data = graunt_poly,
    mapping = aes(x = x, y = y),
    alpha = 0.3, fill = "grey"))
```



```
# ggsave("../pics/graunt_poly_ggplot.png", pg4)
```

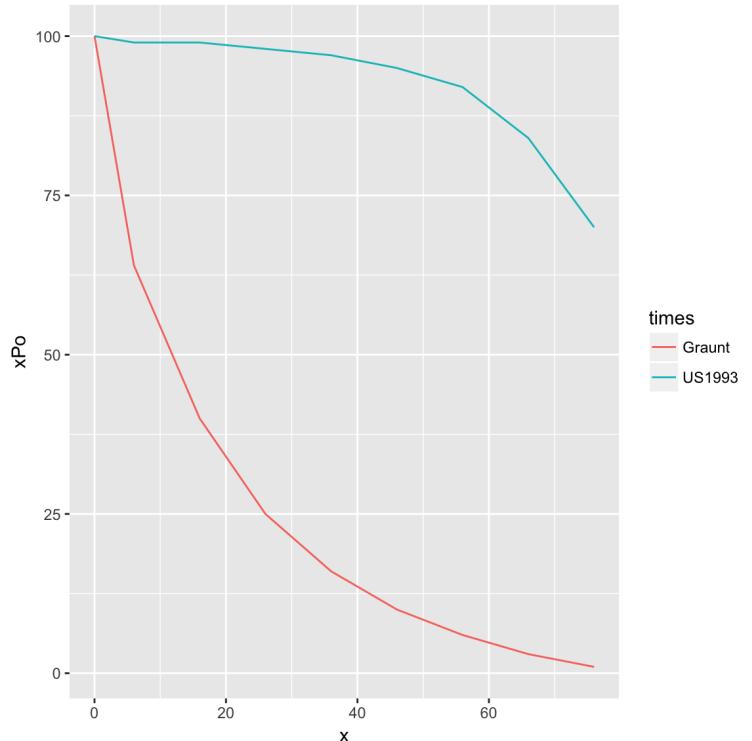
Graunt and US 1993

Points and Lines

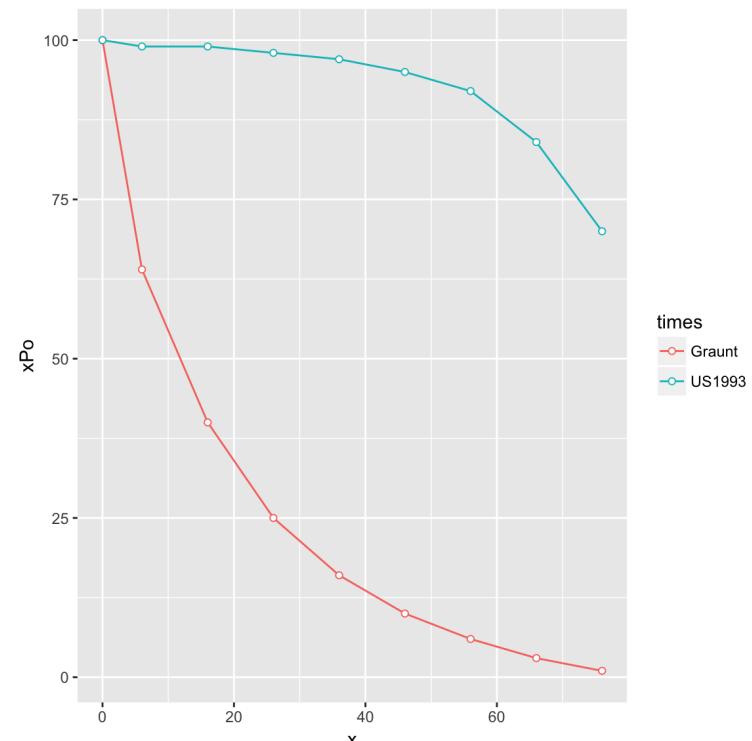
Step by step approach to understand the grammar of ggplot

- We set `ggplot()` to accept varying `data.frame()` and `aes()` in `geom_polygon`

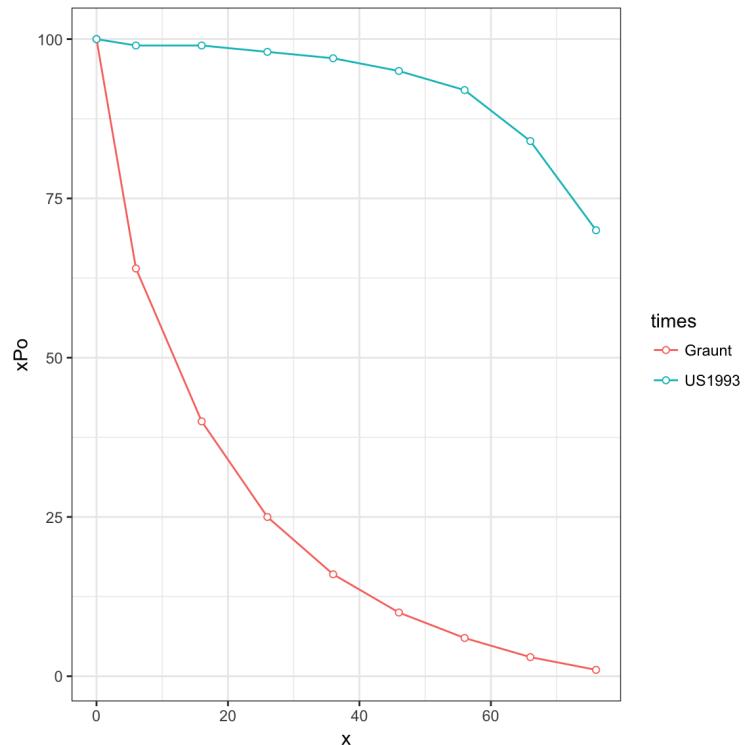
```
(gu1 <- ggplot() +  
  geom_line(data = graunt_us_melt,  
            mapping = aes(x = x, y = xPo, colour = times)))
```



```
(gu2 <- gu1 +  
  geom_point(data = graunt_us_melt,  
             mapping = aes(x = x, y = xPo, colour = times),  
             shape = 21, fill = "white"))
```



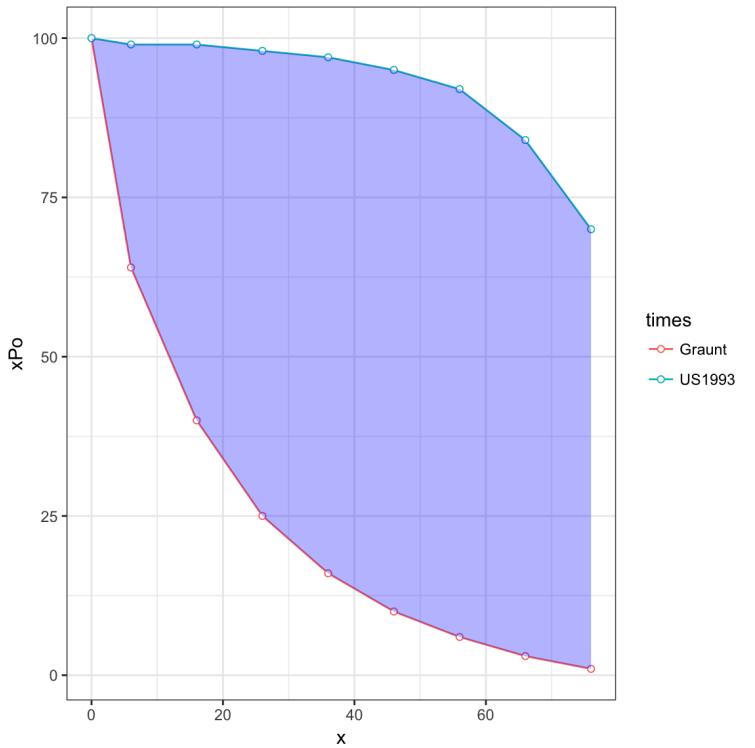
```
(gu3 <- gu2 +  
  theme_bw())
```



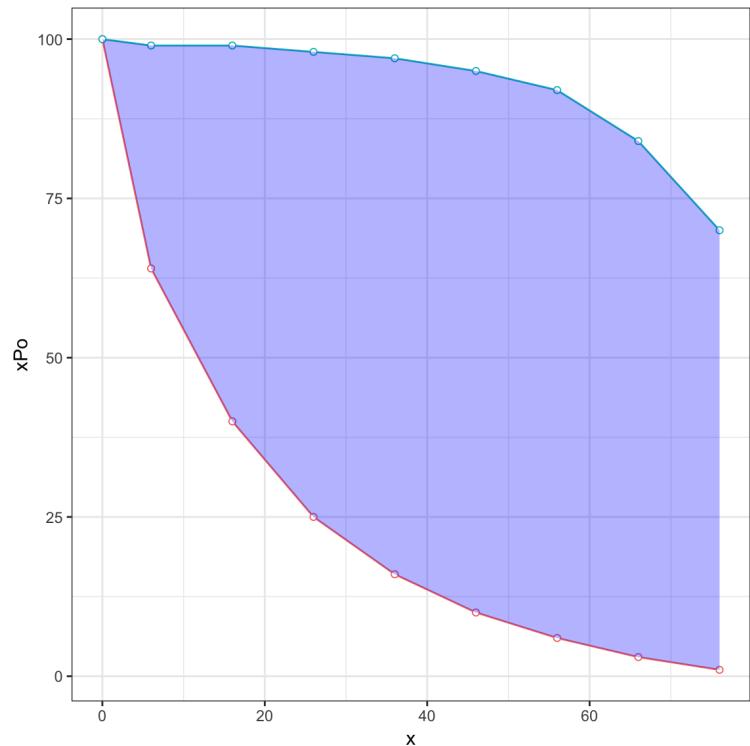
Polygon

Reuse `us_graunt` which contains `x = us_graunt_x` and `y = us_graunt_y` for `polygon()`. Note that we start with `gu3`, and also note how to remove default legends.

```
(gup3 <- gu3 +  
  geom_polygon(data = us_graunt,  
               mapping = aes(x = x, y = y),  
               alpha = 0.3, fill = "blue"))
```



```
(gup4 <- gup3 +  
  guides(colour = "none"))
```

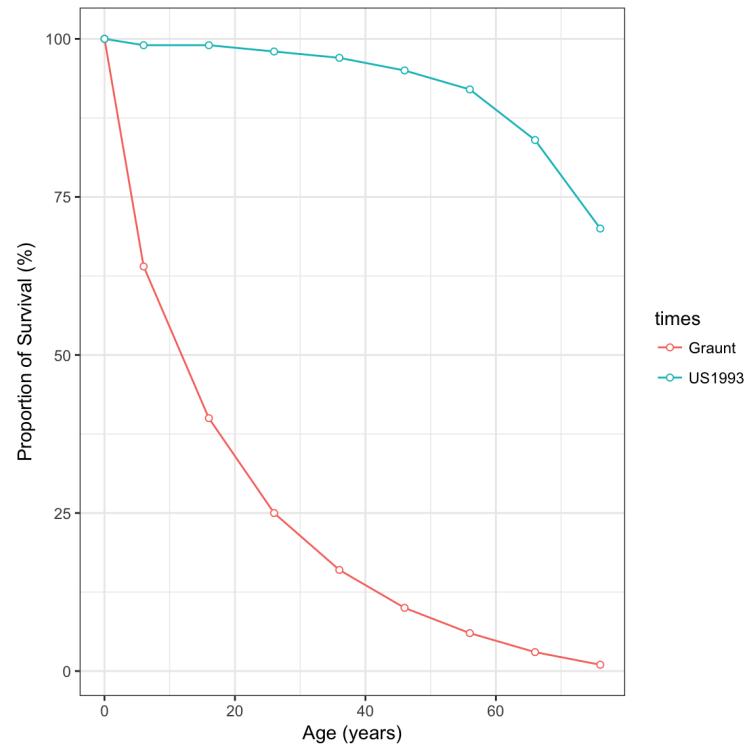


Change default annotations

Points and Lines

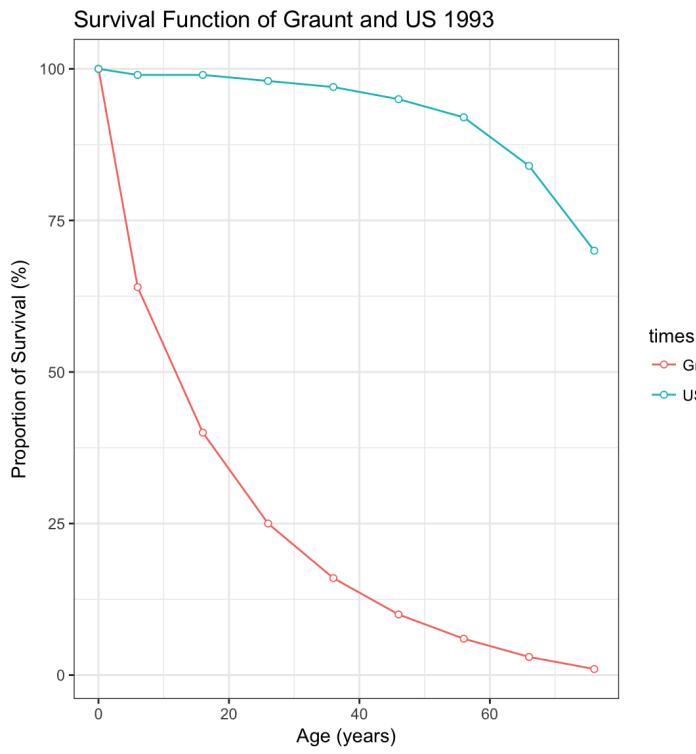
1. Change the x-axis and y-axis labels

```
(gu4 <- gu3 +  
  xlab(x_lab) +  
  ylab(y_lab))
```



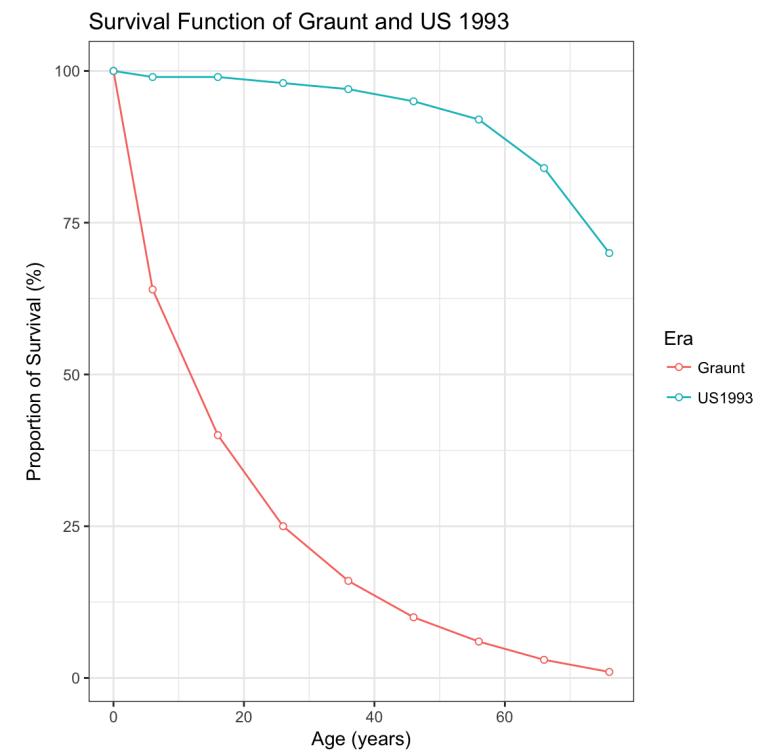
2. Add main title

```
(gu4 <- gu3 +  
  xlab(x_lab) +  
  ylab(y_lab) +  
  ggtitle(main_title_g_us))
```



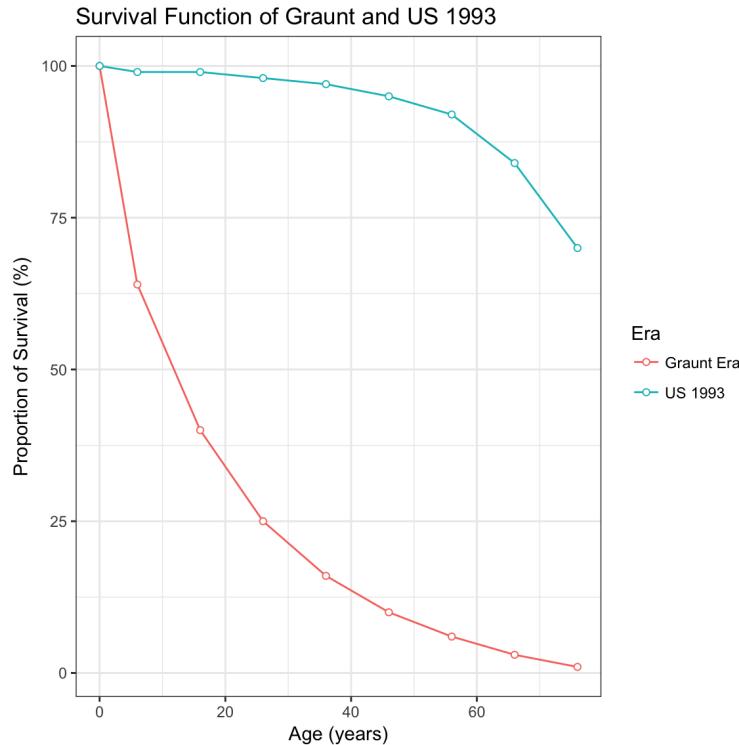
3. Change legend title

```
(gu4 <- gu3 +  
  xlab(x_lab) +  
  ylab(y_lab) +  
  ggtitle(main_title_g_us) +  
  labs(colour = "Era"))
```



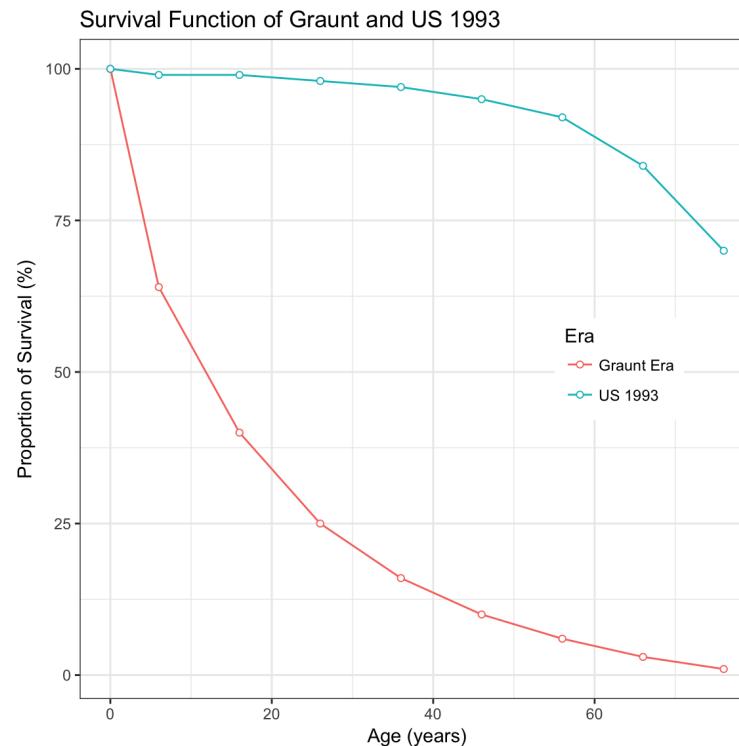
4. Change legends.

```
(gu4 <- gu3 +  
  xlab(x_lab) +  
  ylab(y_lab) +  
  ggtitle(main_title_g_us) +  
  labs(colour = "Era") +  
  scale_colour_discrete(labels = c("Graunt Era", "US 1993")))
```



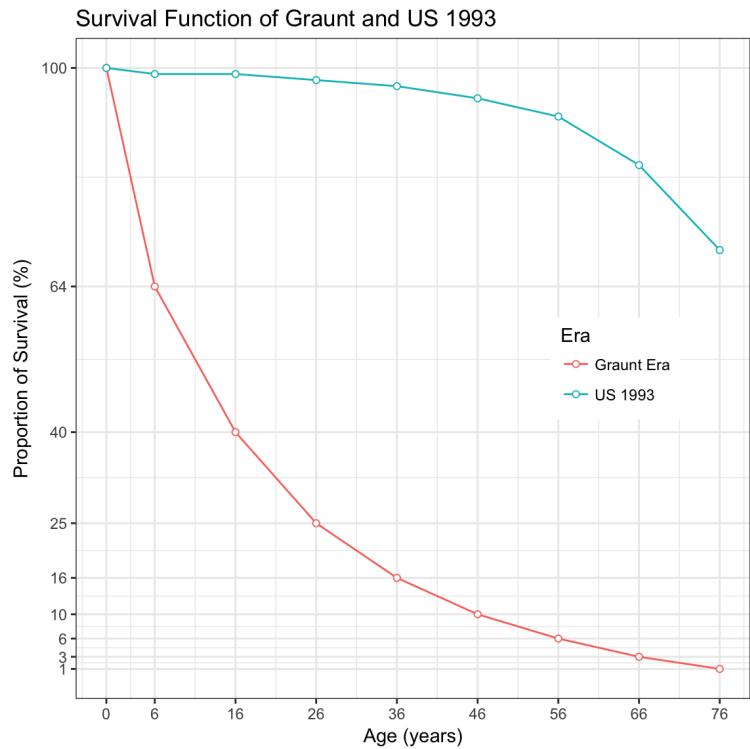
5. Place legends inside the plot

```
(gu5 <- gu4 +  
  theme(legend.position = c(0.8, 0.5)))
```



6. Change x-axis and y-axis tick marks

```
(gu6 <- gu5 +  
  scale_x_continuous(breaks = graunt$x) +  
  scale_y_continuous(breaks = graunt$xPo_g))
```



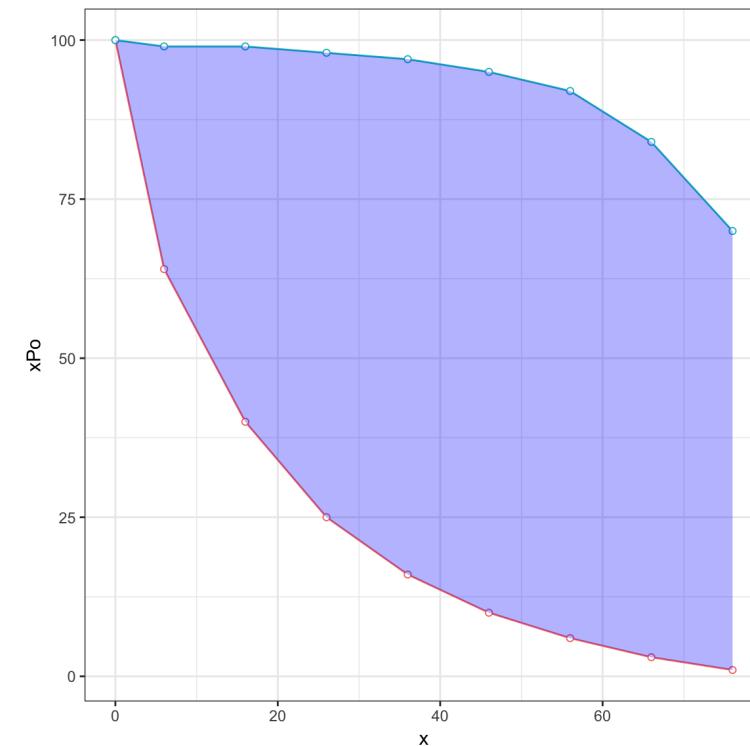
```
# ggsave("../pics/graunt_us_ggplot.png", gu6)
```

Polygon

Add information to the plot drawn with `polygon()`

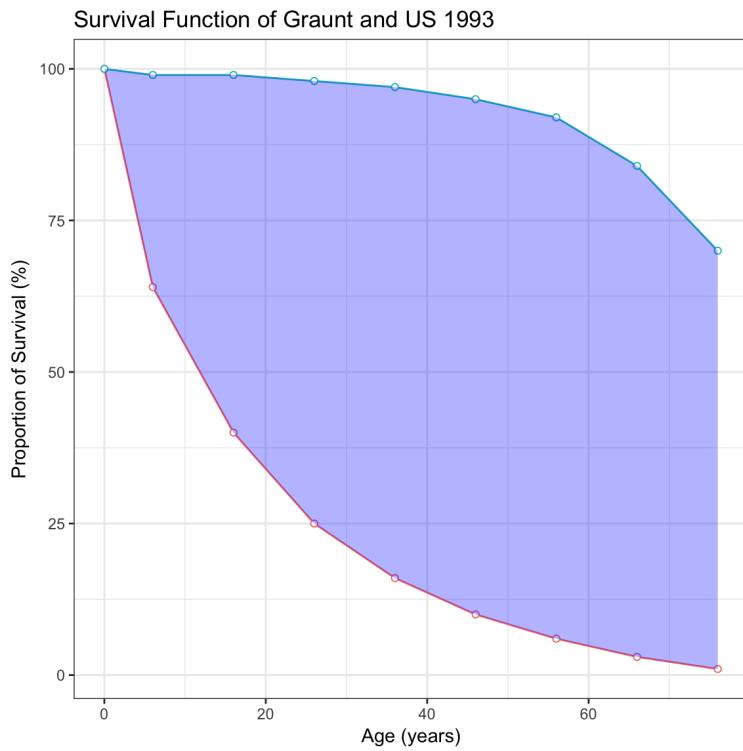
1. Start with `gup4`

gup4



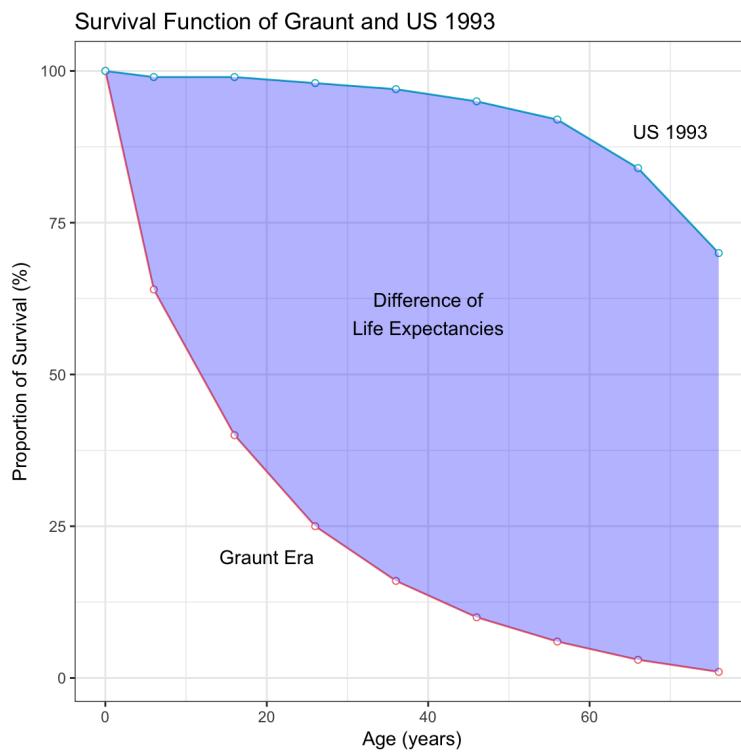
2. Main title, x-axis and y-axis labels

```
(gup5 <- gup4 +  
  xlab(x_lab) +  
  ylab(y_lab) +  
  ggtitle(main_title_g_us))
```



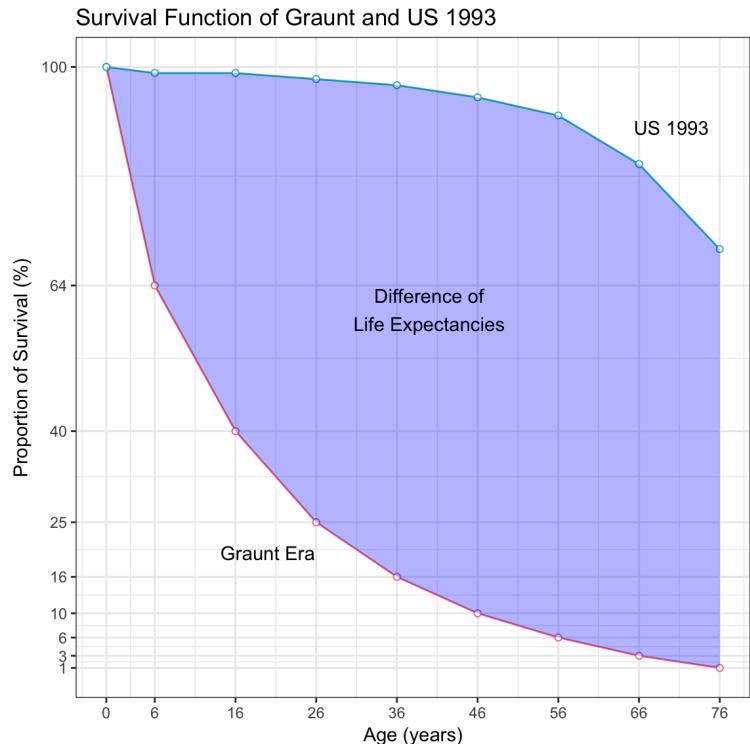
3. "Graunt Era", "US 1993", "Difference of Life Expectancies" at proper positions

```
(gup6 <- gup5 +  
  annotate("text",  
    x = c(20, 40, 70), y = c(20, 60, 90),  
    label = c("Graunt Era", "Difference of\nLife Expectancies", "US 1993"),  
    family = ""))
```



4. x-axis and y-axis tick marks

```
(gup7 <- gup6 +
  scale_x_continuous(breaks = graunt$x) +
  scale_y_continuous(breaks = graunt$xPo_g))
```



```
# ggsave("../pics/graunt_us_poly.png", gup7)
```

Graunt and Halley

Data Reshaping

Since the observed ages are different, we need final structure of the data frame to be melted. So, create copies of `graunt` and `halley` and extract parts of what we need and give feasible names.

```
graunt_halley_melt <- melt(list(graunt_2, halley_2),
  id.vars = "x",
  value.name = "xPo",
  variable.name = "Who")
str(graunt_halley_melt)
```

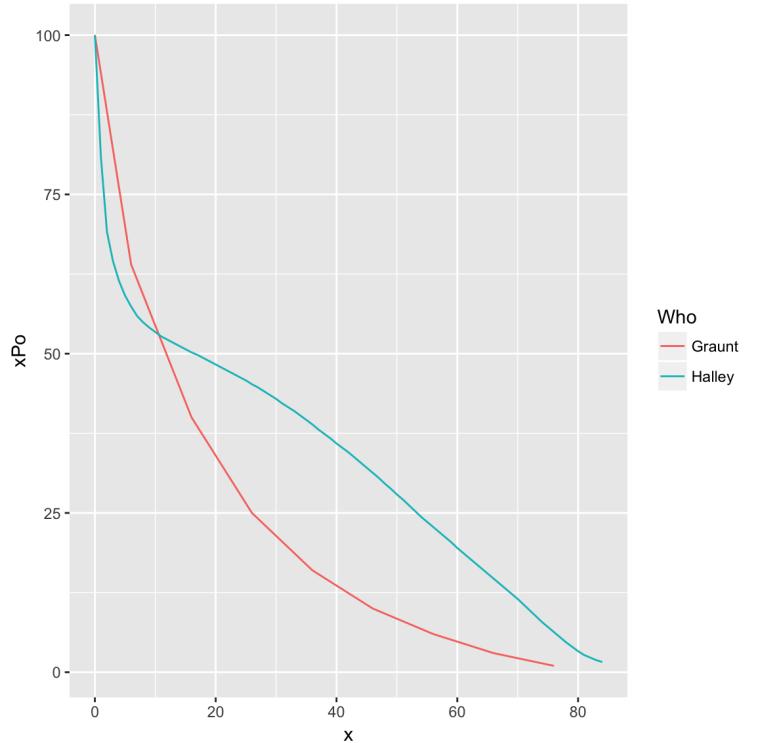
```
## 'data.frame': 94 obs. of 4 variables:
## $ x : num 0 6 16 26 36 46 56 66 76 0 ...
## $ Who: Factor w/ 2 levels "Graunt", "Halley": 1 1 1 1 1 1 1 1 1 2 ...
## $ xPo: num 100 64 40 25 16 10 6 3 1 100 ...
## $ L1 : int 1 1 1 1 1 1 1 1 1 2 ...
```

```
graunt_halley_melt <- graunt_halley_melt[-4]
(graunt_halley_melt_g <- subset(graunt_halley_melt,
  graunt_halley_melt$x %in% graunt$x))
```

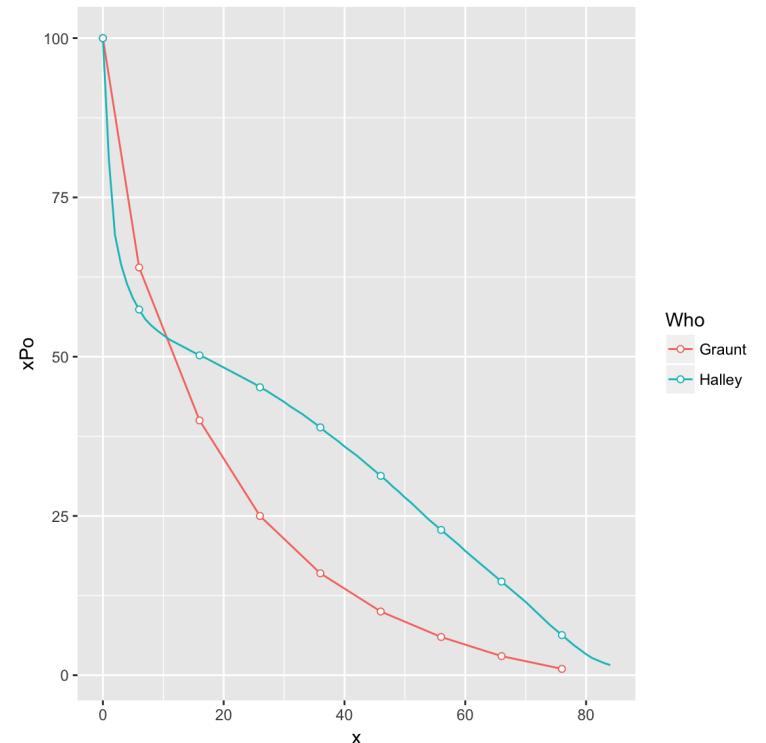
```
##      x     Who   xPo
## 1    0  Graunt 100.0
## 2    6  Graunt  64.0
## 3   16  Graunt  40.0
## 4   26  Graunt  25.0
## 5   36  Graunt  16.0
## 6   46  Graunt  10.0
## 7   56  Graunt   6.0
## 8   66  Graunt   3.0
## 9   76  Graunt   1.0
## 10  0  Halley 100.0
## 11  6  Halley  57.4
## 12 16  Halley  50.2
## 13 26  Halley  45.2
## 14 36  Halley  38.9
## 15 46  Halley  31.3
## 16 56  Halley  22.8
## 17 66  Halley  14.7
## 18 76  Halley   6.3
```

Survival Function, Step by Step

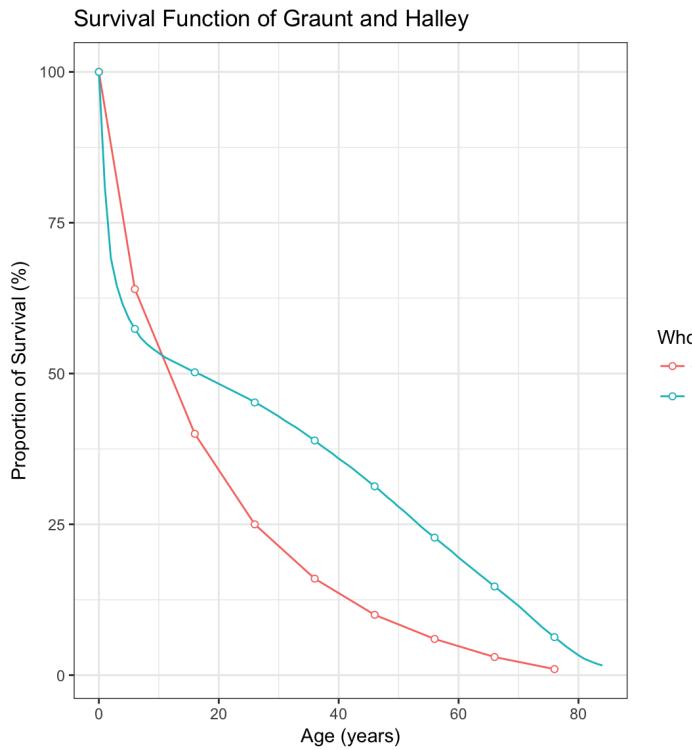
```
(gh1 <- ggplot() +  
  geom_line(data = graunt_halley_melt,  
            mapping = aes(x = x, y = xPo, colour = Who)))
```



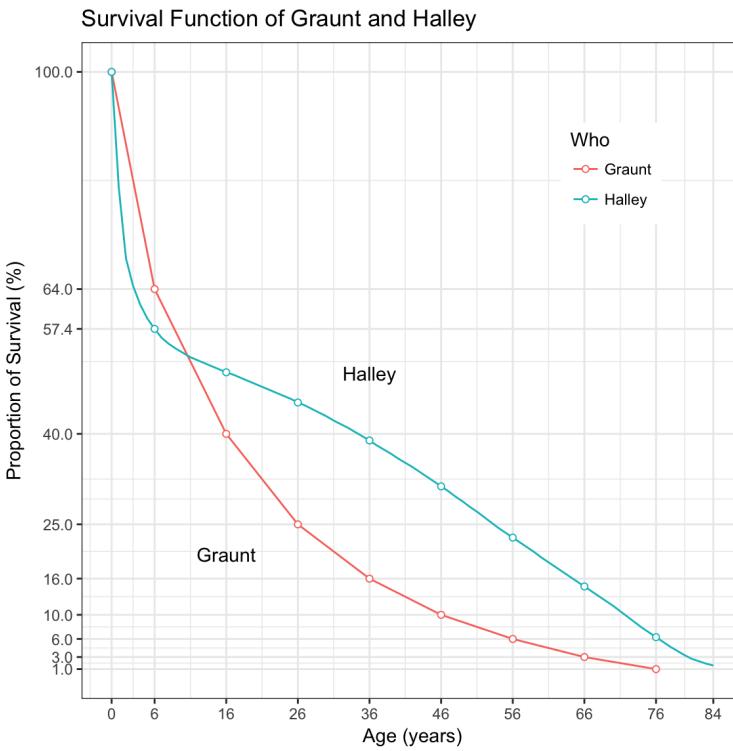
```
(gh2 <- gh1 +  
  geom_point(data = graunt_halley_melt_g,  
             mapping = aes(x = x, y = xPo, colour = Who),  
             shape = 21, fill = "white"))
```



```
(gh3 <- gh2 +
  theme_bw() +
  xlab(x_lab) +
  ylab(y_lab) +
  ggtitle(main_title_2))
```



```
(gh4 <- gh3 +
  theme(legend.position = c(0.8, 0.8)) +
  annotate("text",
    x = c(16, 36), y = c(20, 50),
    label = c("Graunt", "Halley")) +
  scale_x_continuous(breaks = c(graunt$x, 84)) +
  scale_y_continuous(breaks = c(graunt$xPo_g, xPo_halley_age_6)))
```

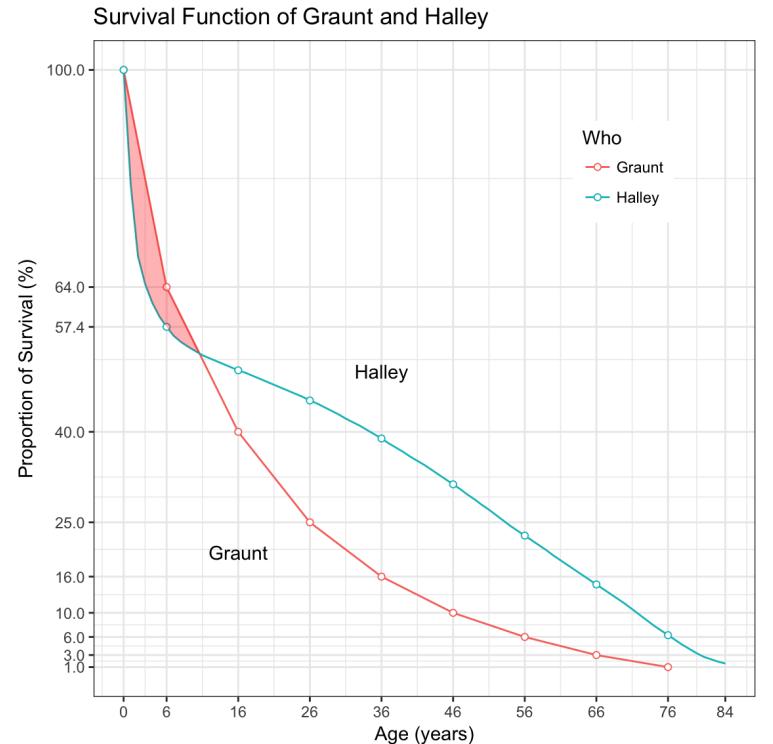


```
# qgsave("../pics/graunt_halley_ggplot.png", gh4)
```

Polygon

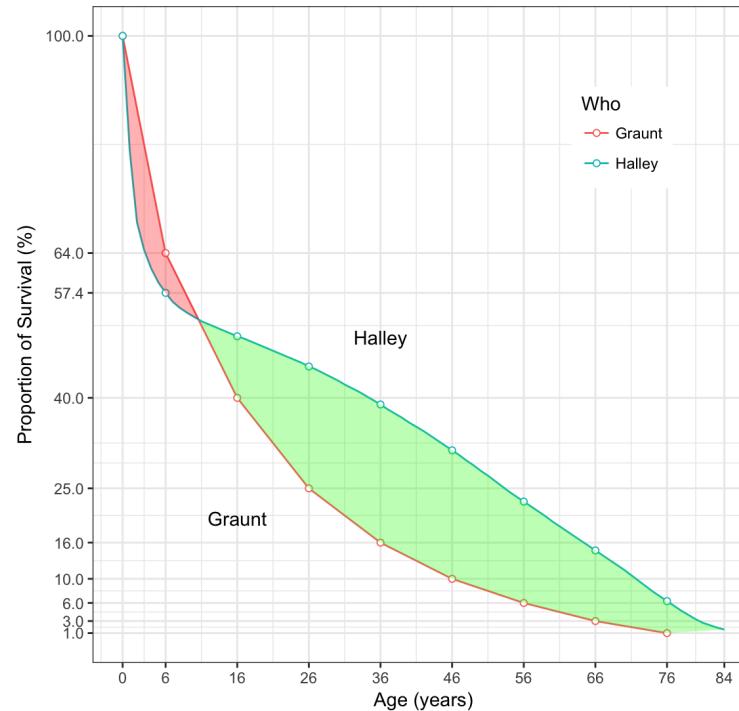
Reuse `poly_upper` data frame and `poly_lower` data frame.

```
(ghp4 <- ghp4 +  
  geom_polygon(data = poly_upper,  
               mapping = aes(x = x, y = y),  
               alpha = 0.3, fill = "red"))
```

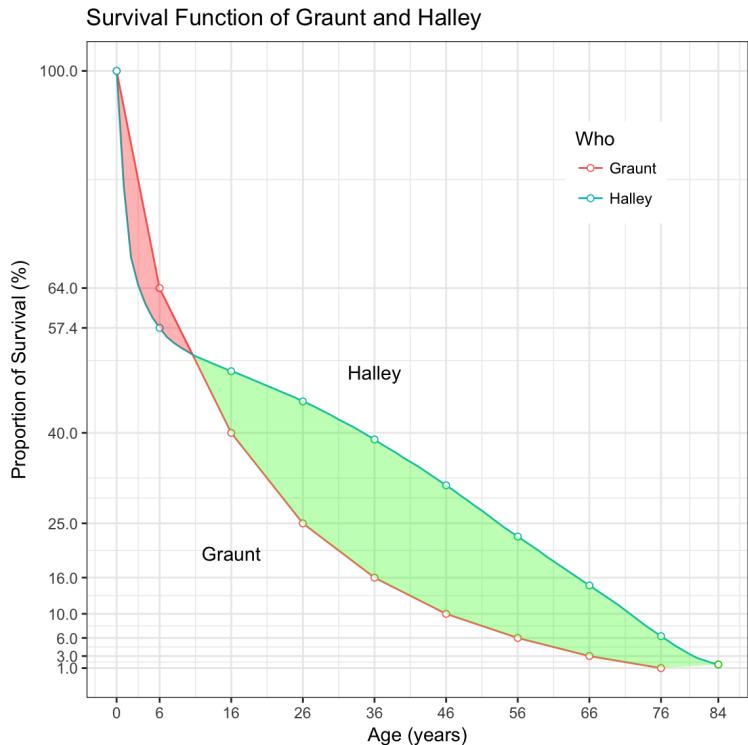


```
(ghp5 <- ghp4 +  
  geom_polygon(data = poly_lower,  
               mapping = aes(x = x, y = y),  
               alpha = 0.3, fill = "green"))
```

Survival Function of Graunt and Halley



```
(ghp5 <- ghp5 +
  geom_point(data = data.frame(x = 84, y = halley$xPo[85]),
             mapping = aes(x = x, y = y),
             colour = 3, shape = 21, fill = "white"))
```



```
# ggsave("../pics/graunt_halley_poly_ggplot.png", ghp5)
```

Graunt, Halley, and US93

Data Reshape

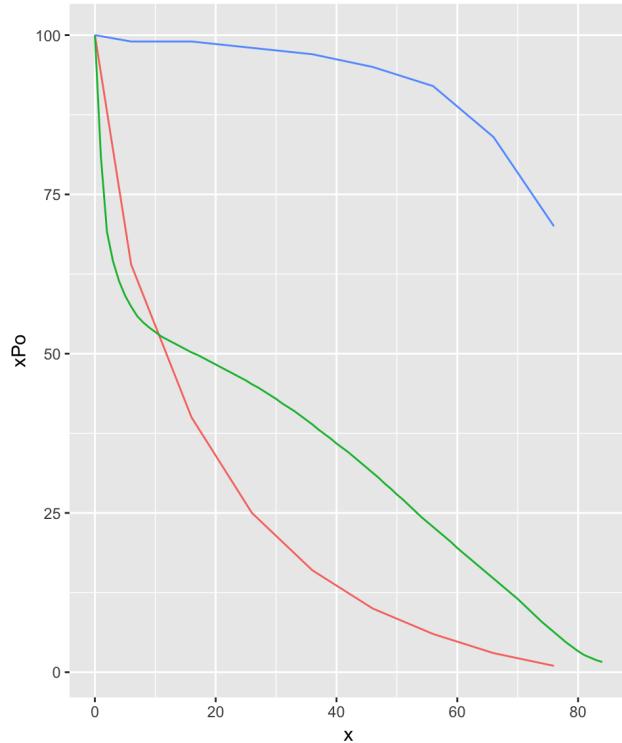
```
# us93_2 <- us93
# names(us93_2) <- c("x", "US93")
ghu_melt <- melt(list(graunt_2, halley_2, us93_2),
                 id.vars = "x",
                 value.name = "xPo",
                 variable.name = "Who")
ghu_melt_g <- ghu_melt[ghu_melt$x %in% graunt$x, ]
ghu_melt_g
```

x	Who	xPo	L1
0	Graunt	100.0	1
6	Graunt	64.0	1
16	Graunt	40.0	1
26	Graunt	25.0	1
36	Graunt	16.0	1
46	Graunt	10.0	1
56	Graunt	6.0	1
66	Graunt	3.0	1
76	Graunt	1.0	1
0	Halley	100.0	2
6	Halley	57.4	2
16	Halley	50.2	2
26	Halley	45.2	2
36	Halley	38.9	2
46	Halley	31.3	2
56	Halley	22.8	2
66	Halley	14.7	2
76	Halley	6.3	2
95	US93	100.0	3
96	US93	99.0	3
97	US93	99.0	3
98	US93	98.0	3
99	US93	97.0	3
100	US93	95.0	3
101	US93	92.0	3
102	US93	84.0	3
103	US93	70.0	3

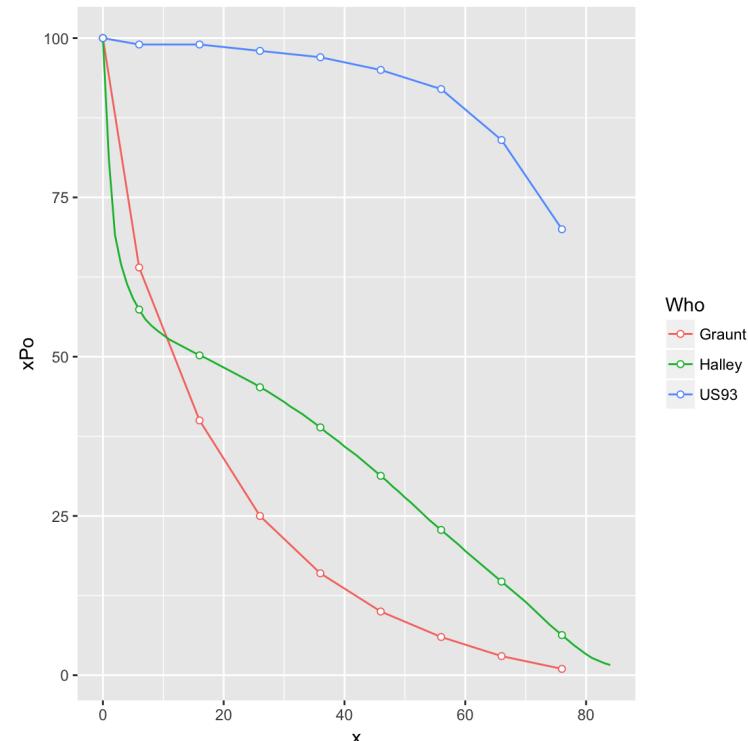
```
# main_title_3 <- "Survival Function Plots"
```

Survival Function Plots with ggplot

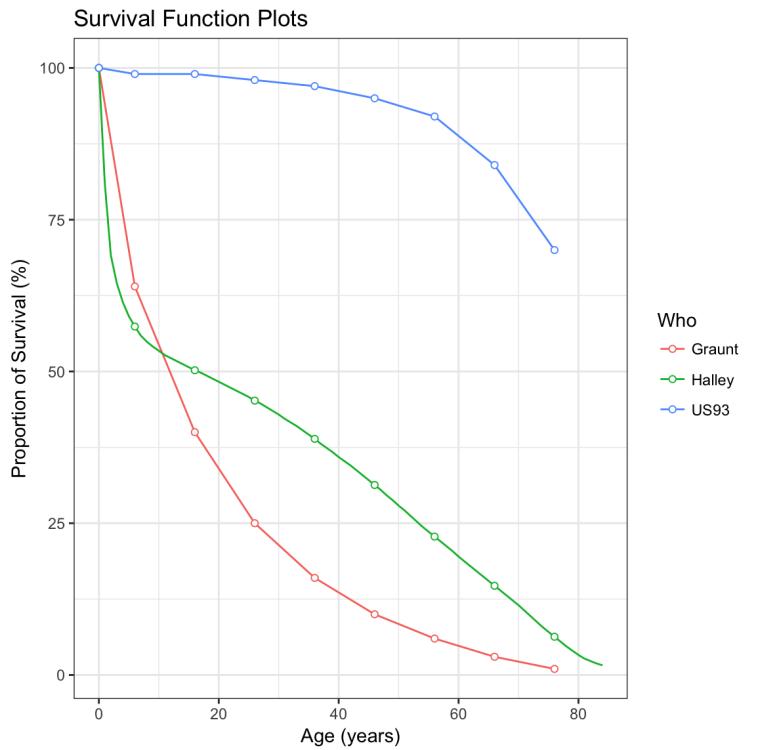
```
(ghu1 <- ggplot() +  
  geom_line(data = ghu_melt,  
            mapping = aes(x = x, y = xPo, colour = Who)))
```



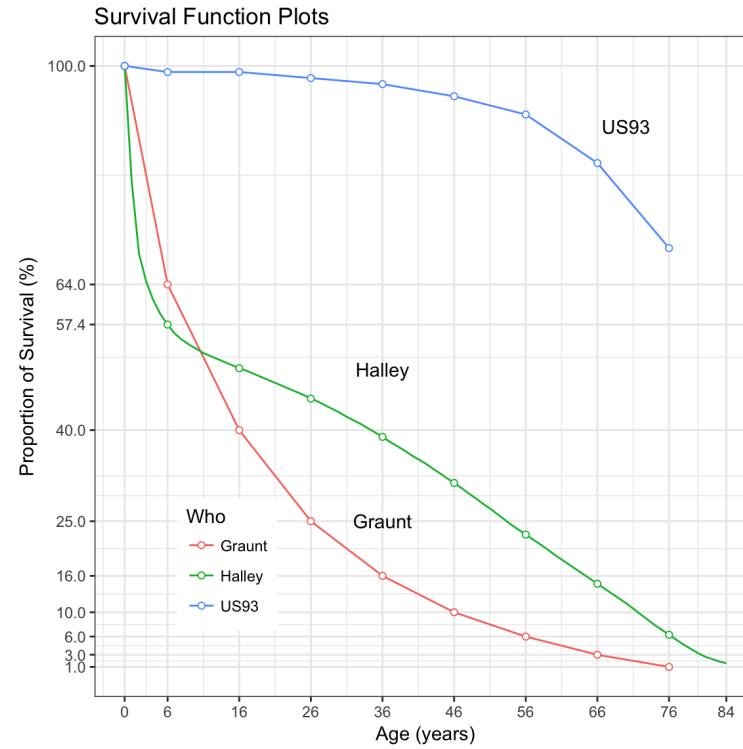
```
(ghu2 <- ghu1 +  
  geom_point(data = ghu_melt_g,  
             mapping = aes(x = x, y = xPo, colour = Who),  
             shape = 21, fill = "white"))
```



```
(ghu3 <- ghu2 +
  theme_bw() +
  xlab(x_lab) +
  ylab(y_lab) +
  ggtitle(main_title_3))
```



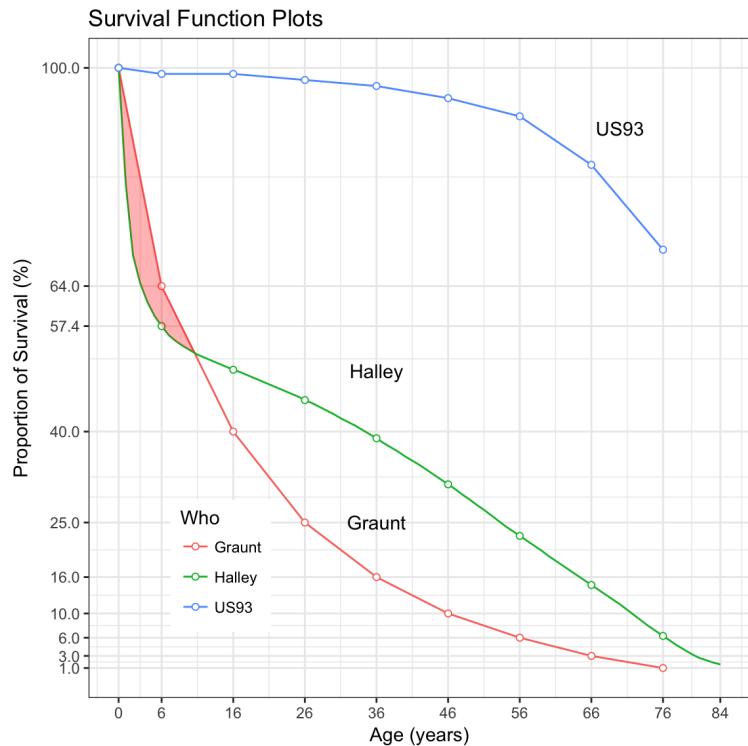
```
(ghu4 <- ghu3 +
  theme(legend.position = c(0.2, 0.2)) +
  annotate("text",
    x = c(36, 36, 70), y = c(25, 50, 90),
    label = c("Graunt", "Halley", "US93")) +
  scale_x_continuous(breaks = c(graunt$x, 84)) +
  scale_y_continuous(breaks = c(graunt$xPo_g, xPo_halley_age_6)))
```



```
# qgsave("../pics/graunt_halley_us_ggplot.png", ghu4)
```

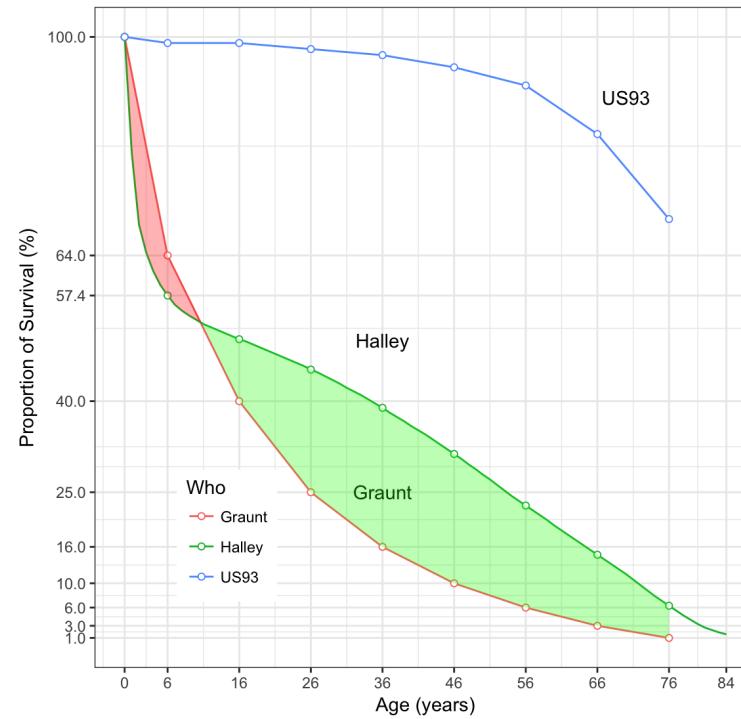
Polygon

```
(ghup4 <- ghu4 +  
  geom_polygon(data = poly_upper,  
               mapping = aes(x = x, y = y),  
               alpha = 0.3, fill = "red"))
```

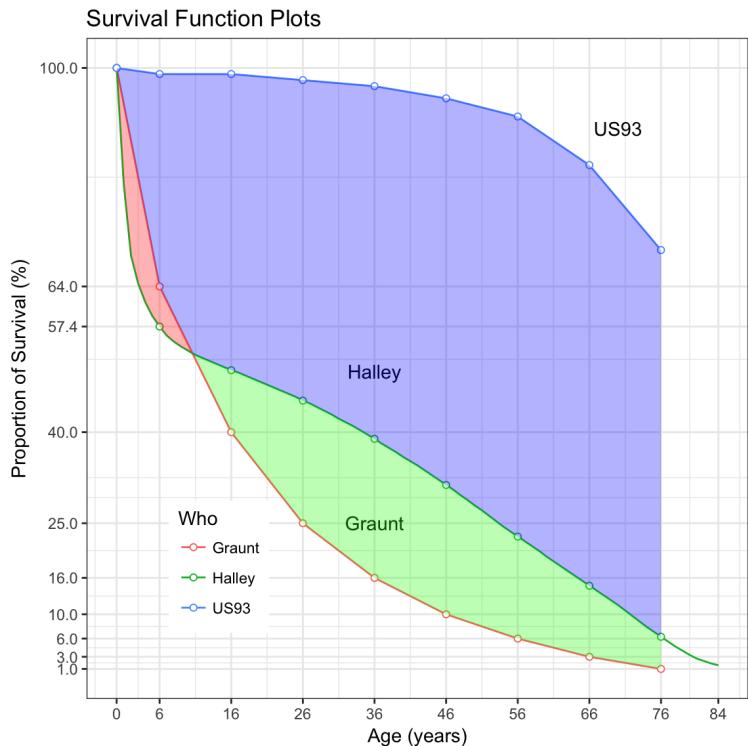


```
(ghup5 <- ghup4 +  
  geom_polygon(data = poly_lower_76,  
               mapping = aes(x = x, y = y),  
               alpha = 0.3, fill = "green"))
```

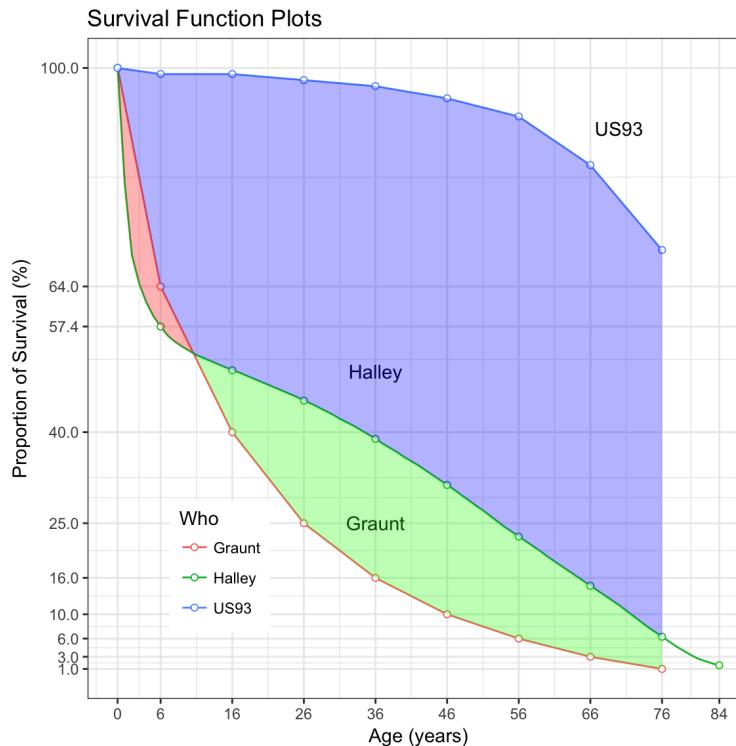
Survival Function Plots



```
(ghup6 <- ghup5 +
  geom_polygon(data = poly_us_76,
               mapping = aes(x = x, y = y),
               alpha = 0.3, fill = "blue"))
```



```
(ghup7 <- ghup6 +
  geom_point(data = data.frame(x = 84, y = halley$xPo[85]),
              mapping = aes(x = x, y = y),
              colour = 3, shape = 21, fill = "white"))
```



```
# ggsave("../pics/graunt_halley_us_poly_ggplot.png", ghup7)
```

dump() and source()

- Check out how to save and retrieve. Use `source()` and `load()` for retrieval.

```
dump("area.R", file = "area.R")
save.image("./graunt_halley_160406.RData")
```