

(c)

$$\left\{ \begin{vmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & -1 & -1 \\ -1 & -1 & 1 & -1 \\ -1 & -1 & 1 & -1 \end{vmatrix} \right\} \begin{array}{l} \text{if } \vec{v} \text{ is } \vec{u} = 12\vec{u} \\ \vec{v} \cdot \vec{u} = 0. \end{array}$$

$$\begin{vmatrix} 1 & -1 & -1 & -1 \\ -1 & 1 & -1 & -1 \\ -1 & -1 & 1 & -1 \\ -1 & -1 & -1 & -1 \end{vmatrix} = \begin{vmatrix} 1 & -1 & -1 & -1 \\ 0 & 0 & -2 & -2 \\ 0 & -2 & 0 & -2 \\ 0 & -2 & -2 & -2 \end{vmatrix}$$

$$= (-1) \begin{vmatrix} 1 & -1 & -1 & -1 & 1 \\ 0 & -2 & -2 & -2 \\ 0 & -2 & 0 & -2 \\ 0 & 0 & -2 & -2 \end{vmatrix} = (-1) \begin{vmatrix} 1 & -1 & -1 & -1 \\ 0 & -2 & -2 & -2 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & -2 & -2 \end{vmatrix}$$

$$= (-1) \begin{vmatrix} 1 & -1 & -1 & -1 \\ 0 & -2 & -2 & -2 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & -2 \end{vmatrix}$$

$$= -8$$