Fitting Normal Distribution

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Data

From Stigler's

```
knitr::include_graphics("../pics/quetelet_soldiers.png")
```


Frequency Table

- 케틀레가 작성한 스코틀랜드 군인 5738명의 가슴둘레(인치) 분포표를 옮기면

```
chest <- 33:48
freq <- c(3, 18, 81, 185, 420, 749, 1073, 1079, 934, 658, 370, 92, 50, 21, 4, 1)
data.frame(chest, freq)
```

```
##    chest freq
## 1     33    3
## 2     34   18
```

```
## 3        35    81
## 4        36   185
## 5        37   420
## 6        38   749
## 7        39  1073
## 8        40  1079
## 9        41   934
## 10       42   658
## 11       43   370
## 12       44    92
## 13       45    50
## 14       46    21
## 15       47     4
## 16       48     1
```

```r
data.frame(Chest = chest, Freq = freq)
```

```
##     Chest Freq
## 1      33    3
## 2      34   18
## 3      35   81
## 4      36  185
## 5      37  420
## 6      38  749
## 7      39 1073
## 8      40 1079
## 9      41  934
## 10     42  658
## 11     43  370
## 12     44   92
## 13     45   50
## 14     46   21
## 15     47    4
## 16     48    1
```

```r
chest_df <- data.frame(Chest = chest, Freq = freq)
chest_df
```

```
##     Chest Freq
## 1      33    3
## 2      34   18
## 3      35   81
## 4      36  185
## 5      37  420
## 6      38  749
## 7      39 1073
## 8      40 1079
## 9      41  934
## 10     42  658
## 11     43  370
## 12     44   92
## 13     45   50
## 14     46   21
```

```
## 15     47     4
## 16     48     1
```

```r
str(chest_df)
```

```
## 'data.frame':    16 obs. of  2 variables:
##  $ Chest: int  33 34 35 36 37 38 39 40 41 42 ...
##  $ Freq : num  3 18 81 185 420 ...
```

Extract Parts of an Object

```r
chest_df$Freq
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
chest_df %>%
  .$Freq
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
str(chest_df$Freq)
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```r
chest_df[, 2]
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
chest_df %>%
  `[`(, 2)
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
str(chest_df[, 2])
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```r
chest_df[, "Freq"]
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```
chest_df %>%
  `[`(, "Freq")
```

```
## [1]     3    18    81   185   420   749  1073  1079   934   658   370    92    50    21     4
## [16]     1
```

```
str(chest_df[, "Freq"])
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```
chest_df["Freq"]
```

```
##    Freq
## 1     3
## 2    18
## 3    81
## 4   185
## 5   420
## 6   749
## 7  1073
## 8  1079
## 9   934
## 10  658
## 11  370
## 12   92
## 13   50
## 14   21
## 15    4
## 16    1
```

```
chest_df %>%
  `[`("Freq")
```

```
##    Freq
## 1     3
## 2    18
## 3    81
## 4   185
## 5   420
## 6   749
## 7  1073
## 8  1079
## 9   934
## 10  658
## 11  370
## 12   92
## 13   50
## 14   21
## 15    4
## 16    1
```

```r
str(chest_df["Freq"])
```

```
## 'data.frame':    16 obs. of  1 variable:
##  $ Freq: num  3 18 81 185 420 ...
```

```r
chest_df["Freq"]$Freq
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
chest_df %>%
  `[`("Freq") %>%
  .$Freq
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
str(chest_df["Freq"]$Freq)
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```r
chest_df["Freq"][[1]]
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
chest_df %>%
  `[`("Freq") %>%
  `[[`(1)
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
#  `[`(, 1)
#    `[`(1)
str(chest_df["Freq"][[1]])
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```r
chest_df[2]
```

```
##    Freq
## 1     3
## 2    18
## 3    81
## 4   185
## 5   420
## 6   749
```

```
## 7  1073
## 8  1079
## 9   934
## 10  658
## 11  370
## 12   92
## 13   50
## 14   21
## 15    4
## 16    1
```

```
chest_df %>%
  `[`(2)
```

```
##      Freq
## 1       3
## 2      18
## 3      81
## 4     185
## 5     420
## 6     749
## 7    1073
## 8    1079
## 9     934
## 10    658
## 11    370
## 12     92
## 13     50
## 14     21
## 15      4
## 16      1
```

```
str(chest_df[2])
```

```
## 'data.frame':    16 obs. of  1 variable:
##  $ Freq: num  3 18 81 185 420 ...
```

```
chest_df[2]$Freq
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```
chest_df %>%
  `[`(2) %>%
  .$Freq
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
str(chest_df[2]$Freq)
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```r
chest_df[2][[1]]
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
chest_df %>%
  `[`(2) %>%
  `[[`(1)
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
str(chest_df[2][[1]])
```

```
##  num [1:16] 3 18 81 185 420 ...
```

```r
chest_df[[2]]
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```

```r
chest_df %>%
  `[[`(2)
```

```
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
```
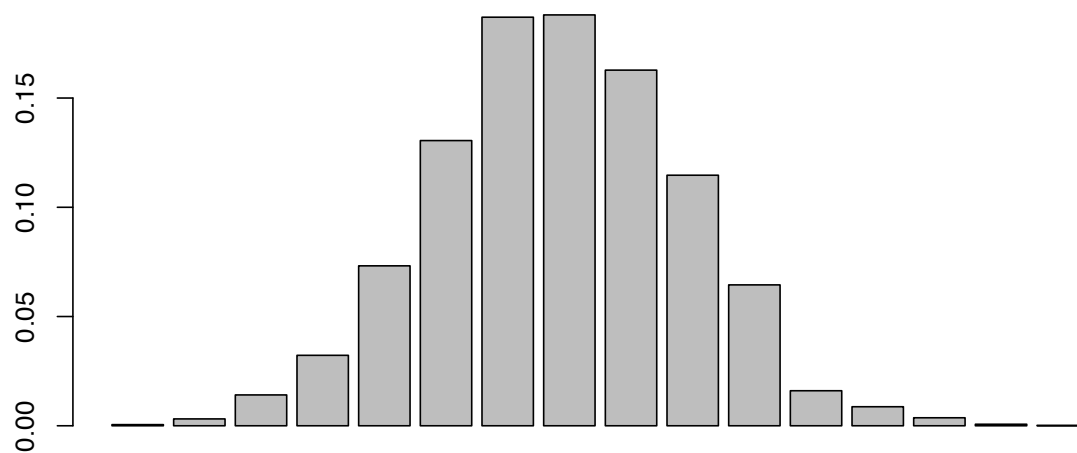
```r
str(chest_df[[2]])
```

```
##  num [1:16] 3 18 81 185 420 ...
```

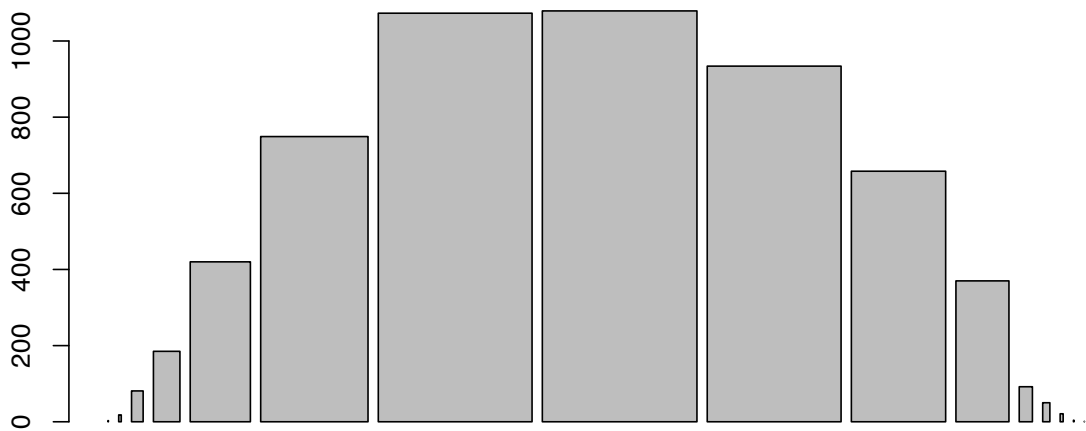- 33인치인 사람이 3명, 34인치인 사람이 18명 등으로 기록되어 있으나 이는 구간의 가운데로 이해하여야 함.

Probability Histogram

- `barplot(height, ...)` 은 기본적으로 `height`만 주어지면 그릴 수 있음. 확률 히스토그램의 기둥 면적의 합은 1이므로, 각 기둥의 높이는 각 계급의 돗수를 전체 돗수, 5738명으로 나눠준 값임.

```r
total <- sum(chest_df$Freq)
barplot(chest_df$Freq / total)
```
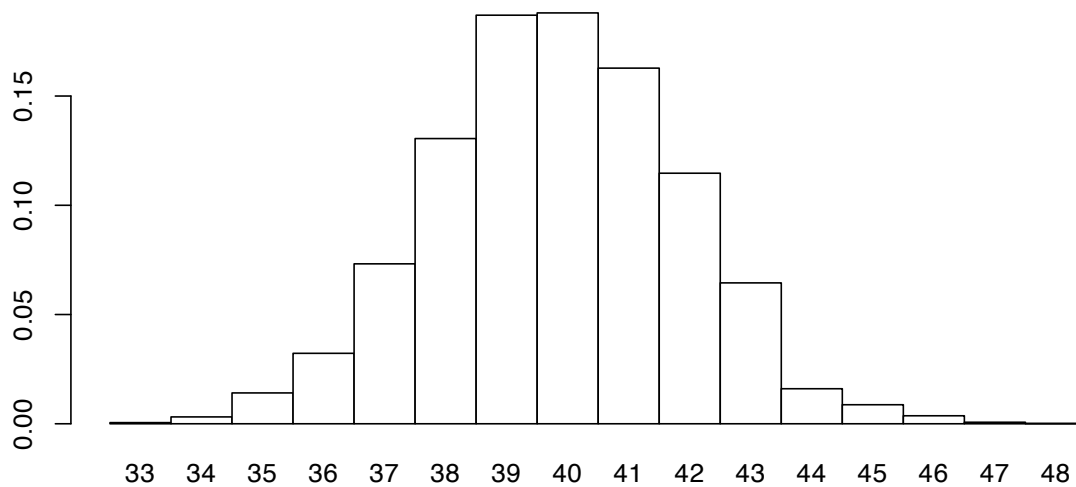
```
#>        %>%      `total`         ...
chest_df$Freq %>%
  `/`(., sum(.)) %>%
  barplot
chest_df$Freq %>%
  prop.table %>%
#> R 4.0.0    proportions
#   proportions %>%
  barplot
#>   !                .
chest_df$Freq %>%
  barplot(. / sum(.))
```

```
chest_df$Freq %>%
  barplot(`/`(., sum(.)))
```

- 각 막대의 이름은 계급을 나타내는 가슴둘레 값으로 표현할 수 있고, 막대 간의 사이를 띄우지 않으며, 디폴트 값으로 주어진 회색 보다는 차라리 백색이 나으므로 이를 설정해 주면,

```
barplot(chest_df$Freq/total,
        names.arg = 33:48,
        space = 0,
        col = "white")
```

```
chest_df$Freq %>%
  `/`(., sum(.)) %>%
  barplot(names.arg = 33:48,
          space = 0,
          col = "white")
```

- 확률 히스토그램의 정의에 따라 이 막대들의 면적을 합하면 1이 됨에 유의.

Summary statistics and SD

- 33인치가 3명, 34인치가 18명 등을 한 줄의 긴 벡터로 나타내어야 평균과 표준편차를 쉽게 계산할 수 있으므로 long format으로 바꾸면,

```
chest_vec <- rep(chest_df$Chest, chest_df$Freq)
chest_vec <- chest_df %$%
  rep(.$Chest, .$Freq)
str(chest_vec)
```

```
##  int [1:5738] 33 33 33 34 34 34 34 34 34 34 ...
```

```
rep()
```

```
rep(1:3, times = 3)
```

```
## [1] 1 2 3 1 2 3 1 2 3
```

```r
rep(1:3, each = 3)
```

```
## [1] 1 1 1 2 2 2 3 3 3
```

```r
rep(1:3, 1:3)
```

```
## [1] 1 2 2 3 3 3
```

- chest_vec 을 이용하여 기초통계와 표준편차를 계산하면,

```r
summary(chest_vec)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##   33.00   38.00   40.00   39.83   41.00   48.00
```
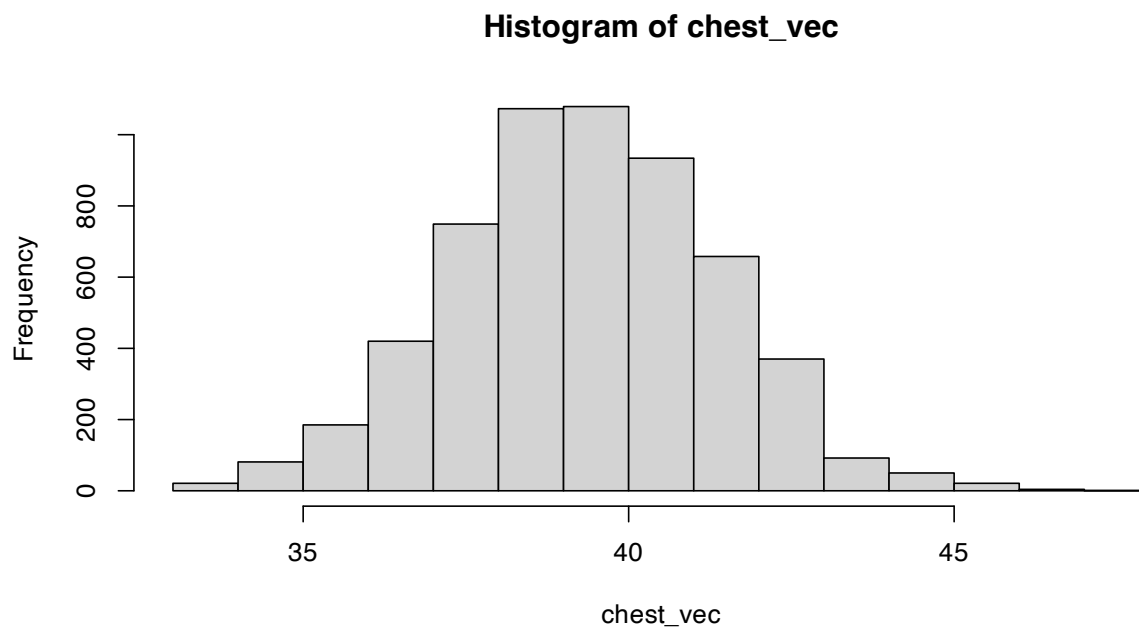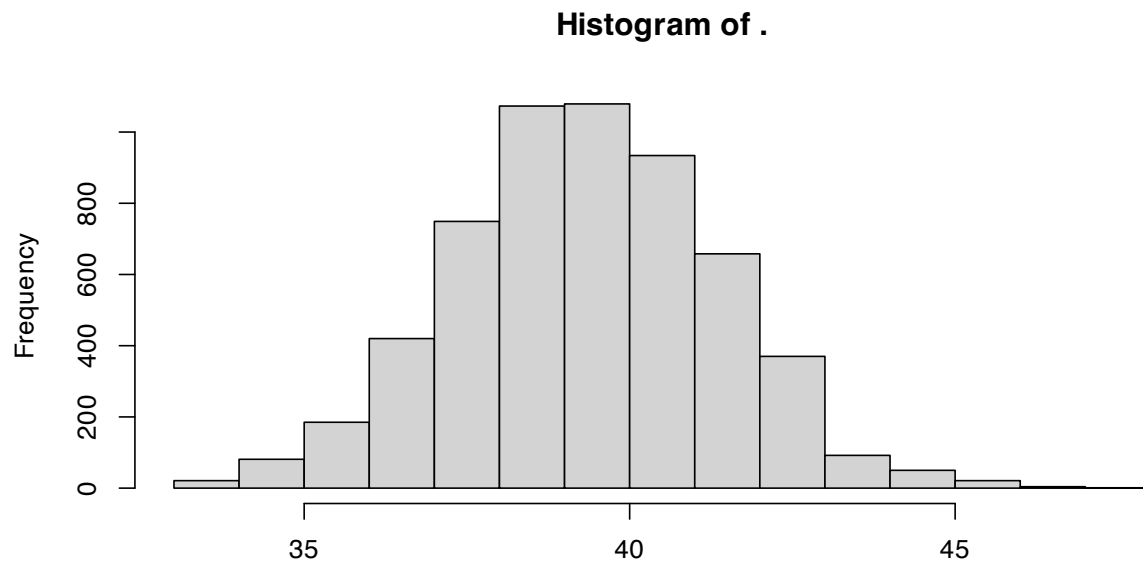
```r
sd(chest_vec)
```

```
## [1] 2.049616
```

Histogram

- 히스토그램을 직관적으로 그려보면 y축은 돗수가 기본값임을 알 수 있음.
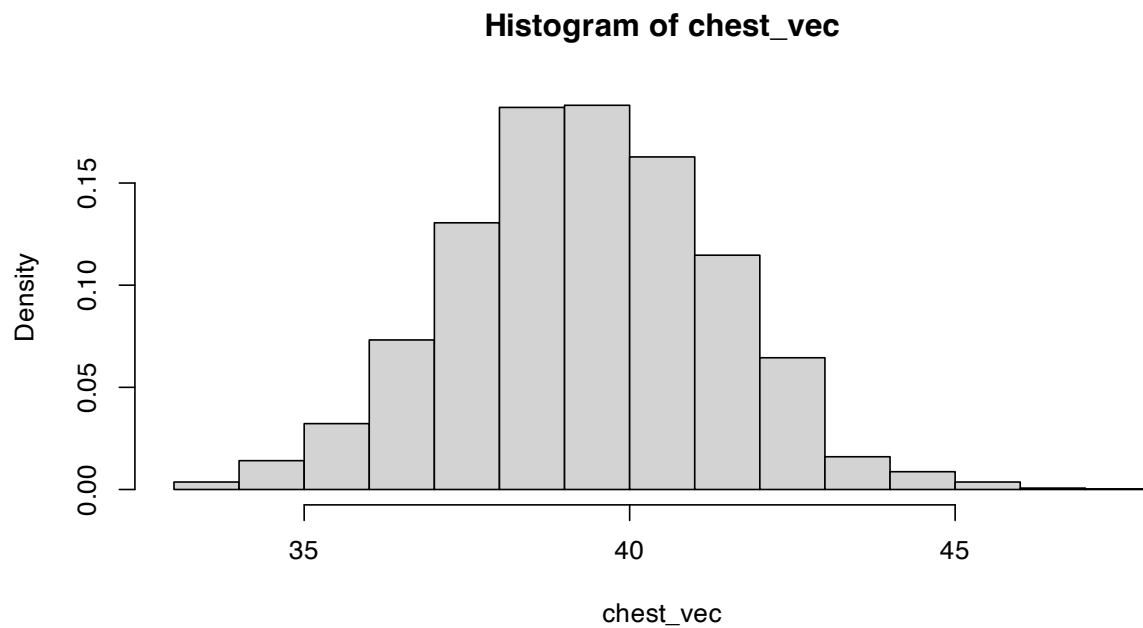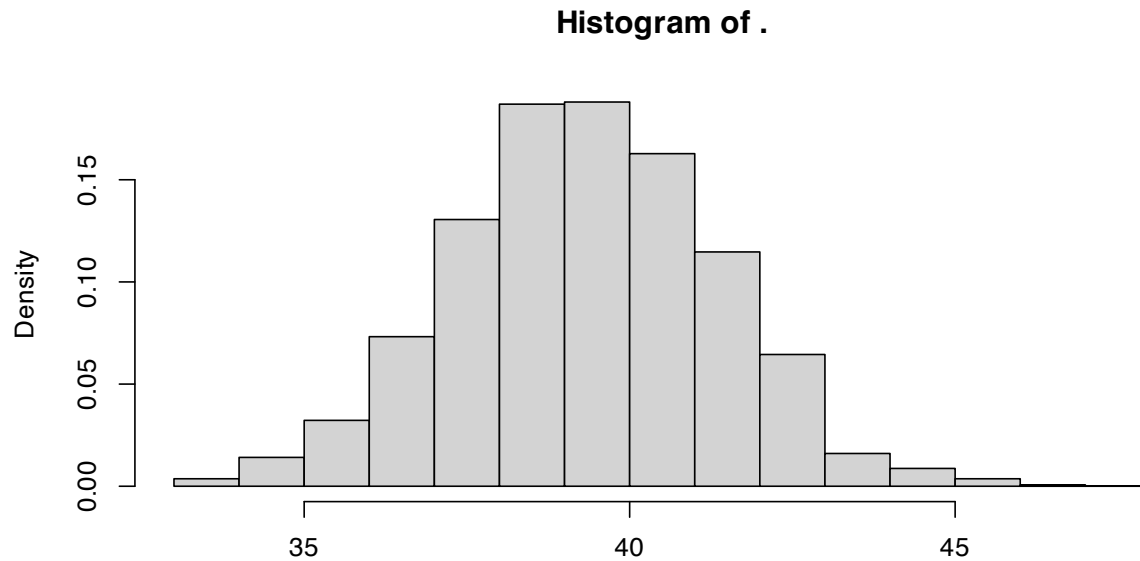
```r
hist(chest_vec)
```

Histogram of chest_vec

```
chest_vec %>%
  hist
```

Histogram of .

.

- 정규분포와 비교하기 위해서 y축을 확률로 나타내려면

```
hist(chest_vec,
     probability = TRUE)
```

Histogram of chest_vec

```r
chest_vec %>%
  hist(probability = TRUE)
```

Histogram of .

Inside the histogram

- 실제로 이 히스토그램을 그리는 데 계산된 값들은?

```r
(h_chest <- hist(chest_vec, plot = FALSE))
```

```
## $breaks
##  [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
##
## $counts
##  [1]   21   81  185  420  749 1073 1079  934  658  370   92   50   21    4    1
##
## $density
##  [1] 0.0036598118 0.0141164169 0.0322411990 0.0731962356 0.1305332869
##  [6] 0.1869989543 0.1880446148 0.1627744859 0.1146741025 0.0644823980
## [11] 0.0160334611 0.0087138376 0.0036598118 0.0006971070 0.0001742768
##
## $mids
##  [1] 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5 47.5
##
## $xname
## [1] "chest_vec"
##
## $equidist
## [1] TRUE
```

```
## 
## attr(,"class")
## [1] "histogram"
```

```r
list(breaks = h_chest$breaks,
     counts = h_chest$counts,
     density = h_chest$density,
     mids = h_chest$mids)
```

```
## $breaks
##  [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
## 
## $counts
##  [1]   21   81  185  420  749 1073 1079  934  658  370   92   50   21    4    1
## 
## $density
##  [1] 0.0036598118 0.0141164169 0.0322411990 0.0731962356 0.1305332869
##  [6] 0.1869989543 0.1880446148 0.1627744859 0.1146741025 0.0644823980
## [11] 0.0160334611 0.0087138376 0.0036598118 0.0006971070 0.0001742768
## 
## $mids
##  [1] 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5 47.5
```

```r
chest_vec %>%
  hist(plot = FALSE) %>%
  list(breaks = .$breaks,
       counts = .$counts,
       density = .$density,
       mids = .$mids)
```

```
## [[1]]
## $breaks
##  [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
## 
## $counts
##  [1]   21   81  185  420  749 1073 1079  934  658  370   92   50   21    4    1
## 
## $density
##  [1] 0.0036598118 0.0141164169 0.0322411990 0.0731962356 0.1305332869
##  [6] 0.1869989543 0.1880446148 0.1627744859 0.1146741025 0.0644823980
## [11] 0.0160334611 0.0087138376 0.0036598118 0.0006971070 0.0001742768
## 
## $mids
##  [1] 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5 47.5
## 
## $xname
## [1] "."
## 
## $equidist
## [1] TRUE
## 
## attr(,"class")
## [1] "histogram"
```

```
## 
## $breaks
##  [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
## 
## $counts
##  [1]   21   81  185  420  749 1073 1079  934  658  370   92   50   21    4    1
## 
## $density
##  [1] 0.0036598118 0.0141164169 0.0322411990 0.0731962356 0.1305332869
##  [6] 0.1869989543 0.1880446148 0.1627744859 0.1146741025 0.0644823980
## [11] 0.0160334611 0.0087138376 0.0036598118 0.0006971070 0.0001742768
## 
## $mids
##  [1] 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5 47.5
```

- 평균값과 표준편차로부터 히스토그램의 위치가 0.5만큼 왼쪽으로 치우쳐 있다는 것을 알 수 있음. 제자리에 옮겨 놓기 위해서 breaks 매개변수를 32.5부터 48.5까지 1간격으로 설정

```r
hist(chest_vec,
     probability = TRUE,
     breaks = 32.5:48.5)
```

Histogram of chest_vec
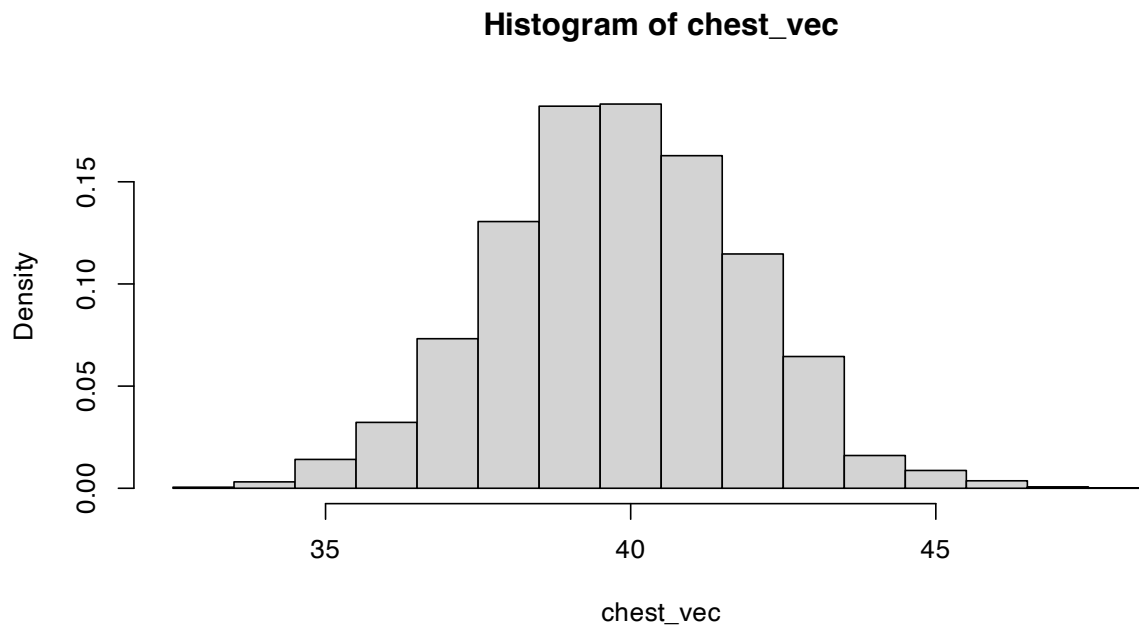
- 위의 히스토그램을 그리느라고 계산된 값들은?

```r
h_chest_2 <- hist(chest_vec,
                  breaks = 32.5:48.5,
                  plot = FALSE)
list(breaks = h_chest_2$breaks,
     counts = h_chest_2$counts,
     density = h_chest_2$density,
     mids = h_chest_2$mids)
```

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```
## $breaks
##  [1] 32.5 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5
## [16] 47.5 48.5
##
## $counts
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
##
## $density
##  [1] 0.0005228303 0.0031369815 0.0141164169 0.0322411990 0.0731962356
##  [6] 0.1305332869 0.1869989543 0.1880446148 0.1627744859 0.1146741025
## [11] 0.0644823980 0.0160334611 0.0087138376 0.0036598118 0.0006971070
## [16] 0.0001742768
##
## $mids
##  [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
```

```r
chest_vec %>%
  hist(breaks = 32.5:48.5,
       plot = FALSE) %>%
  list(breaks = .$breaks,
       counts = .$counts,
       density = .$density,
       mids = .$mids)
```

```
## [[1]]
## $breaks
##  [1] 32.5 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5
## [16] 47.5 48.5
##
## $counts
##  [1]    3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]    1
##
## $density
##  [1] 0.0005228303 0.0031369815 0.0141164169 0.0322411990 0.0731962356
##  [6] 0.1305332869 0.1869989543 0.1880446148 0.1627744859 0.1146741025
## [11] 0.0644823980 0.0160334611 0.0087138376 0.0036598118 0.0006971070
## [16] 0.0001742768
##
## $mids
##  [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
##
## $xname
## [1] "."
##
## $equidist
## [1] TRUE
##
## attr(,"class")
## [1] "histogram"
##
## $breaks
##  [1] 32.5 33.5 34.5 35.5 36.5 37.5 38.5 39.5 40.5 41.5 42.5 43.5 44.5 45.5 46.5
```

```
## [16] 47.5 48.5
##
## $counts
## [1]   3   18   81  185  420  749 1073 1079  934  658  370   92   50   21    4
## [16]   1
##
## $density
## [1] 0.0005228303 0.0031369815 0.0141164169 0.0322411990 0.0731962356
## [6] 0.1305332869 0.1869989543 0.1880446148 0.1627744859 0.1146741025
## [11] 0.0644823980 0.0160334611 0.0087138376 0.0036598118 0.0006971070
## [16] 0.0001742768
##
## $mids
## [1] 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48
```

- 히스토그램을 보기 쉽게 하기 위해서 메인 타이틀과 서브 타이틀, x축 라벨, y축 라벨 설정

```
main_title <- "Fitting Normal Distribution"
# sub_title <- "Chest Circumferences of Scottish Soldiers"
sub_title <- ""
x_lab <- "Chest Circumferences (inches)"
y_lab <- "Proportion"
hist(chest_vec,
    breaks = 32.5:48.5,
    probability = TRUE,
    main = main_title,
    sub = sub_title,
    xlab = x_lab,
    ylab = y_lab)
```


Fitting Normal Distribution
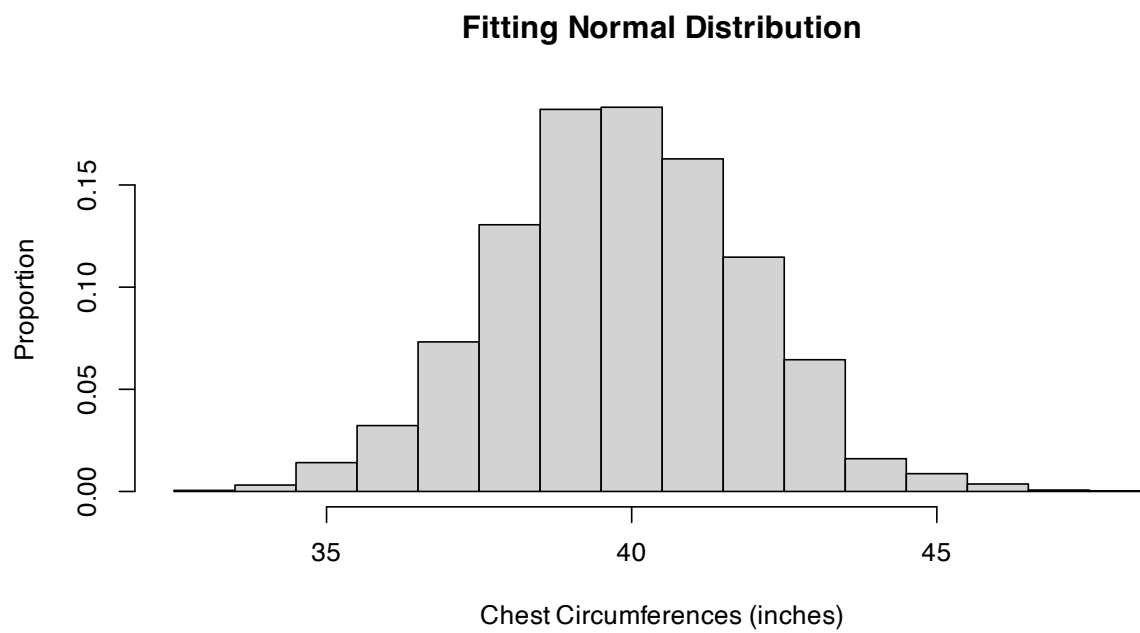
Mean ± SD contains 2/3 of total number of counts

- 평균을 중심으로 ±표준편차 만큼 떨어진 자료를 붉은 색 수직점선으로 표시.

```r
mean_chest <- mean(chest_vec)
sd_chest <- sd(chest_vec)
x_lower <- mean_chest - sd_chest
x_upper <- mean_chest + sd_chest
sd_chest <- chest_vec %>%
  sd
x_lower <- chest_vec %>%
  mean %>%
  `-`(sd_chest)
x_upper <- chest_vec %>%
  mean %>%
  `+`(sd_chest)
hist(chest_vec,
     breaks = 32.5:48.5,
     probability = TRUE,
     main = main_title,
     sub = sub_title,
     xlab = x_lab,
     ylab = y_lab)
abline(v = c(x_lower, x_upper),
       lty = 2,
       col = "red")
```

Fitting Normal Distribution
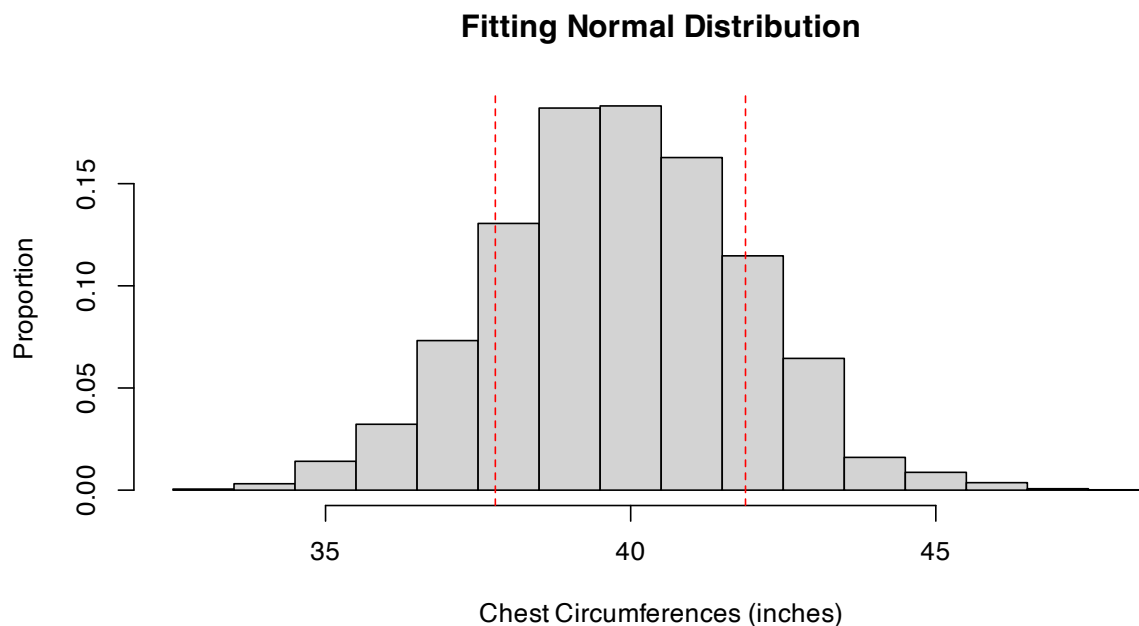
- 그 사이의 영역을 빗금으로 표시하기 위하여 다각형의 좌표를 계산

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```r
h_chest_2$density[6:10]
```

```
## [1] 0.1305333 0.1869990 0.1880446 0.1627745 0.1146741
```

```r
y <- h_chest_2$density[6:10]
```

- 5개의 직사각형으로 파악하고 향후 면적 계산을 쉽게 하기 위하여 다음과 같이 좌표 설정

```r
x_coord <- rep(c(x_lower, 38.5:41.5, x_upper), each = 2)
y_coord <- c(0, rep(y, each = 2), 0)
poly_df <- data.frame(x = x_coord, y = y_coord)
hist(chest_vec,
     breaks = 32.5:48.5,
     probability = TRUE,
     main = main_title,
     sub = sub_title,
     xlab = x_lab,
     ylab = y_lab)
abline(v = c(x_lower, x_upper),
       lty = 2,
       col = "red")
# polygon(x_coord, y_coord, density = 20)
polygon(poly_df,
#        col = "grey",
#        border = NA)
       density = 20)
```

Fitting Normal Distribution

Chest Circumferences (inches)
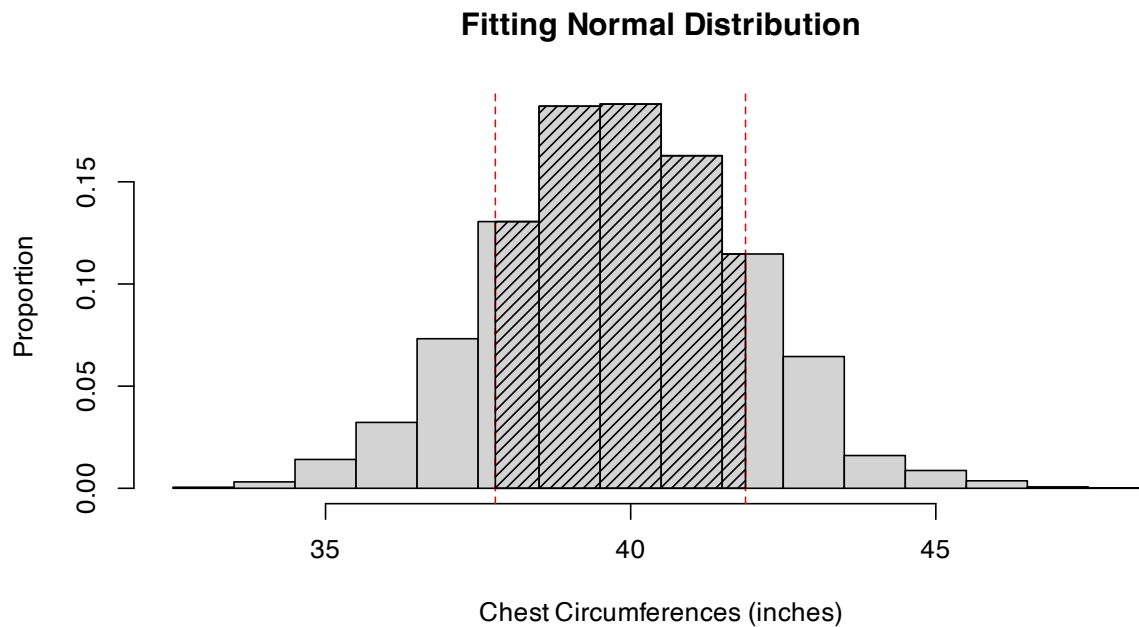
- 이론적으로 빗금친 부분의 면적은 `pnorm(1)` - `pnorm(-1)` =0.6826895에 가까울 것으로 예상. 5개 직사각형의 면적을 구하여 합하는 과정은 다음과 같음.

```r
options(digits = 3)
x_area <- c(x_lower, 38.5:41.5, x_upper)
y
```

```
## [1] 0.131 0.187 0.188 0.163 0.115
```

```r
diff(x_area)
```

```
## [1] 0.718 1.000 1.000 1.000 0.381
```

```r
diff(x_area) * y
```

```
## [1] 0.0937 0.1870 0.1880 0.1628 0.0437
```

```r
sum(diff(x_area) * y)
```

```
## [1] 0.675
```

```r
source("./area.R")
area_R
```

```
## function (x, y)
## {
##     sum(diff(x) * (head(y, -1) + tail(y, -1))/2)
## }
```

```r
area_R(x_coord, y_coord)
```

```
## [1] 0.675
```

Comparison with normal curve

- 이론적인 정규분포 밀도함수 곡선을 히스토그램에 덧붙여 그림.

```r
x_chest <- seq(32.5, 48.5,
               length = 1000)
y_norm <- dnorm(x_chest,
                mean = mean_chest,
                sd = sd_chest)
hist(chest_vec,
     breaks = 32.5:48.5,
     probability = TRUE,
     main = main_title,
     sub = sub_title,
     xlab = x_lab,
     ylab = y_lab)
abline(v = c(x_lower, x_upper),
```

```
        lty = 2,
        col = "red")
# abline(v = c(38, 42), lty = 2, col = "red")
polygon(poly_df,
        density = 20)
# polygon(x_coord, y_coord, density = 20)
lines(x_chest, y_norm, col = "red")
```

Fitting Normal Distribution

Chest Circumferences (inches)
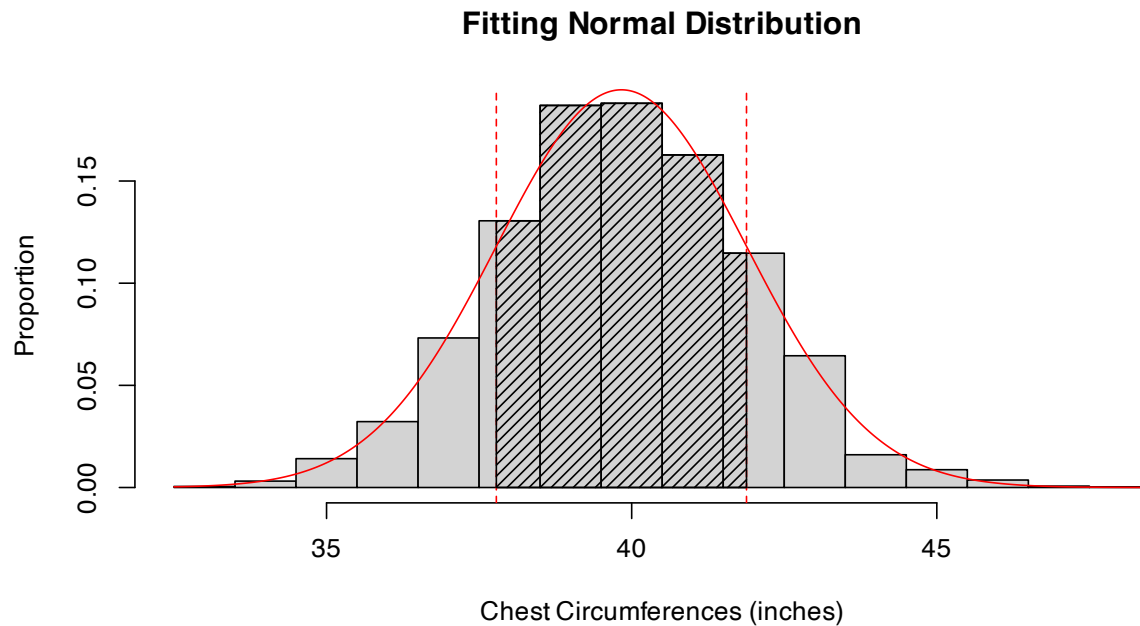
## Changing tick marks of x axis

- default로 주어지는 x축의 눈금을 제대로 볼 수 있게 고치려면,

```
hist(chest_vec,
     breaks = 32.5:48.5,
     probability = TRUE,
     main = main_title,
     sub = sub_title,
     xlab = x_lab,
     ylab = y_lab,
     axes = FALSE)
abline(v = c(x_lower, x_upper),
       lty = 2,
       col = "red")
polygon(poly_df,
        density = 20)
# polygon(x_coord, y_coord, density = 20)
lines(x_chest, y_norm, col = "red")
axis(side = 1,
     at = seq(32, 48, by = 2),
```

```
    labels = seq(32, 48, by = 2))
axis(side = 2)
```
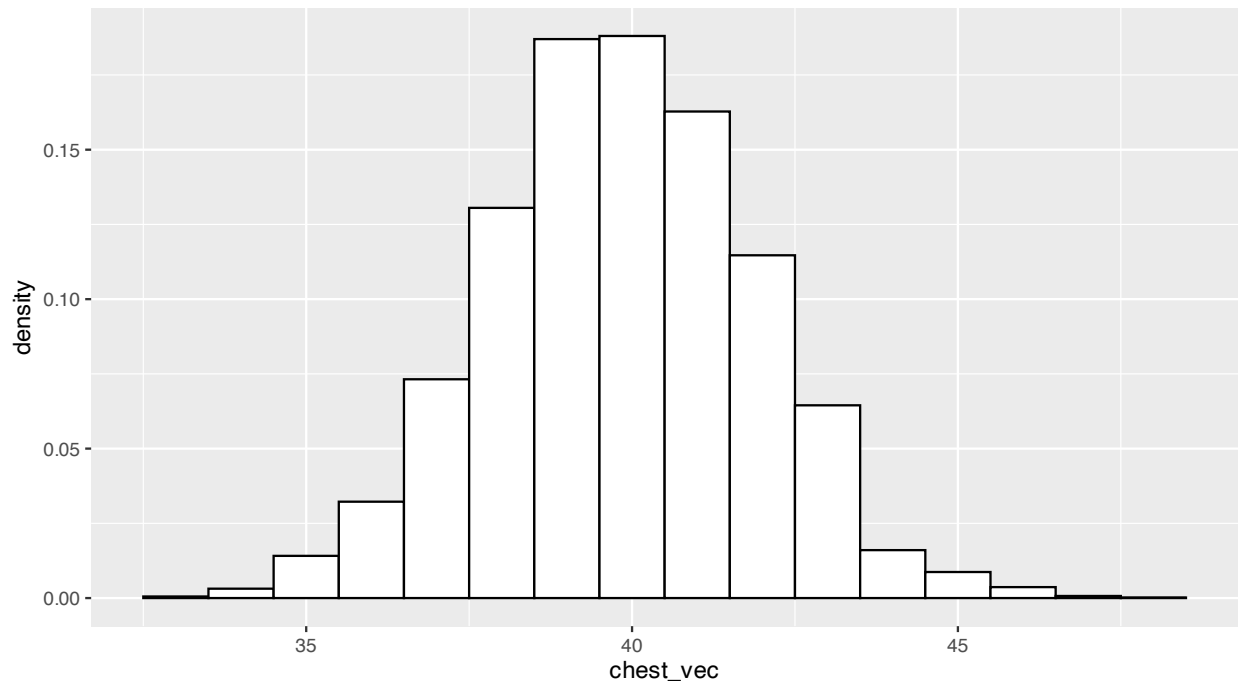
Fitting Normal Distribution
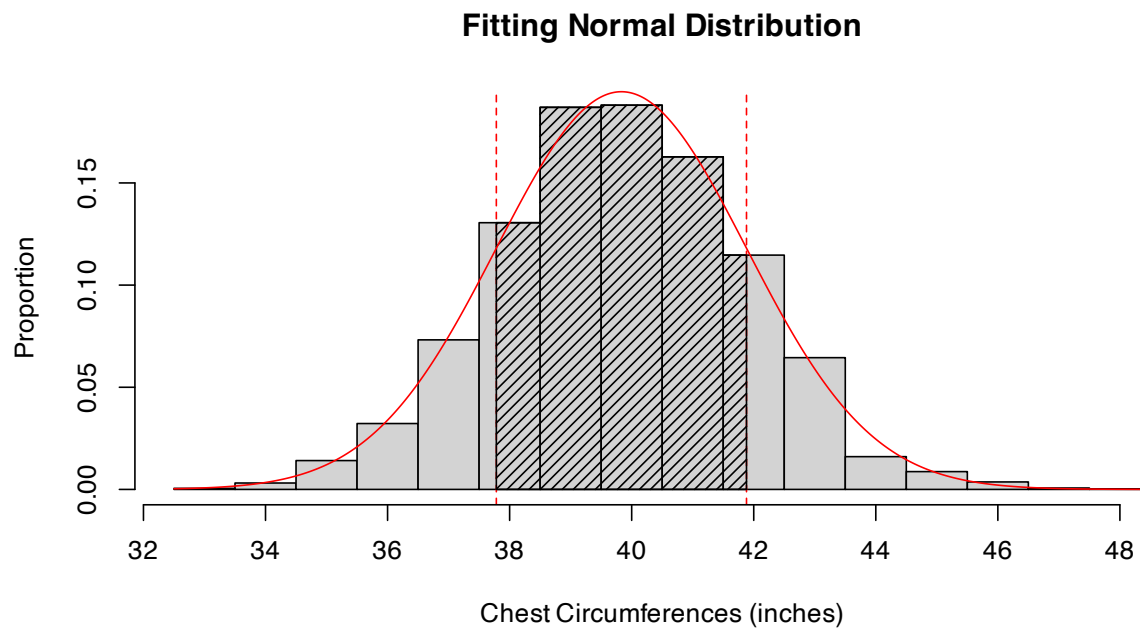
ggplot

- data frame으로 작업.

### Basic histogram

```r
library(ggplot2)
# theme_update(plot.title = element_text(hjust = 0.5))
g0 <- ggplot(data = data.frame(chest_vec),
             mapping = aes(x = chest_vec))
(g1 <- g0 +
    stat_bin(aes(y = after_stat(density)),
#   stat_bin(aes(y = ..density..), #> ggplot
             binwidth = 1,
             fill = "white",
             colour = "black"))
```

```
#>
# (g1 <- g0 +
#   stat_count(fill = "white",
#              colour = "black"))
# (g1 <- g0 +
#   geom_histogram(aes(y = ..density..),
#                  binwidth = 1,
#                  fill = "white",
#                  colour = "black"))
# (g1 <- g0 +
#   geom_histogram(aes(y = ..density..),
#                  binwidth = 1,
#                  breaks = 32.5:48.5,
#                  fill = "white",
#                  colour = "black"))
```
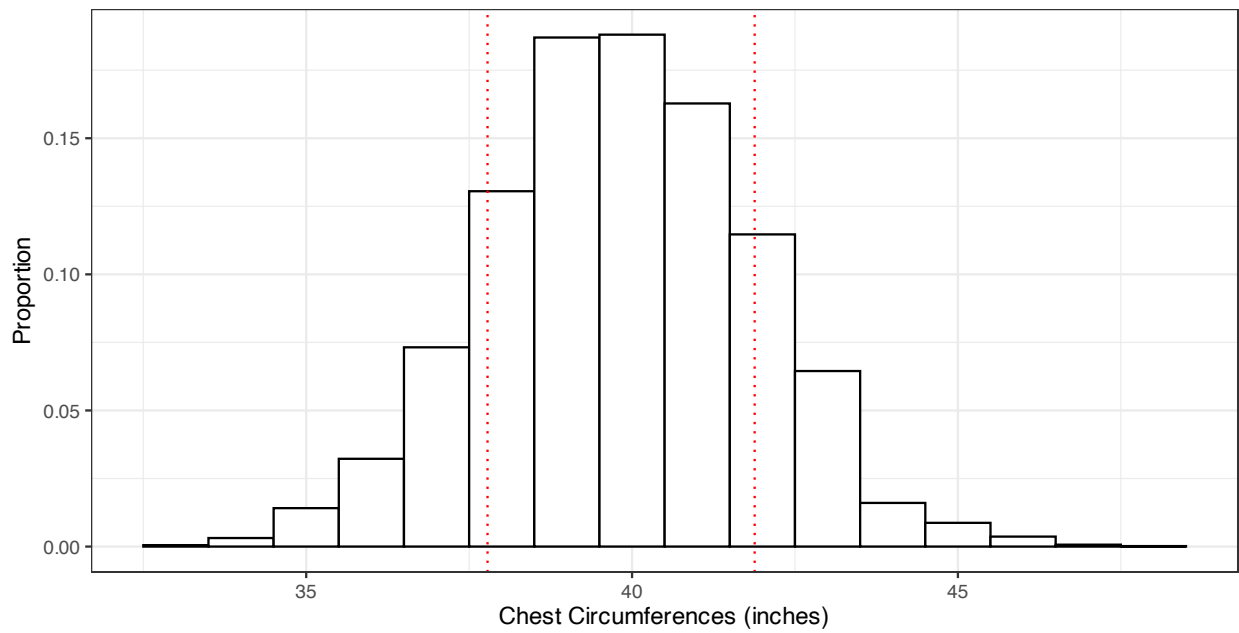
Mean ± SD

```
(g2 <- g1 +
   geom_vline(xintercept = c(x_lower, x_upper),
              linetype = "dotted",
              colour = "red"))
```
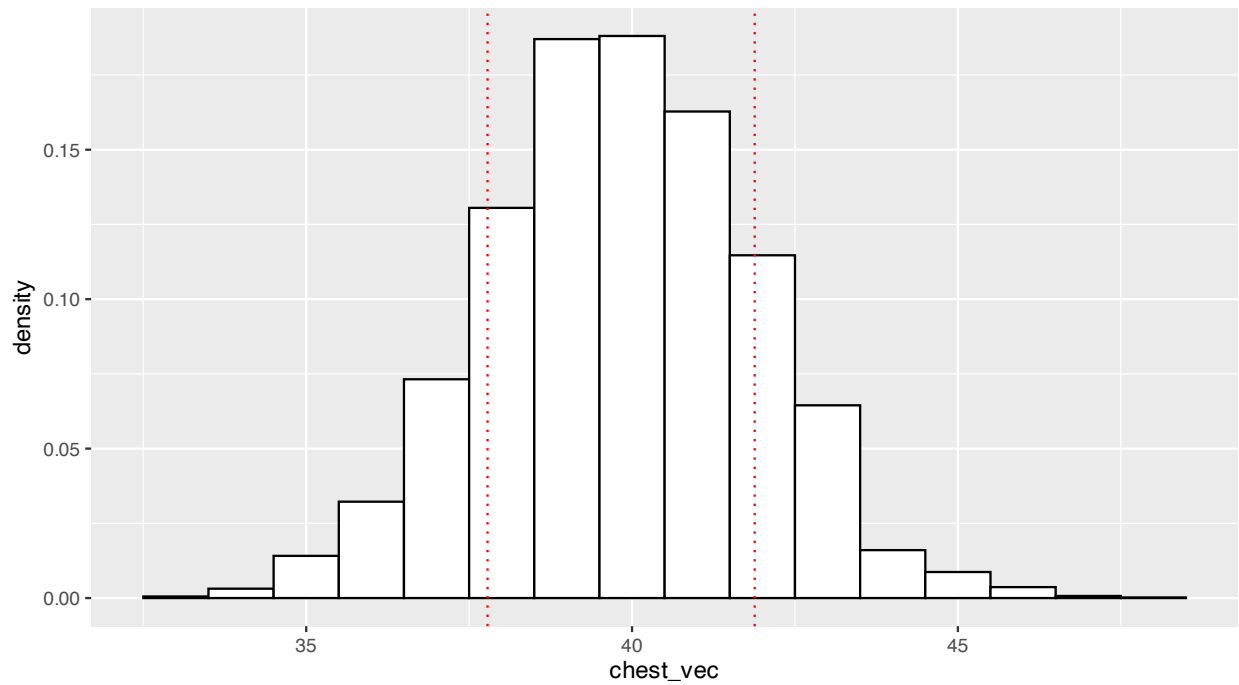
x-axis label and main title

```
(g3 <- g2 +
   theme_bw() +
#   xlab(x_lab) +
#   ylab(y_lab) +
#   ggtitle(main_title) +
#>
   labs(title = main_title,
        x = x_lab,
        y = y_lab) +
   theme(plot.title = element_text(hjust = 0.5,
                                   size = 20)))
```
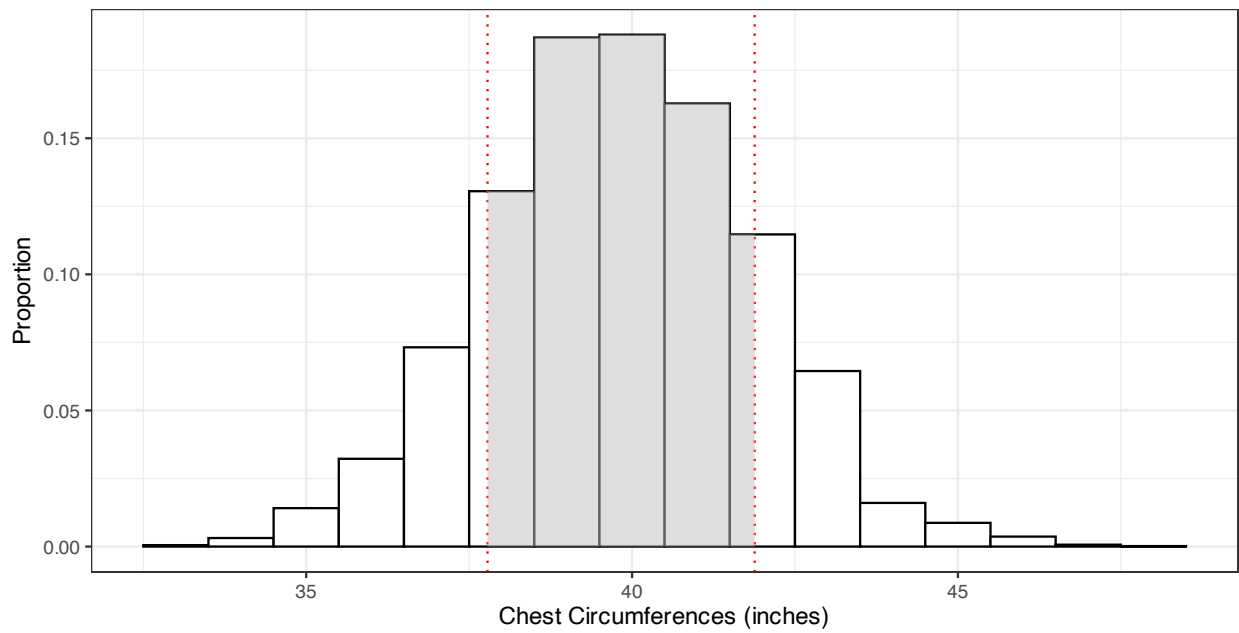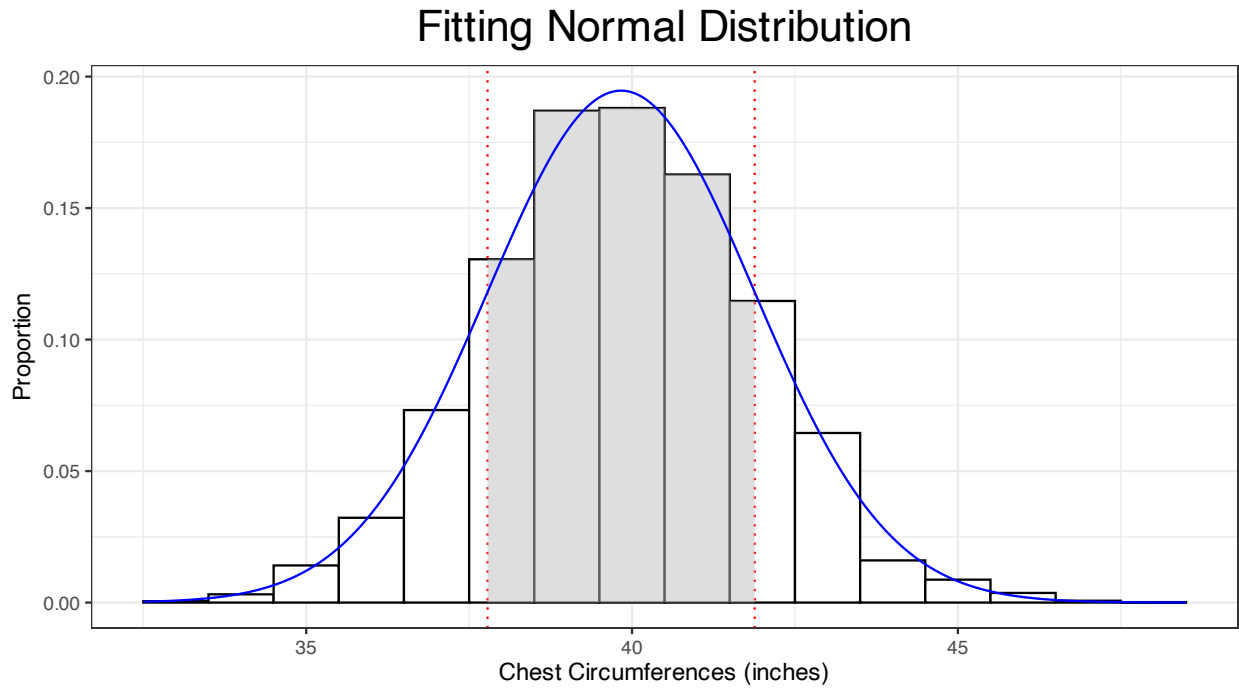
Fitting Normal Distribution

Shading the area

```
(g4 <- g3 +
  geom_polygon(data = poly_df,
               mapping = aes(x = x, y = y),
               alpha = 0.5,
               fill = "grey"))
```
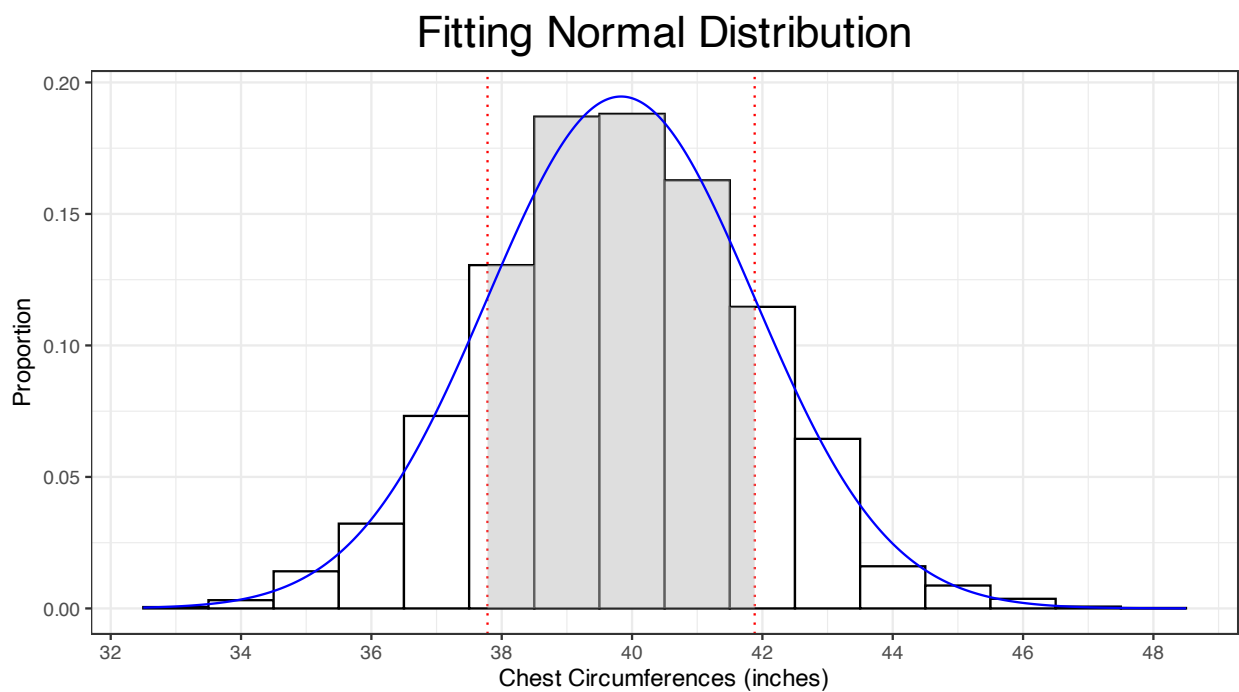
Fitting Normal Distribution

Normal curve added

```r
# x_curve <- seq(32.5, 48.5, length = 100)
# y_curve <- dnorm(x_curve, mean = mean_chest, sd = sd_chest)
curve_df <- data.frame(x = x_chest, y = y_norm)
(g5 <- g4 +
  geom_line(data = curve_df,
            mapping = aes(x = x, y = y),
            colour = "blue"))
```

Fitting Normal Distribution

x-axis tick marks

```
(g6 <- g5 +
    scale_x_continuous(breaks = seq(32, 48, by = 2),
                       labels = seq(32, 48, by = 2)))
```

Fitting Normal Distribution

Comments

R 코드에 대하여 학습한 내용

케틀레가 스코틀랜드 군인 5738명의 가슴둘레 자료를 정규분포에 적합시킨 이야기