Εθνικό Μετσόβιο Πολυτεχνείο
Σχολή Ηλεκτρολόγων Μηχανικών
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Υπολογιστών

# Αποδοτική εξισορρόπηση αδειών εκπομπής αερίων θερμοκηπίου στον μηχανισμό EU-ETS

ΔΙΠΛΩΜΑΤΙΚΗ ΕΡΓΑΣΙΑ

ΚΩΝΣΤΑΝΤΙΝΟΣ ΠΑΠΑΔΟΠΟΥΛΟΣ

**Επιβλέπων :**  Δημήτριος Φωτάκης
              Καθηγητής Ε.Μ.Π.

Αθήνα, Νοέμβριος 2024

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Εγκρίθηκε από την τριμελή εξεταστική επιτροπή την 5η Νοεμβρίου 2024.

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Δημήτριος Φωτάκης            Αριστείδης Παγουρτζής         Αθανάσιος Βουλόδημος
Καθηγητής Ε.Μ.Π.            Καθηγητής Ε.Μ.Π.             Επίκουρος Καθηγητής ΕΜΠ

Αθήνα, Νοέμβριος 2024

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**Κωνσταντίνος Παπαδόπουλος**

Διπλωματούχος Ηλεκτρολόγος Μηχανικός και Μηχανικός Υπολογιστών Ε.Μ.Π.

# Περιεχόμενα

# Κατάλογος σχημάτων

# Κατάλογος πινάκων

# List of Algorithms

# Εκτεταμένη Ελληνική Περίληψη

## 0.1 Εισαγωγή

Εδώ θα μπει κάποια εισαγωγή.

## 0.2 Επόμενα

# Chapter 1

# Emission Trading - EU ETS

Climate change remains one of the most urgent and complex challenges facing the global community. The rapid rise in greenhouse gas (GHG) emissions, driven primarily by industrial activities and fossil fuel consumption, has led to a warming climate with severe consequences for ecosystems, economies, and public health worldwide [9]. Recognizing the gravity of this threat, governments, intergovernmental organizations, and a multitude of stakeholders have rallied to implement agreements, frameworks, and mechanisms aimed at reducing GHG emissions on a global scale. Together, these initiatives underscore the necessity of coordinated action to mitigate climate change.

Among the earliest and most impactful frameworks was the United Nations Framework Convention on Climate Change (UNFCCC) [13], adopted in 1992, which set a foundation for international cooperation on climate action. Since then, landmark agreements have built upon this foundation, each with unique mechanisms and commitments. The Kyoto Protocol [11] of 1997 marked a pivotal step by establishing binding emission reduction targets for developed nations and introducing flexible mechanisms, such as Emissions Trading and the Clean Development Mechanism (CDM) (article 12 of [11], to incentivize reductions. Later, the Paris Agreement of 2015 [12] transformed climate governance by including both developed and developing nations under a common goal to limit global temperature increases to well below 2℃, with each country setting and updating voluntary Nationally Determined Contributions (NDCs) to meet this target.

Furthermore, specialized protocols like the Montreal Protocol [10] and its Kigali Amendment have played a significant role by phasing out hydrofluorocarbons (HFCs), which contribute significantly to both ozone depletion and global warming. Sector-specific initiatives, such as the Carbon Offsetting and Reduction Scheme for International Aviation (CORSIA), underscore the commitment of industry-specific organizations, such as the International Civil Aviation Organization (ICAO), to reducing emissions in high-impact sectors.

In parallel with these global efforts, regional initiatives have demonstrated the efficacy of targeted policies. One of the most notable examples is the European Union Emission Trading System (EU ETS), established in 2005 as the world's largest and most ambitious carbon market. Designed as a cap-and-trade system, the EU ETS sets a limit on emissions from high-emitting sectors across the EU and enables companies to trade allowances within this cap. This market-driven approach has made the EU ETS a cornerstone of Europe's climate policy and serves as a model for other regions aiming to reduce emissions while maintaining economic stability.
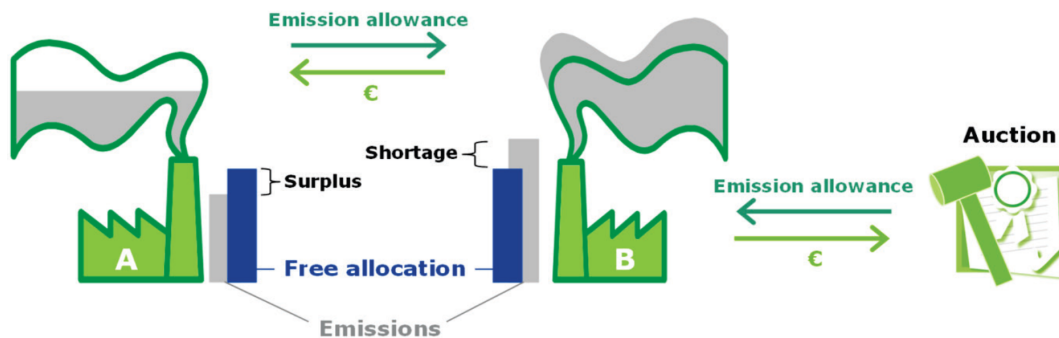
**Figure 1.1**: Diagram of CAT System from EU ETS Handbook [7]

This thesis will explore the cap and Trade Systems (like the EU ETS) and the allocation of free allowances, for which we will talk shortly.

## 1.1    Cap And Trade Systems

A central approach in addressing emissions has been the establishment of Emissions Trading Systems (ETS) or cap-and-trade systems, which differ fundamentally from carbon taxes. While taxes set a fixed cost per unit of emissions, they do not directly ensure reductions in total emissions, as firms may continue emitting if they accept the cost. Cap-and-trade systems, on the other hand, establish a maximum (cap) on emissions and allow the market to determine the price, thereby incentivizing companies to innovate and reduce emissions while aligning with specific reduction targets.

Under cap-and-trade, a government or regulatory body issues a limited number of annual permits, each allowing for a specific amount of carbon dioxide ($CO_2$) emissions. The total number of permits sets the cap, which is typically reduced over time to ensure a progressive decrease in emissions. Companies that emit less than their allotted amount can sell (or "trade") unused permits to others, creating an economic incentive to cut emissions and driving permit prices upward as the cap tightens. This gradual increase in permit costs motivates firms to invest in cleaner technologies, ensuring that emissions reduction targets are met efficiently and at a minimal economic cost.

### 1.1.1    Key Examples of CAT Systems

Cap-and-trade systems have been adopted across various countries and regions as one of the most effective market-based tools for reducing emissions:

**United States**

18

**Sulfur Dioxide (SO$_2$)**    One of the earliest applications of emissions trading was under the Acid Rain Program of the 1990 Clean Air Act, aimed at cutting SO$_2$ emissions. This program succeeded in reducing emissions by 50% from 1980 levels by 2007 and demonstrated the cost-effectiveness of cap-and-trade by reducing control costs by as much as 80% compared to traditional regulation.

**Nitrogen Oxides (NOx)**    In 2003, the NOx Budget Trading Program began operating to lower NOx emissions, a primary cause of ground-level ozone pollution. Between 2003 and 2008, NOx emissions during ozone season dropped by 43%, even as energy demand remained steady.

**Tokyo, Japan**    In 2010, Tokyo launched its own emissions trading scheme targeting high emitters within the city, including large industrial facilities and buildings. By its fourth year, emissions were reduced by 23% compared to baseline levels, with a goal of a 25% reduction by 2020.

**European Union Emission Trading System (EU ETS)**    The EU ETS, launched in 2005, is the largest multinational emissions trading market and is central to the EU's climate policy. Covering over 11,000 installations in the power and industrial sectors, the EU ETS sets a progressively lower cap to reach the EU's target of a 43% reduction in emissions from 2005 levels by 2030. This system has served as a model for other emissions trading programs and continues to be a cornerstone of the EU's commitment to global climate goals.

**South Korea**    South Korea's ETS, launched in 2015, covers 525 entities across 23 sectors, making it the second-largest carbon market globally after the EU ETS. South Korea's scheme aims to reduce emissions in alignment with its commitments to the UNFCCC, covering approximately two-thirds of the country's emissions.

**New Zealand**    Established in 2008, the New Zealand Emissions Trading Scheme (NZ ETS) covers several sectors, including forestry, energy, and waste. The NZ ETS, though initially uncapped, has faced criticism for its high reliance on imported carbon allowances, which has diluted domestic emission reduction incentives.

**China**    China, the world's largest GHG emitter, launched its national carbon market in 2021, initially covering the power sector, which represents over 40% of China's emissions. With a projected coverage of 3.5 billion tons of CO$_2$ from 1700 installations, China's ETS is anticipated to be the world's largest carbon market. China aims to reduce CO$_2$ emissions per unit of GDP by 65% by 2030 from 2005 levels.

### 1.1.2    Benefits of CAT Systems

Although counter-intuitive (to my singleton brain), CAT Systems have some strong arguments against other systems. [7]

**Environmental Certainty** Unlike carbon taxes, which set a price on emissions but don't guarantee a specific reduction level, CAT systems cap the total emissions allowed. This cap provides more certainty about achieving a targeted environmental outcome, making it easier to align with climate goals and international agreements.

**Cost-Effectiveness** By allowing companies to trade emission allowances, CAT systems enable reductions to occur where they are most economically efficient. Firms that can reduce emissions at lower costs can sell their excess allowances to those facing higher reduction costs, minimizing the overall expense of achieving emission targets.

**Compatibility with International Markets** CAT systems can be linked across jurisdictions, facilitating international cooperation and potentially leading to a more unified global approach to emissions reduction. For example, the European Union's Emissions Trading System (EU ETS) has explored linking with other systems to enhance market efficiency and environmental outcomes.

**Minimising risk to Member State budgets** The EU Emissions Trading System (EU ETS) ensures emissions reductions from installations responsible for approximately 50% of the EU's total emissions. This certainty diminishes the likelihood that Member States will need to acquire additional international units to fulfill their obligations under the Kyoto Protocol.

## 1.2 European Union Emissions Trading System (EU ETS)

### 1.2.1 Operation

The European Union Emissions Trading Scheme (EU ETS) operates as a cap-and-trade system to limit greenhouse gas (GHG) emissions from participating entities. It does this by issuing allowances, each representing the right to emit one tonne of $CO_2$ equivalent (tCOe). The total number of allowances is capped and has been decreasing annually by 1.74% since 2013, aligning with progressively ambitious emission reduction targets. Starting in 2021, the factor increased to 2.2% per year.

Annually, certain sectors—particularly those vulnerable to carbon leakage—receive a portion of these allowances for free, while the remaining allowances are sold mainly through auctions. By the end of each year, participants must surrender an allowance for every tonne of COe they have emitted. If they lack sufficient allowances, they are required to either reduce their emissions or purchase additional allowances through auctions or from other participants.

The value of allowances stems from their limited supply and the demand from participants for whom emission reductions are costlier. This market mechanism ensures that emissions are reduced where it is most economically efficient, benefiting both businesses and the broader economy. Compliance is strictly enforced with substantial fines—starting at €100 per tCOe and adjusted for inflation since 2013—for entities that fail to surrender enough allowances, thereby effectively maintaining the emissions cap.

Since Phase 2 began in 2008, participants with surplus allowances at the end of a trading phase can "bank" these allowances for future use, provided they are held in user accounts. For example, unlimited banking from Phase 2 to Phase 3 was permitted, with unused Phase 2 allowances automatically converted to Phase 3 allowances by June 2013 at no additional cost. These banked allowances are incorporated into the Phase 3 cap.

Participants can also "borrow" allowances from their future allocations within the same trading period to meet current obligations. This is feasible because allowances are allocated in February each year, while the surrender deadline for the previous year's allowances is at the end of April. However, borrowing across different trading periods—for instance, using Phase 3 allowances to meet Phase 2 obligations—is prohibited. [7]

### 1.2.2 Brief History and Goals

In this section, information from the European Commission [4] and [5] will be presented

**Phase 1 (2005–2007)**    : Pilot Phase

The first phase served as a three-year pilot to test the system before it became a critical tool for meeting Kyoto Protocol targets in Phase 2.

**Key characteristics**    of Phase 1 included:

- Scope: Limited to carbon dioxide ($CO_2$) emissions from power generators and energy-intensive industries.

- Allowance Allocation: Almost all allowances were distributed to businesses for free.

- Compliance Penalty: A penalty of €40 per tonne of $CO_2$ was imposed for non-compliance.

**Achievements**    of Phase 1:

- Established a carbon pricing mechanism.

- Enabled free trade of emission allowances across EU member states.

- Developed infrastructure for monitoring, reporting, and verifying emissions.

**Challenges**    : Due to the absence of reliable emissions data, caps were based on estimates, leading to an oversupply of allowances. This surplus caused the price of allowances to plummet to zero in 2007, as unused Phase 1 allowances could not be carried over to Phase 2.

**Phase 2 (2008–2012)**    : Aligning with Kyoto Targets

Phase 2 aligned with the first commitment period of the Kyoto Protocol, where EU countries had specific emission reduction obligations.

**Key features** included:

- Reduced Cap: The overall cap was approximately 6.5% lower than 2005 emission levels.

- Expanded Membership: Iceland, Liechtenstein, and Norway joined the EU ETS.

- Broader Scope: Inclusion of nitrous oxide emissions from nitric acid production in some countries.

- Allowance Allocation: Free allocations slightly reduced to around 90%, with some allowances auctioned.

- Compliance Penalty: Increased to €100 per tonne of $CO_2$.

- International Credits: Businesses could purchase international credits totaling about 1.4 billion tonnes of $CO_2$-equivalent.

- Registry Systems: Transitioned to a Union registry and replaced the Community Independent Transaction Log (CITL) with the European Union Transaction Log (EUTL).

- Aviation Sector Inclusion: Aviation was incorporated into the EU ETS starting January 2012, although application to flights to and from non-European countries was temporarily suspended.

Despite adjusting caps based on verified emissions data, the 2008 economic crisis led to greater-than-expected emission reductions. This resulted in a surplus of allowances, exerting downward pressure on carbon prices throughout Phase 2.

**Phase 3 (2013–2020)** : System Overhaul

Significant reforms were introduced to enhance the effectiveness and efficiency of the EU ETS:

- Single EU-wide Cap: Replaced national caps with a unified cap across all member states.

- Auctioning of Allowances: Auctioning became the default method for allocating allowances, moving away from predominantly free allocations.

- Harmonized Allocation Rules: Standardized rules for the free allocation of allowances to address carbon leakage risks.

- Expanded Coverage: More sectors and greenhouse gases were included.

- Innovation Support: Set aside 300 million allowances in the New Entrants Reserve (NER 300) to fund innovative renewable energy technologies and carbon capture and storage projects.

**Market Evolution**    The EU ETS has been instrumental in developing a robust carbon market:

- Trading Volumes: Increased from 321 million allowances in 2005 to over 7.9 billion in 2012.

- Global Influence: In 2010, EU allowances accounted for 84% of the global carbon market's value.

- Economic Impact: Despite challenges, the EU ETS remained a key driver in the international carbon market, with the total value of allowances traded reaching €56 billion in 2012.

**Phase 4 (2021–2030)**    : Enhancing Ambition

Phase 4 aims to further reduce emissions in line with the EU's climate objectives:

- Allowance Allocation: Approximately 57% of total allowances are designated for auctioning, amounting to about 7.855 billion allowances for the entire phase.

- Adjustments and Funds: Portions of auctionable allowances may be redirected to support free allocation buffers, the Innovation Fund, the Modernisation Fund, and the Social Climate Fund.

- Actual Auction Volumes: Due to these adjustments, around 51.5% of the annual cap is expected to be auctioned between 2021 and 2025.

- Market Stability Reserve (MSR): Continues to regulate the supply of allowances to stabilize the market.

- Member State Derogations: Bulgaria, Hungary, and Romania opted to continue providing free allowances to their energy sectors, deducted from their auction volumes, under Article 10c of the ETS Directive.

**Aviation Sector**    in Phase 4

The aviation sector remains a distinct component:

- Allowance Allocation: 15% of aviation allowances are auctioned, with the cap determined using a bottom-up approach.

- Linear Reduction Factor: Applied to the aviation cap to align with overall emission reduction efforts.

- Phase-Out of Free Allocation: Free allocations to aircraft operators will be phased out by 2026, increasing the auctioned share to support sustainable aviation fuels.

- Between 2024 and 2030, 20 million aviation allowances are reserved to support the adoption of alternative fuels.

**Maritime Transport Inclusion**    Starting in 2024, maritime transport is covered by the EU ETS. This sector inclusion increased the cap by 78.4 million allowances, based on emissions data from 2018 and 2019.

**Cap and its Reduction Trajectory**

- Between 2024 and 2027, the annual reduction factor for the emissions cap will increase to 4.3%, and from 2028 onward, it will rise to 4.4%.

- A 2023 revision targets a 62% reduction in emissions by 2030, compared to 2005 levels.

- Scheduled reductions in allowances: 90 million allowances in 2024 and 27 million allowances in 2026.

- The EU ETS cap for 2024 is specified as 1,386,051,745 allowances.

- New Entrant Reserve: A reserve of allowances from Phase 3 (2013–2020) is retained to accommodate new entrants.

By systematically identifying vulnerable sectors and adjusting free allowance allocations, the European Commission aims to prevent carbon leakage while encouraging industries to reduce emissions.

## 1.3    Allocation of Permits

With this groundwork laid, we now arrive at the crux of the ETS introduction: the allocation of emission permits. In the subsequent section, the distribution of permits will take center stage, as the cap established earlier represents the limited resource agents are competing for. This process mirrors the allocation of any scarce resource, underscoring both its value and the complexities in its fair distribution. In our analysis, these agents may be individual firms or entire countries, each with unique stakes in securing their share of this finite resource.

### 1.3.1    Auctioning

According to: [2] (Commission, Auctioning of allowances) Since 2013, auctioning has been the primary method for distributing emission allowances in the EU ETS, upholding the 'polluter pays' principle by requiring emitters to purchase the right to emit pollutants. Member States conduct these auctions under the EU ETS Directive and Auctioning Regulation, ensuring they are open, transparent, harmonized, and non-discriminatory. These rules also apply to Iceland, Liechtenstein, Norway, and the UK's electricity generation in Northern Ireland.

For the 2021–2030 period, the European Commission has specified auction shares for general and aviation allowances. Up to 57% of general allowances are auctioned, with the remainder allocated for free to mitigate carbon leakage risk and promote low-carbon technologies. Of the auctioned allowances:

- 90% are distributed among Member States based on their historical emissions.

- 10% are allocated to 16 specific Member States to promote solidarity.

From July 2023 to August 2026, a portion of allowances is redirected to the Recovery and Resilience Facility to fund the REPowerEU Plan. In aviation, approximately 15% of allowances have been auctioned, increasing gradually so that most are auctioned from 2026 onward.

**Use of Auction Revenues**     Auctioning generates significant revenues for national budgets and funds like the Innovation Fund and Modernisation Fund. Since 2013, the EU ETS has raised over EUR 200 billion, with EUR 43.6 billion generated in 2023 alone, of which EUR 33 billion was distributed to Member States.

Member States are required to use at least 50% of auction revenues—and all revenues from aviation allowances—for climate and energy-related purposes. Between 2013 and 2020, they reported spending an average of 75% of these revenues on projects such as renewable energy, energy efficiency, and low-emission transport. From mid-2023, all EU ETS revenues (or an equivalent amount) must support the green transition, including measures to address social impacts. Member States are also encouraged to fund the decarbonization of maritime transport and protect marine biodiversity.

Under the Regulation on the Governance of the Energy Union and Climate Action, Member States report annually on how they use EU ETS revenues, which the Commission summarizes in its annual Climate Action Progress Reports.

**Auctioning Rules and Platforms**     The Auctioning Regulation outlines the procedures to ensure auctions are conducted fairly. In October 2023, a new regulation was adopted to reflect updates to the EU ETS and the REPowerEU plan.

Currently, 28 countries—including 25 EU Member States plus Iceland, Liechtenstein, and Norway—use the common auction platform, the European Energy Exchange (EEX) in Leipzig, Germany. Germany, Poland, and the UK (for Northern Ireland) have opted out of the common platform but continue to use EEX for their auctions.

**Auction Calendars and Results**     Auction calendars are set by the auctioning platform in accordance with regulatory requirements, detailing the dates and volumes of allowances to be auctioned per Member State and for specific funds. These calendars and daily auction results are available on the platform's website, with detailed quarterly reports providing additional information on auction outcomes, participants, and revenues.

### 1.3.2   Benchmark

As described in [7] EU ETS Handbook.

**Definition** : A benchmark is a reference value for greenhouse gas (GHG) emissions, measured in tonnes of $CO_2$ ($tCO_2$) per unit of production activity. It is used to determine the level of free emission allowances each installation within a sector receives under the EU Emissions Trading System (EU ETS).

**Purpose** : A benchmark is not an emission limit or a reduction target. All installations within a sector receive the same allocation of allowances per unit of activity. Installations with GHG emissions lower than the benchmark may receive more free allowances than they need, potentially allowing them to sell the surplus.

**Basis** : Benchmarks are set on an output basis whenever possible, considering all GHG emissions from the entire production process for a specific product. In the EU ETS, product benchmarks are based on the average GHG performance of the top 10% most efficient installations producing that product in the EU.

To establish these benchmarks, industry sectors collected GHG emissions data from ETS installations during 2007 and 2008, following Article 10a(2) of the EU ETS Directive. By plotting the specific emissions (emissions per unit of output) of all installations in ascending order, a "benchmarking curve" was created for each sector. The average efficiency of the top 10% best-performing installations was then determined from this curve and set as the benchmark for allocation rules. If insufficient data was available, the best available techniques were used as a starting point to develop the benchmarks.

This algorithm provides a systematic method for establishing benchmarks in the EU ETS, ensuring that free allocation of allowances is based on actual performance data and encourages efficiency within sectors. It rewards installations that are more efficient than the benchmark while incentivizing others to reduce their emissions.

### 1.3.3 Free Allocagtion & Carbon Leakage

Carbon leakage occurs when businesses relocate production to countries with less stringent emission constraints due to increased costs from climate policies, rendering the climate policies both useless and harmful to the economy at the regulator. This risk is particularly significant in energy-intensive industries. [3]

**European Commission's Algorithm to Address Carbon Leakage**

To combat carbon leakage, the European Commission implements a systematic approach under the EU Emissions Trading System (EU ETS) [3] [7]

Financial Compensation for Indirect Emissions:

- Member States can offer compensation to electro-intensive sectors for higher electricity costs due to the EU ETS.

---

**Algorithm 1**: Algorithm for Establishing Product Benchmarks in the EU ETS

---

**Result**: Benchmark value BM for each product

**Input**: Set of Installations $I$ producing a specific product;

For each installation $i \in I$:

    GHG emissions data $E(i)$ over the period 2007–2008;

    Production output data $P(i)$ over the same period.

1 **for** *each installation $i$ in $I$* **do**

2     Calculate specific emissions $SE(i)$:

3

$$SE(i) = \frac{E(i)}{P(i)}$$

4 **end for**

5 Sort installations $I$ in ascending order of $SE(i)$.

6 Determine the number of installations representing the top 10% most efficient:

7

$$n_{10\%} = \lceil 0.10 \times |I| \rceil$$

8 Select the set $I_{\text{top}}$ of the $n_{10\%}$ installations with the lowest $SE(i)$.

9 Calculate the benchmark BM as the average specific emissions of $I_{\text{top}}$:

10

$$\text{BM} = \frac{1}{n_{10\%}} \sum_{i \in I_{\text{top}}} SE(i)$$

11 **if** *Insufficient data is available for the product* **then**

12     Use Best Available Techniques (BAT) to estimate BM.

13 **end if**

14 **Output**: Benchmark value BM for the product, to be used in allocation rules.

---

- This is governed by EU state aid rules and is limited to 25% of auction revenues, unless justified otherwise.

- Transparency measures require regular publication of compensation amounts.

With the allocation $A(i)$, we proceed to distribute free emission permits. The algorithm provided above is simplified, as a full exploration of the ETS free allocation mechanism lies outside the scope of this thesis. However, it is worth noting that Article 10c of the EU ETS Directive enables certain lower-income Member States to allocate free permits specifically for modernizing their energy sectors. This mechanism supports investment in energy diversification, infrastructure upgrades, and clean technologies, contributing to fairer and more sustainable emissions reductions. Further details can be found in Article 10c and the allocation for Phase IV and how countries responded to their claim for free Allocation is described on Table 1.1. [1]

**Algorithm 2:** IDENTIFYING AND ADDRESSING CARBON LEAKAGE UNDER THE EU ETS

**Result:** Allocation Plan of Free Emission Allowances to Sectors

**Input:** Set of Sectors $S$;

For each sector $s \in S$: Direct Costs $C_d(s)$, Indirect Costs $C_i(s)$, Gross Value Added GVA$(s)$, Trade Intensity TI$(s)$, Historical Activity Level HAL$(s)$, Benchmark BM$(s)$

1 **for** *each sector $s$ in $S$* **do**
2    Calculate cost impact $CI(s)$:
3

$$CI(s) = \frac{C_d(s) + C_i(s)}{\text{GVA}(s)}$$

4    **if** *($CI(s) \geq 5\%$ **and** TI$(s) \geq 10\%$) **or** ($CI(s) \geq 30\%$ **or** TI$(s) \geq 30\%$)* **then**
5       Mark sector $s$ as **At Significant Risk of Carbon Leakage**
6 **end for**
7 Compile the **Carbon Leakage List** $\mathcal{L}$ with all sectors marked **At Significant Risk**.
8 **for** *each installation $i$ in sector $s$* **do**
9    Determine the applicable benchmark BM$(i)$ based on the product produced. algorithm 1;
10    Calculate the Historical Activity Level HAL$(i)$ as the median production in a baseline period (e.g., 2005–2008 or 2009–2010).
11    Calculate allocation $A(i)$ using:
12

$$A(i) = \text{BM}(i) \times \text{HAL}(i) \times \text{CLEF}(s) \times \text{CF}$$

   where:
13     CLEF$(s)$ is the Carbon Leakage Exposure Factor:
14      **if** *$s$ is **At Significant Risk*** **then**
15       CLEF$(s) = 100\%$
16     **else**
17       CLEF$(s)$ decreases from 80% in 2013 to 30% in 2020.
18     **end if**
19     CF is the Correction Factor:
20      **if** *$i$ is a non-electricity generator* **then**
21       CF = Cross-Sectoral Correction Factor (CSCF), ensuring total allocation stays within limits.
22     **else if** *$i$ is an electricity generator* **then**
23       CF = Linear Reduction Factor (LRF), in line with emission reduction targets.
24     **end if**
25 **end for**
26 **for** *Phase 4 (2021–2030)* **do**
27    Update the Carbon Leakage List using refined criteria based on trade and emissions intensity.
28    **for** *each sector $s$ in $S$* **do**
29     **if** *$s$ is **Highly Exposed*** **then**
30       Continue allocating allowances at 100% of the benchmark.
31     **else if** *$s$ is **Less Exposed*** **then**
32       Allocate allowances at 30% until 2026, then phase out by 2030.
33     **end if**
34    **end for**
35 **end for**
36 **Output:** Detailed allocation plan $A(s)$ for all sectors to mitigate the risk of carbon leakage.

| Eligible Member States | Maximum Article 10c derogation (40% of regular allowances) | Amount to be used under Article 10c | Amount transferred from Article 10c to the Modernisation Fund | Amount to be auctioned |
|---|---|---|---|---|
| Bulgaria | 51,599,838 | 51,599,838 | 0 | 0 |
| Czechia | 111,462,281 | 0 | 111,462,281 | 0 |
| Estonia | 17,583,702 | 0 | 0 | 17,583,702 |
| Croatia | 11,957,703 | 0 | 5,978,852 | 5,978,851 |
| Latvia | 3,794,677 | 0 | 0 | 3,794,677 |
| Lithuania | 8,696,818 | 0 | 8,696,818 | 0 |
| Hungary | 34,610,750 | 20,748,000 | 0 | 13,862,750 |
| Poland | 273,211,665 | 0 | 0 | 273,211,665 |
| Romania | 91,673,704 | 5,600,000 | 86,073,704 | 0 |
| Slovakia | 33,228,414 | 0 | 33,228,414 | 0 |
| **Total** | 637,819,552 | 77,947,838 | 245,440,068 | 314,431,646 |

**Table 1.1**: Allocation of allowances under Article 10c for the modernization of the energy sector in eligible Member States in Phase IV.

# Chapter 2

# Fair Distribution - Fair Division

**2.1  intro + meaning**

**2.2  principles**

**2.3  theory + main concepts of achieving fairness**

**2.4  How fairness consideration influences policy decisions**

**Chapter 3**

# Exploring Fairness in Free Allocation under the EU ETS

## 3.1 Introduction

Fairness in the allocation of free allowances under the European Union Emissions Trading System (EU ETS) is critical to its effectiveness and acceptance among member countries. This chapter presents three experiments that explore different dimensions of fairness using the same dataset of economic and energy attributes of EU member countries.

1. **Experiment 1**: Investigates the relationship between the similarity of countries' profiles and the similarity of their free allowance allocations by analyzing all pairwise combinations of countries.

2. **Experiment 2**: Examines whether using the median country as a reference point improves the explanation of free allowance allocations.

3. **Experiment 3**: Explores the extent to which optimal linear combinations of features can explain the allocations, identifying countries that cannot explain the rest even when overfitting is allowed.

### 3.1.1 Data Collection

The dataset of the following experiments is common. The dataset includes economic and energy attributes for EU member countries from 2005 to 2020. The indicators used are listed in Table 3.1, sourced from the World Bank and Eurostat. The data used are presented in this table, but can also be found in the Appendix more descriptively.

### 3.1.2 Correlation Analysis

The following experiments, investigate the relationship between 2 values. To accomplish this, tools measuring the existence of a correlation between two values are needed. In the upcoming experiments, we will primarily present the $R^2$ value as the key indicator of linearity. Additional metrics—including the Pearson correlation coefficient, p-values from regression analysis, and error metrics such as Mean Squared Error (MSE)—that further support or challenge the linearity assumption will be provided in the Appendix for comprehensive reference.

**Table 3.1**: List of Indicators along with the Allocation Principles of [14] (Zhou & Wang 2016)

| Indicators | Principle | Data Source |
|---|---|---|
| Population | Fairness | `https://data.worldbank.org/indicator/SP.POP.TOTL` |
| GDP per capita | Fairness | `https://data.worldbank.org/indicator/NY.GDP.PCAP.CD` |
| Inflation | Fairness | `https://data.worldbank.org/indicator/FP.CPI.TOTL.ZG` |
| Agriculture | Fairness | `http://wdi.worldbank.org/table/4.2#` |
| Industry | Fairness | `http://wdi.worldbank.org/table/4.2#` |
| Manufacturing | Fairness | `http://wdi.worldbank.org/table/4.2#` |
| Total Energy Supply | Fairness | `https://ec.europa.eu/eurostat/databrowser/view/nrg_bal_s/` |
| Energy Intensity | Economic Efficiency | `https://ec.europa.eu/eurostat/databrowser/view/NRG_IND_EI` |
| Verified Emissions | Fairness | `https://www.eea.europa.eu/data-and-maps/dashboards/emissions-trading-viewer-1` |

## 3.2 Experiment 1: Analyzing Pairwise Similarities Among Countries

**Objective**   To determine whether countries with similar economic and energy attributes receive comparable levels of free allowances by analyzing all possible pairwise combinations of countries, and to assess whether this relationship varies across different phases of the EU ETS.

**Hypothesis**   There is a positive correlation between the Euclidean distances of countries' attribute profiles and the differences in their free allowance allocations across all pairs of countries. Specifically, countries with similar attributes should have similar allocations. We expect that the strength and nature of this correlation may differ depending on the phase of the EU ETS being examined, due to changes in allocation methodologies and regulatory adjustments over time.

### 3.2.1  Methodology

**Data Segmentation by ETS Phases**   The EU ETS has been implemented in distinct phases, each characterized by different allocation rules and market conditions:

- **Phase I (2005-2007)**

- **Phase II (2008-2012)**

- **Phase III (2013-2020)**

For this experiment, we divide the dataset according to these phases and perform the analysis separately for each phase to investigate potential differences in the relationship between countries' attribute similarities and allocation differences.

**Data Normalization**   Normalize all attributes to ensure comparability across different scales. This is achieved by dividing each attribute by its maximum value within each phase to account for temporal changes in the data.

**Calculate Pairwise Distances**

- **Attribute Distance ($D_{x_{ij}}$):** For every pair of countries $i$ and $j$, calculate the Euclidean distance between their attribute vectors $\vec{x_i}$ and $\vec{x_j}$.

$$D_{x_{ij}} = \sqrt{\sum_{k=1}^{n} (x_{ik} - x_{jk})^2}$$

- **Allocation Difference ($D_{Y_{ij}}$):** Calculate the absolute difference between their free allowance allocation $Y_i$ and $Y_j$.

$$D_{Y_{ij}} = |Y_i - Y_j|$$

**Correlation Analysis**

- **Scatter Plot:** Plot $D_{x_{ij}}$ against $D_{Y_{ij}}$ $\forall$ country pairs.

- **Statistical Analysis:** Compute $r^2$ value of the linear regression to assess the strength of the relationship.

### 3.2.2  Results and Analysis

**Table 3.2:** Analytic data for the linear regression of experiment section 3.2

| year | pear-son cor.n | spear-man cor. | ken-dall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|------|------|------|------|------|------|------|------|------|------|------|
| 2005 | 0.84 | 0.71 | 0.53 | 0 | 0.71 | 0.02 | 0.13 | 0.11 | 0 | 0.22 |
| 2006 | 0.84 | 0.69 | 0.52 | 0 | 0.70 | 0.02 | 0.13 | 0.11 | 0 | 0.23 |
| 2007 | 0.79 | 0.65 | 0.48 | 0 | 0.62 | 0.02 | 0.15 | 0.12 | 0 | 0.25 |
| 2008 | 0.80 | 0.69 | 0.51 | 0 | 0.64 | 0.02 | 0.15 | 0.12 | 0 | 0.19 |
| 2009 | 0.76 | 0.62 | 0.46 | 0 | 0.58 | 0.03 | 0.16 | 0.13 | 0 | 0.22 |
| 2010 | 0.74 | 0.59 | 0.43 | 0 | 0.55 | 0.03 | 0.16 | 0.13 | 0 | 0.22 |
| 2011 | 0.79 | 0.64 | 0.47 | 0 | 0.62 | 0.02 | 0.15 | 0.13 | 0 | 0.25 |
| 2012 | 0.79 | 0.64 | 0.46 | 0 | 0.63 | 0.02 | 0.15 | 0.13 | 0 | 0.27 |
| 2013 | 0.77 | 0.60 | 0.44 | 0 | 0.59 | 0.02 | 0.15 | 0.12 | 0 | 0.30 |
| 2014 | 0.77 | 0.59 | 0.44 | 0 | 0.59 | 0.02 | 0.15 | 0.12 | 0 | 0.30 |
| 2015 | 0.80 | 0.62 | 0.47 | 0 | 0.64 | 0.02 | 0.14 | 0.11 | 0 | 0.28 |
| 2016 | 0.77 | 0.59 | 0.44 | 0 | 0.60 | 0.02 | 0.15 | 0.11 | 0 | 0.27 |
| 2017 | 0.79 | 0.60 | 0.44 | 0 | 0.62 | 0.02 | 0.14 | 0.11 | 0 | 0.30 |
| 2018 | 0.81 | 0.63 | 0.47 | 0 | 0.65 | 0.02 | 0.14 | 0.11 | 0 | 0.28 |
| 2019 | 0.81 | 0.63 | 0.47 | 0 | 0.65 | 0.02 | 0.14 | 0.11 | 0 | 0.28 |
| 2020 | 0.77 | 0.57 | 0.42 | 0 | 0.59 | 0.02 | 0.15 | 0.12 | 0 | 0.32 |

The findings from Experiment 1 provide compelling insights into the relationship between economic and energy attribute similarities and free allowance allocations across EU member countries. The results confirm our initial hypothesis, but also reveal intriguing patterns and variations across different phases of the EU ETS, especially as the allocation methodology evolved.

## Key Observations

1. **Positive Correlation between Similarity and Allocation**: The analysis shows a notable correlation between countries' profile similarities (measured by Euclidean distance) and the similarity in their free allowance allocations. This finding supports our hypothesis that countries with comparable economic and energy profiles tend to receive similar levels of allowances, aligning with fairness in allocation.

2. **Impact of ETS Phase on Correlation**: As expected, the strength of this correlation diminishes slightly in Phase III (2013-2020), reflecting changes in allocation methods, including the gradual phase-out of the grandfathering principle. The decline is mostly apparent through the values of Pearson Correlation coefficient, Spearman correlation coefficient, $r^2$, and the prize of the Quadratic coefficient, which can be found on Table 3.2 This decline suggests that adjustments in the regulatory framework influenced the predictability of allocation based on attribute similarity.

3. **Country-Specific Variations**: Analysis of individual countries reveals parallel trends with differing y-intercepts, suggesting that country-specific factors influence baseline

**Figure 3.1**: Experiment 1 Distances from all the countries to all the others
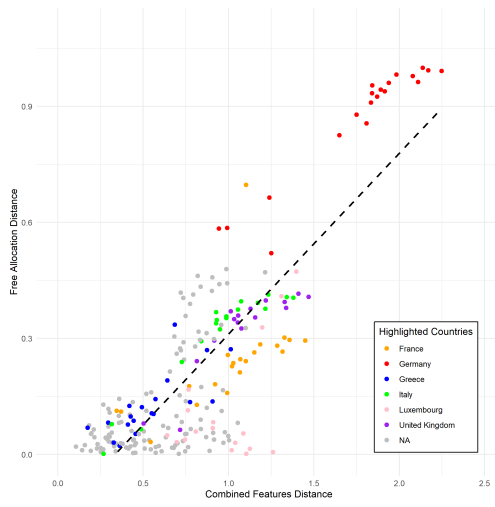
**(a)** Phase I: 2006
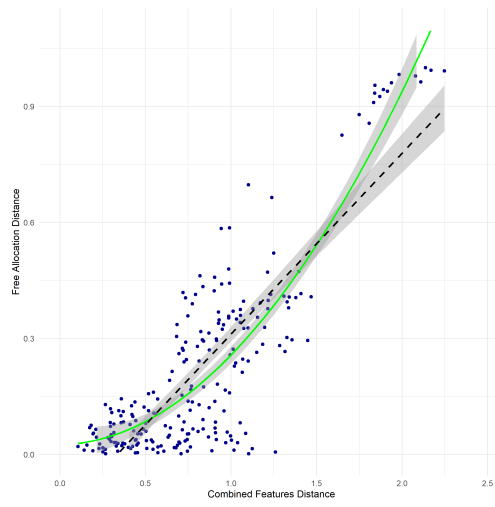
**(b)** Phase I: 2006
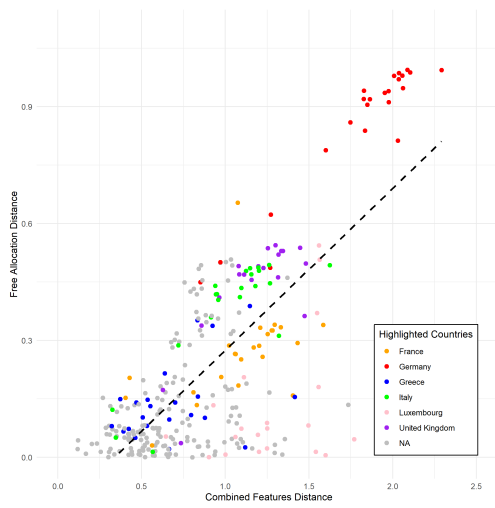
**(c)** Phase II: 2010
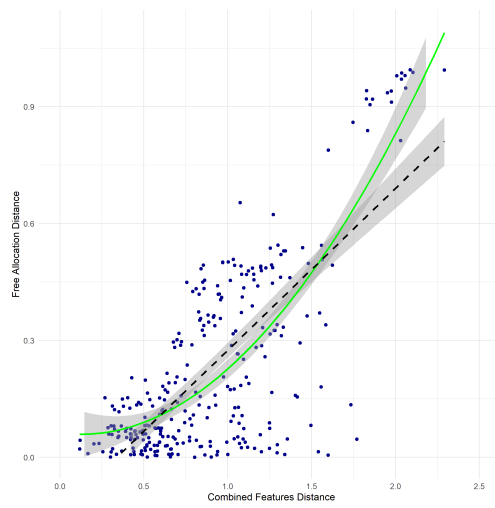
**(d)** Phase II: 2010
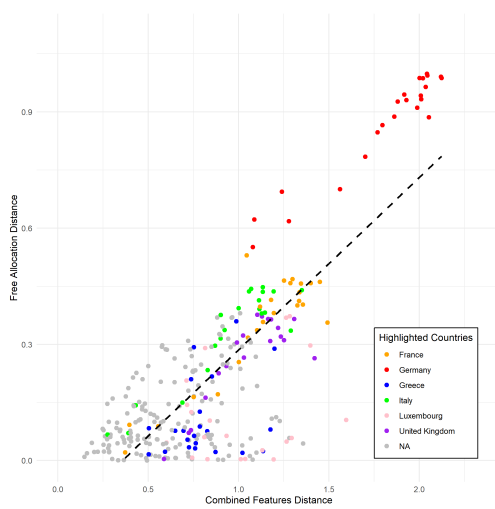
**(e)** Phase III: 2018

**(f)** Phase III: 2018

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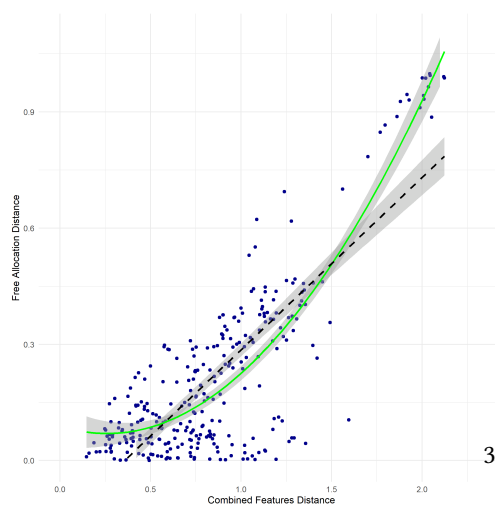
allocations, even among countries with similar profiles. Some of the most influential countries are displayed in different colors.

4. **Quadratic Fit and Country-Based Lines**: A quadratic model appears better to capture the data patterns than a simple linear approximation. However, closer inspection reveals that this improvement may be due to distinct clusters of country-specific lines rather than a single, overarching quadratic relationship. This insight motivates the design of our next experiment, which investigates whether using a single "median" country as a reference point could refine our understanding of allocation consistency across the dataset.

## 3.3 Experiment 2: Using the Median Country as a Reference Point

**Objecive** To investigate whether using the median country as a reference improves the explanation of free allowance allocations, thereby assessing the fairness of allocations relative to a central benchmark.

**Hypothesis** The Euclidean distance of each country's attribute profile from the median country's profile is positively correlated with the difference in their free allowance allocations from that of the median country.

### 3.3.1 Methodology

---

**Algorithm 3**: Find median Country (Ρεαλιστικά αυτό δε λέει τίποτα, αλλά πρόσφατα κάποιο paper εγραφε τόσο και πιο αυτιστικά έναν αλγόειθμο, οπότε αποφάσισα να το κάνω και εγώ)

---

**Result**: The median Country
**Input**: The Attributes $\vec{X}$

1 **Initialize** rank accumulation vector $R$ with $R(c) = 0$ for each country $c$.
2 **for** *each attribute $A_i$ in $\vec{X}$* **do**
3     Sort countries $c$ by $A_i$, assigning ranks $r(c, A_i)$ from 1 to $|C|$.
4 **end for**
5 **for** *each country $c$* **do**
6     Update cumulative rank: $R(c) \leftarrow R(c) + r(c, A_i)$
7 **end for**
8 Sort countries by $R(c)$ in ascending order. Define the median country $c_{\text{median}}$ as:

$$c_{\text{median}} = \text{sorted}(R) \left[ \frac{|C|}{2} \right]$$

9 **Output** $c_{\text{median}}$ to find its $\overrightarrow{X_{mid}}$.

---

**Determine the median country**   Use algorithm 3 to identify the median country based on cumulative attribute rankings.

**Calculating the Distances from the median Country**

- **Attribute Distance** ($D_{X_i}$): Calculate the Euclidean distance between each country's attribute vector $\overrightarrow{x_i}$ and the median country's attribute vector $\overrightarrow{x_{median}}$.

$$D_{x_i} = \sqrt{\sum_{k=1}^{n} x_{ik} - x_{median,k}}$$

- **Allocation Difference** ($D_{Y_i}$): Calculate the absolute difference between each country's free allocation $Y_i$ and that of the median country $Y_{median}$.

$$D_{Y_i} = |Y_i - Y_{median}|$$

### 3.3.2   Results and Analysis

Table 3.4: Analytic data for the linear regression of experiment section 3.3

| Mid country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Sweden | 2005 | 0.76 | 0.42 | 0.28 | 0 | 0.58 | 0.02 | 0.15 | 0.12 | 0.00 | 0.39 |
| Estonia | 2006 | 0.87 | 0.61 | 0.45 | 0 | 0.76 | 0.01 | 0.11 | 0.09 | 0.01 | 0.24 |
| Estonia | 2007 | 0.81 | 0.52 | 0.36 | 0 | 0.66 | 0.02 | 0.13 | 0.10 | 0.01 | 0.30 |
| Lithuania | 2008 | 0.85 | 0.67 | 0.50 | 0 | 0.72 | 0.01 | 0.12 | 0.09 | 0.05 | 0.20 |
| Sweden | 2009 | 0.73 | 0.50 | 0.36 | 0 | 0.53 | 0.02 | 0.15 | 0.11 | 0.04 | 0.30 |
| Bulgaria | 2010 | 0.71 | 0.53 | 0.35 | 0 | 0.51 | 0.02 | 0.14 | 0.10 | 0.03 | 0.31 |
| Austria | 2011 | 0.78 | 0.61 | 0.45 | 0 | 0.61 | 0.02 | 0.13 | 0.11 | 0.00 | 0.35 |
| Sweden | 2012 | 0.75 | 0.45 | 0.34 | 0 | 0.56 | 0.02 | 0.14 | 0.11 | 0.00 | 0.46 |
| Estonia | 2013 | 0.71 | 0.46 | 0.34 | 0 | 0.51 | 0.03 | 0.16 | 0.12 | 0.01 | 0.42 |
| Bulgaria | 2014 | 0.76 | 0.52 | 0.39 | 0 | 0.58 | 0.02 | 0.14 | 0.11 | 0.01 | 0.33 |
| Ireland | 2015 | 0.79 | 0.31 | 0.23 | 0 | 0.62 | 0.02 | 0.13 | 0.11 | 0.00 | 0.76 |
| Hungary | 2016 | 0.76 | 0.47 | 0.36 | 0 | 0.57 | 0.02 | 0.14 | 0.10 | 0.02 | 0.29 |
| Austria | 2017 | 0.69 | 0.37 | 0.30 | 0 | 0.48 | 0.02 | 0.13 | 0.09 | 0.00 | 0.43 |
| United Kingdom | 2018 | 0.76 | 0.67 | 0.49 | 0 | 0.57 | 0.01 | 0.09 | 0.06 | 0.33 | -0.23 |
| Austria | 2019 | 0.75 | 0.43 | 0.33 | 0 | 0.56 | 0.01 | 0.11 | 0.08 | 0.00 | 0.39 |
| Bulgaria | 2020 | 0.75 | 0.47 | 0.36 | 0 | 0.56 | 0.02 | 0.14 | 0.11 | 0.01 | 0.34 |

**Figure 3.2**: Experiment 2 Distances from from the median country
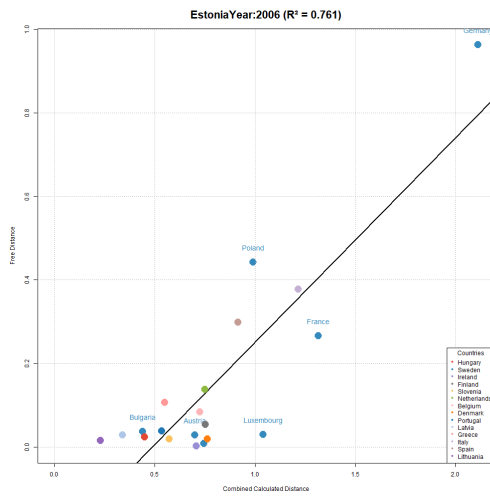


**(a)** Phase I: 2006
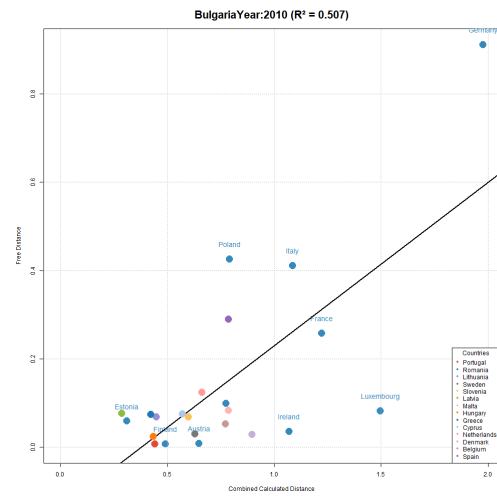


**(b)** Phase II: 2010
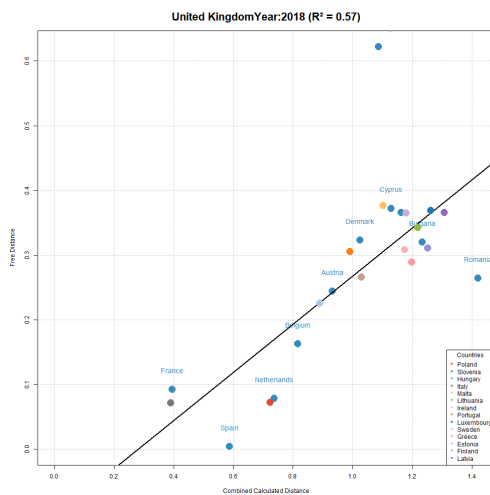


**(c)** Phase III: 2018
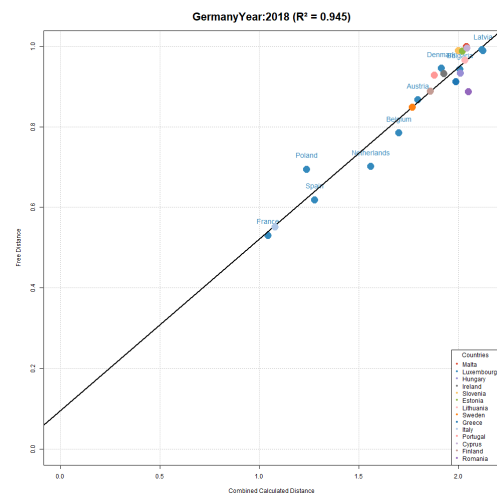


**(d)** Phase III: 2018 NOT THE MEDIAN

**Key Observations**

1. **Limited Explanatory Power of the Median Country**: The median country does not serve as an effective benchmark for explaining free allowance allocations across other countries, indicating that central tendencies alone may not capture the nuances in allocations.

2. **Potential Explanatory Role of Specific Countries**: Certain countries, like Germany, display inherent differences that make them potentially better reference points for explaining allocations in other countries. This suggests that specific national profiles might be more representative than a simple median.

3. **Phase-Independence of Results**: The weak correlation observed in this experiment appears largely unaffected by the phase of the EU ETS, suggesting that these poor results are consistent across different regulatory periods.

## 3.4   Experiment 3: Optimal Feature Weights

**Objective**   To find the best linear combination of attributes (allowing for potential overfitting) for each country to assess whether some countries cannot explain the allocations of others, regardless of the model used.

**Hypothesis**   Even with optimized models that allow overfitting, certain countries cannot adequately explain the free allocations of others, highlighting disparities in the allocation mechanism.

### 3.4.1   Methodology

**Feature Selection and Model Building**:

- For each country $i$, build a linear regression model to predict free allocations $Y$ of other countries using their attributes $Y$ and the country's own attributes $\vec{x_i}$. The following attributes were included:

  1. Total energy supply
  2. GDP per capita
  3. Population
  4. Inflation
  5. Agriculture
  6. Industry
  7. Manufacturing
  8. Energy Intensity

  In this experiment, we avoided using verified emissions as this would be too correlated on its own.

- Allow the model to find the optimal weights for each attribute, using algorithm R's built in optim package that utilizes "L-BFGS-B" (a general purpose optimizer), potentially leading to overfitting.

**Evaluation of Model Performance**:   Record all the $R^2$ values using another country every time.

### 3.4.2 Results and Analysis

**Table 3.6:** $R^2$ values for all the countries throughout the years of the ETS section 3.4

| Country | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 | 2018 | 2019 | 2020 |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Austria | 0.82 | 0.81 | 0.80 | 0.84 | 0.83 | 0.83 | 0.82 | 0.82 | 0.89 | NA | 0.89 | 0.90 | 0.89 | 0.87 | 0.85 | 0.87 |
| Belgium | 0.77 | 0.75 | 0.73 | 0.77 | 0.75 | 0.77 | 0.75 | 0.75 | 0.81 | 0.80 | 0.79 | 0.81 | 0.78 | 0.75 | 0.74 | 0.75 |
| Bulgaria | 0.83 | 0.82 | NA | 0.83 | 0.81 | 0.83 | 0.80 | 0.80 | 0.92 | NA | 0.92 | 0.93 | 0.92 | 0.91 | 0.91 | 0.92 |
| Denmark | 0.82 | 0.82 | 0.80 | 0.85 | 0.84 | 0.84 | 0.83 | 0.83 | 0.92 | 0.92 | 0.92 | 0.93 | 0.92 | 0.92 | 0.91 | 0.92 |
| Estonia | 0.84 | 0.83 | 0.81 | 0.86 | 0.85 | 0.86 | 0.84 | NA | 0.93 | 0.93 | NA | 0.93 | 0.93 | 0.92 | 0.92 | 0.93 |
| Finland | 0.80 | 0.79 | 0.77 | 0.82 | 0.81 | 0.82 | 0.81 | 0.81 | 0.89 | 0.89 | 0.90 | 0.91 | NA | 0.89 | 0.89 | 0.90 |
| France | 0.31 | 0.35 | 0.23 | NA | 0.09 | 0.20 | 0.18 | NA | 0.73 | 0.71 | 0.56 | 0.58 | 0.55 | 0.53 | 0.52 | 0.50 |
| Germany | 0.83 | 0.82 | 0.80 | 0.86 | 0.85 | 0.85 | 0.84 | 0.84 | 0.93 | 0.93 | 0.93 | 0.94 | 0.94 | 0.93 | 0.92 | 0.93 |
| Greece | 0.74 | 0.72 | 0.67 | 0.71 | 0.71 | 0.70 | 0.68 | 0.72 | 0.92 | 0.92 | 0.91 | 0.92 | 0.92 | 0.90 | NA | 0.91 |
| Hungary | 0.82 | 0.81 | 0.80 | 0.84 | 0.82 | 0.83 | 0.82 | 0.82 | 0.91 | NA | 0.91 | 0.92 | 0.91 | 0.90 | 0.90 | 0.91 |
| Ireland | 0.84 | 0.82 | 0.81 | NA | 0.85 | 0.85 | 0.84 | 0.83 | 0.92 | 0.92 | 0.92 | 0.93 | 0.92 | NA | 0.90 | 0.91 |
| Italy | 0.72 | NA | 0.64 | 0.86 | 0.85 | 0.85 | 0.83 | 0.77 | 0.87 | 0.84 | 0.85 | 0.86 | 0.85 | 0.81 | 0.81 | 0.84 |
| Latvia | 0.84 | 0.83 | 0.82 | 0.87 | 0.86 | 0.86 | 0.85 | 0.85 | 0.93 | 0.93 | 0.93 | 0.94 | 0.93 | 0.92 | 0.92 | 0.93 |
| Lithuania | 0.84 | 0.83 | 0.82 | 0.86 | 0.86 | 0.86 | 0.85 | 0.84 | 0.93 | 0.93 | 0.93 | 0.93 | 0.93 | NA | 0.92 | 0.93 |
| Luxembourg | 0.84 | 0.83 | 0.82 | 0.87 | 0.86 | 0.86 | 0.85 | 0.85 | 0.93 | 0.93 | 0.93 | 0.94 | 0.93 | 0.92 | 0.92 | 0.93 |
| Netherlands | 0.69 | 0.68 | 0.64 | 0.67 | 0.60 | 0.62 | 0.57 | 0.59 | 0.69 | 0.68 | 0.62 | 0.65 | 0.60 | 0.55 | 0.53 | 0.59 |
| Poland | 0.72 | 0.72 | 0.69 | 0.68 | NA | 0.62 | 0.64 | 0.68 | 0.79 | 0.79 | 0.78 | 0.81 | 0.80 | 0.78 | 0.78 | 0.80 |
| Portugal | NA | 0.80 | 0.79 | 0.83 | 0.82 | 0.83 | 0.81 | 0.82 | 0.92 | 0.92 | 0.91 | 0.92 | 0.92 | NA | 0.91 | 0.92 |
| Slovenia | 0.84 | 0.83 | 0.82 | 0.87 | 0.86 | 0.86 | 0.85 | 0.84 | 0.93 | 0.93 | 0.93 | 0.93 | 0.93 | NA | 0.92 | 0.93 |
| Spain | 0.67 | 0.68 | 0.57 | 0.72 | 0.66 | 0.66 | 0.62 | 0.66 | 0.83 | 0.84 | 0.82 | 0.84 | 0.83 | 0.80 | 0.79 | 0.82 |
| Sweden | 0.82 | 0.81 | 0.80 | 0.84 | 0.83 | 0.83 | 0.81 | 0.81 | 0.86 | 0.87 | 0.87 | 0.88 | 0.87 | 0.86 | 0.86 | 0.88 |
| United Kingdom | 0.64 | 0.66 | 0.63 | 0.82 | 0.83 | 0.83 | 0.86 | 0.90 | 0.75 | 0.79 | 0.71 | 0.76 | 0.67 | 0.64 | 0.58 | 0.65 |

**Table 3.8:** The weights for all the countries throughout the years of the ETS section 3.4

| Country | Period | Energy Supply | GDPpc | Population | Inflation | Agriculture | Industry | Manufacturing | Energy Intensity | Max Std |
|---|---|---|---|---|---|---|---|---|---|---|
| Austria | Period 1 | 7.51 | 0.00 | 100.00 | 0.02 | 0.70 | 1.71 | 1.18 | 0.84 | 12.01 |
| | Period 2 | 50.53 | 0.17 | 78.39 | 0.00 | 0.21 | 2.27 | 0.28 | 0.00 | 43.53 |
| | Period 3 | 100.00 | 1.12 | 0.00 | 0.15 | 0.00 | 1.91 | 0.00 | 0.37 | 2.02 |
| Belgium | Period 1 | 30.30 | 6.51 | 99.99 | 0.61 | 1.31 | 6.29 | 0.00 | 1.59 | 27.68 |
| | Period 2 | 78.00 | 5.17 | 56.29 | 0.54 | 0.00 | 0.00 | 2.11 | 2.15 | 51.91 |
| | Period 3 | 99.99 | 9.20 | 0.00 | 0.37 | 0.28 | 0.00 | 1.07 | 0.83 | 1.31 |
| Bulgaria | Period 1 | 4.22 | 0.00 | 99.98 | 3.87 | 0.15 | 0.50 | 0.53 | 0.29 | 8.43 |
| | Period 2 | 54.38 | 0.01 | 82.49 | 0.54 | 0.00 | 2.28 | 2.83 | 0.04 | 48.80 |
| | Period 3 | 100.00 | 0.00 | 3.98 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.63 |

*(continued)*

| Country | Period | Energy Supply | GDPpc | Popu-lation | Inflation | Agricul-ture | Industry | Manufac-turing | Energy Inten-sity | Max Std |
|---|---|---|---|---|---|---|---|---|---|---|
| Denmark | Period 1 | 8.56 | 0.42 | 99.91 | 0.76 | 0.96 | 5.42 | 0.63 | 0.67 | 13.04 |
| | Period 2 | 61.90 | 0.00 | 67.08 | 0.18 | 0.21 | 4.55 | 0.00 | 0.31 | 45.30 |
| | Period 3 | 100.00 | 0.00 | 3.32 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 2.93 |
| Estonia | Period 1 | 6.22 | 0.00 | 100.00 | 0.51 | 0.37 | 1.55 | 5.63 | 0.00 | 9.92 |
| | Period 2 | 57.65 | 0.00 | 61.58 | 0.03 | 0.00 | 1.39 | 0.02 | 0.00 | 48.90 |
| | Period 3 | 100.00 | 0.00 | 5.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 4.02 |
| Finland | Period 1 | 31.42 | 6.35 | 99.98 | 0.41 | 2.04 | 0.00 | 0.74 | 1.34 | 35.50 |
| | Period 2 | 82.92 | 0.45 | 53.95 | 0.13 | 0.00 | 2.17 | 0.24 | 0.00 | 50.78 |
| | Period 3 | 100.00 | 0.00 | 0.00 | 0.00 | 0.10 | 0.00 | 0.00 | 0.00 | 0.16 |
| France | Period 1 | 0.00 | 9.43 | 8.84 | 10.34 | 3.07 | 0.00 | 99.94 | 13.15 | 19.52 |
| | Period 2 | 0.00 | 4.29 | 42.90 | 11.46 | 0.00 | 0.00 | 99.00 | 15.03 | 23.34 |
| | Period 3 | 0.00 | 6.09 | 80.11 | 7.68 | 22.89 | 54.66 | 55.70 | 0.00 | 50.64 |
| Germany | Period 1 | 4.28 | 0.00 | 85.35 | 1.45 | 16.15 | 67.19 | 58.46 | 7.30 | 43.12 |
| | Period 2 | 53.63 | 0.00 | 73.23 | 0.00 | 13.90 | 0.00 | 77.29 | 12.62 | 41.06 |
| | Period 3 | 84.75 | 0.00 | 3.11 | 8.31 | 9.57 | 16.67 | 75.05 | 11.87 | 40.82 |
| Greece | Period 1 | 5.36 | 4.26 | 99.99 | 6.08 | 8.63 | 12.72 | 3.97 | 0.94 | 17.42 |
| | Period 2 | 59.33 | 2.63 | 68.22 | 0.47 | 0.00 | 0.00 | 2.26 | 2.88 | 52.30 |
| | Period 3 | 100.00 | 0.00 | 3.64 | 0.00 | 0.09 | 0.00 | 0.00 | 0.00 | 2.12 |
| Hungary | Period 1 | 8.17 | 0.00 | 99.99 | 0.01 | 1.57 | 2.58 | 1.60 | 0.44 | 14.68 |
| | Period 2 | 60.50 | 0.00 | 82.76 | 0.37 | 0.01 | 3.79 | 0.00 | 0.00 | 35.12 |
| | Period 3 | 100.00 | 0.00 | 7.53 | 0.01 | 0.23 | 0.00 | 0.00 | 0.00 | 2.53 |
| Ireland | Period 1 | 7.67 | 0.00 | 99.99 | 0.00 | 0.08 | 0.59 | 1.79 | 1.01 | 11.33 |
| | Period 2 | 62.09 | 0.20 | 67.49 | 0.08 | 0.35 | 4.49 | 0.00 | 0.48 | 44.79 |
| | Period 3 | 100.00 | 0.00 | 1.37 | 0.00 | 0.00 | 0.04 | 0.12 | 0.09 | 1.87 |
| Italy | Period 1 | 99.87 | 0.00 | 15.25 | 0.00 | 2.47 | 0.00 | 0.01 | 0.00 | 17.86 |
| | Period 2 | 99.96 | 0.05 | 17.30 | 3.15 | 1.89 | 0.73 | 2.73 | 0.00 | 11.61 |
| | Period 3 | 99.98 | 0.35 | 2.06 | 1.08 | 4.04 | 0.91 | 0.00 | 0.24 | 3.69 |
| Latvia | Period 1 | 4.30 | 0.00 | 100.00 | 0.58 | 0.00 | 0.00 | 0.18 | 1.00 | 7.92 |
| | Period 2 | 59.54 | 0.00 | 69.29 | 0.00 | 0.00 | 0.00 | 0.00 | 0.04 | 43.22 |
| | Period 3 | 100.00 | 0.00 | 4.87 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 4.00 |
| Lithuania | Period 1 | 6.44 | 0.00 | 100.00 | 0.94 | 0.00 | 0.00 | 1.20 | 0.32 | 9.52 |
| | Period 2 | 60.19 | 0.00 | 68.12 | 0.00 | 0.03 | 0.00 | 0.00 | 0.00 | 43.86 |
| | Period 3 | 100.00 | 0.00 | 3.60 | 0.00 | 0.07 | 0.00 | 0.03 | 0.01 | 3.31 |
| Luxembourg | Period 1 | 6.72 | 0.00 | 100.00 | 0.43 | 0.00 | 0.39 | 0.18 | 0.71 | 11.14 |
| | Period 2 | 59.65 | 0.00 | 69.55 | 0.00 | 0.00 | 0.02 | 0.00 | 0.05 | 44.08 |
| | Period 3 | 100.00 | 0.00 | 5.64 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 4.13 |
| Netherlands | Period 1 | 44.27 | 14.34 | 99.77 | 1.09 | 2.26 | 0.99 | 15.57 | 1.65 | 33.97 |
| | Period 2 | 98.51 | 9.55 | 41.52 | 2.43 | 0.00 | 0.00 | 8.15 | 16.93 | 45.54 |
| | Period 3 | 100.00 | 12.09 | 0.00 | 3.77 | 4.25 | 0.00 | 0.84 | 29.53 | 9.96 |

| Country | Period | Energy Supply | GDPpc | Popu- lation | Inflation | Agricul- ture | Industry | Manufac- turing | Energy Inten- sity | Max Std |
|---|---|---|---|---|---|---|---|---|---|---|
| Poland | Period 1 | 0.00 | 0.12 | 99.87 | 8.05 | 18.01 | 0.00 | 3.21 | 0.00 | 17.34 |
| | Period 2 | 23.00 | 0.00 | 99.99 | 6.55 | 2.53 | 0.00 | 3.12 | 0.00 | 32.88 |
| | Period 3 | 96.36 | 0.00 | 34.96 | 2.69 | 2.77 | 0.00 | 0.00 | 4.44 | 39.15 |
| Portugal | Period 1 | 18.11 | 0.00 | 99.99 | 0.00 | 2.49 | 2.01 | 0.45 | 0.17 | 11.91 |
| | Period 2 | 73.47 | 0.00 | 67.41 | 0.00 | 0.30 | 6.47 | 0.00 | 0.00 | 44.94 |
| | Period 3 | 100.00 | 0.00 | 1.70 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 2.34 |
| Slovenia | Period 1 | 8.49 | 0.00 | 100.00 | 0.00 | 0.03 | 0.00 | 0.19 | 1.01 | 13.46 |
| | Period 2 | 59.30 | 0.00 | 69.99 | 0.00 | 0.00 | 0.00 | 0.00 | 0.08 | 43.79 |
| | Period 3 | 100.00 | 0.00 | 7.29 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 4.31 |
| Spain | Period 1 | 100.00 | 0.45 | 40.90 | 7.94 | 18.04 | 0.00 | 38.87 | 0.11 | 31.84 |
| | Period 2 | 100.00 | 1.49 | 62.89 | 2.20 | 0.00 | 0.00 | 34.49 | 0.00 | 22.45 |
| | Period 3 | 100.00 | 0.00 | 29.18 | 3.71 | 0.00 | 14.26 | 0.00 | 0.00 | 7.11 |
| Sweden | Period 1 | 0.00 | 0.00 | 99.91 | 0.00 | 0.90 | 2.50 | 2.26 | 0.83 | 3.26 |
| | Period 2 | 40.52 | 1.04 | 63.11 | 0.10 | 0.59 | 3.28 | 0.35 | 0.00 | 54.31 |
| | Period 3 | 100.00 | 0.42 | 0.96 | 0.02 | 0.00 | 0.02 | 0.00 | 0.00 | 1.47 |
| United King- dom | Period 1 | 91.27 | 0.00 | 10.68 | 16.05 | 0.00 | 0.00 | 42.88 | 0.09 | 43.90 |
| | Period 2 | 99.98 | 0.00 | 11.57 | 0.00 | 0.00 | 0.00 | 15.02 | 0.46 | 21.23 |
| | Period 3 | 100.00 | 0.00 | 0.00 | 0.38 | 0.00 | 2.66 | 15.15 | 0.00 | 8.92 |

The outcomes of Experiment 3 offer profound insights into the complexities of modeling free allowance allocations among EU member countries. By seeking the optimal linear combination of eight key economic and energy attributes for each country, we aimed to determine the extent to which individual countries can explain the allocation patterns of others, even when overfitting is permitted.

**Variability in Predictive Accuracy**: Table Table 3.6 presents the highest $R^2$ values achieved for each country across different years using any linear combination of the selected attributes. The results reveal significant variability in predictive accuracy among countries:

- **High Predictive Power**: Countries like Austria, Denmark, Sweden, and Germany consistently achieved high $R^2$ values, often exceeding 0.85 across all EU ETS phases. This suggests that these countries' economic and energy profiles are sufficiently representative to model the allocations of other member states effectively.

- **Low Predictive Power**: Conversely, countries such as Poland and France exhibited lower $R^2$ values, indicating a weaker ability to explain others' allocations. Poland's $R^2$ values, for instance, hovered around 0.72 in Phase I and only marginally improved in later

phases, highlighting inherent differences in its profile that are not captured by the linear models.

**Diversity in Optimal Attribute Weights**: Table Table 3.8 illustrates the optimal weights assigned to each attribute that yielded the best $R^2$ values for each country during the three EU ETS phases. Key observations include:

- **Attribute Dominance**: Many countries heavily weighted the Total Energy Supply attribute. For example, Italy, Spain, and Germany assigned nearly 100% weight to this attribute in certain periods, underscoring its significance in their allocation models.

- **Varied Attribute Importance**: Other countries displayed a more diversified weighting. France, for instance, placed substantial weight on attributes like Manufacturing and Agriculture, reflecting the unique aspects of its economic structure.

- **Shifts Across Phases**: The optimal weights for some countries changed notably across different ETS phases, indicating adjustments in their economic profiles or in the allocation mechanism itself.

**Systematic Patterns and Anomalies**:

1. **Consistent Underperformance**: Despite overfitting allowances, some countries like Poland and Netherlands struggled to achieve high $R^2$ values consistently. This suggests that the selected attributes may not fully capture the factors influencing their allocation patterns or that their allocations are influenced by unique, unmodeled factors.

2. **Robust Predictors**: Countries such as Sweden and Denmark maintained high predictive power without significant overfitting, indicating that their economic and energy profiles are more aligned with the overall allocation mechanisms of the EU ETS.

3. **Influence of Data Availability**: Some entries are marked as Not Available (NA) due to data limitations or optimization errors, highlighting challenges in data consistency and the need for comprehensive datasets for accurate modeling.

### 3.4.3 Discussion

The findings of Experiment 3, combined with insights from Experiments 1 and 2, reveal the complexities and nuances in attempting to model the fairness of EU ETS free allowance allocations. The observed variability in predictive accuracy among member states highlights the limitations of linear models when applied to the unique economic and energy profiles of each country. Given these findings, a cluster analysis may provide a more effective approach to account for the diversity among member states, grouping countries with similar economic and energy profiles to better understand underlying patterns in allocation outcomes.

The limitations observed, such as Poland's distinct reliance on coal or France's diverse economic activities, indicate that these countries may belong to clusters that differ significantly

from the rest of the EU. Instead of striving for a one-size-fits-all model, cluster analysis would allow for the identification of groups of countries that share similar structural characteristics, thereby enabling a more granular approach to modeling their allocation patterns.

## 3.5   Conclusion

The analysis across the three experiments underscores the need for a more nuanced approach to modeling free allowance allocations within the EU ETS. Notably, the significant differences in predictive accuracy suggest that a cluster analysis could uncover groups of countries with similar economic and energy profiles, offering insights beyond those provided by linear models. This approach would allow for a better understanding of shared allocation patterns and reduce the risk of oversimplification inherent in standardized linear models.

## 3.6   INCLUDE RADAR PLOTS, ADD OTHER PLOTS

# Chapter 4

# Understanding EU ETS through clustering

[6] (Dimos et al., 2023)

## 4.1   Introduction

In this chapter, we aim to deepen our understanding of the free allowance allocation under the European Union Emissions Trading System (EU ETS) by employing a clustering analysis of EU Member States based on selected economic and energy indicators. The allocation of emission allowances is a critical component of the EU ETS, impacting the fairness and efficiency of the system. By examining how different countries are grouped according to relevant attributes, we can gain insights into the underlying principles governing the allocation process and assess whether the allocation aligns with notions of equity and economic efficiency.

Building upon the analyses conducted in the previous chapter, where we examined the fairness of free allowance allocations through various experiments, this chapter introduces a clustering approach to categorize EU Member States and explores the relationship between these clusters and the allocation of free allowances.

## 4.2   Data Collection and Indicator Selection

Following the indicator selection methodology outlined by [14] Zhou and Wang (2016), we select a set of economic and energy indicators that represent the principles of fairness and economic efficiency in the context of emission allowance allocation. The indicators are chosen to capture various aspects of each country's profile, including population size, economic health, energy consumption, and intensity.

The selected indicators, along with their associated allocation principles and data sources, are presented in Table 4.1.

We consider data from 2005 to 2020, covering the first three phases of the EU ETS:

- **Phase I** (2005-2007): The pilot phase, primarily utilizes grandfathering allocation methods.

**Table 4.1**: List of Indicators along with the Allocation Principles (Adapted from Zhou & Wang, 2016)

| Indicators | Principle | Data Source |
|---|---|---|
| Population | Fairness | `https://data.worldbank.org/indicator/SP.POP.TOTL` |
| GDP per capita | Fairness | `https://data.worldbank.org/indicator/NY.GDP.PCAP.CD` |
| Inflation | Fairness | `https://data.worldbank.org/indicator/FP.CPI.TOTL.ZG` |
| Agriculture | Fairness | `http://wdi.worldbank.org/table/4.2#` |
| Industry | Fairness | `http://wdi.worldbank.org/table/4.2#` |
| Manufacturing | Fairness | `http://wdi.worldbank.org/table/4.2#` |
| Total Energy Supply | Fairness | `https://ec.europa.eu/eurostat/databrowser/view/nrg_bal_s/` |
| Energy Intensity | Economic Efficiency | `https://ec.europa.eu/eurostat/databrowser/view/NRG_IND_EI` |
| Verified Emissions | Fairness | `https://www.eea.europa.eu/data-and-maps/dashboards/emissions-trading-viewer-1` |
| Free Allocated Allowances | - | `https://www.eea.europa.eu/data-and-maps/dashboards/emissions-trading-viewer-1` |

- **Phase II** (2008-2012): The first commitment period under the Kyoto Protocol, with continued use of grandfathering.

- **Phase III** (2013-2020): A shift towards benchmarking and auctioning, with more centralized allocation rules.

The selection of these indicators aims to capture the principles of fairness, such as the ability to pay and vertical equity, and economic efficiency, which relates to the effective use of resources in reducing emissions.

## 4.3   Methodology

### 4.3.1   Data Normalization

Before conducting the cluster analysis, it is essential to normalize the data to ensure that each indicator contributes equally to the clustering process. **In this chapter, we focus on normalizing each indicator by dividing the value for each country by the corresponding average across all countries for each year**. This approach provides a straightforward and balanced comparison across countries, ensuring that each indicator's influence on clustering is consistent.

Nonetheless, other normalization methods could be employed, each offering unique advantages:

- **Division by Maximum**: Dividing each value by the maximum of the dataset ensures that all values lie between zero and one, emphasizing the relative size of each country's indicator.

- **Linear Normalization or "Max-Min" Method**: Using the $(x - x_{\min})/(x_{\max} - x_{\min})$ formula allows for a balanced scaling between minimum and maximum values, helping to mitigate the impact of outliers.

- **Principal Component Analysis (PCA) Normalization**: PCA employs a normalization that focuses on preserving the variance structure, highlighting the most impactful indicators across dimensions.

Each of these alternative methods provides a distinct perspective and could influence how clusters are perceived and interpreted. However, for the purposes of this chapter, the average-based normalization remains the primary method used in the analysis.

### 4.3.2   Clustering Method

We employ the k-means clustering algorithm to categorize the EU Member States based on the selected indicators. K-means clustering is a partitioning method that aims to divide a set of observations into $k$ clusters in which each observation belongs to the cluster with the nearest mean, serving as a prototype of the cluster.

### 4.3.3   Determination of Optimal Number of Clusters

Determining the optimal number of clusters, $k$, is a crucial step in the clustering process. We utilize the NbClust package in R to identify the best number of clusters. The NbClust function provides 30 indices for determining the number of clusters and proposes the best clustering scheme based on the majority rule.

Given the relatively small number of countries (25 EU Member States considered), we restrict the possible number of clusters to between 3 and 5 to ensure meaningful and interpretable groupings.

For every year, those indicators are summarized in a table like that:

```
    **************************************************************
* Among all indices:
* 9 proposed 3 as the best number of clusters
* 2 proposed 4 as the best number of clusters
* 8 proposed 5 as the best number of clusters
* 5 proposed 7 as the best number of clusters

                     ***** Conclusion *****

* According to the majority rule, the best number of clusters is  3
```

Table 4.2 presents the results from every year with the votes on every Number of clusters. The algorithm used normalized data -using the mean of each attribute - and the range in which the indices could search was 3 to 7.

It is clear that the clustering is not unique, but we need to standardize one clustering to perform our analysis. We chose the clustering that results from the data of 2018 by using the mean for normalization. Here we can observe its difference from other clusterings produced on data from other years. In the first plot we let each year produce the best clustering, even with a different number of clusters. On the second, we forced it to be equal to the 3 clusters of 2018.

### 4.3.4  Results of Clustering

The NbClust analysis suggests that the optimal number of clusters is 3. The resulting clusters of EU Member States are illustrated in Figure 4.2

**Temporal Consistency of Clustering**

To assess the stability of these clusters over time, we compared the clustering results of 2018 with those from other years. When allowing each year to determine its optimal number of clusters (Figure 4.2a), we observed variations in cluster composition and number. However, when we fixed the number of clusters to three for all years (Figure 4.2 b), the clusters remained relatively consistent over time. This consistency suggests that the clustering based on the 2018 data provides a reasonable representation of the Member States' grouping throughout the EU ETS phases.

**Cluster Composition**

- **Cluster 1**: France, Germany, Italy, Poland, Spain, United Kingdom

- **Cluster 2**: Bulgaria, Estonia, Hungary, Latvia, Lithuania, Romania

**Figure 4.1**: Comparisons of clusters of 2018 vs other years
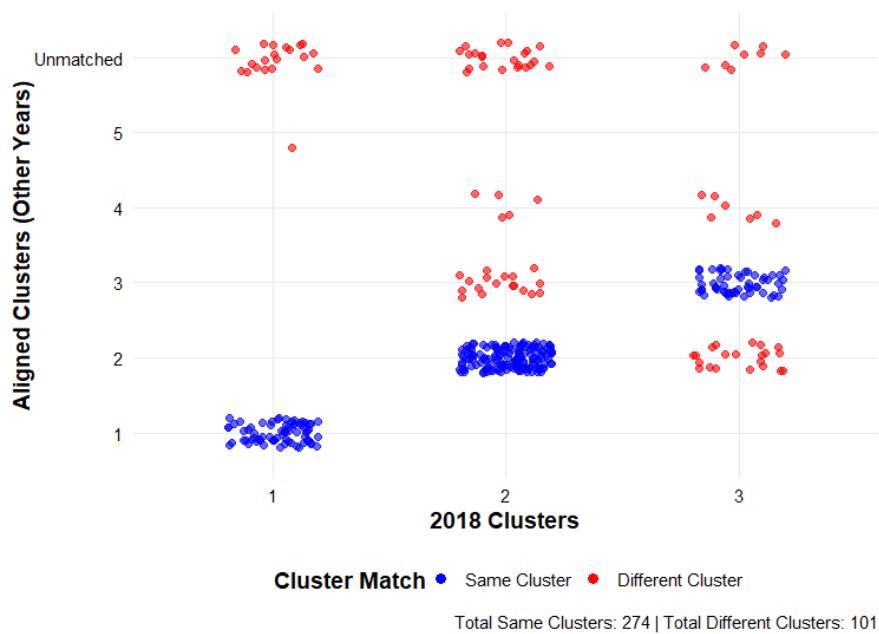


**(a)** Each year could yield different number of clusters
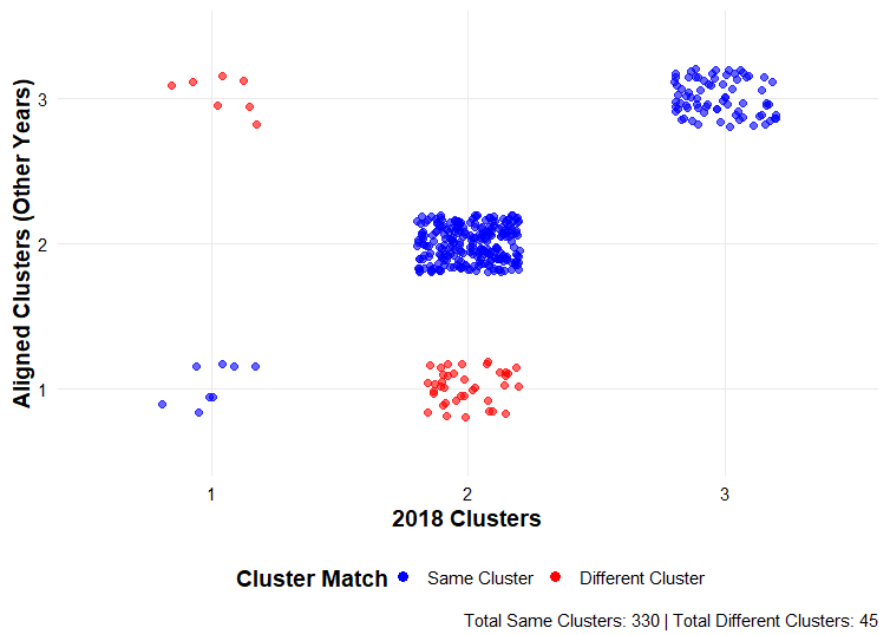


**(b)** All years forced to have 3 clusters

| Year | Clusters = 3 | Clusters = 4 | Clusters = 5 | Clusters = 6 | Clusters = 7 | Majority Cluster |
|------|-----------|-----------|-----------|-----------|-----------|-------------------|
| **Phase I (2005-2007)** | | | | | | |
| 2005 | 9 | 2 | 8 | 0 | 5 | 3 |
| 2006 | 6 | 7 | 7 | 2 | 1 | 4 |
| 2007 | 10 | 2 | 10 | 2 | 0 | 3 |
| **Summary** | Phase I shows a preference for clusters of 3 and 5, with the majority clustering at 3 in most years. | | | | | |
| **Phase II (2008-2012)** | | | | | | |
| 2008 | 5 | 3 | 13 | 0 | 2 | 5 |
| 2009 | 8 | 9 | 1 | 3 | 3 | 4 |
| 2010 | 6 | 1 | 6 | 2 | 9 | 7 |
| 2011 | 8 | 2 | 3 | 6 | 4 | 3 |
| 2012 | 6 | 3 | 2 | 10 | 3 | 6 |
| **Summary** | Phase II exhibits more variation, with clusters of 4, 5, 6, and 7 all being favored in different years, although cluster 3 remains the most voted. | | | | | |
| **Phase III (2013-2020)** | | | | | | |
| 2013 | 10 | 6 | 1 | 3 | 4 | 3 |
| 2014 | 10 | 4 | 5 | 1 | 4 | 3 |
| 2015 | 6 | 2 | 4 | 7 | 5 | 6 |
| 2016 | 10 | 6 | 2 | 2 | 3 | 3 |
| 2017 | 13 | 3 | 6 | 0 | 2 | 3 |
| 2018 | 10 | 4 | 3 | 0 | 7 | 3 |
| 2019 | 10 | 4 | 3 | 0 | 7 | 3 |
| 2020 | 4 | 4 | 6 | 4 | 6 | 5 |
| **Summary** | Phase III heavily favors cluster 3, with occasional years leaning towards clusters 5 or 6, but the majority rule for most years remains at 3. | | | | | |

Table 4.2: Yearly cluster analysis with majority votes for optimal clusters in each phase.

- **Cluster 3**: Austria, Belgium, Cyprus, Denmark, Finland, Greece, Ireland, Luxembourg, Malta, Netherlands, Portugal, Slovenia, Sweden

**Cluster 1** comprises some of the largest economies and most populous countries in the EU. These countries have significant industrial sectors, higher total energy consumption, and larger verified emissions. Their economies are diverse, with substantial contributions from industry and manufacturing, which are energy-intensive sectors.

**Cluster 2** includes several Eastern European countries with smaller economies and lower GDP per capita. These countries often have higher energy intensity due to less efficient energy use and reliance on older technologies. Their industrial sectors may be significant relative to their economies, but in absolute terms, they are smaller than those in Cluster 1.
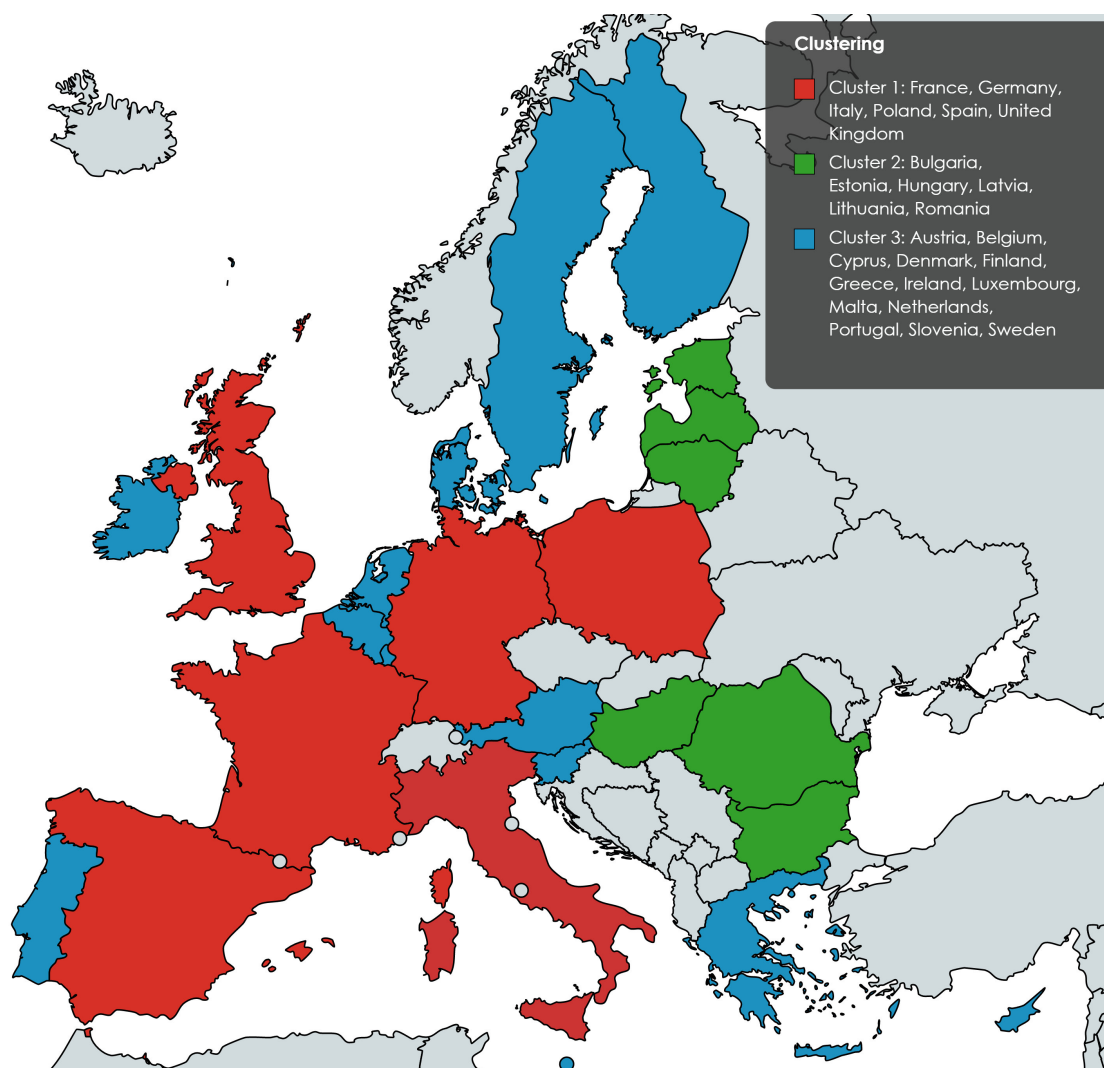
**Figure 4.2**: Map of Clustering

**Cluster 3** consists of a mix of smaller and medium-sized economies, many of which have higher GDP per capita and more advanced energy efficiency measures. These countries often have significant service sectors and have made substantial investments in renewable energy and energy efficiency technologies.

**Analysis of Clusters in Terms of Free Allowance Allocation**

The Figure 4.3 show the allocation of free emission permits. TO be precise, to shows:

1. Average Free Allocation Across Countries and Phases. This plot shows the average free allocation for each country across three phases: Phase 1 (2005-2007), Phase 2 (2008-2012),

and Phase 3 (2013-2020), grouped by clusters.

2. Average Free Allocation Across Countries and Phases (Log Scale). This plot uses a logarithmic scale to visualize average free allocation across countries and phases, allowing better comparison of data with a wide range of values.

3. Average Free Allocation per Capita Across Countries and Phases. This plot displays the average free allocation per capita for each country across the three phases, facilitating comparison of allocations on a per-person basis.

**Key Observations**:

1. **Declining Allocation Over Phases**: There is a clear declining trend in the allocation of free allowances across all clusters from Phase I to Phase III. This reflects the EU ETS's design, which progressively reduces the total number of allowances to encourage emissions reductions.

2. **Differences in Absolute Allocation**: Cluster 1 countries receive the highest absolute amounts of free allowances, consistent with their larger economies and higher emissions. Cluster 2 receives the lowest absolute allocations, while Cluster 3 sits between the other two clusters.

3. **Per Capita Allocation Differences**: When considering free allocation per capita (Figure 4.3c), Cluster 2 and 3 countries receive significantly higher allocations compared to Cluster 1, particularly in Phases I and II.

4. **Shift Towards Uniformity**: Over time, the per capita allocations among the clusters converge, indicating a shift towards a more uniform allocation approach in Phase III.

## 4.4 Regression Analysis

To further investigate the relationship between the selected indicators and the free allowance allocation, we perform a regression analysis. The goal is to assess which indicators are significant predictors of the allocation and how this relationship varies across the different phases of the EU ETS.

### 4.4.1 Regression Model Specification

Due to multicollinearity among some of the indicators, we select a subset of variables to include in the regression model:

- Population

- GDP per capita

- Composite Indicator: Total Energy Supply multiplied by Energy Intensity

The composite indicator captures the overall energy consumption adjusted for efficiency, providing a meaningful variable for analysis.

### 4.4.2 Regression Results

We perform the regression analysis separately for each phase of the EU ETS to account for changes in allocation rules and market conditions.

Table 4.3 summarizes the regression results of the different attributes, of different clusters through the phases.

<div align="center">

**Table 4.3:** $R^2$ Values Across Phases and Clusters

</div>

| Attribute | Phase | Cluster 1 $R^2$ | Cluster 2 $R^2$ | Cluster 3 $R^2$ |
|---|---|---|---|---|
| *Last Year's Verified emissions* | Phase I | All clusters | 0.9842 | — |
| | Phase II | All clusters | 0.9793 | — |
| | Phase III | All clusters | 0.9111 | — |
| *Last Year's Verified emissions* | Phase I | 0.9510 | 0.7115 | 0.9798 |
| | Phase II | 0.9573 | 0.9315 | 0.9697 |
| | Phase III | 0.8224 | 0.8245 | 0.7859 |
| Population | Phase I | 0.4515 | 0.08624 | 0.8275 |
| | Phase II | 0.4247 | 0.8879 | 0.8353 |
| | Phase III | 0.2807 | 0.7941 | 0.8011 |
| GDP per Capita | Phase I | 0.005165 | 0.127 | 0.006142 |
| | Phase II | 0.06907 | 0.4672 | 0.01339 |
| | Phase III | 0.07561 | 0.4774 | $6.58 \times 10^{-7}$ |
| Total Energy Supply | Phase I | 0.3634 | 0.1156 | 0.7121 |
| | Phase II | 0.3593 | 0.8039 | 0.7248 |
| | Phase III | 0.4334 | 0.6891 | 0.9706 |
| Total Energy Supply $\times$ Energy Intensity | Phase I | 0.3639 | 0.01803 | 0.6036 |
| | Phase II | 0.2556 | 0.6993 | 0.6321 |
| | Phase III | 0.4269 | 0.5703 | 0.9140 |

### 4.4.3 Key Observations

The regression analysis yields several important insights regarding the predictors of free allowance allocations across different phases and clusters:

1. **Verified Emissions**

- Exhibits consistently high $R^2$ values ranging from 0.78 to 0.98 across all phases and clusters.
- Indicates that verified emissions are a strong and reliable predictor of free allowance allocations.

2. **Population**

- Shows variable $R^2$ values, from as low as 0.08 to as high as 0.89.
- Significant predictor in Cluster 2 and Cluster 3, particularly during Phase II.

3. **GDP per Capita**

- Generally low $R^2$ values below 0.5 across all phases and clusters.
- Suggests that GDP per capita is not a significant determinant of free allowance allocations.

4. **Total Energy Supply**

- Displays moderate to high $R^2$ values, increasing in later phases.
- Strong predictor in Cluster 3 during Phase III with an $R^2$ of 0.9706.

5. **Composite Indicator (Total Energy Supply $\times$ Energy Intensity)**

- Exhibits a wide range of $R^2$ values from 0.02 to 0.91.
- Particularly strong predictor in Cluster 3 during Phase III ($R^2 = 0.9140$).

6. **Overall Trends**

- Increasing relevance of energy-related indicators in later phases of the EU ETS.
- Declining influence of GDP per capita over time, highlighting a shift towards energy efficiency and emissions-focused allocation criteria.

### 4.4.4  Implications of the Results

- **Grandfathering and Energy**: The near perfect $R^2$ values for verified emissions can be attributed to the grandfathering which, even though is declining, it was prevalent on Phase I and Phase II

- **Fairness Considerations**: The varying impact of population metrics suggests that fairness principles, such as per capita allocations, are significant, especially in certain clusters and phases.

- **Limited Role of Economic Wealth**: The minimal influence of GDP per capita indicates that economic prosperity per individual is not a primary factor in the allocation process, potentially avoiding biases towards wealthier nations.

## 4.5  Conclusion

This chapter has provided an in-depth analysis of the allocation of free emission allowances under the EU ETS by employing clustering and regression techniques. The clustering of EU Member States based on economic and energy indicators revealed three distinct groups, each with unique characteristics influencing their allocation of free allowances.

Our findings highlight that:

- **The Allocation Mechanism is Multifaceted**: The allocation of free allowances is not solely based on emissions levels but also incorporates considerations of economic size, energy intensity, and fairness principles.

- **Verified Emissions are a Key Determinant**: Across all clusters and phases, verified emissions are a strong predictor of free allocations, aligning with the economic efficiency principle by incentivizing reductions where they are most impactful.

- **Fairness Considerations are Evident**: Higher per capita allocations to less affluent, more energy-intensive countries suggest that the allocation mechanism accounts for differing capacities and challenges among Member States.

- **Policy Evolution Reflects Shifting Priorities**: The decreasing trend in free allocations and increasing significance of energy efficiency indicators indicate a shift towards stricter emissions control and a greater emphasis on sustainable energy practices.

Overall, the allocation of free allowances under the EU ETS appears to be guided by a nuanced approach that balances efficiency and equity.

## 4.6  PCA, CORRELATION MATRIX, OTHER NORMALIZATION METHODS

## 4.7  VALE STO APPENDIX TA ANALYTIKA DATA TOU NBclust GIA TA INDICES
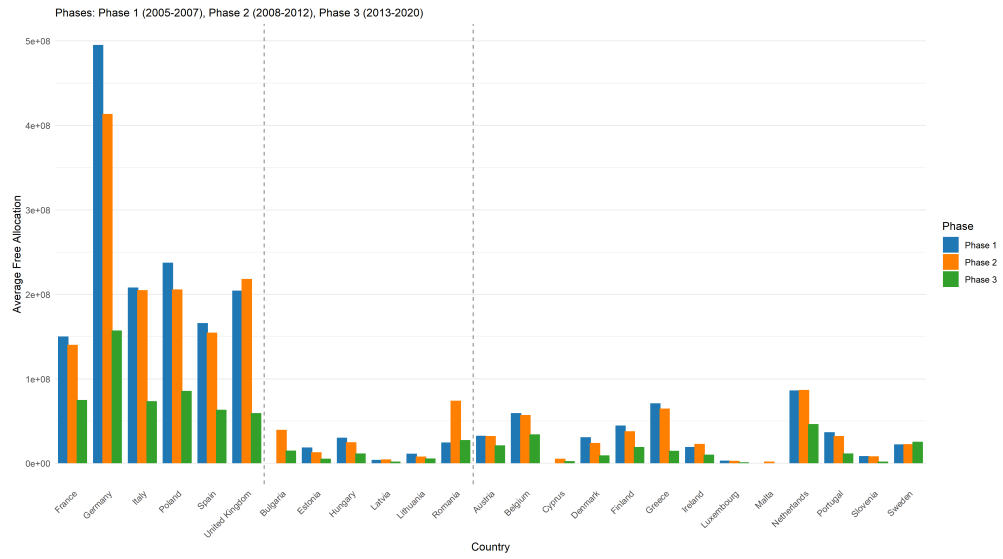
**(a)** Average Free Allocation Across Countries and Phases.
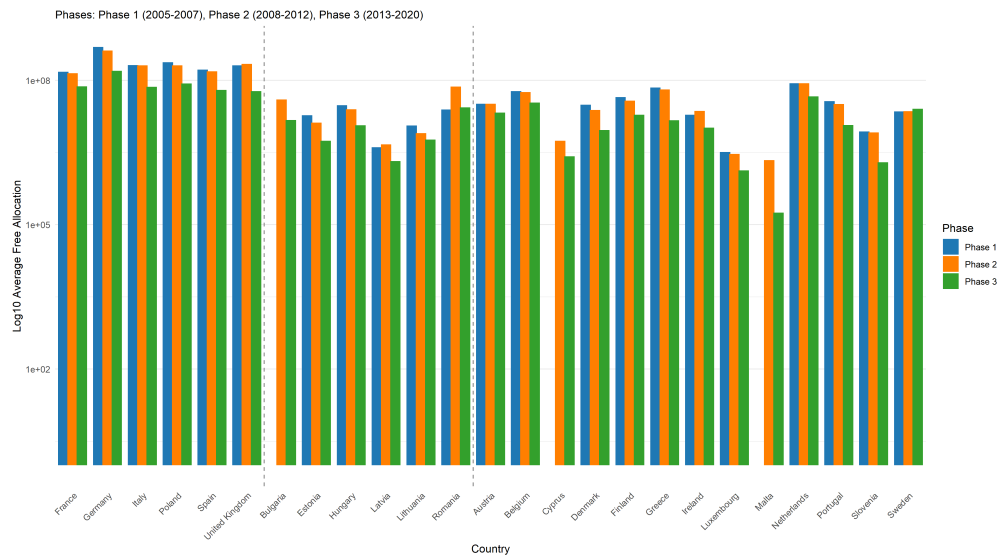


**(b)** Average Free Allocation Across Countries and Phases (Log Scale).
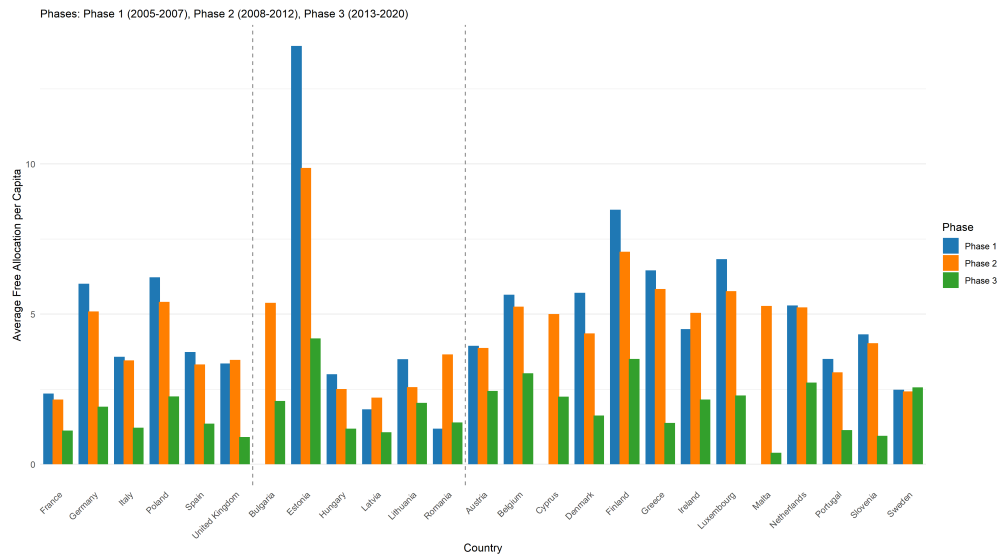
**(c)** Average Free Allocation per Capita Across Countries and Phases.

**Figure 4.3:** Comparison of Free Allocations Across Countries and Phases.
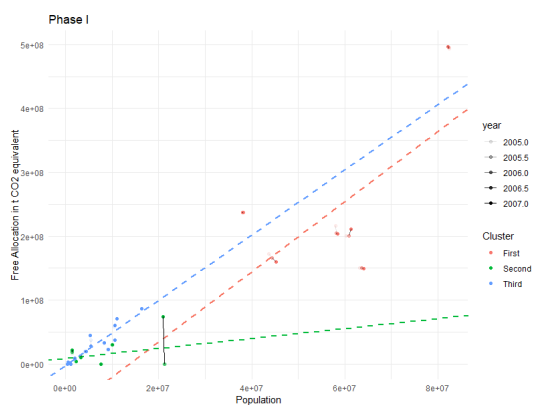
**(a)** Plot 1: Free Allocation vs Population for Phase I
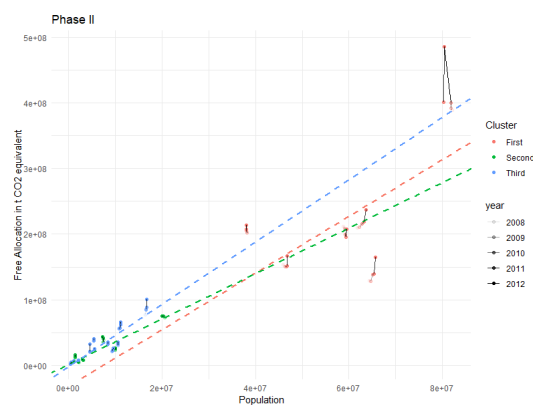


**(b)** Plot 2: Free Allocation vs Population for Phase II
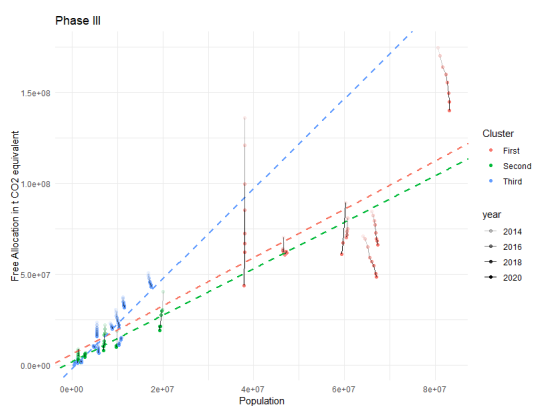


**(c)** Plot 3: Free Allocation vs Population for Phase III
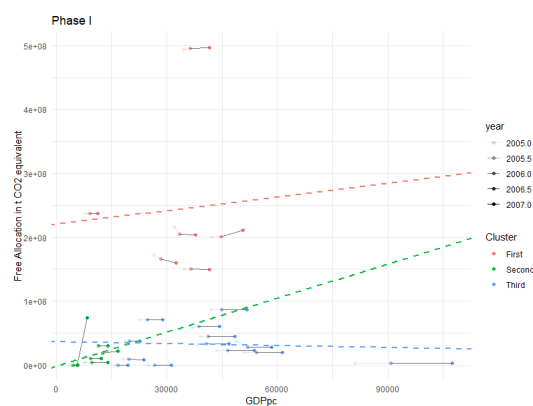


**(d)** Plot 4: Free Allocation vs GDP per capita for Phase I
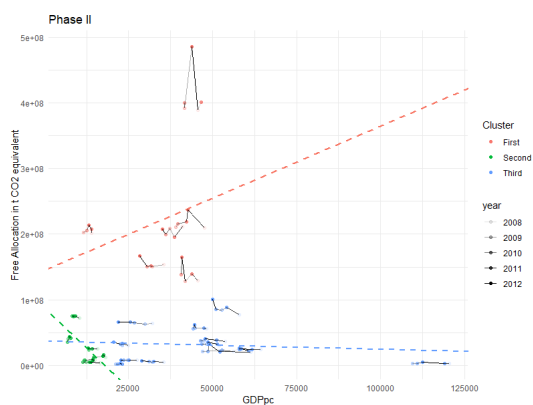


**(e)** Plot 5: Free Allocation vs GDP per capita for Phase II
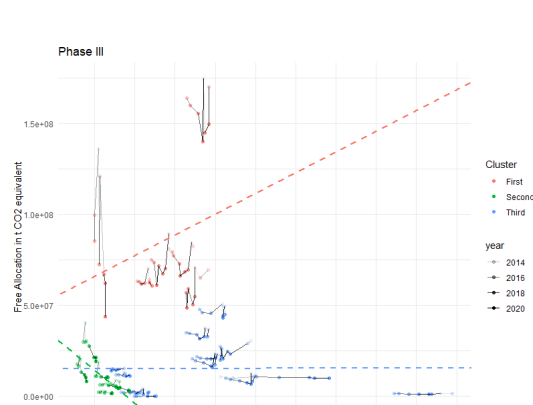


**(f)** Free Allocation vs GDP per capita for Phase III

**Figure** 4.4: Free Allocation vs Population and GDP per capita
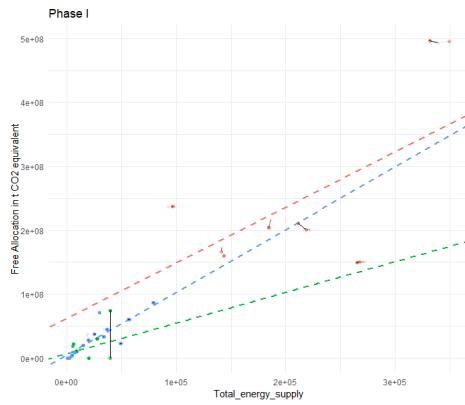
**(a)** Plot 1: Free Allocation vs Total Energy Supply for Phase I
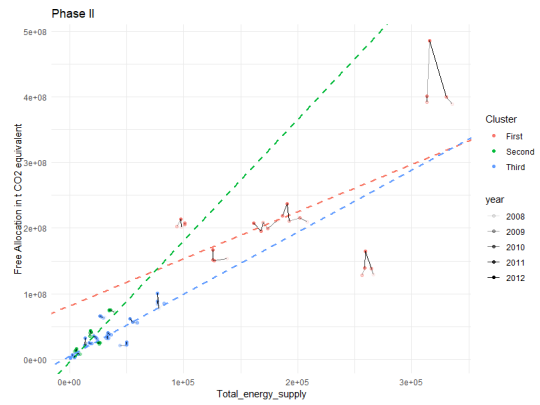


**(b)** Plot 2: Free Allocation vs Total Energy Supply for Phase II
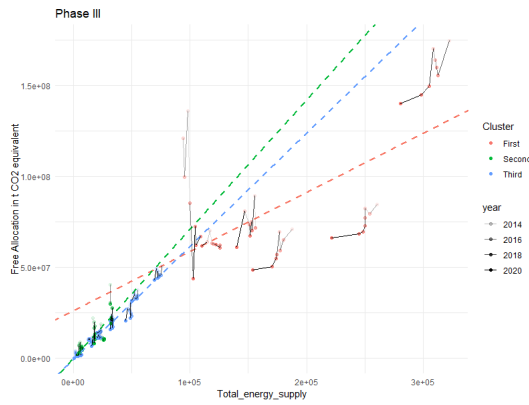


**(c)** Plot 3: Free Allocation vs Total Energy Supply for Phase III
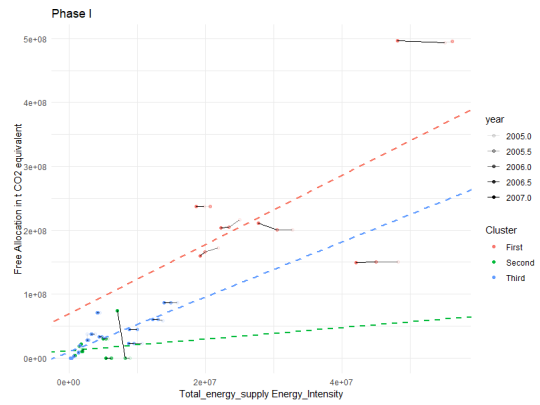


**(d)** Plot 4: Free Allocation vs Total Energy Supply times Energy Intensity for Phase I
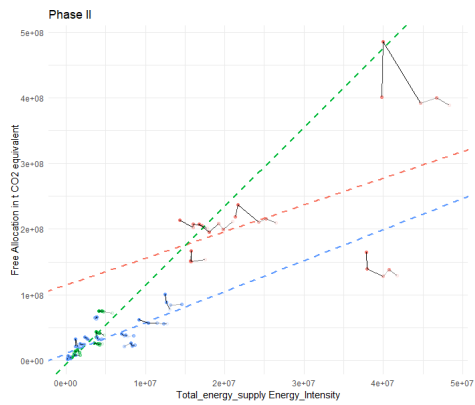


**(e)** Plot 5: Free Allocation vs Total Energy Supply times Energy Intensity for Phase II
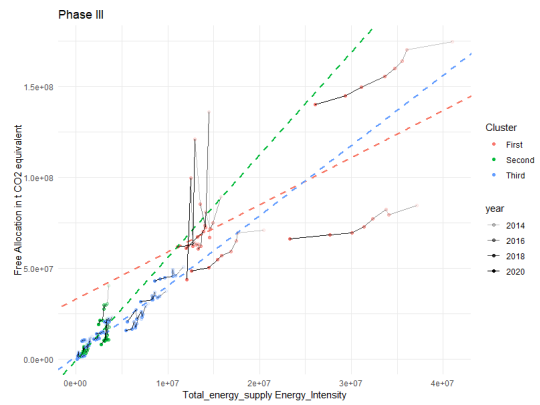


**(f)** Free Allocation vs Total Energy Supply times Energy Intensity for Phase III

**Figure** 4.5: Free Allocation vs Total Energy Supply or Total Energy Supply times Energy Intensity

# Chapter 5

# Allowance Allocation as an Optimization Problem

## 5.1 Introduction

In this chapter, we transition from analyzing the fairness and efficiency of current allocation practices to proposing an optimized allocation model for the European Union Emissions Trading System (EU ETS). Based on the findings from previous chapters, particularly the clustering and regression analyses, we aim to balance the principles of fairness and economic efficiency in the allocation of free emission allowances.

The primary contribution of the optimization model is to standardize the allocation criteria by expressing all factors on an equal basis, effectively attempting to balance social welfare across Member States. The model seeks to integrate both country-centric and sector-based approaches, recognizing that viewing the allocation of free permits solely as a country-centric problem is not entirely unjustifiable. By combining these approaches within an optimization framework, we can capture the nuances of both perspectives.

In this model, economic efficiency is encapsulated in the objective function, while fairness is represented through the constraints. Our goal is to provide a versatile tool that can analyze different allocation principles using a straightforward allocation mechanism. By adjusting the constraints and parameters, the model can simulate various fairness principles and assess their impact on the allocation outcomes.

At the end of this chapter, we will present different formulations of the problem to illustrate how alternative fairness considerations can be incorporated into the allocation mechanism.

## 5.2 Mathematical Formulation

### 5.2.1 Variables and Parameters

To formalize the optimization problem, we define the following variables and parameters:

1. **Countries** $i \in C$: The set of EU Member States participating in the EU ETS.

2. **Sectors** $j \in S$: The set of sectors subject to emission allowances.

3. **Years** $t$: The time periods under consideration.

4. **Percentage of Free Allocation** $v_{i,j,t}$: The percentage of the total free allocation assigned to country $i$, sector $j$, in year $t$. The year $t$ will be omitted when context allows, and $t-1$ will be used to refer to the previous year.

5. **Gross Domestic Product** $GDP_{i,j}$: The GDP produced by sector $j$ in country $i$.

6. **Verified Emissions** $e_{i,j}$: The verified emissions of sector $j$ in country $i$.

7. **Purchasing Power Standards Multiplier** $PPS_i$: A factor similar to the Purchasing Power Parity (PPP), used to convert euros into purchasing power in country $i$.

8. **Aggregate Free Allocation** $v_i$: The total percentage of free allocation given to country $i$.

9. **Aggregate Free Allocation** $v_j$: The total percentage of free allocation given to sector $j$.

10. **Multipliers** $\alpha_k$: Parameters used to encapsulate fairness and efficiency principles, controlling the allowable deviations in allocations.

### 5.2.2 Objective Function

The optimization model aims to maximize the overall economic efficiency of the allocation, measured by the ability of countries and sectors to transform allowances into economic value, adjusted for purchasing power. The objective function is defined as:

$$\text{maximize} \quad Z = \sum_{i \in C} \sum_{j \in S} v_{i,j} \cdot \frac{GDP_{i,j}}{e_{i,j}} \cdot PPS_i \tag{5.1}$$

This function rewards allocations to sectors and countries that can generate more GDP per unit of emissions, adjusted for purchasing power, thereby promoting economic efficiency.

### 5.2.3 Constraints

The optimization is subject to several constraints that incorporate fairness principles and practical considerations.

**Total Cap Constraint**

The total allocation must not exceed the EU's emission cap, which is normalized to 1 in terms of percentages.

$$\sum_{i \in C} \sum_{j \in S} v_{i,j} = 1 \tag{5.1}$$

## Country and Sector Allocation Constraints

The total allocation for each country is the sum of allocations across all sectors, and similarly for each sector:

$$v_i = \sum_{j \in S} v_{i,j} \quad \forall i \in C \tag{5.2}$$

$$v_j = \sum_{i \in C} v_{i,j} \quad \forall j \in S \tag{5.3}$$

## Historical Deviation Bounds

To maintain stability and prevent abrupt changes in allocations, we impose bounds on the allowable deviation from the previous year's allocations.

For countries:

$$\alpha_1 \cdot v_{i,t-1} \leq v_{i,t} \leq \alpha_2 \cdot v_{i,t-1} \quad \forall i \in C \tag{5.4}$$

For sectors:

$$\alpha_3 \cdot v_{j,t-1} \leq v_{j,t} \leq \alpha_4 \cdot v_{j,t-1} \quad \forall j \in S \tag{5.5}$$

## Population-Based Fairness

To incorporate fairness based on population, we constrain the country allocations to be proportional to their share of the total EU population:

$$v_i \approx \frac{\text{Population}_i}{\sum_{i \in C} \text{Population}_i} \quad \forall i \in C \tag{5.6}$$

This can be formulated as an equality or an inequality with acceptable deviation bounds.

## Economic Activity Proportionality

To ensure that sectoral allocations within each country reflect the sector's contribution to the country's economy, we include:

$$v_{i,j} \approx \frac{GDP_{i,j}}{GDP_i} \cdot v_i \quad \forall i \in C, \forall j \in S \tag{5.7}$$

Again, this can be formulated with acceptable deviations.

**Definition of Multipliers**

The multipliers $\alpha_k$ are parameters that control the allowable deviations and can be adjusted to simulate different fairness principles.

Example definitions:

$$\alpha_1 = \min\left(0.8, \frac{\overline{GDP}}{GDP_i}\right) \tag{5.8}$$

$$\alpha_2 = \max\left(1.2, \frac{\overline{GDP}}{GDP_i}\right) \tag{5.9}$$

Where $\overline{GDP}$ is the average GDP across all countries. These definitions allow countries with lower GDP to have smaller allowable decreases and larger allowable increases in allocations.

### 5.2.4 Explanation of the Constraints

The constraints serve to balance fairness and efficiency:

- **Total Cap Constraint** ensures that the total allocation does not exceed the cap set by the EU ETS.

- **Country and Sector Allocation Constraints** maintain consistency in how allocations are aggregated across countries and sectors.

- **Historical Deviation Bounds** prevent sudden changes in allocations that could disrupt economies or industries, allowing for gradual transitions.

- **Population-Based Fairness** aligns allocations with the principle of equal per capita entitlements, supporting vertical equity.

- **Economic Activity Proportionality** ensures that sectors contributing more to the economy receive allocations commensurate with their economic significance.

- **Multipliers** $\alpha_k$ allow for flexibility in the model to incorporate different fairness principles, such as ability to pay or historical responsibility.

## 5.3 Solution and Methodology

### 5.3.1 Algorithm Selection

The optimization model is a linear programming (LP) problem, as both the objective function and the constraints are linear in the decision variables $v_{i,j}$. Linear programming is suitable for efficiently solving such problems, even with a large number of variables and constraints.

In cases where non-linear constraints or integer variables are introduced, the problem may become a Mixed Integer Programming (MIP) or a convex optimization problem, requiring appropriate solution methods.

### 5.3.2 Data Inputs

The data required for the model include:

- **GDP Data** ($GDP_{i,j}$): Sourced from national statistics and Eurostat, representing the economic output of each sector in each country.

- **Verified Emissions** ($e_{i,j}$): Obtained from the European Environment Agency (EEA), reflecting the actual emissions reported by sectors.

- **Population Data**: From the World Bank or Eurostat, used in the population-based fairness constraint.

- **Purchasing Power Standards** ($PPS_i$): Provided by Eurostat, used to adjust GDP for purchasing power differences between countries.

- **Historical Allocations** ($v_{i,t-1}$, $v_{j,t-1}$): Past allocation data required for the historical deviation constraints.

These data inputs are consistent with those used in previous analyses, ensuring continuity and comparability.

### 5.3.3 Data Limitations and Model Simplification

In our effort to implement the optimization model with detailed sectoral data, we encountered significant challenges due to inconsistencies between the coding systems used by different data sources. The EU ETS database utilizes specific activity codes for sectors, whereas Eurostat and other statistical agencies use the NACE (Nomenclature statistique des activités économiques dans la Communauté européenne) codes. Although these two classification schemes overlap, aligning them precisely proved difficult.

**NACE Definition**   The Statistical Classification of Economic Activities in the European Community, commonly referred to as **NACE** (for the French term *nomenclature statistique des activités économiques dans la Communauté européenne*), is the industry standard classification system used in the European Union. The current version is revision 2 and was established by Regulation (EC) No 1893/2006. It is the European implementation of the UN classification ISIC, revision 4.

**Sector Classification Mapping**   Despite efforts to reconcile the sector classifications, we were only able to compile five broad supersectors by grouping codes from both the EU ETS and NACE systems. The following table illustrates the mapping between the ETS activity codes, their descriptions, and the corresponding NACE codes and definitions:

**Table 5.1:** Mapping between EU ETS Activity Codes and NACE Codes

| ETS Code | EU ETS Activity Type | NACE Code | NACE Definition | Supersector |
|---|---|---|---|---|
| 22 | Production of coke | C19.10 | Manufacture of coke and refined petroleum products | C19 |
| 3 | Coke ovens | C19.10 | Manufacture of coke and refined petroleum products | C19 |
| 2 | Mineral oil refineries | C19.20 | Manufacture of refined petroleum products | C19 |
| 21 | Refining of mineral oil | C19.10 | Manufacture of coke and refined petroleum products | C19 |
| *— Manufacture of Coke and Refined Petroleum Products —* | | | | |
| 23 | Metal ore roasting or sintering | C24.41 | Precious metals production | C24 |
| 24 | Production of pig iron or steel | C24.10 | Manufacture of basic iron and steel and of ferro-alloys | C24 |
| 25 | Production or processing of ferrous metals | C24.10 | Manufacture of basic iron and steel and of ferro-alloys | C24 |
| 26 | Production of primary aluminium | C24.42 | Aluminium production | C24 |
| 27 | Production of secondary aluminium | C24.42 | Aluminium production | C24 |
| 28 | Production or processing of non-ferrous metals | C24.4 | Manufacture of basic precious and other non-ferrous metals | C24 |
| *— Production of Basic Metals —* | | | | |
| 29 | Production of cement clinker | C23.51 | Manufacture of cement | C23 |
| 30 | Production of lime or calcination of dolomite | C23.52 | Manufacture of lime and plaster | C23 |
| 31 | Manufacture of glass | C23.1 | Manufacture of glass and glass products | C23 |
| 32 | Manufacture of ceramics | C23.3 C23.4 | Manufacture of clay building materials Manufacture of other porcelain and ceramic products | C23 |

| ETS Code | EU ETS Activity Type | NACE Code | NACE Definition | Supersector |
|---|---|---|---|---|
| 33 | Manufacture of mineral wool | C23.99 | Manufacture of other non-metallic mineral products n.e.c. | C23 |
| 34 | Production or processing of gypsum or plaster-board | C23.52 | Manufacture of lime and plaster | C23 |
| *— Manufacture of Other Non-Metallic Mineral Products —* | | | | |
| 35 | Production of pulp | C17.11 | Manufacture of pulp | C17 |
| 36 | Production of paper or cardboard | C17.12 | Manufacture of paper and paperboard | C17 |
| *— Manufacture of Paper and Paper Products —* | | | | |
| 37 | Production of carbon black | C20.14 | Manufacture of other organic basic chemicals | C20 |
| 38 | Production of nitric acid | C20.15 | Manufacture of fertilizers and nitrogen compounds | C20 |
| *— Manufacture of Chemicals and Chemical Products —* | | | | |

**Limitations**   While this mapping provides a general correspondence between the ETS activity types and NACE codes, it is not precise enough for detailed sectoral analysis required in our optimization model. The aggregation into broad supersectors limits the granularity of the data, making it unsuitable for accurately capturing the sector-specific dynamics within each country.

Due to these data limitations, we concluded that the available sectoral data are not sufficient for implementing the optimization model at the desired level of detail.

### Model Simplification

To proceed with our analysis despite the lack of detailed sectoral data, we simplify the model by focusing solely on country-level information, removing the sector dimension. This adjustment allows us to continue exploring the optimization framework using the available data, while acknowledging the limitations imposed by the data constraints.

### 5.3.4   Reformulated Optimization Model

By eliminating the sectoral index $j$, the optimization model is reformulated as follows:

**Variables and Parameters**

- **Countries** $i \in C$: The set of EU Member States.

- **Years** $t$: The time periods under consideration.

- **Percentage of Free Allocation** $v_{i,t}$: The percentage of the total free allocation assigned to country $i$ in year $t$.

- **Gross Domestic Product** $GDP_i$: The total GDP of country $i$.

- **Verified Emissions** $e_i$: The total verified emissions of country $i$.

- **Purchasing Power Standards Multiplier** $PPS_i$: The PPS adjustment factor for country $i$.

- **Multipliers** $\alpha_k$: Parameters controlling deviation tolerances.

**Objective Function**

$$\text{maximize} \quad Z = \sum_{i \in C} v_i \cdot \frac{GDP_i}{e_i} \cdot PPS_i \tag{5.1}$$

**Constraints**

1. **Total Cap Constraint:**

$$\sum_{i \in C} v_i = 1 \tag{5.2}$$

2. **Historical Deviation Bounds:**

$$\alpha_1 \cdot v_{i,t-1} \leq v_{i,t} \leq \alpha_2 \cdot v_{i,t-1} \quad \forall i \in C \tag{5.3}$$

3. **Population-Based Fairness:**

$$v_i \approx \frac{\text{Population}_i}{\sum_{i \in C} \text{Population}_i} \quad \forall i \in C \tag{5.4}$$

4. **Definition of Multipliers:**

$$\alpha_1 = \min\left(0.8, \frac{\overline{GDP}}{GDP_i}\right) \tag{5.5}$$

$$\alpha_2 = \max\left(1.2, \frac{\overline{GDP}}{GDP_i}\right) \tag{5.6}$$

This simplified model retains the essential structure of the optimization problem while operating at the country level. It allows us to analyze the allocation of free allowances among countries based on their economic efficiency and fairness considerations, despite the limitations in sectoral data.

## 5.4 Example Runs

To illustrate the application of the model, we present example runs under different scenarios.

### 5.4.1 Scenario 1: Base Case

In the base case, we set the multipliers $\alpha_k$ to allow for moderate deviations:

$$\alpha_1 = 0.8$$
$$\alpha_2 = 1.2$$
$$\alpha_3 = 0.8$$
$$\alpha_4 = 1.2$$

We solve the LP problem using the data inputs and observe the allocation results.

### 5.4.2 Scenario 2: Increased Flexibility

In this scenario, we allow for greater deviations to explore how allocations change:

$$\alpha_1 = 0.5$$
$$\alpha_2 = 2$$
$$\alpha_3 = 0.5$$
$$\alpha_4 = 2$$

This permits allocations to decrease or increase by up to 50% from the previous year.

### 5.4.3 Scenario 3: GDP-Adjusted Deviations

We adjust the multipliers based on GDP per capita in PPS to reflect the economic capacity of countries:

$$\alpha_1 = \min\left(0.8, \frac{\overline{GDP^{PPS}}}{GDP_i^{PPS}}\right)$$
$$\alpha_2 = \max\left(1.2, \frac{\overline{GDP^{PPS}}}{GDP_i^{PPS}}\right)$$

## 5.5 Results and Discussion

### 5.5.1 Analysis of Allocation Changes

We present the allocation results from each scenario, focusing on:

1. **Percentage Changes in Free Allowance Allocations**: How allocations to each country and sector change compared to historical allocations.

2. **Ranking of Countries and Sectors**: How the rankings in terms of allocations shift under different scenarios.

3. **Cluster-Based Analysis**: Examining changes within the clusters established in previous chapters to assess the impact on groups of similar countries.

### 5.5.2 Comparison with Historical Data

We compare the model's allocation results with historical allocations to understand the differences and implications. The key observations include:

- **Demonstrating Different Allocations**: The purpose of the model is to showcase how different fairness principles and constraints can lead to alternative allocation outcomes, rather than to prescribe a specific "better" allocation.

- **Flexibility of the Model**: The model shows versatility in accommodating various fairness considerations by adjusting parameters.

- **Impact on Social Welfare**: By standardizing efficiency across sectors and countries, the model attempts to balance social welfare, ensuring that allocations promote economic value generation.

- **Cluster Insights**: Analyzing allocations within clusters helps understand how similar countries are affected, providing deeper insights into the fairness of the allocation.

### 5.5.3 Example Findings

For instance, in Scenario 2, countries like Hungary might see an increase in allocation due to the relaxed deviation constraints, reflecting their economic capacity as adjusted by PPS. Conversely, countries like Germany might experience a decrease, highlighting how the model reallocates allowances based on efficiency and fairness criteria.

**Percentage Changes in Allocations**

We observe that under increased flexibility, some countries experience significant changes in their allocations:

- **Hungary**: Allocation increases by up to 51% in Scenario 2 compared to the base case.

- **Germany**: Allocation decreases by up to 12% in Scenario 2.

**Ranking Changes**

The ranking of countries by allocation amount shifts under different scenarios, indicating how the model prioritizes efficiency and fairness:

- Countries with higher efficiency (GDP per unit of emissions) and lower PPS-adjusted GDP may move up in ranking.

- Countries with lower efficiency or higher GDP may move down.

**Cluster-Based Analysis**

Within the clusters:

- **Cluster 2 Countries**: Generally see increases in allocations under scenarios that adjust for economic capacity, aligning with fairness principles favoring less affluent countries.

- **Cluster 1 Countries**: May experience reductions, reflecting a shift towards efficiency and equity.

### 5.5.4 Interpretation of Results

These results demonstrate the model's ability to reflect different policy priorities:

- **Efficiency vs. Fairness Trade-off**: Adjusting constraints affects the balance between rewarding efficient sectors and supporting less affluent countries.

- **Policy Implications**: Policymakers can use the model to understand the impact of different allocation rules and to design policies that align with their objectives.

- **Not Prescriptive but Illustrative**: The model is a tool for exploration rather than prescribing a specific allocation, highlighting the potential outcomes of various fairness considerations.

## 5.6 Conclusion

In this chapter, we have developed an optimization model that integrates both efficiency and fairness principles into the allocation of emission allowances under the EU ETS. By formulating the allocation as a linear programming problem, we can systematically explore how different constraints and parameters influence the distribution of allowances.

By balancing social welfare through standardized efficiency metrics and incorporating fairness constraints, the model offers a comprehensive approach to designing allocation strategies that align with the EU's environmental and economic objectives.

# Chapter 6

# Simulations / Comparison with another model

## 6.1 Introduction to the Uniform Linear Mechanism Model

This chapter addresses a critical issue with the optimization model from Chapter 4: the lack of a comparative baseline. To resolve this, we incorporate the Uniform Linear Mechanism (ULM) for permit allocation, as presented in the paper "Allocating Emission Permits Efficiently via Uniform Linear Mechanisms" by [8] Lin and Lu (2023). This model offers a structured approach to emission permit allocation that maximizes efficiency within the EU ETS framework, thus providing a point of comparison.

## 6.2 Definition and Structure of the Uniform Linear Mechanism

copy paste τον ορισμό του προβλήματος

## 6.3 Implementation of the Uniform Linear Mechanism Model with Modified Best Responce

Εδώ θα μπουν πολλά... Ακόμα και αυτό :P

## 6.4 Implementation of the Uniform Linear Mechanism Model with Optimization

Εδώ όπως πρέπει τα πράγματα

## 6.5 Example Runs

Διαγράμματα έχουμε σορρό για εδώ.
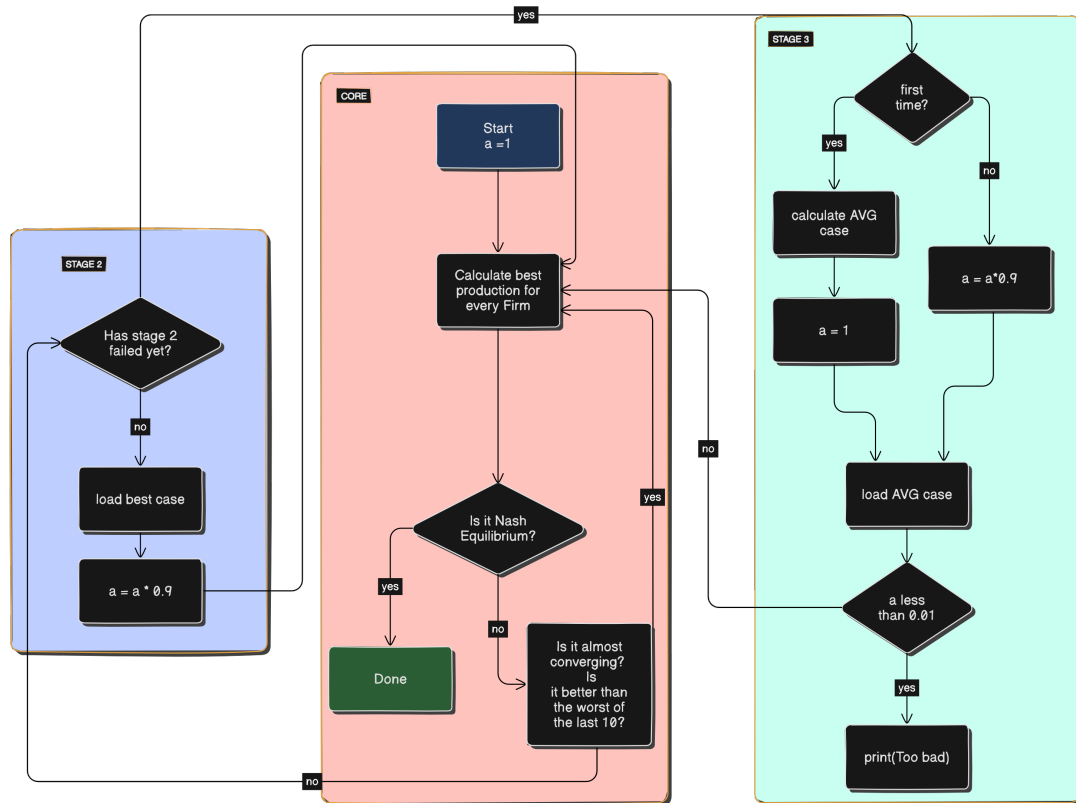
**Figure 6.1**: Bad Algorithm

## 6.6 Generated data for both models

Θέλουμε συνεθτικά δεδομένα τα οποία πλέον να έχουν και τις χώρες μέσα στην φάση. Ουσιαστικά να είανι όλα μαζί.

Εδώ αρχίζουν τα σκούρα

## 6.7 Comparative Analysis of Optimization and ULM Model

Εδώ το σημαντικό θα είναι πως και για τα δύο θα μπορεί να υπολογιστεί το social Welfare = Consumer Surplus - Damage (βιβλιογραφία να βρεις για αυτό) όπου το Damage θα είναι κοινό και για τους δύο. Επομένως, είναι εφικτό να κάνουμε συγκρίσεις για χωρίς να γνωρίζουμε πραγματικά για τις επιπτώσεις στην κοινωνία.

# Chapter 7

# Conclusions and Policy Implications (πολύ φιλόδοξο :P)

# Chapter 8

# Future Work

# Chapter 9

# Random Ideas for chapters

## 9.1 Literature Review

πριν το chapter 1

## 9.2 Methodology

Ίσως να μπουν όλες οι τεχνικές και όλα τα μαθηματικά εργαλεία σε ένα σημείο για να είναι όλα τους καλά οργανωμένα και να μην γίνονται αναφορές σε αυτά σε τυχαία σημεία της διπλωματικής. Ίσως πριν την παράγραφο 3, αμέσως μετά την ουσιαστική εισαγωγή.

## 9.3 Theoretical Foundations

Ίσως κάποια εισαγωγικά για κάποιον που δεν είναι σχετικός με τα μαθηματικα εργαλεία; Τρολλιές λέω τώρα, το ξέρω.

## 9.4 Sensitivity Analysis and Robustness of the Models

Μου αρέσει να έχω όνειρα στη ζωή μου. Κάποια τα βλέπω από μικρό παιδί και συνεχίζω να τα βλέπω και να διανθίζονται...

## 9.5 Stakeholder Analysis and Social Acceptance

Εδώ θα μπορούσε να μπει το κομμάτι του Mulin αλλά από άλλες σκοπιές. Ήδη οι χώρες δεν είναι οι stakeholders πρεος τους οποίους το σύστημα προσπαθεί να είναι δίκαιο, οπότε γιατί όχι και άλλους.

## 9.6 Θεωρητική αναφορά σε κυρτή βελτιστοποίηση

# Table of Symbols

**Table 9.1**: Table of Symbols

| Symbol | Description | Units |
|--------|-------------|-------|
| $q_i$ | Quantity produced by firm $i$ | units |
| $x_i$ | Emissions by firm $i$ | kg |
| $\tau$ | Permit price | \$/kg |
| $C_A$ | Abatement cost function | \$ |

**Table 9.2**: Table of Abbreviations

| Abbreviation | Full Meaning |
|--------------|--------------|
| PPS | Purchasing Power Standard |
| CAT | Cap and Trade system |
| EU ETS | European Union Emissions Trading System |
| GDP | Gross Domestic Product |
| $CO_2$ | Carbon Dioxide |
| GHG | GreenHouse Gases |
| UN | United Nations |
| EU | European Union |
| UNFCCC | United Nations Framework Con- vention on Climate Change |
| HFCs | hydrofluorocarbons |
| CORSIA | Carbon Off- setting and Reduction Scheme for International Aviation |
| ICAO | International Civil Aviation Organization |
| NACE | Statistical Classification of Economic Activities in the European Community |

**Chapter 10**

# Appendix

## 10.1 Data selection

**Energy Intensity** measures the amount of energy used per unit of GDP, indicating a country's efficiency in energy use relative to economic output. Lower energy intensity reflects greater energy efficiency, suggesting a reduced need for free allowances. This attribute helps ensure that allowance distribution aligns with the goal of incentivizing efficient energy usage and reducing overall emissions across the EU.

- Principle: Economic Efficiency

- File: nrg_ind_ei_linear.csv

- Source: `https://ec.europa.eu/eurostat/databrowser/view/NRG_IND_EI__custom_5726612/default/table?lang=en`

- Field in question on nrg_bal is "EI_GDP_PPS"

- Country: All countries

- Year: 1996 - 2021

- Unit: KGOE_TEUR_PPS

**Verified Emissions** directly quantify a country's annual emissions and represent its environmental impact. Including verified emissions allows for an accurate reflection of each country's contribution to total emissions, thus supporting a fair allocation of allowances. By aligning the allowances with verified emissions, the EU ETS ensures that countries receive allocations proportional to their emissions levels, thereby supporting a fair distribution that respects actual emissions data.

- Principle: Fairness

- File: Historical emissions_data.csv

- Source: `https://www.eea.europa.eu/data-and-maps/dashboards/emissions-trading-viewer-1`

- Country: All countries

- Year: 1990 - 2021

- Unit: K tons of Co2 equivalent

| | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 27.36 | 29.61 | 30.51 | 30.87 | 32.08 | 1.27 |
| Belgium | 45.03 | 45.17 | 45.99 | 46.29 | 55.46 | 3.16 |
| Bulgaria | 31.28 | 33.24 | 34.57 | 35.95 | 40.00 | 2.63 |
| Cyprus | 4.19 | 4.58 | 4.61 | 4.92 | 5.58 | 0.41 |
| Denmark | 15.50 | 17.05 | 19.46 | 23.71 | 26.55 | 4.05 |
| Estonia | 10.38 | 13.50 | 13.89 | 14.76 | 16.00 | 1.55 |
| Finland | 26.18 | 27.81 | 30.68 | 34.72 | 41.30 | 4.74 |
| France | 101.40 | 104.86 | 110.90 | 114.46 | 124.13 | 7.10 |
| Germany | 428.29 | 448.66 | 462.35 | 469.31 | 489.86 | 18.24 |
| Greece | 47.34 | 50.74 | 58.84 | 61.09 | 69.85 | 7.10 |
| Hungary | 20.08 | 21.23 | 22.40 | 22.61 | 27.24 | 1.91 |
| Ireland | 15.77 | 18.88 | 23.63 | 27.08 | 28.53 | 4.72 |
| Italy | 148.37 | 157.09 | 166.78 | 187.42 | 220.68 | 21.98 |
| Latvia | 2.43 | 2.59 | 2.74 | 2.96 | 3.24 | 0.26 |
| Lithuania | 5.61 | 5.92 | 6.23 | 6.65 | 7.56 | 0.59 |
| Luxembourg | 1.73 | 1.83 | 2.06 | 2.17 | 3.62 | 0.52 |
| Malta | 0.84 | 1.09 | 1.89 | 1.92 | 2.28 | 0.51 |
| Netherlands | 79.97 | 82.27 | 89.14 | 92.79 | 96.47 | 6.31 |
| Poland | 191.17 | 198.28 | 199.73 | 203.07 | 206.35 | 4.12 |
| Portugal | 24.17 | 25.64 | 26.99 | 28.75 | 31.42 | 2.23 |
| Romania | 40.53 | 42.21 | 43.07 | 48.72 | 63.82 | 6.83 |
| Slovenia | 6.18 | 6.60 | 7.45 | 8.03 | 8.86 | 0.91 |
| Spain | 121.48 | 128.26 | 132.69 | 140.52 | 163.46 | 11.31 |
| Sweden | 17.49 | 21.05 | 22.51 | 22.63 | 22.86 | 1.71 |
| United Kingdom | 141.76 | 172.90 | 220.88 | 236.57 | 265.06 | 42.22 |

Table 10.1: Verified emissions in G tons of $CO_2$ equivalent

**Historical Emissions**

- File: Historical emissions_data.csv

- Source: https://www.eea.europa.eu/data-and-maps/dashboards/emissions-trading-viewe

- Country: All countries

- Year: 1990 - 2021

- Unit: K tons of Co2 equivalent

**GPD per capita** reflects a country's economic wealth and ability to fund emissions reductions independently. Including this metric in the analysis acknowledges that wealthier countries have more financial capacity to invest in green technologies, potentially reducing their need for free allowances. Incorporating GDP per capita aligns with a fairness-based approach, as it considers vertical equity—ensuring that countries with lower economic resources are not disproportionately burdened in the transition to greener economies.

- Principle: Fairness

- File: GDP_per_capita_1960_2021.csv

- Source: `https://data.worldbank.org/indicator/NY.GDP.PCAP.CD`

- Data: GDP per capita (current US$)

- Country: All countries

- Year: 1960 - 2021

- Unit: US$

**Inflation** affects purchasing power and the overall cost of living, influencing a country's economic stability and its ability to absorb additional costs associated with emissions trading. High inflation rates may signal economic vulnerabilities, making it harder for countries to manage fluctuations in emissions trading markets. By including inflation as an attribute, the analysis respects the fairness principle by accounting for economic conditions that might otherwise disadvantage certain countries.

- Principle: Fairness

- File: Inflation_1960_2021.csv

- Source: `https://data.worldbank.org/indicator/FP.CPI.TOTL.ZG`

- Data: Inflation, consumer prices (annual

- Country: All countries

- Year: 1960 - 2021

- Unit:

|  | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 44.20 | 47.17 | 48.56 | 51.46 | 51.92 | 2.75 |
| Belgium | 41.01 | 44.19 | 44.76 | 47.48 | 48.30 | 2.43 |
| Bulgaria | 6.85 | 7.17 | 7.57 | 7.88 | 9.45 | 0.74 |
| Cyprus | 23.41 | 26.89 | 28.91 | 31.57 | 35.40 | 3.57 |
| Denmark | 53.25 | 57.83 | 58.51 | 61.67 | 64.32 | 3.39 |
| Estonia | 14.66 | 17.40 | 18.20 | 19.66 | 23.06 | 2.45 |
| Finland | 42.80 | 46.46 | 47.71 | 50.16 | 53.77 | 3.25 |
| France | 36.65 | 39.73 | 41.59 | 42.84 | 45.52 | 2.75 |
| Germany | 41.10 | 41.89 | 44.65 | 46.50 | 48.02 | 2.61 |
| Greece | 17.92 | 19.17 | 21.79 | 26.10 | 32.13 | 4.84 |
| Hungary | 12.72 | 13.09 | 13.72 | 14.46 | 16.43 | 1.21 |
| Ireland | 48.66 | 51.83 | 55.60 | 62.44 | 79.11 | 9.57 |
| Italy | 30.24 | 33.51 | 35.56 | 36.63 | 40.94 | 3.17 |
| Latvia | 11.42 | 13.56 | 14.33 | 15.72 | 17.87 | 1.87 |
| Lithuania | 11.82 | 14.32 | 14.94 | 16.14 | 19.19 | 2.11 |
| Luxembourg | 105.46 | 109.81 | 112.58 | 119.51 | 123.68 | 6.14 |
| Malta | 21.08 | 22.37 | 24.77 | 26.19 | 31.57 | 3.23 |
| Netherlands | 45.19 | 49.37 | 52.20 | 52.97 | 57.88 | 3.66 |
| Poland | 11.53 | 12.60 | 13.70 | 13.94 | 15.47 | 1.08 |
| Portugal | 19.25 | 21.03 | 22.10 | 23.18 | 24.95 | 1.68 |
| Romania | 8.21 | 8.76 | 9.55 | 10.24 | 12.40 | 1.23 |
| Slovenia | 20.89 | 23.07 | 23.53 | 24.96 | 27.60 | 1.92 |
| Spain | 25.74 | 28.25 | 29.50 | 31.11 | 35.51 | 2.74 |
| Sweden | 46.95 | 52.42 | 54.59 | 59.03 | 61.13 | 4.45 |
| United Kingdom | 38.95 | 41.18 | 42.69 | 44.56 | 47.79 | 2.92 |

Table 10.2: GDP per capita in thousands USD

**Population** is a fundamental indicator of a country's size and resource needs. Larger populations imply greater demand for energy and, subsequently, higher emissions, suggesting that allocation should consider the number of inhabitants to ensure an equitable distribution of allowances. Population-based allocation also aligns with fairness principles, as it supports the idea that countries with more people should have proportionate access to resources under a shared system.

- Principle: Fairness

- File: API_SP.POP.TOTL_DS2_en_csv_v2_4701113.csv

- Source: https://data.worldbank.org/indicator/SP.POP.TOTL

- Country: All countries

- Year: 1960 - 2021

| Inflation | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 0.87 | 1.71 | 1.85 | 2.01 | 2.30 | 0.45 |
| Belgium | 0.53 | 1.30 | 1.81 | 1.90 | 1.96 | 0.47 |
| Bulgaria | 0.07 | 1.23 | 3.32 | 4.52 | 8.10 | 2.45 |
| Cyprus | -1.33 | -0.66 | 1.00 | 1.65 | 4.73 | 1.74 |
| Denmark | 0.25 | 0.58 | 0.89 | 1.78 | 4.13 | 1.27 |
| Estonia | -0.39 | 2.00 | 3.59 | 4.05 | 6.80 | 2.02 |
| Finland | 0.09 | 1.22 | 1.77 | 2.59 | 3.04 | 1.02 |
| France | 0.07 | 0.55 | 0.95 | 1.10 | 2.37 | 0.58 |
| Germany | 0.65 | 1.20 | 1.50 | 1.87 | 1.97 | 0.46 |
| Greece | -2.05 | -0.44 | -0.18 | 0.62 | 4.34 | 1.85 |
| Hungary | 1.32 | 2.66 | 2.89 | 4.11 | 4.85 | 1.15 |
| Ireland | -4.62 | -0.28 | 0.71 | 1.22 | 7.70 | 3.10 |
| Italy | 0.44 | 0.92 | 1.13 | 1.58 | 2.40 | 0.54 |
| Latvia | -9.67 | 0.49 | 1.92 | 3.77 | 11.65 | 5.17 |
| Lithuania | -3.30 | 1.06 | 2.53 | 3.88 | 9.71 | 3.30 |
| Luxembourg | -1.11 | 1.94 | 2.28 | 3.36 | 6.61 | 1.99 |
| Malta | 1.12 | 2.06 | 2.22 | 2.75 | 4.22 | 0.82 |
| Netherlands | 0.19 | 0.35 | 0.94 | 1.36 | 2.44 | 0.79 |
| Poland | 0.30 | 0.75 | 1.65 | 2.82 | 3.89 | 1.34 |
| Portugal | -0.39 | 0.67 | 1.51 | 1.78 | 2.25 | 0.90 |
| Romania | 1.80 | 3.33 | 3.77 | 4.38 | 16.02 | 3.88 |
| Slovenia | -1.03 | 0.68 | 1.04 | 1.86 | 4.47 | 1.49 |
| Spain | -0.22 | 0.06 | 0.32 | 0.90 | 2.25 | 0.76 |
| Sweden | 0.93 | 1.04 | 1.74 | 2.25 | 3.24 | 0.75 |
| United Kingdom | 0.51 | 1.60 | 1.82 | 2.03 | 3.23 | 0.65 |

Table 10.3: Inflation between 2008-2018

- Unit: Persons

**Total Energy Supply** represents a country's energy consumption needs, which correlates with its emissions output. Countries with higher energy supply requirements typically have higher emissions, necessitating a proportional allocation to meet their demand. This attribute respects the fairness principle, as it aligns the allowances with the actual energy demand of each country, thereby supporting a distribution that reflects each country's energy usage and emissions potential.

- Principle: Fairness

- File: nrg_bal_s__custom_4143365_linear.csv

- Source: Eurostat

| Population | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 8.32 | 8.38 | 8.48 | 8.69 | 8.84 | 0.19 |
| Belgium | 10.71 | 10.97 | 11.16 | 11.30 | 11.43 | 0.24 |
| Bulgaria | 7.03 | 7.15 | 7.27 | 7.37 | 7.49 | 0.15 |
| Cyprus | 1.08 | 1.12 | 1.14 | 1.17 | 1.19 | 0.03 |
| Denmark | 5.49 | 5.56 | 5.61 | 5.71 | 5.79 | 0.10 |
| Estonia | 1.31 | 1.32 | 1.32 | 1.33 | 1.34 | 0.01 |
| Finland | 5.31 | 5.38 | 5.44 | 5.49 | 5.52 | 0.07 |
| France | 64.37 | 65.19 | 66.00 | 66.64 | 67.10 | 0.93 |
| Germany | 80.27 | 80.81 | 81.78 | 82.23 | 82.91 | 0.91 |
| Greece | 10.73 | 10.80 | 10.97 | 11.09 | 11.12 | 0.15 |
| Hungary | 9.78 | 9.83 | 9.89 | 9.99 | 10.04 | 0.09 |
| Ireland | 4.49 | 4.57 | 4.62 | 4.73 | 4.87 | 0.12 |
| Italy | 58.83 | 59.33 | 60.23 | 60.58 | 60.79 | 0.73 |
| Latvia | 1.93 | 1.97 | 2.01 | 2.08 | 2.18 | 0.08 |
| Lithuania | 2.80 | 2.89 | 2.96 | 3.06 | 3.20 | 0.13 |
| Luxembourg | 0.49 | 0.51 | 0.54 | 0.58 | 0.61 | 0.04 |
| Malta | 0.41 | 0.42 | 0.43 | 0.45 | 0.48 | 0.03 |
| Netherlands | 16.45 | 16.65 | 16.80 | 16.99 | 17.23 | 0.25 |
| Poland | 37.97 | 37.98 | 38.04 | 38.06 | 38.15 | 0.06 |
| Portugal | 10.28 | 10.34 | 10.46 | 10.56 | 10.57 | 0.12 |
| Romania | 19.47 | 19.76 | 19.98 | 20.20 | 20.54 | 0.33 |
| Slovenia | 2.02 | 2.05 | 2.06 | 2.06 | 2.07 | 0.01 |
| Spain | 45.95 | 46.46 | 46.58 | 46.68 | 46.80 | 0.24 |
| Sweden | 9.22 | 9.41 | 9.60 | 9.86 | 10.18 | 0.31 |
| United Kingdom | 61.81 | 63.01 | 64.13 | 65.36 | 66.46 | 1.55 |

**Table 10.4**: Population in millions 2008-2018

- Data tree : All data -> Environment and energy -> Energy -> Energy statistics -> quantities Energy statistics -> quantities, annual data -> Energy balances

- Data name on Eurostat: Simplified energy balances

- Data: Energy balance

- Country: All countries

- Year: 1990 - 2020

- Unit: Thousand tonnes of oil equivalent

- nrg_bal codes:

- Primary production -> PPRD

- Imports -> IMP

- Exports -> EXP

- Gross Available Energy -> GAE

- Total energy supply -> NRGSUP

- Available for final consumption -> AFC

|  | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 32011.29 | 33031.17 | 33177.75 | 33562.30 | 34166.28 | 660.54 |
| Belgium | 52238.38 | 53015.79 | 55039.87 | 55272.03 | 59313.06 | 2255.37 |
| Bulgaria | 16923.38 | 17726.43 | 18234.79 | 18722.35 | 19823.90 | 813.92 |
| Cyprus | 1955.96 | 2121.56 | 2262.44 | 2440.09 | 2616.93 | 221.87 |
| Denmark | 16374.16 | 16838.22 | 17383.65 | 18304.45 | 19558.31 | 1128.72 |
| Estonia | 4399.62 | 5378.58 | 5648.48 | 5846.32 | 5978.41 | 496.84 |
| Finland | 32022.99 | 33165.71 | 33582.86 | 34469.06 | 36251.74 | 1195.84 |
| France | 248383.41 | 250072.60 | 256292.91 | 259845.13 | 266394.54 | 6206.33 |
| Germany | 305036.83 | 310746.75 | 313107.91 | 318940.66 | 335474.27 | 9403.81 |
| Greece | 22748.62 | 23240.71 | 23407.97 | 27231.17 | 30404.91 | 2854.85 |
| Hungary | 23652.51 | 24816.51 | 25609.63 | 26395.50 | 26900.70 | 1096.99 |
| Ireland | 12776.63 | 13293.33 | 13625.33 | 14225.86 | 15022.14 | 727.58 |
| Italy | 146769.88 | 152859.01 | 156093.49 | 168758.58 | 181736.20 | 10969.89 |
| Latvia | 4259.46 | 4307.46 | 4407.65 | 4465.42 | 4640.00 | 129.86 |
| Lithuania | 6946.51 | 7067.95 | 7290.53 | 7647.47 | 9553.50 | 819.46 |
| Luxembourg | 3682.05 | 3785.50 | 3948.40 | 4127.44 | 4212.94 | 195.48 |
| Malta | 594.33 | 687.68 | 780.25 | 834.21 | 881.48 | 97.20 |
| Netherlands | 71379.09 | 73882.75 | 75619.51 | 77123.41 | 82743.78 | 3132.34 |
| Poland | 93773.11 | 96236.75 | 97971.41 | 101131.11 | 108970.23 | 4555.35 |
| Portugal | 21439.29 | 22060.46 | 22651.14 | 23433.93 | 24716.20 | 1092.37 |
| Romania | 31378.66 | 31668.07 | 33454.78 | 34845.41 | 39485.27 | 2432.37 |
| Slovenia | 6473.51 | 6722.90 | 6875.85 | 7127.16 | 7982.69 | 419.35 |
| Spain | 114522.76 | 119335.11 | 125486.61 | 126434.02 | 138166.04 | 6411.76 |
| Sweden | 44092.81 | 48432.69 | 49103.98 | 49874.22 | 50118.89 | 1857.82 |
| United Kingdom | 174024.39 | 177000.66 | 186386.17 | 191789.70 | 208268.88 | 11384.30 |

Table 10.5: Total energy supply between 2008-2018

**Sectoral GDP Composition (Agriculture, Industry, Manufacturing).** The economic structure of a country, represented by the composition of its sectoral GDP, directly impacts its emissions profile. Countries with a higher reliance on industry or manufacturing tend to have greater emissions intensity, which should be considered in allocation. Analyzing sectoral GDP

composition supports a fair allocation by recognizing that countries with emissions-intensive economies face distinct challenges compared to those with service-based economies. This attribute thus enhances vertical equity and ensures allowances are distributed in line with each country's economic activity type.

- Principle: Fairness

|  | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 4.32 | 4.79 | 5.14 | 5.46 | 6.05 | 0.55 |
| Belgium | 2.99 | 3.22 | 3.39 | 3.62 | 3.88 | 0.27 |
| Bulgaria | 2.04 | 2.20 | 2.39 | 2.56 | 3.20 | 0.33 |
| Cyprus | 0.37 | 0.44 | 0.49 | 0.52 | 0.59 | 0.07 |
| Denmark | 2.68 | 3.02 | 3.87 | 4.49 | 5.41 | 0.91 |
| Estonia | 0.49 | 0.63 | 0.65 | 0.80 | 0.85 | 0.13 |
| Finland | 5.29 | 5.82 | 6.03 | 6.41 | 6.59 | 0.43 |
| France | 35.54 | 39.60 | 42.43 | 44.42 | 47.28 | 3.91 |
| Germany | 22.99 | 25.78 | 29.91 | 32.78 | 35.20 | 4.54 |
| Greece | 6.79 | 7.71 | 8.33 | 8.85 | 9.99 | 0.90 |
| Hungary | 4.01 | 4.87 | 5.31 | 5.51 | 5.67 | 0.60 |
| Ireland | 1.32 | 2.28 | 2.61 | 3.06 | 3.96 | 0.71 |
| Italy | 36.20 | 38.32 | 40.70 | 43.21 | 45.94 | 3.17 |
| Latvia | 0.85 | 0.96 | 0.97 | 1.07 | 1.24 | 0.11 |
| Lithuania | 0.95 | 1.38 | 1.55 | 1.66 | 1.71 | 0.24 |
| Luxembourg | 0.13 | 0.14 | 0.15 | 0.17 | 0.20 | 0.02 |
| Malta | 0.09 | 0.10 | 0.11 | 0.11 | 0.13 | 0.01 |
| Netherlands | 13.20 | 13.89 | 15.07 | 15.49 | 15.71 | 0.92 |
| Poland | 11.25 | 13.13 | 14.22 | 15.96 | 16.76 | 1.91 |
| Portugal | 4.16 | 4.38 | 4.64 | 4.77 | 5.17 | 0.32 |
| Romania | 7.87 | 8.47 | 9.88 | 10.88 | 13.51 | 1.74 |
| Slovenia | 0.89 | 0.91 | 0.92 | 1.01 | 1.22 | 0.10 |
| Spain | 31.90 | 34.18 | 34.84 | 36.07 | 39.19 | 2.23 |
| Sweden | 6.27 | 7.53 | 8.11 | 8.47 | 9.59 | 0.87 |
| United Kingdom | 14.74 | 16.11 | 17.05 | 18.33 | 22.84 | 2.28 |

Table 10.6: Agriculture as a percentage of GDP

## 10.2 Experiment Data

|  | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 96.16 | 102.24 | 106.03 | 111.06 | 116.48 | 6.50 |
| Belgium | 90.94 | 98.13 | 100.59 | 104.53 | 111.72 | 6.42 |
| Bulgaria | 12.04 | 13.16 | 13.62 | 14.01 | 14.87 | 0.87 |
| Cyprus | 2.03 | 2.45 | 2.95 | 3.63 | 4.98 | 0.90 |
| Denmark | 60.50 | 64.40 | 68.89 | 69.76 | 79.84 | 5.40 |
| Estonia | 4.61 | 5.63 | 5.97 | 6.42 | 7.36 | 0.81 |
| Finland | 54.66 | 61.38 | 63.49 | 65.70 | 84.47 | 7.78 |
| France | 431.14 | 459.74 | 479.72 | 506.08 | 551.30 | 36.97 |
| Germany | 843.80 | 934.68 | 1000.01 | 1014.25 | 1085.27 | 69.42 |
| Greece | 27.44 | 28.64 | 35.83 | 42.48 | 55.73 | 9.66 |
| Hungary | 32.23 | 32.95 | 33.99 | 36.13 | 40.79 | 2.98 |
| Ireland | 51.79 | 57.18 | 62.99 | 110.85 | 141.75 | 32.57 |
| Italy | 383.06 | 431.67 | 449.66 | 474.26 | 568.48 | 50.60 |
| Latvia | 4.90 | 5.37 | 5.81 | 6.01 | 7.81 | 0.78 |
| Lithuania | 9.38 | 11.12 | 12.22 | 13.05 | 13.97 | 1.52 |
| Luxembourg | 5.99 | 6.42 | 6.93 | 7.48 | 7.80 | 0.62 |
| Malta | 1.36 | 1.48 | 1.54 | 1.59 | 1.84 | 0.14 |
| Netherlands | 138.29 | 155.19 | 166.89 | 173.29 | 204.75 | 19.28 |
| Poland | 129.76 | 146.41 | 150.02 | 156.35 | 169.32 | 10.65 |
| Portugal | 38.81 | 41.82 | 43.54 | 47.46 | 53.70 | 4.42 |
| Romania | 54.81 | 61.02 | 63.42 | 67.76 | 78.81 | 7.80 |
| Slovenia | 12.08 | 12.77 | 13.77 | 13.95 | 16.62 | 1.31 |
| Spain | 240.11 | 268.98 | 278.66 | 328.16 | 429.02 | 57.54 |
| Sweden | 97.80 | 114.87 | 122.21 | 126.94 | 135.67 | 10.52 |
| United Kingdom | 448.57 | 473.78 | 494.10 | 522.75 | 583.44 | 40.55 |

Table 10.7: Industry as a percentage of GDP

| All the data from experiment of section 3.4 | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
| Austria | 2008 | 1.00 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.47 | 0.01 |
| Austria | 2009 | 1.00 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.38 | 0.01 |
| Austria | 2010 | 1.00 | 0.98 | 0.90 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.51 | 0.01 |
| Austria | 2011 | 1.00 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.37 | 0.01 |
| Austria | 2012 | 1.00 | 0.96 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.48 | 0.01 |
| Austria | 2013 | 0.92 | 0.90 | 0.75 | 0 | 0.84 | 0.00 | 0.07 | 0.04 | 0.16 | 0.07 |
| Austria | 2014 | 0.94 | 0.95 | 0.84 | 0 | 0.88 | 0.00 | 0.06 | 0.03 | 0.06 | 0.09 |
| Austria | 2015 | 0.96 | 0.95 | 0.86 | 0 | 0.92 | 0.00 | 0.05 | 0.02 | 0.02 | 0.08 |
| Austria | 2016 | 0.97 | 0.96 | 0.85 | 0 | 0.95 | 0.00 | 0.04 | 0.02 | 0.02 | 0.07 |

| country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Austria | 2017 | 0.98 | 0.98 | 0.90 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.02 | 0.05 |
| Austria | 2018 | 0.99 | 0.98 | 0.91 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.00 | 0.06 |
| Austria | 2019 | 0.99 | 0.99 | 0.94 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.00 | 0.06 |
| Austria | 2020 | 1.00 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.01 | 0.03 |
| Belgium | 2008 | 0.99 | 0.88 | 0.81 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.63 | 0.01 |
| Belgium | 2009 | 0.99 | 0.97 | 0.89 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.55 | 0.01 |
| Belgium | 2010 | 0.99 | 0.93 | 0.80 | 0 | 0.98 | 0.00 | 0.02 | 0.02 | 0.70 | 0.01 |
| Belgium | 2011 | 0.99 | 0.93 | 0.81 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.63 | 0.01 |
| Belgium | 2012 | 0.99 | 0.89 | 0.72 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.94 | 0.00 |
| Belgium | 2013 | 0.85 | 0.88 | 0.79 | 0 | 0.73 | 0.01 | 0.07 | 0.04 | 0.17 | 0.12 |
| Belgium | 2014 | 0.88 | 0.81 | 0.70 | 0 | 0.77 | 0.00 | 0.07 | 0.03 | 0.05 | 0.14 |
| Belgium | 2015 | 0.92 | 0.82 | 0.73 | 0 | 0.85 | 0.00 | 0.05 | 0.03 | 0.02 | 0.13 |
| Belgium | 2016 | 0.95 | 0.82 | 0.72 | 0 | 0.90 | 0.00 | 0.04 | 0.02 | 0.02 | 0.11 |
| Belgium | 2017 | 0.98 | 0.86 | 0.79 | 0 | 0.95 | 0.00 | 0.03 | 0.02 | 0.17 | 0.05 |
| Belgium | 2018 | 0.98 | 0.85 | 0.79 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.16 | 0.05 |
| Belgium | 2019 | 0.98 | 0.92 | 0.85 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.26 | 0.04 |
| Belgium | 2020 | 0.99 | 0.94 | 0.82 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.43 | 0.02 |
| Bulgaria | 2008 | 0.99 | 0.99 | 0.95 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.21 | 0.02 |
| Bulgaria | 2009 | 0.99 | 0.98 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.15 | 0.02 |
| Bulgaria | 2010 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.22 | 0.02 |
| Bulgaria | 2011 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.19 | 0.02 |
| Bulgaria | 2012 | 0.99 | 0.97 | 0.87 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.10 | 0.02 |
| Bulgaria | 2013 | 0.94 | 0.69 | 0.56 | 0 | 0.88 | 0.01 | 0.07 | 0.05 | 0.46 | 0.03 |
| Bulgaria | 2014 | 0.95 | 0.69 | 0.56 | 0 | 0.90 | 0.00 | 0.07 | 0.05 | 0.29 | 0.04 |
| Bulgaria | 2015 | 0.97 | 0.72 | 0.57 | 0 | 0.94 | 0.00 | 0.05 | 0.04 | 0.20 | 0.04 |
| Bulgaria | 2016 | 0.98 | 0.79 | 0.64 | 0 | 0.96 | 0.00 | 0.04 | 0.03 | 0.35 | 0.02 |
| Bulgaria | 2017 | 0.99 | 0.94 | 0.83 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.25 | 0.02 |
| Bulgaria | 2018 | 0.99 | 0.92 | 0.80 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.08 | 0.02 |
| Bulgaria | 2019 | 0.99 | 0.98 | 0.91 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.03 |
| Bulgaria | 2020 | 1.00 | 0.98 | 0.91 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.05 | 0.01 |
| Cyprus | 2008 | 1.00 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.34 | 0.01 |
| Cyprus | 2009 | 0.99 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.31 | 0.01 |
| Cyprus | 2010 | 1.00 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.31 | 0.01 |
| Cyprus | 2011 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.27 | 0.02 |
| Cyprus | 2012 | 0.99 | 0.97 | 0.88 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.31 | 0.01 |
| Cyprus | 2013 | 0.96 | 0.96 | 0.84 | 0 | 0.91 | 0.00 | 0.07 | 0.04 | 0.57 | 0.02 |
| Cyprus | 2014 | 0.97 | 0.96 | 0.87 | 0 | 0.93 | 0.00 | 0.06 | 0.03 | 0.35 | 0.03 |
| Cyprus | 2015 | 0.98 | 0.97 | 0.88 | 0 | 0.96 | 0.00 | 0.05 | 0.03 | 0.14 | 0.04 |
| Cyprus | 2016 | 0.99 | 0.97 | 0.88 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.11 | 0.03 |
| Cyprus | 2017 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.06 | 0.03 |

(continued)

| country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Cyprus | 2018 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.03 | 0.03 |
| Cyprus | 2019 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.01 | 0.04 |
| Cyprus | 2020 | 1.00 | 1.00 | 0.97 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.03 | 0.02 |
| Denmark | 2008 | 0.99 | 0.98 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.32 | 0.01 |
| Denmark | 2009 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.29 | 0.01 |
| Denmark | 2010 | 0.99 | 0.97 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.33 | 0.01 |
| Denmark | 2011 | 0.99 | 0.96 | 0.90 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.27 | 0.01 |
| Denmark | 2012 | 0.99 | 0.92 | 0.83 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.24 | 0.01 |
| Denmark | 2013 | 0.95 | 0.94 | 0.83 | 0 | 0.90 | 0.00 | 0.07 | 0.04 | 0.24 | 0.04 |
| Denmark | 2014 | 0.96 | 0.96 | 0.87 | 0 | 0.92 | 0.00 | 0.06 | 0.03 | 0.12 | 0.05 |
| Denmark | 2015 | 0.98 | 0.95 | 0.83 | 0 | 0.95 | 0.00 | 0.05 | 0.03 | 0.04 | 0.05 |
| Denmark | 2016 | 0.98 | 0.96 | 0.87 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.03 | 0.04 |
| Denmark | 2017 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.03 |
| Denmark | 2018 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.03 |
| Denmark | 2019 | 0.99 | 0.98 | 0.92 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.00 | 0.04 |
| Denmark | 2020 | 1.00 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.01 | 0.02 |
| Estonia | 2008 | 0.99 | 0.97 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.30 | 0.01 |
| Estonia | 2009 | 0.99 | 0.96 | 0.88 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.32 | 0.01 |
| Estonia | 2010 | 0.99 | 0.96 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.36 | 0.01 |
| Estonia | 2011 | 0.99 | 0.90 | 0.80 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.29 | 0.01 |
| Estonia | 2012 | 0.99 | 0.93 | 0.82 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.28 | 0.01 |
| Estonia | 2013 | 0.95 | 0.87 | 0.73 | 0 | 0.91 | 0.00 | 0.07 | 0.04 | 0.69 | 0.02 |
| Estonia | 2014 | 0.96 | 0.85 | 0.71 | 0 | 0.93 | 0.00 | 0.06 | 0.04 | 0.43 | 0.03 |
| Estonia | 2015 | 0.98 | 0.91 | 0.78 | 0 | 0.95 | 0.00 | 0.05 | 0.03 | 0.21 | 0.03 |
| Estonia | 2016 | 0.98 | 0.92 | 0.79 | 0 | 0.97 | 0.00 | 0.04 | 0.03 | 0.25 | 0.02 |
| Estonia | 2017 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.18 | 0.02 |
| Estonia | 2018 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.05 | 0.03 |
| Estonia | 2019 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.02 | 0.03 |
| Estonia | 2020 | 1.00 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.17 | 0.01 |
| Finland | 2008 | 0.99 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.37 | 0.01 |
| Finland | 2009 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.26 | 0.02 |
| Finland | 2010 | 1.00 | 0.99 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.34 | 0.01 |
| Finland | 2011 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.27 | 0.02 |
| Finland | 2012 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.30 | 0.02 |
| Finland | 2013 | 0.92 | 0.91 | 0.79 | 0 | 0.85 | 0.00 | 0.07 | 0.04 | 0.15 | 0.08 |
| Finland | 2014 | 0.94 | 0.96 | 0.87 | 0 | 0.88 | 0.00 | 0.06 | 0.03 | 0.06 | 0.09 |
| Finland | 2015 | 0.96 | 0.94 | 0.83 | 0 | 0.93 | 0.00 | 0.05 | 0.02 | 0.02 | 0.08 |
| Finland | 2016 | 0.98 | 0.95 | 0.84 | 0 | 0.96 | 0.00 | 0.04 | 0.02 | 0.02 | 0.06 |
| Finland | 2017 | 0.99 | 0.96 | 0.87 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.05 |
| Finland | 2018 | 0.99 | 0.98 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.05 |

| country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Finland | 2019 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.00 | 0.05 |
| Finland | 2020 | 1.00 | 0.97 | 0.91 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.02 | 0.02 |
| France | 2008 | 0.92 | 0.94 | 0.83 | 0 | 0.84 | 0.00 | 0.04 | 0.03 | 0.00 | 0.31 |
| France | 2009 | 0.91 | 0.95 | 0.83 | 0 | 0.82 | 0.00 | 0.05 | 0.03 | 0.00 | 0.34 |
| France | 2010 | 0.94 | 0.97 | 0.87 | 0 | 0.88 | 0.00 | 0.04 | 0.02 | 0.00 | 0.26 |
| France | 2011 | 0.94 | 0.97 | 0.87 | 0 | 0.89 | 0.00 | 0.04 | 0.02 | 0.00 | 0.27 |
| France | 2012 | 0.96 | 0.96 | 0.85 | 0 | 0.93 | 0.00 | 0.03 | 0.02 | 0.00 | 0.21 |
| France | 2013 | 0.98 | 0.97 | 0.88 | 0 | 0.95 | 0.00 | 0.03 | 0.01 | 0.55 | 0.05 |
| France | 2014 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.96 | 0.00 |
| France | 2015 | 1.00 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.94 | 0.00 |
| France | 2016 | 1.00 | 0.98 | 0.91 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.48 | -0.02 |
| France | 2017 | 1.00 | 0.98 | 0.92 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.83 | 0.00 |
| France | 2018 | 1.00 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.98 | 0.00 |
| France | 2019 | 1.00 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.32 | 0.03 |
| France | 2020 | 1.00 | 0.99 | 0.93 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.94 | 0.00 |
| Germany | 2008 | 0.98 | 0.96 | 0.87 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.79 | -0.02 |
| Germany | 2009 | 0.98 | 0.97 | 0.89 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.85 | -0.01 |
| Germany | 2010 | 0.98 | 0.96 | 0.84 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.94 | -0.01 |
| Germany | 2011 | 0.98 | 0.97 | 0.86 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.94 | 0.01 |
| Germany | 2012 | 0.98 | 0.95 | 0.83 | 0 | 0.95 | 0.00 | 0.03 | 0.02 | 0.46 | 0.07 |
| Germany | 2013 | 0.98 | 0.97 | 0.86 | 0 | 0.95 | 0.00 | 0.03 | 0.02 | 0.03 | 0.13 |
| Germany | 2014 | 0.98 | 0.98 | 0.89 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.02 | 0.13 |
| Germany | 2015 | 0.98 | 0.97 | 0.88 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.06 | 0.09 |
| Germany | 2016 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.02 | 0.02 | 0.12 | 0.07 |
| Germany | 2017 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.13 | 0.06 |
| Germany | 2018 | 0.99 | 0.99 | 0.93 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.19 | 0.05 |
| Germany | 2019 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.17 | 0.05 |
| Germany | 2020 | 1.00 | 0.99 | 0.92 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.06 | 0.06 |
| Greece | 2008 | 0.98 | 0.99 | 0.95 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.50 | 0.02 |
| Greece | 2009 | 0.98 | 0.98 | 0.92 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.35 | 0.02 |
| Greece | 2010 | 0.98 | 0.99 | 0.93 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.34 | 0.02 |
| Greece | 2011 | 0.98 | 0.99 | 0.94 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.26 | 0.03 |
| Greece | 2012 | 0.98 | 0.97 | 0.86 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.19 | 0.03 |
| Greece | 2013 | 0.95 | 0.93 | 0.82 | 0 | 0.90 | 0.00 | 0.07 | 0.04 | 0.37 | 0.04 |
| Greece | 2014 | 0.96 | 0.91 | 0.77 | 0 | 0.92 | 0.00 | 0.06 | 0.03 | 0.23 | 0.05 |
| Greece | 2015 | 0.97 | 0.90 | 0.78 | 0 | 0.95 | 0.00 | 0.04 | 0.03 | 0.07 | 0.05 |
| Greece | 2016 | 0.98 | 0.95 | 0.83 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.13 | 0.03 |
| Greece | 2017 | 0.99 | 0.97 | 0.87 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.11 | 0.03 |
| Greece | 2018 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.07 | 0.03 |
| Greece | 2019 | 0.99 | 0.97 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.02 | 0.04 |

*(continued)*

| country | year | pear-son cor.n | spear man cor. | ken-dall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Greece | 2020 | 1.00 | 0.97 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.33 | 0.01 |
| Hungary | 2008 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.39 | 0.01 |
| Hungary | 2009 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.38 | 0.01 |
| Hungary | 2010 | 0.99 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.38 | 0.01 |
| Hungary | 2011 | 0.99 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.37 | 0.01 |
| Hungary | 2012 | 0.99 | 0.96 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.40 | 0.01 |
| Hungary | 2013 | 0.94 | 0.86 | 0.71 | 0 | 0.89 | 0.00 | 0.07 | 0.04 | 0.42 | 0.03 |
| Hungary | 2014 | 0.96 | 0.95 | 0.84 | 0 | 0.92 | 0.00 | 0.06 | 0.03 | 0.19 | 0.04 |
| Hungary | 2015 | 0.98 | 0.94 | 0.81 | 0 | 0.95 | 0.00 | 0.05 | 0.03 | 0.06 | 0.04 |
| Hungary | 2016 | 0.98 | 0.97 | 0.88 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.05 | 0.03 |
| Hungary | 2017 | 0.99 | 0.98 | 0.90 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.03 | 0.03 |
| Hungary | 2018 | 0.99 | 0.97 | 0.88 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.01 | 0.03 |
| Hungary | 2019 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.00 | 0.03 |
| Hungary | 2020 | 1.00 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.07 | 0.01 |
| Ireland | 2008 | 1.00 | 0.96 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.40 | 0.01 |
| Ireland | 2009 | 0.99 | 0.96 | 0.88 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.38 | 0.01 |
| Ireland | 2010 | 1.00 | 0.94 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.37 | 0.01 |
| Ireland | 2011 | 0.99 | 0.94 | 0.85 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.31 | 0.01 |
| Ireland | 2012 | 0.99 | 0.96 | 0.86 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.36 | 0.01 |
| Ireland | 2013 | 0.95 | 0.90 | 0.77 | 0 | 0.90 | 0.00 | 0.07 | 0.04 | 0.32 | 0.05 |
| Ireland | 2014 | 0.96 | 0.93 | 0.83 | 0 | 0.92 | 0.00 | 0.06 | 0.03 | 0.17 | 0.05 |
| Ireland | 2015 | 0.98 | 0.95 | 0.84 | 0 | 0.95 | 0.00 | 0.05 | 0.03 | 0.07 | 0.05 |
| Ireland | 2016 | 0.98 | 0.96 | 0.86 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.07 | 0.04 |
| Ireland | 2017 | 0.99 | 0.98 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.04 | 0.04 |
| Ireland | 2018 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.02 | 0.04 |
| Ireland | 2019 | 0.99 | 0.98 | 0.91 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.05 |
| Ireland | 2020 | 1.00 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.05 | 0.02 |
| Italy | 2008 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.70 | -0.01 |
| Italy | 2009 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.04 | -0.07 |
| Italy | 2010 | 0.99 | 0.99 | 0.95 | 0 | 0.97 | 0.00 | 0.02 | 0.01 | 0.11 | -0.07 |
| Italy | 2011 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.28 | -0.04 |
| Italy | 2012 | 0.99 | 0.99 | 0.92 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.53 | -0.02 |
| Italy | 2013 | 0.97 | 0.97 | 0.86 | 0 | 0.94 | 0.00 | 0.03 | 0.02 | 0.57 | -0.03 |
| Italy | 2014 | 0.97 | 0.97 | 0.88 | 0 | 0.95 | 0.00 | 0.03 | 0.02 | 0.64 | -0.02 |
| Italy | 2015 | 0.99 | 0.95 | 0.87 | 0 | 0.97 | 0.00 | 0.02 | 0.01 | 0.68 | -0.01 |
| Italy | 2016 | 1.00 | 0.96 | 0.89 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.32 | -0.02 |
| Italy | 2017 | 1.00 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.52 | 0.01 |
| Italy | 2018 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.38 | 0.03 |
| Italy | 2019 | 0.99 | 0.99 | 0.93 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.05 | 0.05 |
| Italy | 2020 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.05 | -0.05 |

| country | year | pear-son cor.n | spear man cor. | ken-dall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---------|------|------|------|------|------|------|------|------|------|------|------|
| Latvia | 2008 | 0.99 | 0.97 | 0.88 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.84 | 0.00 |
| Latvia | 2009 | 0.99 | 0.95 | 0.86 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.57 | -0.01 |
| Latvia | 2010 | 0.99 | 0.88 | 0.76 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.99 | 0.00 |
| Latvia | 2011 | 0.99 | 0.96 | 0.85 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.82 | 0.00 |
| Latvia | 2012 | 0.99 | 0.93 | 0.79 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.60 | 0.01 |
| Latvia | 2013 | 0.95 | 0.95 | 0.83 | 0 | 0.91 | 0.00 | 0.07 | 0.04 | 0.52 | 0.03 |
| Latvia | 2014 | 0.96 | 0.93 | 0.80 | 0 | 0.93 | 0.00 | 0.06 | 0.03 | 0.36 | 0.04 |
| Latvia | 2015 | 0.98 | 0.96 | 0.86 | 0 | 0.96 | 0.00 | 0.05 | 0.03 | 0.14 | 0.05 |
| Latvia | 2016 | 0.99 | 0.96 | 0.85 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.14 | 0.04 |
| Latvia | 2017 | 0.99 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.09 | 0.03 |
| Latvia | 2018 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.06 | 0.04 |
| Latvia | 2019 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.02 | 0.04 |
| Latvia | 2020 | 1.00 | 0.98 | 0.90 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.33 | 0.01 |
| Lithuania | 2008 | 1.00 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.63 | 0.01 |
| Lithuania | 2009 | 0.99 | 0.97 | 0.89 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.70 | 0.01 |
| Lithuania | 2010 | 0.99 | 0.95 | 0.83 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.68 | 0.01 |
| Lithuania | 2011 | 0.99 | 0.98 | 0.90 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.61 | 0.01 |
| Lithuania | 2012 | 0.99 | 0.94 | 0.80 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.71 | 0.01 |
| Lithuania | 2013 | 0.95 | 0.92 | 0.78 | 0 | 0.91 | 0.00 | 0.07 | 0.04 | 0.41 | 0.04 |
| Lithuania | 2014 | 0.96 | 0.90 | 0.79 | 0 | 0.93 | 0.00 | 0.06 | 0.03 | 0.23 | 0.05 |
| Lithuania | 2015 | 0.98 | 0.89 | 0.77 | 0 | 0.96 | 0.00 | 0.05 | 0.03 | 0.07 | 0.05 |
| Lithuania | 2016 | 0.99 | 0.88 | 0.76 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.06 | 0.04 |
| Lithuania | 2017 | 0.99 | 0.94 | 0.82 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.04 | 0.04 |
| Lithuania | 2018 | 0.99 | 0.96 | 0.87 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.04 |
| Lithuania | 2019 | 0.99 | 0.96 | 0.88 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.00 | 0.04 |
| Lithuania | 2020 | 1.00 | 0.96 | 0.87 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.05 | 0.02 |
| Luxembourg | 2008 | 1.00 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.40 | 0.01 |
| Luxembourg | 2009 | 0.99 | 0.99 | 0.96 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.36 | 0.01 |
| Luxembourg | 2010 | 1.00 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.36 | 0.01 |
| Luxembourg | 2011 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.31 | 0.01 |
| Luxembourg | 2012 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.35 | 0.01 |
| Luxembourg | 2013 | 0.96 | 0.96 | 0.84 | 0 | 0.91 | 0.00 | 0.07 | 0.04 | 0.51 | 0.03 |
| Luxembourg | 2014 | 0.97 | 0.96 | 0.86 | 0 | 0.93 | 0.00 | 0.06 | 0.03 | 0.29 | 0.03 |
| Luxembourg | 2015 | 0.98 | 0.96 | 0.87 | 0 | 0.96 | 0.00 | 0.05 | 0.02 | 0.10 | 0.04 |
| Luxembourg | 2016 | 0.99 | 0.96 | 0.87 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.08 | 0.03 |
| Luxembourg | 2017 | 0.99 | 0.98 | 0.91 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.04 | 0.03 |
| Luxembourg | 2018 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.02 | 0.03 |
| Luxembourg | 2019 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.01 | 0.03 |
| Luxembourg | 2020 | 1.00 | 0.99 | 0.94 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.03 | 0.02 |
| Malta | 2008 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.44 | 0.01 |

| country | year | pear-son cor.n | spear-man cor. | ken-dall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Malta | 2009 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.39 | 0.01 |
| Malta | 2010 | 1.00 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.39 | 0.01 |
| Malta | 2011 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.35 | 0.01 |
| Malta | 2012 | 0.99 | 0.98 | 0.90 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.35 | 0.01 |
| Malta | 2013 | 0.96 | 0.96 | 0.84 | 0 | 0.92 | 0.00 | 0.07 | 0.04 | 0.52 | 0.02 |
| Malta | 2014 | 0.97 | 0.96 | 0.87 | 0 | 0.93 | 0.00 | 0.06 | 0.03 | 0.31 | 0.03 |
| Malta | 2015 | 0.98 | 0.97 | 0.89 | 0 | 0.96 | 0.00 | 0.04 | 0.02 | 0.12 | 0.03 |
| Malta | 2016 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.04 | 0.02 | 0.10 | 0.03 |
| Malta | 2017 | 0.99 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.06 | 0.02 |
| Malta | 2018 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.03 | 0.03 |
| Malta | 2019 | 0.99 | 1.00 | 0.97 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.01 | 0.03 |
| Malta | 2020 | 1.00 | 1.00 | 0.97 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.04 | 0.01 |
| Netherlands | 2008 | 0.98 | 0.93 | 0.84 | 0 | 0.97 | 0.00 | 0.03 | 0.01 | 0.94 | 0.00 |
| Netherlands | 2009 | 0.99 | 0.98 | 0.89 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.99 | 0.00 |
| Netherlands | 2010 | 0.99 | 0.96 | 0.87 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.97 | 0.00 |
| Netherlands | 2011 | 0.98 | 0.92 | 0.79 | 0 | 0.97 | 0.00 | 0.02 | 0.02 | 0.39 | 0.03 |
| Netherlands | 2012 | 0.99 | 0.95 | 0.82 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.26 | -0.03 |
| Netherlands | 2013 | 0.77 | 0.74 | 0.67 | 0 | 0.60 | 0.01 | 0.08 | 0.04 | 0.31 | 0.11 |
| Netherlands | 2014 | 0.82 | 0.69 | 0.64 | 0 | 0.68 | 0.00 | 0.07 | 0.03 | 0.22 | 0.11 |
| Netherlands | 2015 | 0.89 | 0.72 | 0.67 | 0 | 0.79 | 0.00 | 0.06 | 0.03 | 0.26 | 0.09 |
| Netherlands | 2016 | 0.94 | 0.88 | 0.82 | 0 | 0.88 | 0.00 | 0.04 | 0.02 | 0.99 | 0.00 |
| Netherlands | 2017 | 0.97 | 0.95 | 0.84 | 0 | 0.94 | 0.00 | 0.03 | 0.02 | 0.50 | -0.03 |
| Netherlands | 2018 | 0.97 | 0.98 | 0.91 | 0 | 0.95 | 0.00 | 0.03 | 0.01 | 0.24 | -0.05 |
| Netherlands | 2019 | 0.98 | 0.99 | 0.95 | 0 | 0.96 | 0.00 | 0.02 | 0.01 | 0.08 | -0.06 |
| Netherlands | 2020 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.62 | -0.01 |
| Poland | 2008 | 0.64 | 0.75 | 0.71 | 0 | 0.40 | 0.01 | 0.10 | 0.07 | 0.01 | -0.42 |
| Poland | 2009 | 0.65 | 0.77 | 0.71 | 0 | 0.42 | 0.01 | 0.10 | 0.07 | 0.01 | -0.42 |
| Poland | 2010 | 0.68 | 0.83 | 0.72 | 0 | 0.46 | 0.01 | 0.09 | 0.07 | 0.01 | -0.38 |
| Poland | 2011 | 0.70 | 0.83 | 0.74 | 0 | 0.48 | 0.01 | 0.09 | 0.06 | 0.01 | -0.41 |
| Poland | 2012 | 0.67 | 0.78 | 0.73 | 0 | 0.44 | 0.01 | 0.09 | 0.06 | 0.05 | -0.25 |
| Poland | 2013 | 0.84 | 0.96 | 0.86 | 0 | 0.70 | 0.00 | 0.07 | 0.04 | 0.02 | 0.48 |
| Poland | 2014 | 0.88 | 0.97 | 0.87 | 0 | 0.78 | 0.00 | 0.06 | 0.03 | 0.00 | 0.54 |
| Poland | 2015 | 0.92 | 0.93 | 0.84 | 0 | 0.85 | 0.00 | 0.05 | 0.03 | 0.00 | 0.34 |
| Poland | 2016 | 0.93 | 0.93 | 0.83 | 0 | 0.86 | 0.00 | 0.05 | 0.03 | 0.00 | 0.27 |
| Poland | 2017 | 0.93 | 0.93 | 0.85 | 0 | 0.87 | 0.00 | 0.05 | 0.03 | 0.00 | 0.21 |
| Poland | 2018 | 0.90 | 0.94 | 0.87 | 0 | 0.81 | 0.00 | 0.05 | 0.03 | 0.00 | 0.28 |
| Poland | 2019 | 0.91 | 0.95 | 0.87 | 0 | 0.83 | 0.00 | 0.05 | 0.03 | 0.00 | 0.25 |
| Poland | 2020 | 0.96 | 0.90 | 0.79 | 0 | 0.91 | 0.00 | 0.04 | 0.02 | 0.01 | 0.11 |
| Portugal | 2008 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.38 | 0.01 |
| Portugal | 2009 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.33 | 0.02 |

| country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---------|------|------|------|------|------|------|------|------|------|------|------|
| Portugal | 2010 | 0.99 | 0.98 | 0.92 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.36 | 0.01 |
| Portugal | 2011 | 0.99 | 0.99 | 0.93 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.26 | 0.02 |
| Portugal | 2012 | 0.99 | 0.96 | 0.87 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.15 | 0.02 |
| Portugal | 2013 | 0.95 | 0.95 | 0.82 | 0 | 0.91 | 0.00 | 0.06 | 0.03 | 0.29 | 0.04 |
| Portugal | 2014 | 0.96 | 0.94 | 0.83 | 0 | 0.93 | 0.00 | 0.05 | 0.03 | 0.14 | 0.05 |
| Portugal | 2015 | 0.98 | 0.94 | 0.84 | 0 | 0.96 | 0.00 | 0.04 | 0.02 | 0.06 | 0.05 |
| Portugal | 2016 | 0.99 | 0.97 | 0.88 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.05 | 0.04 |
| Portugal | 2017 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.03 | 0.03 |
| Portugal | 2018 | 0.99 | 0.98 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.02 | 0.04 |
| Portugal | 2019 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.01 | 0.01 | 0.04 |
| Portugal | 2020 | 1.00 | 0.98 | 0.93 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.02 | 0.02 |
| Romania | 2008 | 0.97 | 0.95 | 0.88 | 0 | 0.94 | 0.00 | 0.04 | 0.02 | 0.60 | 0.02 |
| Romania | 2009 | 0.96 | 0.94 | 0.87 | 0 | 0.93 | 0.00 | 0.04 | 0.03 | 0.43 | 0.03 |
| Romania | 2010 | 0.97 | 0.95 | 0.87 | 0 | 0.94 | 0.00 | 0.04 | 0.02 | 0.41 | 0.03 |
| Romania | 2011 | 0.97 | 0.95 | 0.86 | 0 | 0.94 | 0.00 | 0.04 | 0.02 | 0.34 | 0.03 |
| Romania | 2012 | 0.97 | 0.98 | 0.90 | 0 | 0.95 | 0.00 | 0.04 | 0.02 | 0.11 | 0.05 |
| Romania | 2013 | 0.92 | 0.80 | 0.65 | 0 | 0.84 | 0.00 | 0.07 | 0.05 | 0.10 | 0.11 |
| Romania | 2014 | 0.95 | 0.92 | 0.79 | 0 | 0.90 | 0.00 | 0.06 | 0.04 | 0.09 | 0.08 |
| Romania | 2015 | 0.97 | 0.92 | 0.79 | 0 | 0.94 | 0.00 | 0.05 | 0.03 | 0.09 | 0.06 |
| Romania | 2016 | 0.98 | 0.91 | 0.77 | 0 | 0.96 | 0.00 | 0.03 | 0.02 | 0.13 | 0.04 |
| Romania | 2017 | 0.99 | 0.94 | 0.80 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.21 | 0.03 |
| Romania | 2018 | 0.99 | 0.97 | 0.89 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.11 | 0.03 |
| Romania | 2019 | 0.99 | 0.99 | 0.92 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.04 |
| Romania | 2020 | 1.00 | 0.99 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.04 | 0.03 |
| Slovenia | 2008 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.37 | 0.01 |
| Slovenia | 2009 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.33 | 0.01 |
| Slovenia | 2010 | 1.00 | 0.98 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.33 | 0.01 |
| Slovenia | 2011 | 0.99 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.29 | 0.01 |
| Slovenia | 2012 | 0.99 | 0.97 | 0.89 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.32 | 0.01 |
| Slovenia | 2013 | 0.96 | 0.96 | 0.86 | 0 | 0.91 | 0.00 | 0.07 | 0.04 | 0.50 | 0.02 |
| Slovenia | 2014 | 0.97 | 0.96 | 0.88 | 0 | 0.93 | 0.00 | 0.06 | 0.03 | 0.29 | 0.03 |
| Slovenia | 2015 | 0.98 | 0.97 | 0.89 | 0 | 0.96 | 0.00 | 0.05 | 0.02 | 0.10 | 0.04 |
| Slovenia | 2016 | 0.99 | 0.97 | 0.90 | 0 | 0.97 | 0.00 | 0.04 | 0.02 | 0.09 | 0.03 |
| Slovenia | 2017 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.03 | 0.02 | 0.05 | 0.03 |
| Slovenia | 2018 | 0.99 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.02 | 0.03 |
| Slovenia | 2019 | 0.99 | 0.99 | 0.96 | 0 | 0.99 | 0.00 | 0.03 | 0.01 | 0.01 | 0.03 |
| Slovenia | 2020 | 1.00 | 1.00 | 0.96 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.04 | 0.01 |
| Spain | 2008 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.01 | 0.01 | 0.19 | -0.03 |
| Spain | 2009 | 0.99 | 1.00 | 0.97 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.03 | -0.04 |
| Spain | 2010 | 0.99 | 0.99 | 0.94 | 0 | 0.97 | 0.00 | 0.02 | 0.01 | 0.02 | -0.06 |

*(continued)*

| country | year | pearson cor.n | spearman cor. | kendall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Spain | 2011 | 0.99 | 0.97 | 0.88 | 0 | 0.97 | 0.00 | 0.02 | 0.02 | 0.07 | -0.05 |
| Spain | 2012 | 0.98 | 0.96 | 0.85 | 0 | 0.97 | 0.00 | 0.02 | 0.02 | 0.04 | -0.06 |
| Spain | 2013 | 0.84 | 0.86 | 0.77 | 0 | 0.70 | 0.00 | 0.07 | 0.03 | 0.79 | 0.03 |
| Spain | 2014 | 0.87 | 0.87 | 0.77 | 0 | 0.76 | 0.00 | 0.06 | 0.03 | 0.57 | 0.05 |
| Spain | 2015 | 0.95 | 0.96 | 0.85 | 0 | 0.91 | 0.00 | 0.04 | 0.02 | 0.87 | 0.01 |
| Spain | 2016 | 0.99 | 0.98 | 0.90 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.26 | -0.03 |
| Spain | 2017 | 1.00 | 0.98 | 0.93 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.05 | 0.02 |
| Spain | 2018 | 1.00 | 0.99 | 0.94 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.00 | 0.05 |
| Spain | 2019 | 0.99 | 0.99 | 0.95 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.00 | 0.13 |
| Spain | 2020 | 0.99 | 1.00 | 0.97 | 0 | 0.97 | 0.00 | 0.02 | 0.01 | 0.00 | 0.12 |
| Sweden | 2008 | 1.00 | 0.96 | 0.87 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.77 | 0.00 |
| Sweden | 2009 | 0.99 | 0.91 | 0.78 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.97 | 0.00 |
| Sweden | 2010 | 1.00 | 0.92 | 0.81 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.68 | -0.01 |
| Sweden | 2011 | 1.00 | 0.94 | 0.82 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.66 | -0.01 |
| Sweden | 2012 | 0.99 | 0.94 | 0.83 | 0 | 0.99 | 0.00 | 0.02 | 0.02 | 0.47 | -0.01 |
| Sweden | 2013 | 0.90 | 0.95 | 0.82 | 0 | 0.81 | 0.00 | 0.07 | 0.03 | 0.13 | 0.11 |
| Sweden | 2014 | 0.92 | 0.97 | 0.89 | 0 | 0.85 | 0.00 | 0.06 | 0.03 | 0.04 | 0.12 |
| Sweden | 2015 | 0.95 | 0.97 | 0.87 | 0 | 0.91 | 0.00 | 0.05 | 0.02 | 0.01 | 0.11 |
| Sweden | 2016 | 0.97 | 0.97 | 0.89 | 0 | 0.94 | 0.00 | 0.04 | 0.02 | 0.02 | 0.08 |
| Sweden | 2017 | 0.98 | 0.98 | 0.90 | 0 | 0.97 | 0.00 | 0.03 | 0.02 | 0.02 | 0.06 |
| Sweden | 2018 | 0.99 | 0.98 | 0.91 | 0 | 0.97 | 0.00 | 0.03 | 0.01 | 0.01 | 0.06 |
| Sweden | 2019 | 0.99 | 0.99 | 0.94 | 0 | 0.98 | 0.00 | 0.03 | 0.02 | 0.01 | 0.06 |
| Sweden | 2020 | 1.00 | 1.00 | 0.98 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.03 | 0.03 |
| United Kingdom | 2008 | 0.99 | 0.99 | 0.95 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.41 | -0.02 |
| United Kingdom | 2009 | 0.99 | 0.99 | 0.93 | 0 | 0.98 | 0.00 | 0.02 | 0.01 | 0.09 | -0.05 |
| United Kingdom | 2010 | 0.99 | 0.99 | 0.92 | 0 | 0.99 | 0.00 | 0.02 | 0.01 | 0.08 | -0.05 |
| United Kingdom | 2011 | 0.99 | 0.99 | 0.93 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.46 | -0.02 |
| United Kingdom | 2012 | 0.95 | 0.88 | 0.79 | 0 | 0.90 | 0.00 | 0.04 | 0.02 | 0.53 | -0.06 |
| United Kingdom | 2013 | 0.87 | 0.89 | 0.79 | 0 | 0.76 | 0.00 | 0.07 | 0.03 | 0.95 | 0.01 |
| United Kingdom | 2014 | 0.94 | 0.95 | 0.84 | 0 | 0.88 | 0.00 | 0.05 | 0.02 | 0.75 | 0.03 |
| United Kingdom | 2015 | 0.98 | 0.95 | 0.86 | 0 | 0.95 | 0.00 | 0.03 | 0.02 | 0.73 | 0.02 |
| United Kingdom | 2016 | 0.97 | 0.97 | 0.86 | 0 | 0.94 | 0.00 | 0.03 | 0.03 | 0.00 | -0.14 |

*(continued)*

| country | year | pear-son cor.n | spear man cor. | ken-dall tau | linear p value | linear $r^2$ | mse | rmse | mae | quad p value | quad coeff |
|---|---|---|---|---|---|---|---|---|---|---|---|
| United King-dom | 2017 | 1.00 | 0.99 | 0.94 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.22 | -0.01 |
| United King-dom | 2018 | 1.00 | 0.99 | 0.95 | 0 | 1.00 | 0.00 | 0.01 | 0.01 | 0.56 | 0.01 |
| United King-dom | 2019 | 1.00 | 0.99 | 0.96 | 0 | 0.99 | 0.00 | 0.01 | 0.01 | 0.08 | -0.02 |
| United King-dom | 2020 | 0.97 | 0.94 | 0.81 | 0 | 0.94 | 0.00 | 0.03 | 0.02 | 0.91 | 0.00 |

Table 10.10: Analytic data for the linear regression of experiment section 3.4

|  | min | 25-quantile | median | 75-quantile | max | Std |
|---|---|---|---|---|---|---|
| Austria | 63.75 | 66.61 | 70.28 | 72.47 | 76.57 | 4.24 |
| Belgium | 58.69 | 62.46 | 64.21 | 66.70 | 72.39 | 4.02 |
| Bulgaria | -470.74 | -453.31 | -432.37 | -420.07 | -399.33 | 22.79 |
| Cyprus | 0.85 | 0.95 | 1.12 | 1.33 | 1.52 | 0.23 |
| Denmark | 35.21 | 37.47 | 40.47 | 41.64 | 46.70 | 3.45 |
| Estonia | 2.41 | 3.20 | 3.35 | 3.56 | 4.13 | 0.47 |
| Finland | 34.44 | 38.11 | 39.73 | 42.29 | 59.40 | 6.76 |
| France | 254.30 | 268.11 | 278.31 | 292.38 | 325.40 | 20.87 |
| Germany | 603.23 | 697.07 | 743.97 | 755.59 | 796.43 | 56.32 |
| Greece | 15.64 | 16.78 | 18.19 | 22.95 | 30.27 | 4.63 |
| Hungary | 22.45 | 24.56 | 25.39 | 27.39 | 29.71 | 2.23 |
| Ireland | 43.26 | 47.00 | 49.10 | 100.06 | 126.39 | 31.76 |
| Italy | 264.39 | 290.81 | 301.69 | 308.97 | 372.63 | 28.24 |
| Latvia | 2.57 | 2.85 | 3.20 | 3.32 | 3.63 | 0.32 |
| Lithuania | 5.65 | 7.20 | 8.00 | 8.15 | 8.91 | 0.96 |
| Luxembourg | 2.53 | 2.88 | 3.14 | 3.41 | 3.93 | 0.42 |
| Malta | 0.83 | 0.96 | 1.00 | 1.06 | 1.23 | 0.11 |
| Netherlands | 82.70 | 89.39 | 91.54 | 95.12 | 109.07 | 7.43 |
| Poland | 71.81 | 82.05 | 85.70 | 88.28 | 98.64 | 7.14 |
| Portugal | 24.20 | 25.62 | 27.24 | 27.71 | 31.35 | 2.12 |
| Romania | 35.95 | 37.70 | 39.72 | 44.53 | 49.91 | 4.70 |
| Slovenia | 8.43 | 8.69 | 9.28 | 9.90 | 11.00 | 0.87 |
| Spain | 135.09 | 148.07 | 155.06 | 166.17 | 207.17 | 19.84 |
| Sweden | 60.02 | 69.65 | 72.99 | 77.49 | 83.80 | 6.77 |
| United Kingdom | 218.33 | 242.14 | 251.42 | 268.16 | 286.56 | 20.19 |

**Table 10.8**: Manufacturing as a percentage of GDP

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