28th TJIMO Alexandria, Virginia

Round: Practice Guts

Problem 1. Alfredo rolls a fair, six-sided die. What is the probability that he rolls an odd number?

Problem 2. The expression $(2x-3) \times (5x+2)$ can be written as $ax^2 + bx + c$. Find a+b+c. **Problem 3.** Simplify the fraction $\frac{\frac{12}{33}}{\frac{24}{35}}$. **Problem 4.** How many factors does $2^4 \cdot 3^2 \cdot 4^3$ have?

Problem 5. Triangle \overrightarrow{ABC} has $\overrightarrow{AB} = 25$ and $\overrightarrow{BC} = 7$. If $\angle C = 90^{\circ}$, find the length of AC.

Problem 6. Let $f(x) = 7x - \sqrt{x} + 3$. Compute f(4).

Problem 7. How many squares have all 4 vertices in the array of 16 points below?



Problem 8. Express $0.\overline{47} = 0.47474747...$ as a simplified fraction.

Problem 9. Compute 25×316484 .

Problem 10. What is the largest prime factor of $25^2 - 14^2$?

Problem 11. Three consecutive odd integers add up to 27. If I subtract 1 from each of these numbers and multiply them all by 6, what is their new sum?

Problem 12. Rectangle A has side lengths 5 and 4, and Rectangle B has side lengths 7 and 2. What percentage of Rectangle A's area is Rectangle B's area?