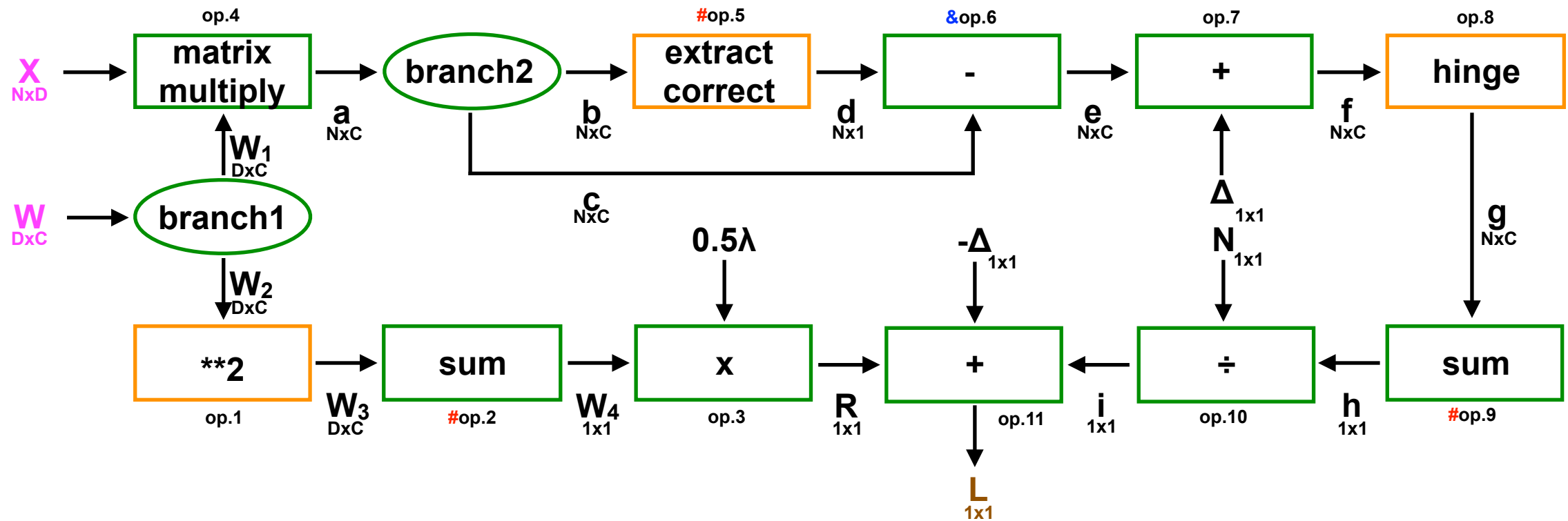


SVM



FORWARD PROP

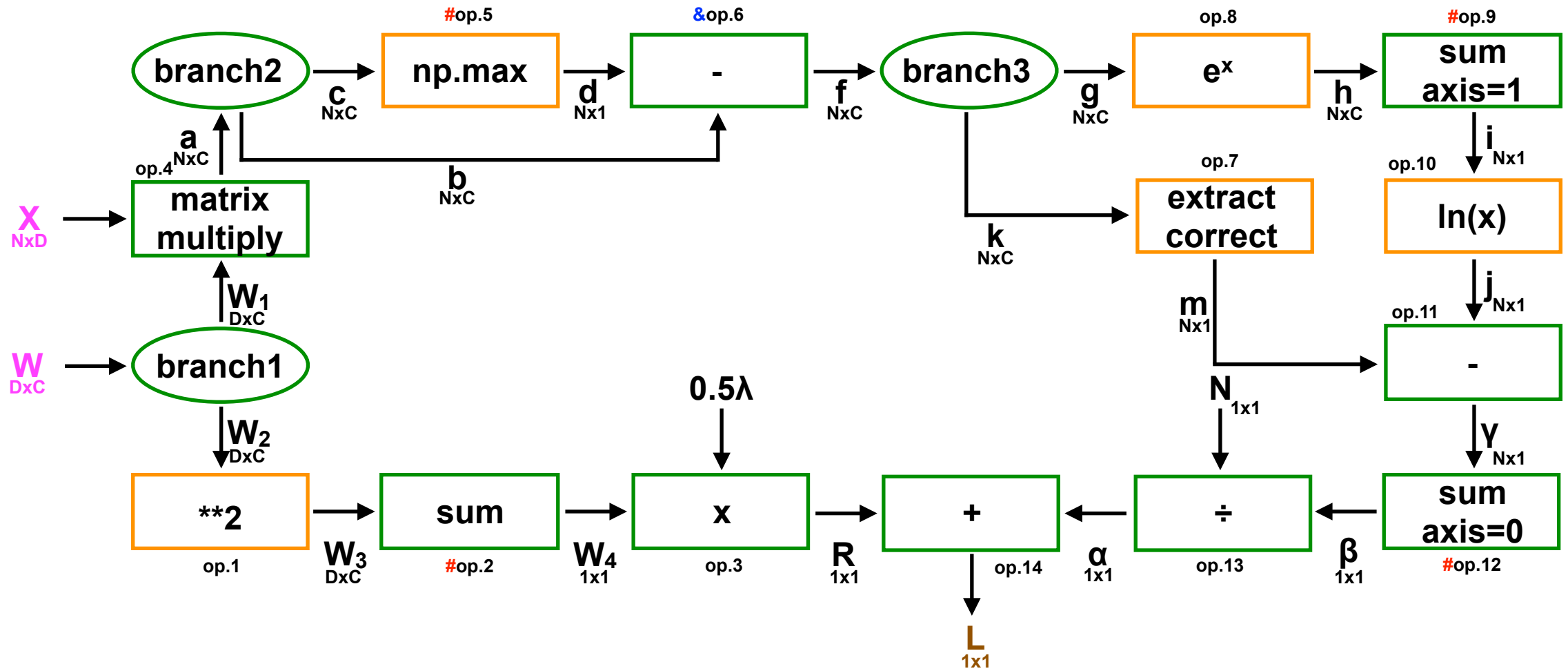
branch1: $W_1 = W_2 = W$
op. 1: $W_3 = W_2^{**2}$
op. 2: $W_4 = \text{np.sum}(W_3)$
op. 3: $R = 0.5\lambda W_4$
op. 4: $a = X.W_1$
branch2: $b = c = a$
op. 5: $d = b[\text{np.arange}(N), y]$
 $\rightarrow d = d.\text{reshape}((N, -1))$
& op. 6: $e = c - d$
op. 7: $f = e + \Delta$
op. 8: $g = \text{np.maximum}(0, f)$
op. 9: $h = \text{np.sum}(g)$
op. 10: $i = h / N$
op. 11: $L = i + R + \Delta$

BACK PROP

$dW = dW_1 + dW_2$
 $dW_2 = dW_3^{*2} W_2$
 $dW_3 = dW_4^{*1} (D, C)$
 $dW_4 = dR^{*0.5\lambda}$
 $dX = da.W_1^T$ $dW_1 = X^T.da$
 $da = db + dc$
 $dddb = 0_{(N, C)} \rightarrow dddb[\text{np.arange}(N), y] = 1.0$
 $\rightarrow db = dd * dddb$
 $dc = de$ $dd = -de.1(C, 1)$
 $de = df$
 $dgdf = \text{np.greater}(f, 0) \rightarrow df = dg * dgdf$
 $dg = dh^{*1} (N, C)$
 $dh = di / N$
 $dR = 1$ $di = 1$

... dimensional reduction
& ... broadcasting
green ... linear operations
orange ... non-linear operations
pink ... inputs needing gradients
brown ... outputs

softmax



FORWARD PROP

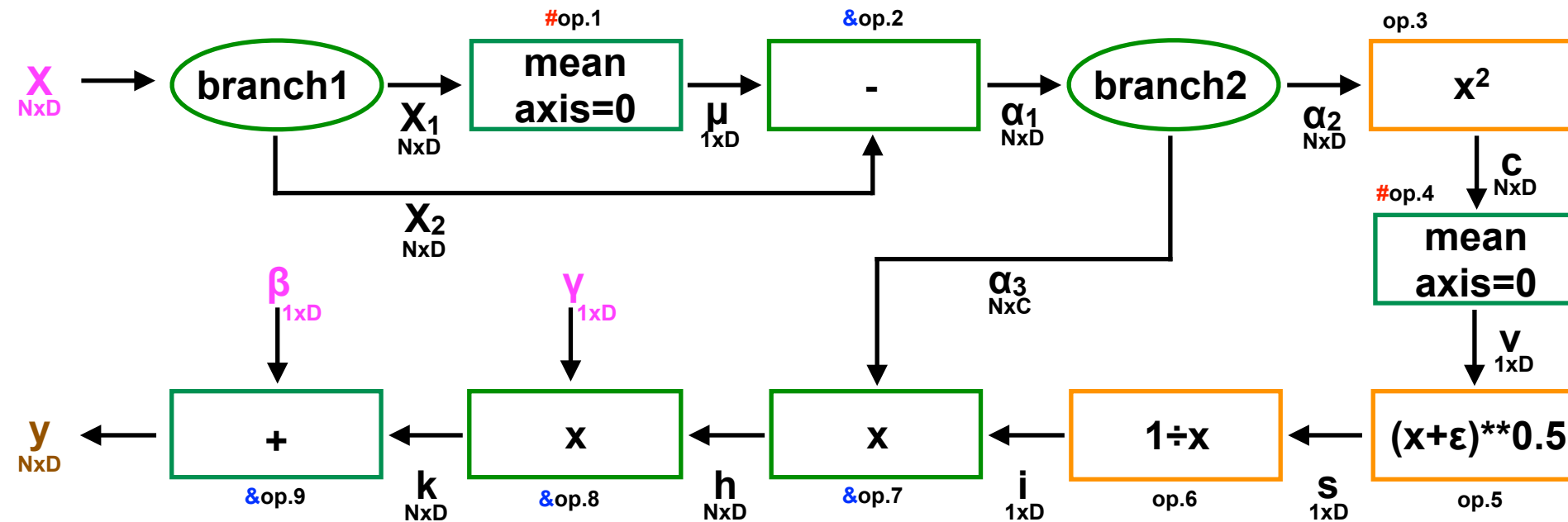
branch1: $W_1 = W_2 = W$
op. 1: $W_3 = W_2^{**2}$
op. 2: $W_4 = np.sum(W_3)$
op. 3: $R = 0.5\lambda W_4$
op. 4: $a = X.W_1$
branch2: $b = c = a$
op. 5: $d = np.max(c)$
& op. 6: $f = b - d$
branch3: $k = g = f$
op. 7: $m = k[np.arange(N), y]$
 $\rightarrow m = m.reshape((N, -1))$
op. 8: $h = \exp(g)$
op. 9: $i = np.sum(h, axis=1)$
op. 10: $j = \ln(i)$
op. 11: $y = j - m$
op. 12: $\beta = np.sum(y)$
op. 13: $\alpha = \beta / N$
op. 14: $L = R + \alpha$

BACK PROP

dW = dW₁ + dW₂
 $dW_2 = dW_3 * 2W_2$
 $dW_3 = dW_4 * 1_{(D,C)}$
 $dW_4 = dR * 0.5\lambda$
dX = da.W₁^T $dW_1 = X^T.da$
 $da = db + dc$
 $dddc = 0_{(N,C)} \rightarrow dddc[np.argmax(c)] = 1.0$
 $\rightarrow dddc = dddc.reshape((N, -1)) \rightarrow dc = dd * dddc$
 $dd = -1_{(1,N)}.df.1_{(C,1)}$ $db = df$
 $df = dk + dg$
 $dmdk = 0_{(N,C)} \rightarrow dmdk[np.arange(N), y] = 1.0 \rightarrow dk = dm * dmdk$
 $dg = dh * \exp(g)$
 $dh = di * 1_{(N,C)}$
 $di = dj / i$
 $dm = -dy$ $dj = dy$
 $dy = d\beta * 1_{(N,1)}$
 $d\beta = d\alpha / N$
 $dR = 1$ $d\alpha = 1$

... dimensional reduction
& ... broadcasting
green ... linear operations
orange ... non-linear operations
pink ... inputs needing gradients
brown ... outputs

batch norm



FORWARD PROP

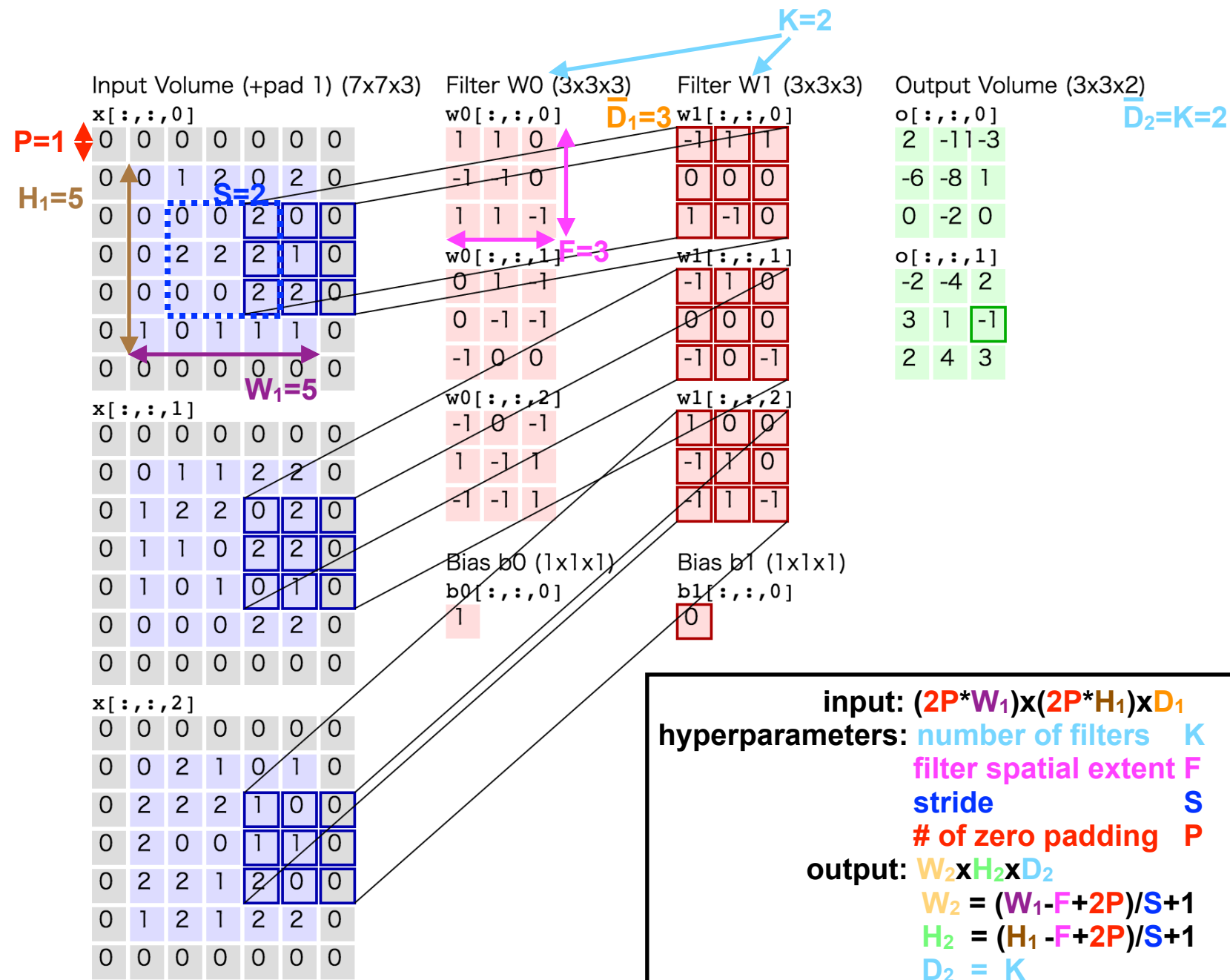
branch1: $X_1 = X_2 = X$
op. 1 : $\mu = \text{np.mean}(X_1, \text{axis}=0)$
& op. 2 : $\alpha_1 = X_2 - \mu$
branch2: $\alpha_2 = \alpha_3 = \alpha_1$
op. 3 : $c = \alpha_2^{**2}$
op. 4 : $v = \text{np.mean}(c, \text{axis}=0)$
op. 5 : $s = \text{np.sqrt}(v + \epsilon)$
op. 6 : $i = 1/s$
& op. 7 : $h = \alpha_3 * i$
& op. 8 : $k = h * y$
& op. 9 : $y = k + \beta$

BACK PROP

$dX = dX_1 + dX_2$
 $dX_1 = d\mu * \mathbf{1}_{(N,D)}/N$
 $d\mu = \mathbf{1}_{(1,N)} \cdot (-d\alpha_1)$
 $dX_2 = d\alpha_1$
 $d\alpha_1 = d\alpha_2 + d\alpha_3$
 $d\alpha_2 = dc * 2 * \alpha_2$
 $dc = dv * (\mathbf{1}_{(N,D)}/N)$
 $dv = ds * 0.5 * (v + \epsilon)^{**(-0.5)}$
 $ds = di * (-1/s^{**2})$
 $di = \mathbf{1}_{(1,N)} \cdot dh * \alpha_3$
 $\alpha_3 = dh * i$
 $dh = dk * y$
 $dk = dy$
 $dy = \mathbf{1}_{(1,N)} \cdot dk * h$
 $d\beta = \mathbf{1}_{(1,N)} \cdot dy$

... dimensional reduction
& ... broadcasting
green ... linear operations
orange ... non-linear operations
pink ... inputs needing gradients
brown ... outputs

convolutional layer overview



OUTPUT CALCULATION:

$$\text{np.sum}\left(\begin{bmatrix} 2 & 0 & 0 \\ 2 & 1 & 0 \\ 2 & 2 & 0 \end{bmatrix} * \begin{bmatrix} -1 & 1 & 1 \\ 0 & 0 & 0 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 0 & 2 & 0 \\ 2 & 2 & 0 \\ 0 & 1 & 0 \end{bmatrix} * \begin{bmatrix} -1 & 1 & 0 \\ 0 & 0 & 0 \\ -1 & 0 & -1 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 2 & 0 & 0 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ -1 & 1 & -1 \end{bmatrix}\right) + 0 = -1$$