CSCI 320 – Matrix Multiplication

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Objective

The objective of this lab is to demonstrate 3x3 matrix multiplication in CISC and RISC

Equipment Used

EASy 68K simulator

RISC-V Venus Extension https://marketplace.visualstudio.com/items?itemName=hm.riscv-venus

Gnu assembler: gcc-riscv64-linux-gn - install with: sudo apt install gcc-riscv64-linux-gn

Visual Studio Code

Procedure

First I came up with the equations for each element of the product of two 3x3 matrices, A and B. The equations were as follows:

Row 0:

$$AB[0,0] = (A0 * B0) + (A1 * B3) + (A2 * B6)$$

$$AB[0,1] = (A0 * B1) + (A1 * B4) + (A2 * B7)$$

$$AB[0,2] = (A0 * B2) + (A1 * B5) + (A2 * B8)$$

Row 1:

$$AB[1,0] = (A3 * B0) + (A4 * B3) + (A5 * B6)$$

$$AB[1,1] = (A3 * B1) + (A4 * B4) + (A5 * B7)$$

$$AB[1,2] = (A3 * B2) + (A4 * B5) + (A5 * B8)$$

Row 2:

$$AB[2,0] = (A6 * B0) + (A7 * B3) + (A8 * B6)$$

$$AB[2,1] = (A6 * B1) + (A7 * B4) + (A8 * B7)$$

$$AB[2,2] = (A6 * B2) + (A7 * B5) + (A8 * B8)$$

Such that for a matrix in the $K \in \mathbb{R}^n$ vector space, element [1,1] would be represented as K0, and [1,3] would be represented as K2.

Using these equations, I first loaded the memory addresses into the appropriate address registers, loaded the matrixes using addressing with offsets for each element. Then I evaluated each matrix index and loaded the index into the resultant matrix AB address, starting at 0x1040.

New Operations Learned

Representation of a matrix in \mathbb{R}^n as a flattened matrix, such that no columns exist, and at the end of a row, the next row begins as the previous row number plus 1.

The following RISC-V instructions/items

- 1. JAL
- 2. SB
- 3. LI
- 4. MUL
- 5. ADD
- 6. SW
- 7. The syntax of register access and memory offsets during register access

Program Description

The program first loads memory locations, offset by 0x20 bytes, for each flattened matrix.

Then the program branches to the populate the A and B 3x3 matrices. This is done precisely using the register indirect with offset addressing mode, and offsetting each element by increments of 0x1 each time.

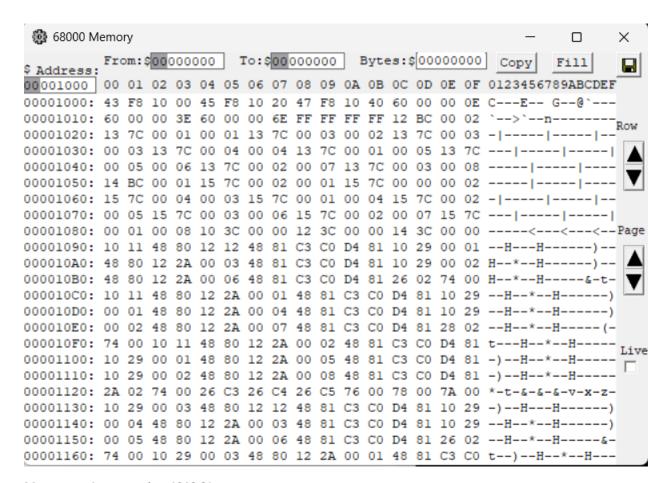
Finally, the AB resultant matrix is evaluated using the above formulas.

The same operations were done in the RISC-V implementation

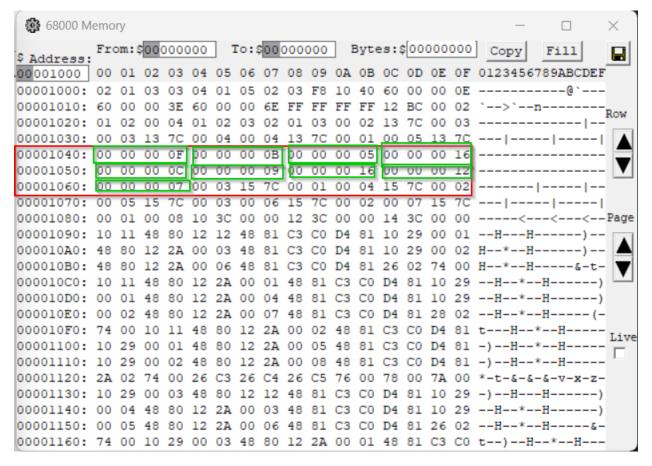
Conclusion

This was a phenomenal introduction to nxn matrix multiplication. The only item that I would have liked to have changed would have been to generalize the formula to be able to evaluate the product of two matrices A, B, such that $\{A,B \in \mathbb{R}^n \mid n \in Z+\}$

Memory before running (CISC)



Memory after running (CISC)



Code Listing (CISC)

SIMHALT

```
POPULATE A:
   ; [row 1]
   MOVE.B #$2, (A1)
   MOVE.B #$1, 1(A1)
   MOVE.B #$3, 2(A1)
   ; [row 2]
   MOVE.B #$3, 3(A1)
   MOVE.B #$4, 4(A1)
   MOVE.B #$1, 5(A1)
    ; [row 3]
   MOVE.B #$5, 6(A1)
   MOVE.B #$2, 7(A1)
   MOVE.B #$3, 8(A1)
POPULATE B:
    ; [row 1]
   MOVE.B #$1, (A2)
MOVE.B #$2, 1(A2)
   MOVE.B #$0, 2(A2)
   ; [row 2]
   MOVE.B #$4, 3(A2)
   MOVE.B #$1, 4(A2)
   MOVE.B #$2, 5(A2)
   ; [row 3]
   MOVE.B #$3, 6(A2)
   MOVE.B #$2, 7(A2)
   MOVE.B #$1, 8(A2)
CALCULATE A B PRODUCT:
    ;D0 working data register
    ;D1 working data register
    ;D2 working sum register
   MOVE.B #0, D0
   MOVE.B #0, D1
   MOVE.B #0, D2
   ;D3 AB(k,0) value
   ;D4 AB(k,1) value
   ;D5 AB(k,2) value
    ; Reset D3, D4, D5 after each row has been evaluated
```

; Compute AB[0,0] = [(A0B0) + (A1B3) + (A2B6)]

```
;Evaluate AOBO, Add to sum
                                        ;0[0,0]
;BEGIN BLOCK
   MOVE.B (A1), D0 ; -> move A0 to D0
   EXT.W D0 ; \rightarrow extend D0 from byte to word size
   MOVE.B (A2), D1 ; -> move B0 to D1
   EXT.W D1 ; -> extend D1 from byte to word size
   MULS.W D0, D1 ; \rightarrow multiply D0 by D1, store in D1. D1 should now be \rightarrow1
   ADD.L D1, D2 ; D2 now contains I0*K0
; END BLOCK
;NOTE - All subsequent Evalute Ii*Kj blocks are repititions of the above
block
   ;Evaluate A1B3, Add to sum
   MOVE.B 1(A1), D0
   EXT.W DO
   MOVE.B 3(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ;Evaluate A2B6, Add to sum
   MOVE.B 2(A1), D0
   EXT.W DO
   MOVE.B 6(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[0,0] into D3
   MOVE.L D2, D3
   ; Reset sum register
   MOVE.L #0, D2
   ______
   ; Compute AB[0,1] = [(A0B1) + (A1B4) + (A2B7)]
   ; Evaluate AOB1, Add to sum
   MOVE.B (A1), D0
   EXT.W DO
   MOVE.B 1(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A1B4, Add to sum
   MOVE.B 1(A1), D0
   EXT.W DO
   MOVE.B 4(A2), D1
```

```
EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A2B7, Add to sum
   MOVE.B 2(A1), D0
   EXT.W DO
   MOVE.B 7(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[0,1] into D4
   MOVE.L D2, D4
   ; Reset sum register
   MOVE.L #0, D2
   ;============ AB[0,2]
______
______
   ; Compute AB[0,1] = [(A0B2) + (A1B5) + (A2B8)]
   ; Evaluate AOB2, Add to sum
   MOVE.B (A1), D0
   EXT.W D0
   MOVE.B 2(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A1B5, Add to sum
   MOVE.B 1(A1), D0
   EXT.W DO
   MOVE.B 5(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A2B8, Add to sum
   MOVE.B 2(A1), D0
   EXT.W D0
   MOVE.B 8(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[0,2] into D5
   MOVE.L D2, D5
```

```
; Reset sum register
   MOVE.L #0, D2
   ;======= LOAD FIRST ROW INTO RESULTANT
MATRIX REGISTER
______
  MOVE.L D3, (A3) +
  MOVE.L D4, (A3) +
  MOVE.L D5, (A3) +
   ; Reset element registers
  MOVE.L #0, D3
  MOVE.L #0, D4
   MOVE.L #0, D5
   ;========= AB[1,0]
______
_____
   ; Compute AB[1,0] = [(A3B0) + (A4B3) + (A5B6)]
   ; Evaluate A3B0, Add to sum
   MOVE.B 3(A1), D0
   EXT.W D0
  MOVE.B (A2), D1
  EXT.W D1
  MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A4B3, Add to sum
   MOVE.B 4(A1), D0
   EXT.W D0
  MOVE.B 3(A2), D1
   EXT.W D1
  MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A5B6, Add to sum
   MOVE.B 5(A1), D0
   EXT.W D0
   MOVE.B 6(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[0,0] into D3
   MOVE.L D2, D3
   ; Reset sum register
   MOVE.L #0, D2
```

```
;======== AB[1,1]
______
   ; Compute AB[1,1] = [(A3B1) + (A4B4) + (A5B7)]
   ; Evaluate A3B1, Add to sum
  MOVE.B 3(A1), D0
   EXT.W D0
   MOVE.B 1(A2), D1
   EXT.W D1
  MULS.W DO, D1
  ADD.L D1, D2
   ; Evaluate A4B4, Add to sum
   MOVE.B 4(A1), D0
   EXT.W D0
  MOVE.B 4(A2), D1
   EXT.W D1
  MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A5B7, Add to sum
   MOVE.B 5(A1), D0
   EXT.W D0
  MOVE.B 7(A2), D1
  EXT.W D1
  MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[1,1] into D4
   MOVE.L D2, D4
   ; Reset sum register
   MOVE.L #0, D2
;======== AB[1,2]
______
_____
   ; Compute AB[1,2] = [(A3B2) + (A4B5) + (A5B8)]
   ;Evaluate A3B2, Add to sum
   MOVE.B 3(A1), D0
   EXT.W D0
  MOVE.B 2(A2), D1
   EXT.W D1
  MULS.W DO, D1
  ADD.L D1, D2
   ; Evaluate A4B5, Add to sum
   MOVE.B 4(A1), D0
   EXT.W D0
```

```
EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A5B8, Add to sum
   MOVE.B 5(A1), D0
   EXT.W D0
   MOVE.B 8(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[1,2] into D5
   MOVE.L D2, D5
   ; Reset sum register
   MOVE.L #0, D2
;========================== LOAD SECOND ROW INTO RESULTANT MATRIX
REGISTER
=========
   MOVE.L D3, (A3) +
   MOVE.L D4, (A3) +
   MOVE.L D5, (A3) +
   ;Reset element registers
   MOVE.L #0, D3
   MOVE.L #0, D4
   MOVE.L #0, D5
;========= AB[2,0]
______
______
   ; Compute AB[2,0] = [(A6B0) + (A7B3) + (A8B6)]
   ; Evaluate A6B0, Add to sum
   MOVE.B 6(A1), D0
   EXT.W D0
   MOVE.B 0(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A7B3, Add to sum
   MOVE.B 7(A1), D0
   EXT.W D0
   MOVE.B 3(A2), D1
   EXT.W D1
   MULS.W DO, D1
```

MOVE.B 5(A2), D1

```
ADD.L D1, D2
   ; Evaluate A8B6, Add to sum
   MOVE.B 8(A1), D0
   EXT.W D0
   MOVE.B 6(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[2,0] into D3
   MOVE.L D2, D3
   ; Reset sum register
   MOVE.L #0, D2
______
_____
   ; Compute AB[2,1] = [(A6B1) + (A7B4) + (A8B7)]
   ; Evaluate A6B1, Add to sum
   MOVE.B 6(A1), D0
   EXT.W D0
   MOVE.B 1(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A7B4, Add to sum
   MOVE.B 7(A1), D0
   EXT.W D0
   MOVE.B 4(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A8B7, Add to sum
   MOVE.B 8(A1), D0
   EXT.W D0
   MOVE.B 7(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place OB[2,1] into D4
   MOVE.L D2, D4
   ; Reset sum register
   MOVE.L #0, D2
```

```
;========= AB[2,2]
______
_____
   ; Compute AB[2,2] = [(A6B2) + (A7B5) + (A8B8)]
   ; Evaluate A6B2, Add to sum
   MOVE.B 6(A1), D0
   EXT.W D0
   MOVE.B 2(A2), D1
   EXT.W D1
  MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A7B5, Add to sum
   MOVE.B 7(A1), D0
   EXT.W D0
   MOVE.B 5(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Evaluate A8B8, Add to sum
   MOVE.B 8(A1), D0
   EXT.W D0
   MOVE.B 8(A2), D1
   EXT.W D1
   MULS.W DO, D1
   ADD.L D1, D2
   ; Finally, place AB[2,2] into D5
   MOVE.L D2, D5
   ; Reset sum register
   MOVE.L #0, D2
;=============================== LOAD THIRD ROW INTO RESULTANT MATRIX
_____
  MOVE.L D3, (A3) +
   MOVE.L D4, (A3) +
   MOVE.L D5, (A3) +
   END START
```

```
# CSCI 320 Computer Architecture 2
# 3x3 Matrix Multiplication RISC V implementation
# Kevin Gutierrez
# 4/1/25
.text
boot:
   # Load addresses for matrices
   li x2, 0x1020
li x3, 0x1040
                     # x2 -> Matrix B (Base Address)
# x3 -> Matrix Result (Base Address)
   # Branch to POPULATE Matrix A
   jal x0, POPULATE A
   # Branch to POPULATE Matrix B
   jal x0, POPULATE B
   # Branch to CALCULATE A * B Product
   jal x0, CALCULATE A B PRODUCT
   # End execution
POPULATE A:
   # Matrix A [row 1]
   li t0, 2
   sb t0, 0(x1) # A[0][0]
   li t0, 1
   sb t0, 1(x1)
                       # A[0][1]
   li t0, 3
   sb t0, 2(x1) # A[0][2]
   # Matrix A [row 2]
   li t0, 3
   sb t0, 3(x1)
                  # A[1][0]
   li t0, 4
   sb t0, 4(x1) # A[1][1]
   li t0, 1
   sb t0, 5(x1) # A[1][2]
   # Matrix A [row 3]
   li t0, 5
   sb t0, 6(x1) # A[2][0]
   li t0, 2
   sb t0, 7(x1)
                      # A[2][1]
   li t0, 3
   sb t0, 8(x1) # A[2][2]
```

```
POPULATE B:
    # Matrix B [row 1]
   li t0, 1
   sb t0, 0(x2)
                  # B[0][0]
   li t0, 2
   sb t0, 1(x2)
                   # B[0][1]
   li t0, 0
   sb t0, 2(x2) # B[0][2]
   # Matrix B [row 2]
   li t0, 4
   sb t0, 3(x2) # B[1][0]
   li t0, 1
   sb t0, 4(x2) # B[1][1]
   li t0, 2
   sb t0, 5(x2)
                 # B[1][2]
   # Matrix B [row 3]
   li t0, 3
   sb t0, 6(x2)
                       # B[2][0]
   li t0, 2
                   # B[2][1]
   sb t0, 7(x2)
   li t0, 1
   sb t0, 8(x2) # B[2][2]
CALCULATE A B PRODUCT:
    # Registers: t0, t1, t2 for working; t3, t4, t5 for results
   # Compute AB[0][0], AB[0][1], AB[0][2] (Row 0)
   li t2, 0
                       # Reset sum register
   1b t0, 0(x1)
                       # Load A00
                       # Load B00
   1b t1, 0(x2)
                       # A00 * B00
   mul t0, t0, t1
                      # Sum += A00 * B00
   add t2, t2, t0
   1b t0, 1(x1)
   1b t1, 3(x2)
   mul t0, t0, t1
   add t2, t2, t0
   1b t0, 2(x1)
   1b t1, 6(x2)
   mul t0, t0, t1
   add t2, t2, t0
   sw t2, 0(x3)
                      # Store AB[0][0]
                      # Reset sum register
# Load A00
   li t2, 0
   1b t0, 0(x1)
   lb t1, 1(x2)
                       # Load B01
   mul t0, t0, t1
                       # A00 * B01
   add t2, t2, t0
   lb t0, 1(x1)
   lb t1, 4(x2)
```

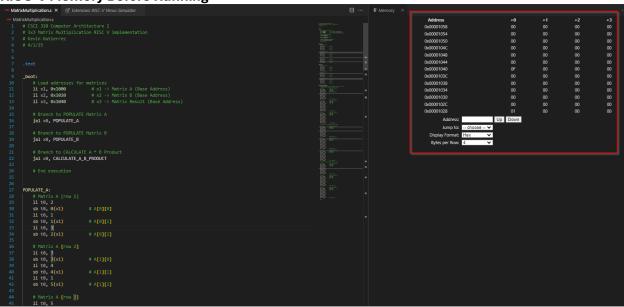
```
mul t0, t0, t1
add t2, t2, t0
1b t0, 2(x1)
1b t1, 7(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 4(x3)
                     # Store AB[0][1]
li t2, 0
                      # Reset sum register
1b t0, 0(x1)
                      # Load A00
lb t1, 2(x2)
                      # Load B02
mul t0, t0, t1
                      # A00 * B02
add t2, t2, t0
1b t0, 1(x1)
1b t1, 5(x2)
mul t0, t0, t1
add t2, t2, t0
1b t0, 2(x1)
1b t1, 8(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 8(x3)
                      # Store AB[0][2]
# Compute AB[1][0], AB[1][1], AB[1][2] (Row 1)
li t2, 0
                      # Reset sum register
1b t0, 3(x1)
                      # Load A10
1b t1, 0(x2)
                      # Load B00
                      # A10 * B00
mul t0, t0, t1
add t2, t2, t0
lb t0, 4(x1)
1b t1, 3(x2)
mul t0, t0, t1
add t2, t2, t0
1b t0, 5(x1)
lb t1, 6(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 12(x3)
                     # Store AB[1][0]
li t2, 0
                      # Reset sum register
1b t0, 3(x1)
                      # Load A10
lb t1, 1(x2)
                      # Load B01
mul t0, t0, t1
                      # A10 * B01
add t2, t2, t0
lb t0, 4(x1)
lb t1, 4(x2)
mul t0, t0, t1
add t2, t2, t0
1b t0, 5(x1)
lb t1, 7(x2)
mul t0, t0, t1
```

```
add t2, t2, t0
sw t2, 16(x3)
                   # Store AB[1][1]
li t2, 0
                     # Reset sum register
1b t0, 3(x1)
                     # Load A10
                     # Load B02
1b t1, 2(x2)
                     # A10 * B02
mul t0, t0, t1
add t2, t2, t0
1b t0, 4(x1)
1b t1, 5(x2)
mul t0, t0, t1
add t2, t2, t0
1b t0, 5(x1)
1b t1, 8(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 20(x3)
              # Store AB[1][2]
# Compute AB[2][0], AB[2][1], AB[2][2] (Row 2)
li t2, 0
                      # Reset sum register
                     # Load A20
lb t0, 6(x1)
1b t1, 0(x2)
                     # Load B00
mul t0, t0, t1
                     # A20 * B00
add t2, t2, t0
1b t0, 7(x1)
1b t1, 3(x2)
mul t0, t0, t1
add t2, t2, t0
1b t0, 8(x1)
lb t1, 6(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 24(x3)
                   # Store AB[2][0]
li t2, 0
                     # Reset sum register
1b t0, 6(x1)
                     # Load A20
lb t1, 1(x2)
                     # Load B01
                     # A20 * B01
mul t0, t0, t1
add t2, t2, t0
1b t0, 7(x1)
1b t1, 4(x2)
mul t0, t0, t1
add t2, t2, t0
1b t0, 8(x1)
1b t1, 7(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 28(x3)
                     # Store AB[2][1]
li t2, 0
                     # Reset sum register
                   # Load A20
1b t0, 6(x1)
```

```
lb t1, 2(x2)  # Load B02
mul t0, t0, t1  # A20 * B02
add t2, t2, t0
lb t0, 7(x1)
lb t1, 5(x2)
mul t0, t0, t1
add t2, t2, t0
lb t0, 8(x1)
lb t1, 8(x2)
mul t0, t0, t1
add t2, t2, t0
sw t2, 32(x3)  # Store AB[2][2]
```

ret

RISC-V Memory Before Running



RISC-V Memory After Running

