CSCI 320 – Matrix Multiplication

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**Objective**

The objective of this lab is to demonstrate 3x3 matrix multiplication in CISC and RISC

**Equipment Used**

EASy 68K simulator

RISC-V Assembler <https://venus.kvakil.me/>

**Procedure**

First I came up with the equations for each element of the product of two 3x3 matrices, A and B. The equations were as follows:

Row 0:

AB[0,0] = (A0 \* B0) + (A1 \* B3) + (A2 \* B6)

AB[0,1] = (A0 \* B1) + (A1 \* B4) + (A2 \* B7)

AB[0,2] = (A0 \* B2) + (A1 \* B5) + (A2 \* B8)

Row 1:

AB[1,0] = (A3 \* B0) + (A4 \* B3) + (A5 \* B6)

AB[1,1] = (A3 \* B1) + (A4 \* B4) + (A5 \* B7)

AB[1,2] = (A3 \* B2) + (A4 \* B5) + (A5 \* B8)

Row 2:

AB[2,0] = (A6 \* B0) + (A7 \* B3) + (A8 \* B6)

AB[2,1] = (A6 \* B1) + (A7 \* B4) + (A8 \* B7)

AB[2,2] = (A6 \* B2) + (A7 \* B5) + (A8 \* B8)

Such that for a matrix in the K ∈ ℝn vector space, element [1,1] would be represented as K0, and [1,3] would be represented as K2.

Using these equations, I first loaded the memory addresses into the appropriate address registers, loaded the matrixes using addressing with offsets for each element. Then I evaluated each matrix index and loaded the index into the resultant matrix AB address, starting at 0x1040.

**New Operations Learned**

Representation of a matrix in ℝn as a flattened matrix, such that no columns exist, and at the end of a row, the next row begins as the previous row number plus 1.

The following RISC-V instructions/items

1. JAL
2. SB
3. LI
4. MUL
5. ADD
6. SW
7. The syntax of register access and memory offsets during register access

**Program Description**

The program first loads memory locations, offset by 0x20 bytes, for each flattened matrix.

Then the program branches to the populate the A and B 3x3 matrices. This is done precisely using the register indirect with offset addressing mode, and offsetting each element by increments of 0x1 each time.

Finally, the AB resultant matrix is evaluated using the above formulas.

The same operations were done in the RISC-V implementation

**Conclusion**

This was a phenomenal introduction to nxn matrix multiplication. The only item that I would have liked to have changed would have been to generalize the formula to be able to evaluate the product of two matrices A, B, such that {A,B ∈ ℝn | n ∈ Z+ }

**Memory before running (CISC)**

**A screenshot of a computer

AI-generated content may be incorrect.**

**Memory after running (CISC)**

**A screenshot of a computer

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**Code Listing (CISC)**

\*-----------------------------------------------------------

\* Title : 3x3 Matrix Multiplication

\* Written by : Kevin Gutierrez

\* Date : 3/31/25

\* Description: 3x3 matrix multiplication program

\*-----------------------------------------------------------

ORG $1000

START:

;A1 -> Matrix A

LEA.L $00001000, A1

;A2 -> Matrix B

LEA.L $00001020, A2

;A3 -> A \* B result

LEA.L $00001040, A3

BRA POPULATE\_A

BRA POPULATE\_B

BRA CALCULATE\_A\_B\_PRODUCT

SIMHALT

POPULATE\_A:

; [row 1]

MOVE.B #$2, (A1)

MOVE.B #$1, 1(A1)

MOVE.B #$3, 2(A1)

; [row 2]

MOVE.B #$3, 3(A1)

MOVE.B #$4, 4(A1)

MOVE.B #$1, 5(A1)

; [row 3]

MOVE.B #$5, 6(A1)

MOVE.B #$2, 7(A1)

MOVE.B #$3, 8(A1)

POPULATE\_B:

; [row 1]

MOVE.B #$1, (A2)

MOVE.B #$2, 1(A2)

MOVE.B #$0, 2(A2)

; [row 2]

MOVE.B #$4, 3(A2)

MOVE.B #$1, 4(A2)

MOVE.B #$2, 5(A2)

; [row 3]

MOVE.B #$3, 6(A2)

MOVE.B #$2, 7(A2)

MOVE.B #$1, 8(A2)

CALCULATE\_A\_B\_PRODUCT:

;D0 working data register

;D1 working data register

;D2 working sum register

MOVE.B #0, D0

MOVE.B #0, D1

MOVE.B #0, D2

;D3 AB(k,0) value

;D4 AB(k,1) value

;D5 AB(k,2) value

;Reset D3,D4,D5 after each row has been evaluated

;==================================== AB[0,0] ==============================================================================================================================

; Compute AB[0,0] = [(A0B0)+(A1B3)+(A2B6)]

;Evaluate A0B0, Add to sum ;BEGIN BLOCK ;O[0,0]

MOVE.B (A1), D0 ; -> move A0 to D0

EXT.W D0 ; -> extend D0 from byte to word size

MOVE.B (A2), D1 ; -> move B0 to D1

EXT.W D1 ; -> extend D1 from byte to word size

MULS.W D0, D1 ; -> multiply D0 by D1, store in D1. D1 should now be -1

ADD.L D1, D2 ; D2 now contains I0\*K0 ;END BLOCK

;NOTE - All subsequent Evalute Ii\*Kj blocks are repititions of the above block

;Evaluate A1B3, Add to sum

MOVE.B 1(A1), D0

EXT.W D0

MOVE.B 3(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A2B6, Add to sum

MOVE.B 2(A1), D0

EXT.W D0

MOVE.B 6(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[0,0] into D3

MOVE.L D2, D3

; Reset sum register

MOVE.L #0, D2

;==================================== AB[0,1] ==============================================================================================================================

; Compute AB[0,1] = [(A0B1)+(A1B4)+(A2B7)]

;Evaluate A0B1, Add to sum

MOVE.B (A1), D0

EXT.W D0

MOVE.B 1(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A1B4, Add to sum

MOVE.B 1(A1), D0

EXT.W D0

MOVE.B 4(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A2B7, Add to sum

MOVE.B 2(A1), D0

EXT.W D0

MOVE.B 7(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[0,1] into D4

MOVE.L D2, D4

; Reset sum register

MOVE.L #0, D2

;==================================== AB[0,2] ==============================================================================================================================

; Compute AB[0,1] = [(A0B2)+(A1B5)+(A2B8)]

;Evaluate A0B2, Add to sum

MOVE.B (A1), D0

EXT.W D0

MOVE.B 2(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A1B5, Add to sum

MOVE.B 1(A1), D0

EXT.W D0

MOVE.B 5(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A2B8, Add to sum

MOVE.B 2(A1), D0

EXT.W D0

MOVE.B 8(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[0,2] into D5

MOVE.L D2, D5

; Reset sum register

MOVE.L #0, D2

;==================================== LOAD FIRST ROW INTO RESULTANT MATRIX REGISTER ========================================================================================

MOVE.L D3, (A3)+

MOVE.L D4, (A3)+

MOVE.L D5, (A3)+

;Reset element registers

MOVE.L #0, D3

MOVE.L #0, D4

MOVE.L #0, D5

;==================================== AB[1,0] ==============================================================================================================================

; Compute AB[1,0] = [(A3B0)+(A4B3)+(A5B6)]

;Evaluate A3B0, Add to sum

MOVE.B 3(A1), D0

EXT.W D0

MOVE.B (A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A4B3, Add to sum

MOVE.B 4(A1), D0

EXT.W D0

MOVE.B 3(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A5B6, Add to sum

MOVE.B 5(A1), D0

EXT.W D0

MOVE.B 6(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[0,0] into D3

MOVE.L D2, D3

; Reset sum register

MOVE.L #0, D2

;==================================== AB[1,1] ==============================================================================================================================

; Compute AB[1,1] = [(A3B1)+(A4B4)+(A5B7)]

;Evaluate A3B1, Add to sum

MOVE.B 3(A1), D0

EXT.W D0

MOVE.B 1(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A4B4, Add to sum

MOVE.B 4(A1), D0

EXT.W D0

MOVE.B 4(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A5B7, Add to sum

MOVE.B 5(A1), D0

EXT.W D0

MOVE.B 7(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[1,1] into D4

MOVE.L D2, D4

; Reset sum register

MOVE.L #0, D2

;==================================== AB[1,2] ==============================================================================================================================

; Compute AB[1,2] = [(A3B2)+(A4B5)+(A5B8)]

;Evaluate A3B2, Add to sum

MOVE.B 3(A1), D0

EXT.W D0

MOVE.B 2(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A4B5, Add to sum

MOVE.B 4(A1), D0

EXT.W D0

MOVE.B 5(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A5B8, Add to sum

MOVE.B 5(A1), D0

EXT.W D0

MOVE.B 8(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[1,2] into D5

MOVE.L D2, D5

; Reset sum register

MOVE.L #0, D2

;==================================== LOAD SECOND ROW INTO RESULTANT MATRIX REGISTER ========================================================================================

MOVE.L D3, (A3)+

MOVE.L D4, (A3)+

MOVE.L D5, (A3)+

;Reset element registers

MOVE.L #0, D3

MOVE.L #0, D4

MOVE.L #0, D5

;==================================== AB[2,0] ==============================================================================================================================

; Compute AB[2,0] = [(A6B0)+(A7B3)+(A8B6)]

;Evaluate A6B0, Add to sum

MOVE.B 6(A1), D0

EXT.W D0

MOVE.B 0(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A7B3, Add to sum

MOVE.B 7(A1), D0

EXT.W D0

MOVE.B 3(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A8B6, Add to sum

MOVE.B 8(A1), D0

EXT.W D0

MOVE.B 6(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[2,0] into D3

MOVE.L D2, D3

; Reset sum register

MOVE.L #0, D2

;==================================== AB[2,1] ==============================================================================================================================

; Compute AB[2,1] = [(A6B1)+(A7B4)+(A8B7)]

;Evaluate A6B1, Add to sum

MOVE.B 6(A1), D0

EXT.W D0

MOVE.B 1(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A7B4, Add to sum

MOVE.B 7(A1), D0

EXT.W D0

MOVE.B 4(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A8B7, Add to sum

MOVE.B 8(A1), D0

EXT.W D0

MOVE.B 7(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place OB[2,1] into D4

MOVE.L D2, D4

; Reset sum register

MOVE.L #0, D2

;==================================== AB[2,2] ==============================================================================================================================

; Compute AB[2,2] = [(A6B2)+(A7B5)+(A8B8)]

;Evaluate A6B2, Add to sum

MOVE.B 6(A1), D0

EXT.W D0

MOVE.B 2(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A7B5, Add to sum

MOVE.B 7(A1), D0

EXT.W D0

MOVE.B 5(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Evaluate A8B8, Add to sum

MOVE.B 8(A1), D0

EXT.W D0

MOVE.B 8(A2), D1

EXT.W D1

MULS.W D0, D1

ADD.L D1, D2

;Finally, place AB[2,2] into D5

MOVE.L D2, D5

; Reset sum register

MOVE.L #0, D2

;==================================== LOAD THIRD ROW INTO RESULTANT MATRIX REGISTER ========================================================================================

MOVE.L D3, (A3)+

MOVE.L D4, (A3)+

MOVE.L D5, (A3)+

END START

**Code Listing - RISC Implementation**

.text

\_boot:

# Load addresses for matrices

li x1, 0x1000 # x1 -> Matrix A (Base Address)

li x2, 0x1020 # x2 -> Matrix B (Base Address)

li x3, 0x1040 # x3 -> Matrix Result (Base Address)

# Branch to POPULATE Matrix A

jal x0, POPULATE\_A

# Branch to POPULATE Matrix B

jal x0, POPULATE\_B

# Branch to Calculite A \* B Product

jal x0, CALCUliTE\_A\_B\_PRODUCT

# End execution

POPULATE\_A:

# Matrix A [row 1]

li t0, 2

sb t0, 0(x1) # A[0][0]

li t0, 1

sb t0, 1(x1) # A[0][1]

li t0, 3

sb t0, 2(x1) # A[0][2]

# Matrix A [row 2]

li t0, 3

sb t0, 3(x1) # A[1][0]

li t0, 4

sb t0, 4(x1) # A[1][1]

li t0, 1

sb t0, 5(x1) # A[1][2]

# Matrix A [row 3]

li t0, 5

sb t0, 6(x1) # A[2][0]

li t0, 2

sb t0, 7(x1) # A[2][1]

li t0, 3

sb t0, 8(x1) # A[2][2]

POPULATE\_B:

# Matrix B [row 1]

li t0, 1

sb t0, 0(x2) # B[0][0]

li t0, 2

sb t0, 1(x2) # B[0][1]

li t0, 0

sb t0, 2(x2) # B[0][2]

# Matrix B [row 2]

li t0, 4

sb t0, 3(x2) # B[1][0]

li t0, 1

sb t0, 4(x2) # B[1][1]

li t0, 2

sb t0, 5(x2) # B[1][2]

# Matrix B [row 3]

li t0, 3

sb t0, 6(x2) # B[2][0]

li t0, 2

sb t0, 7(x2) # B[2][1]

li t0, 1

sb t0, 8(x2) # B[2][2]

CALCUliTE\_A\_B\_PRODUCT:

# Registers: t0, t1, t2 for working; t3, t4, t5 for results

# Compute AB[0][0], AB[0][1], AB[0][2] (Row 0)

li t2, 0 # Reset sum register

lb t0, 0(x1) # Load A00

lb t1, 0(x2) # Load B00

mul t0, t0, t1 # A00 \* B00

add t2, t2, t0 # Sum += A00 \* B00

lb t0, 1(x1)

lb t1, 3(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 2(x1)

lb t1, 6(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 0(x3) # Store AB[0][0]

li t2, 0 # Reset sum register

lb t0, 0(x1) # Load A00

lb t1, 1(x2) # Load B01

mul t0, t0, t1 # A00 \* B01

add t2, t2, t0

lb t0, 1(x1)

lb t1, 4(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 2(x1)

lb t1, 7(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 4(x3) # Store AB[0][1]

li t2, 0 # Reset sum register

lb t0, 0(x1) # Load A00

lb t1, 2(x2) # Load B02

mul t0, t0, t1 # A00 \* B02

add t2, t2, t0

lb t0, 1(x1)

lb t1, 5(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 2(x1)

lb t1, 8(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 8(x3) # Store AB[0][2]

# Compute AB[1][0], AB[1][1], AB[1][2] (Row 1)

li t2, 0 # Reset sum register

lb t0, 3(x1) # Load A10

lb t1, 0(x2) # Load B00

mul t0, t0, t1 # A10 \* B00

add t2, t2, t0

lb t0, 4(x1)

lb t1, 3(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 5(x1)

lb t1, 6(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 12(x3) # Store AB[1][0]

li t2, 0 # Reset sum register

lb t0, 3(x1) # Load A10

lb t1, 1(x2) # Load B01

mul t0, t0, t1 # A10 \* B01

add t2, t2, t0

lb t0, 4(x1)

lb t1, 4(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 5(x1)

lb t1, 7(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 16(x3) # Store AB[1][1]

li t2, 0 # Reset sum register

lb t0, 3(x1) # Load A10

lb t1, 2(x2) # Load B02

mul t0, t0, t1 # A10 \* B02

add t2, t2, t0

lb t0, 4(x1)

lb t1, 5(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 5(x1)

lb t1, 8(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 20(x3) # Store AB[1][2]

# Compute AB[2][0], AB[2][1], AB[2][2] (Row 2)

li t2, 0 # Reset sum register

lb t0, 6(x1) # Load A20

lb t1, 0(x2) # Load B00

mul t0, t0, t1 # A20 \* B00

add t2, t2, t0

lb t0, 7(x1)

lb t1, 3(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 8(x1)

lb t1, 6(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 24(x3) # Store AB[2][0]

li t2, 0 # Reset sum register

lb t0, 6(x1) # Load A20

lb t1, 1(x2) # Load B01

mul t0, t0, t1 # A20 \* B01

add t2, t2, t0

lb t0, 7(x1)

lb t1, 4(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 8(x1)

lb t1, 7(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 28(x3) # Store AB[2][1]

li t2, 0 # Reset sum register

lb t0, 6(x1) # Load A20

lb t1, 2(x2) # Load B02

mul t0, t0, t1 # A20 \* B02

add t2, t2, t0

lb t0, 7(x1)

lb t1, 5(x2)

mul t0, t0, t1

add t2, t2, t0

lb t0, 8(x1)

lb t1, 8(x2)

mul t0, t0, t1

add t2, t2, t0

sw t2, 32(x3) # Store AB[2][2]

ret

**RISC-V Simulator Output**

A screenshot of a computer

AI-generated content may be incorrect.

A screenshot of a math form

AI-generated content may be incorrect.