



**ELECTRICAL & COMPUTER  
ENGINEERING**  
TEXAS A&M UNIVERSITY

# Pre-Lab 5: Operational Amplifiers

## Part 3

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ECEN 325 -501

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# Pre-Lab

## Calculations:

### Lossy Integrator

1. For the lossy integrator in Fig. 2, derive the time-domain equation for the output in terms of the input.

$$V_o = - \left( \frac{\frac{R_2}{R_1}}{1 + sR_2C} \right) V_i$$

$$V_o(t) = V_i(t) \frac{R_1}{R_1 + R_2} e^{\frac{-t}{\tau}} ; \tau = \frac{R_1 R_2 C}{R_1 + R_2}$$

$$V_o(t) = V_i(t) \frac{R_1}{R_1 + R_2} e^{\frac{-t(R_1 + R_2)}{(R_1 R_2 C)}}$$

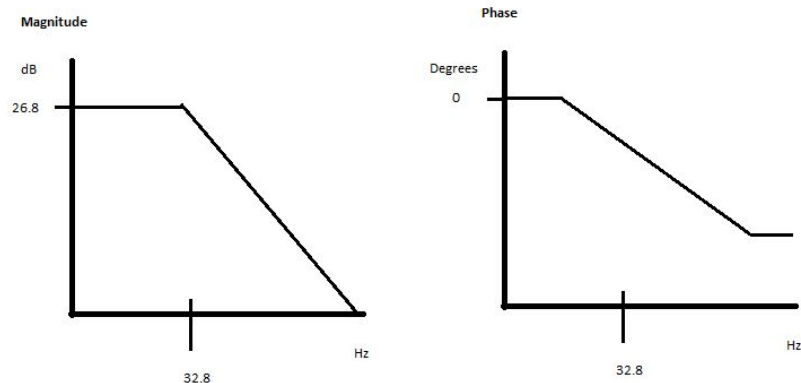
2. Find R1 to have a low-frequency gain of -22 if R2 = 22kΩ and C = 220nF, and calculate the 3-dB frequency

$$V_o = \frac{-R_2}{R_1} \frac{1}{1 + sR_2C} V_i \Rightarrow \frac{V_o}{V_i} = \frac{-R_2}{R_1} \frac{1}{1 + sR_2C}$$

$$\text{Low } f \text{ frequency gain: } -\frac{R_2}{R_1} = -22 = \frac{-22k}{R_1} \Rightarrow R_1 = 1k\Omega$$

$$3dB - f \text{ frequency: } \frac{1}{2\pi R_f C} = \frac{1}{2\pi \cdot 22k \cdot 220n} = 32.88Hz$$

3. Sketch the magnitude and phase Bode plots for the transfer function  $V_o / V_i$ .  $20 \log(22) = 26.8$



dB

4. Calculate  $V_o(t)$  for  $V_i(t) = 0.5 \sin(2\pi 1000t)$ .

$$32.88 \text{ Hz} = 206.6 \text{ rad/s}$$

$$\frac{V_o}{V_i} = - \left( \frac{\frac{R_2}{R_2}}{1 + sR_2C} \right) = - \left( \frac{\frac{22k}{1k}}{1 + s(22k)(220nF)} \right) = \frac{-22}{1 + 4.84 \cdot 10^{-3}s}$$

$$H(w) = \frac{-4545.45}{jw + 206.6} ; w = 2\pi 1000$$

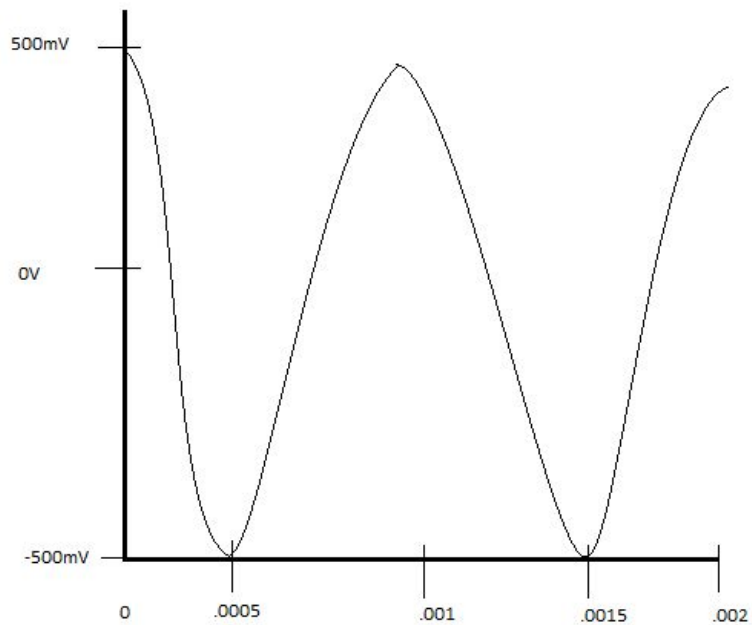
$$\frac{V_o}{V_i} = -0.024 + j0.723 = 0.73 \angle 91.88^\circ, V_i = 0.5 \sin(2\pi 1000t) = 0.5 \angle 0^\circ$$

$$V_o = 0.73 \angle 91.88^\circ (0.5 \angle 0^\circ) = 0.3615 \angle 91.88^\circ$$

$$V_o(t) = 0.3615 \sin(2\pi 1000t + 91.88^\circ) \text{ V}$$

5. Sketch the output waveform if the input is a 500mV 1kHz square wave signal.

Tried to make the sketch accurate but it is hard in paint.



## Pseudo Differentiator

- For the first order high-pass filter in Fig. 4, derive the time-domain equation for the output in terms of the input.

$$V_o(t) = \frac{R_2}{R_1 + R_2} V_i(t)$$

$$V_o(t) = V_i(t) \cdot \frac{R_2}{R_1 + R_2} e^{-\frac{t}{\tau}} ; \text{ As } t \rightarrow \infty, V_o = 0 \text{ and } \tau = (R_1 + R_2)C$$

$$V_o(t) = V_i(t) \cdot \frac{R_2}{R_1 + R_2} e^{-\frac{t}{(R_1 + R_2)C}}$$

- Find  $R_2$  to have a high-frequency gain of -22 if  $R_1 = 1k\Omega$  and  $C = 33nF$ , and calculate the 3-dB frequency.

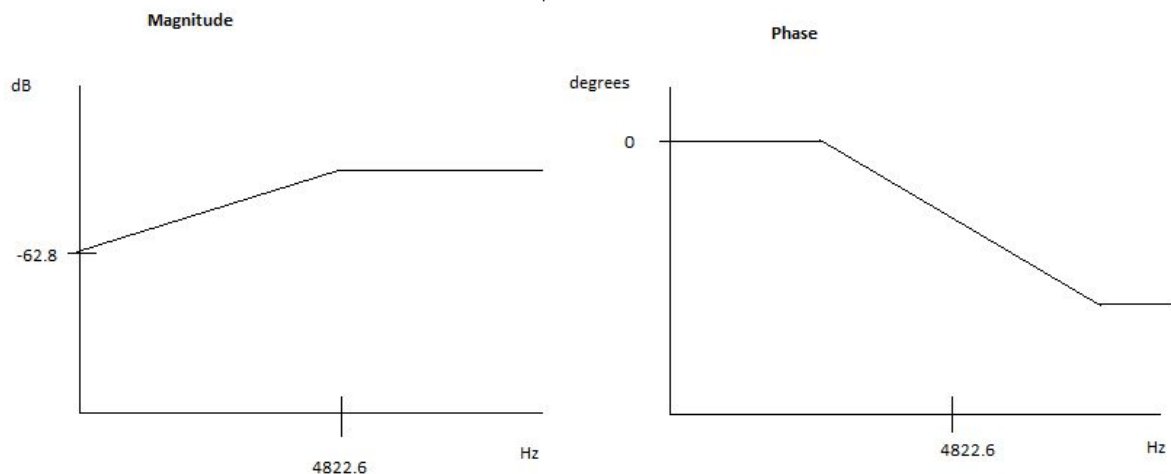
High frequency:

$$-22 = -\frac{R_2}{R_1} = -\frac{R_2}{1k} ; R_2 = 22k\Omega$$

3dB frequency:

$$\frac{1}{R_1 C} = \frac{1}{1k\Omega \cdot 33nF} = 30303 \text{ rad/s} = 4822.88 \text{ Hz}$$

- Sketch the magnitude and phase Bode plots for the transfer function  $V_o/V_i$ .



4. Calculate  $V_o(t)$  for  $V_i(t) = 0.1 \sin(2\pi 1000t)$ .

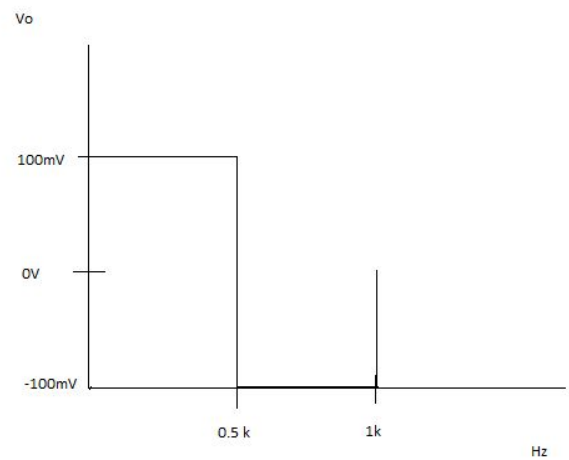
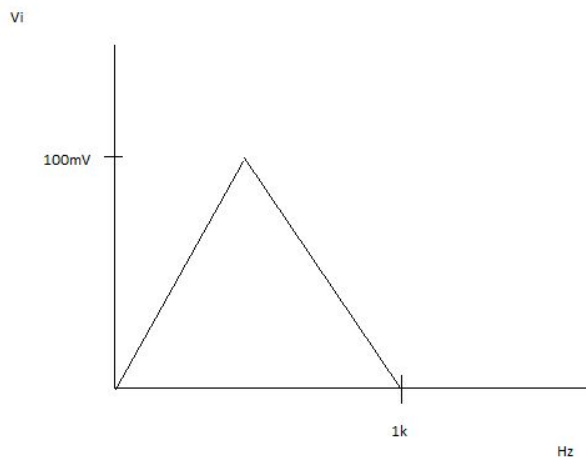
$$\frac{V_o}{V_i} = \frac{-sCR_2}{1 + sCR_1} = \frac{7.26 \cdot 10^{-4} \omega}{\sqrt{1 + (7.59 \cdot 10^{-4} \omega)^2}}$$

$$|H(j\omega)| = \frac{7.26 \cdot 10^{-4} (2\pi 1000)}{\sqrt{1 + (7.59 \cdot 10^{-4} (2\pi 1000))^2}} = 0.936$$

$$\angle H(j\omega) = 90^\circ - \tan^{-1}(7.59 \cdot 10^{-4} (2\pi 1000)) = 11.84^\circ$$

$$V_o(t) = 0.1 \angle 0^\circ (0.936 \angle 11.84^\circ) = 0.0936 \sin(2\pi 1000t + 11.84^\circ)$$

5. Sketch the output waveform if the input is a 100mV 1kHz triangular wave signal.



## Finite GBW Limitations

1. For the non-inverting amplifier in Fig. 5, assume  $R_1 = 1k\Omega$ . Find the values of  $R_2$  to set the low-frequency gain to 23, 57, and 83.

$$\frac{V_o}{V_i} = \frac{G_o}{1 + \frac{s}{w_o}}; G_o = 1 + \frac{R_2}{R_1}, w_o = \frac{w_t}{G_o}$$

$$\text{Gain} = 23$$

$$23 = 1 + \frac{R_2}{1k} \Rightarrow R_2 = 22k\Omega$$

$$\text{Gain} = 57$$

$$57 = 1 + \frac{R_2}{1k} \Rightarrow R_2 = 56k\Omega$$

$$\text{Gain} = 83$$

$$83 = 1 + \frac{R_2}{1k} \Rightarrow R_2 = 82k\Omega$$

2. Find the transfer function  $V_o/V_i(s)$  for each gain value.

$$\text{Gain} = 23$$

$$\frac{V_o}{V_i} = \frac{23}{1 + \frac{s}{\frac{w_t}{23}}} = \frac{w_t}{s + \frac{w_t}{23}}$$

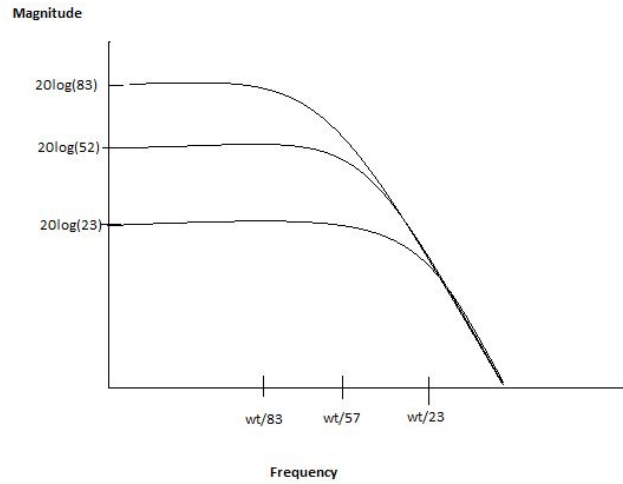
$$\text{Gain} = 57$$

$$\frac{V_o}{V_i} = \frac{w_t}{s + \frac{w_t}{57}}$$

$$\text{Gain} = 83$$

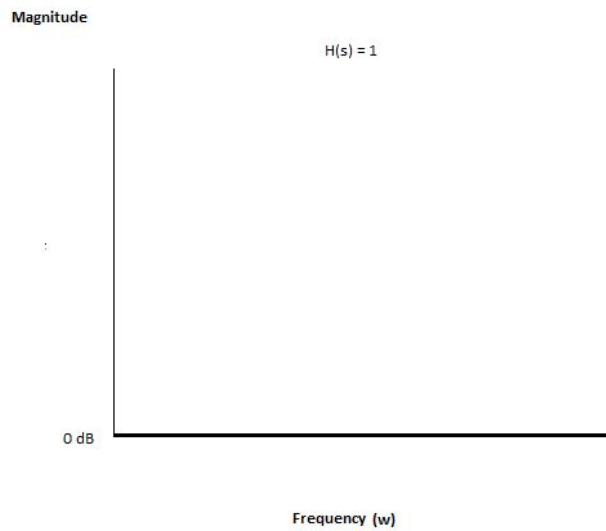
$$\frac{V_o}{V_i} = \frac{w_t}{s + \frac{w_t}{83}}$$

- Sketch the magnitude Bode plots of the three transfer functions on the same plot.



### Slew Rate Limitations

- For the unity-gain buffer in Fig. 6, find the transfer function  $V_o/V_i(s)$ , and sketch the magnitude Bode plot



2. If the slew rate of the opamp is  $0.5\text{V}/\mu\text{s}$ , find the maximum frequency of the  $1\text{V}$  sine wave input signal before the output is distorted

$$\text{slew rate} = 0.5\text{V}/\mu\text{s} = 0.5 \cdot 10^6 \text{ V/s}$$

$$v_i = 1 \sin(t)$$

$$v_o = v_i = 1 \sin(t) \quad \& \quad v_{o, \max} = \sqrt{2}$$

$$f_{\max} = \frac{0.5 \cdot 10^6}{2\pi \cdot \sqrt{2}} = 56269.8 \text{ Hz}$$

3. If the slew rate of the opamp is  $0.5\text{V}/\mu\text{s}$ , find the maximum amplitude of the  $75\text{kHz}$  sine wave input signal before the output is distorted.

$$\text{slew rate} = 0.5 \cdot 10^6 \text{ V/s}$$

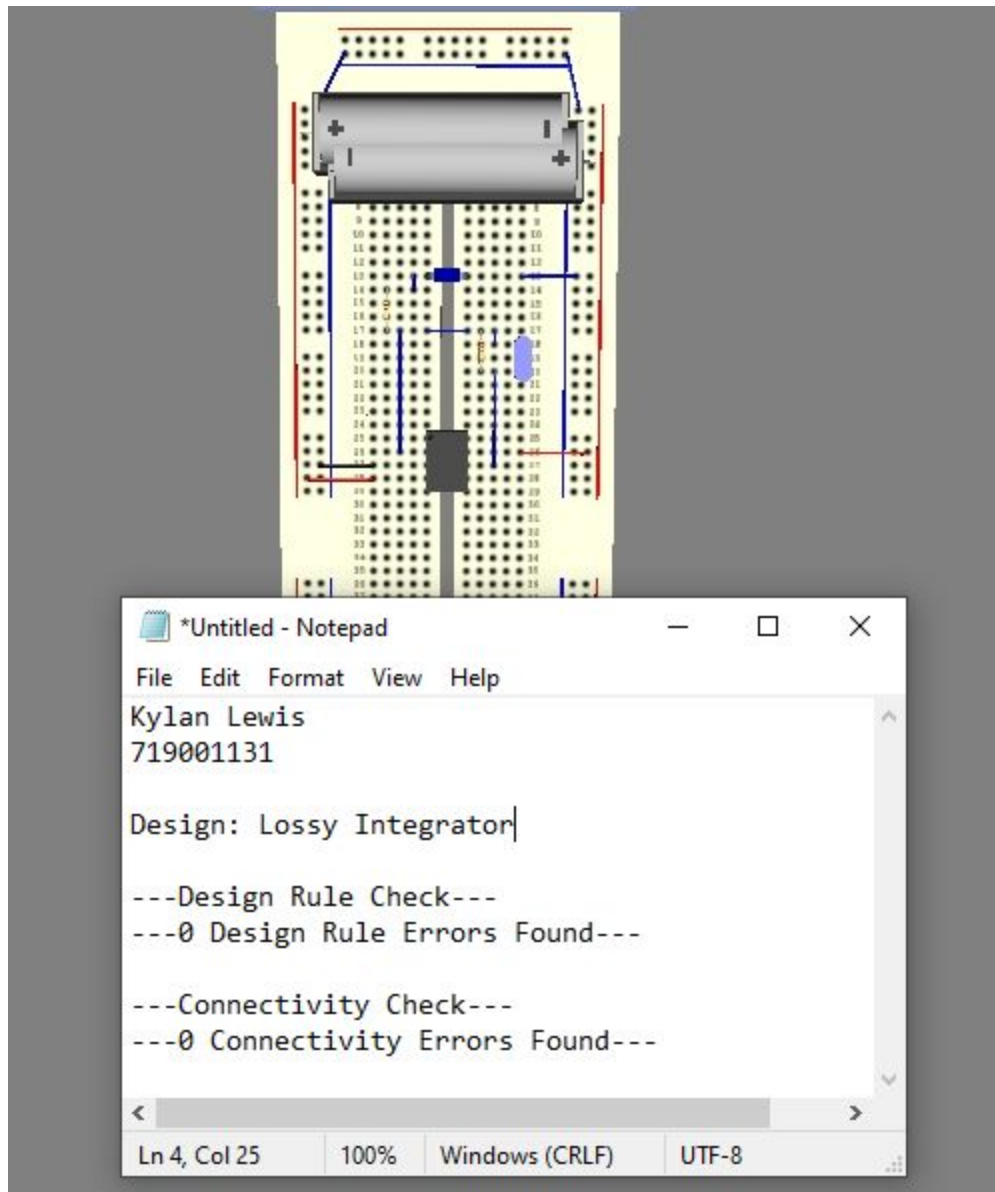
$$f_{\max} = 75\text{kHz}$$

$$v_{o, \max} = \frac{0.5 \cdot 10^6 \text{ V/s}}{2\pi \cdot 75\text{k}} = 1.06 \text{ V}$$

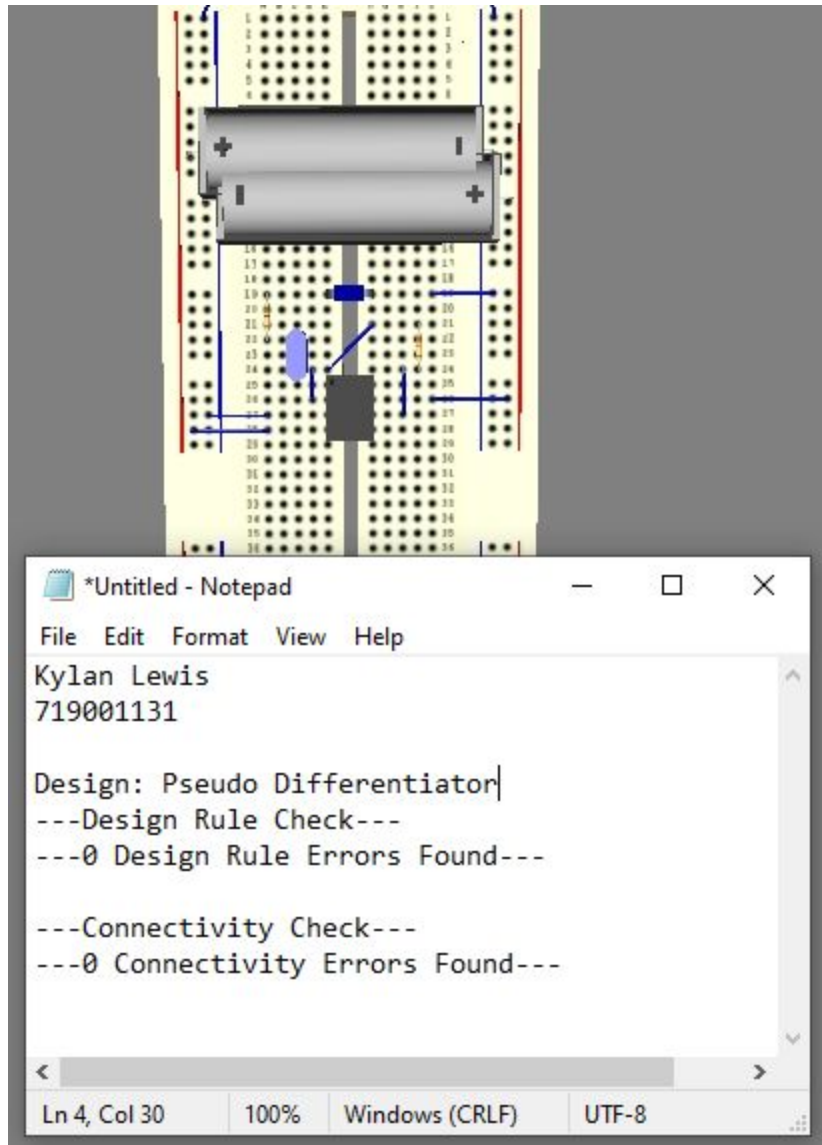


# Multisim Breadboard Wiring:

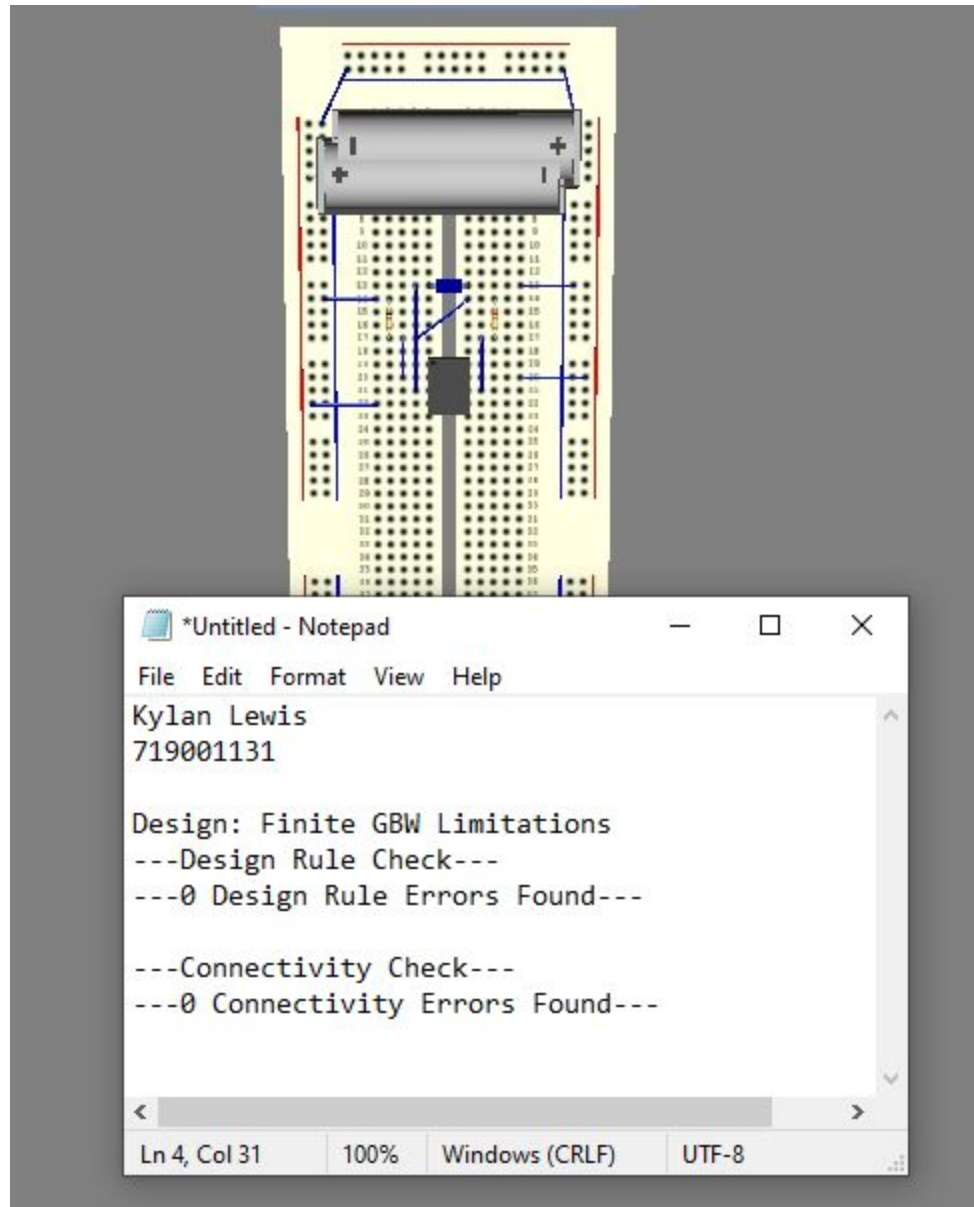
## Lossy Integrator:



## Pseudo Differentiator:



## Finite GBW Limitations:



## Slew Rate Limitation:

