Reinforcement Learning I

Types of machine learning

	Supervised Learning	Unsupervised Learning	Reinforcement Learning
Goal	**Predict** …from examples	**Describe** ...structure in data	**Strategize** learn by trial and error
Data	(x, y)	x	delayed feedback
Types	• Classification • Regression	• Density estimation • Clustering • Dimensionality reduction • Anomaly detection	• Model-free learning • Model-based learning

Card game problem as reinforcement learning

Trial/episode: play one hand until zero cards remain

Action: play a card or discard a card

Reward: how much you win or lose at each

Return: total rewards (money won/lost)

Action-Value: expected reward for taking each action

State: card showing and your hand

Policy: How do we choose actions to maximize our total rewards

Reinforcement Learning Roadmap

1 Core concepts in reinforcement learning

Actions, Rewards, Value, Environments, and Policies

Knowledge of **Environment**

Perfect knowledge
Known Markov
Decision Process

2 Markov decision processes

…and Markov chains and Markov reward processes

3 Dynamic Programming

How do we find optimal policies?
(Bellman equations)

No knowledge
Must learn from
experience

4 Monte Carlo Control

How do we estimate our value functions?
How do we use the value functions to choose actions?
How do we learn optimal policies from experience?

Resources

Sutton and Barto, 2nd edition, 2018

Reinforcement Learning: An Introduction

Draft of updated edition available free online:
http://www.incompleteideas.net/book/the-book-2nd.html

David Silver, 2015
University College London
Advanced Topics 2015 (COMPM050/COMPGI13)

Course website:
http://www0.cs.ucl.ac.uk/staff/D.Silver/web/Teaching.html

Video series:
https://www.youtube.com/watch?v=2pWv7GOvuf0&list=PL7-jPKtc4r78-wCZcQn5IqyuWhBZ8fOxT

Image from Amazon.com (where the book may be purchased)
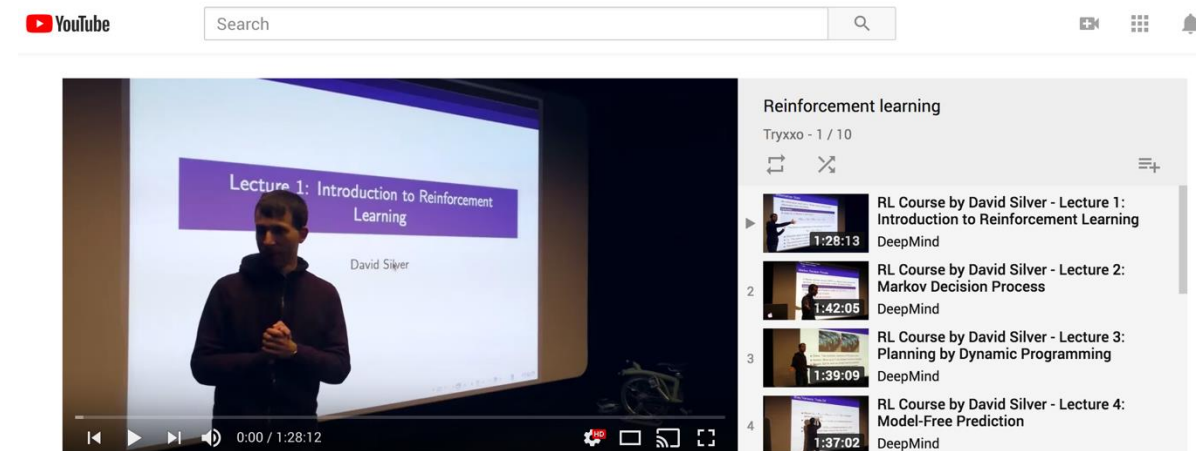
Image from Youtube.com

Reinforcement learning

Control Theory (optimal control)

Psychology and Neuroscience

Reinforcement Learning

Machine Learning / Artificial Intelligence

Operations Research
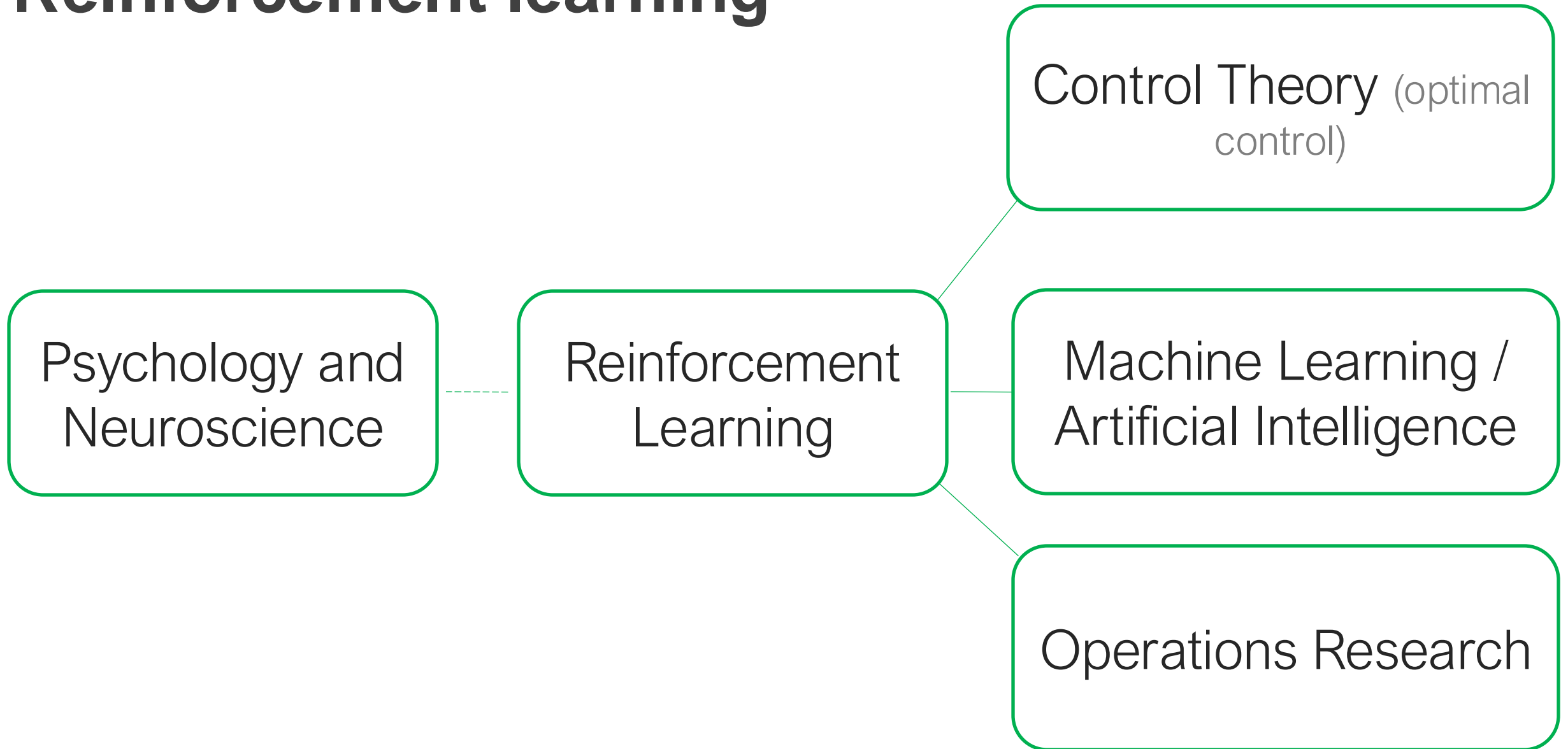
Reinforcement learning facets & challenges

Goal: select actions to maximize total long-term rewards

Sequential decision making
Challenge: an action needs to be taken at each step

Evaluation of rewards versus instruction (examples of correct actions)
Challenge: this leads to a trial-and-error approach to learning

May be better to sacrifice immediate reward for long-term gains
Challenge: exploration (of untried actions) vs exploitation (of current knowledge)

Rewards may be delayed
Challenge: credit assignment: which action(s) led to the reward(s)?

David Silver, 2015

Reinforcement Learning Applications

- Self-driving cars (link)

- Energy-efficient data center cooling control (link)

- Financial trading (link)

- Medical diagnosis and treatment (link)

- Gaming (AlphaGo, Atari, StarCraft)

Industry Leaders: Google Deepmind (link)

Reinforcement Learning Examples

Winning at Atari: https://youtu.be/V1eYniJ0Rnk

Balancing an inverted pendulum: https://youtu.be/b1c0N_Fs9wc
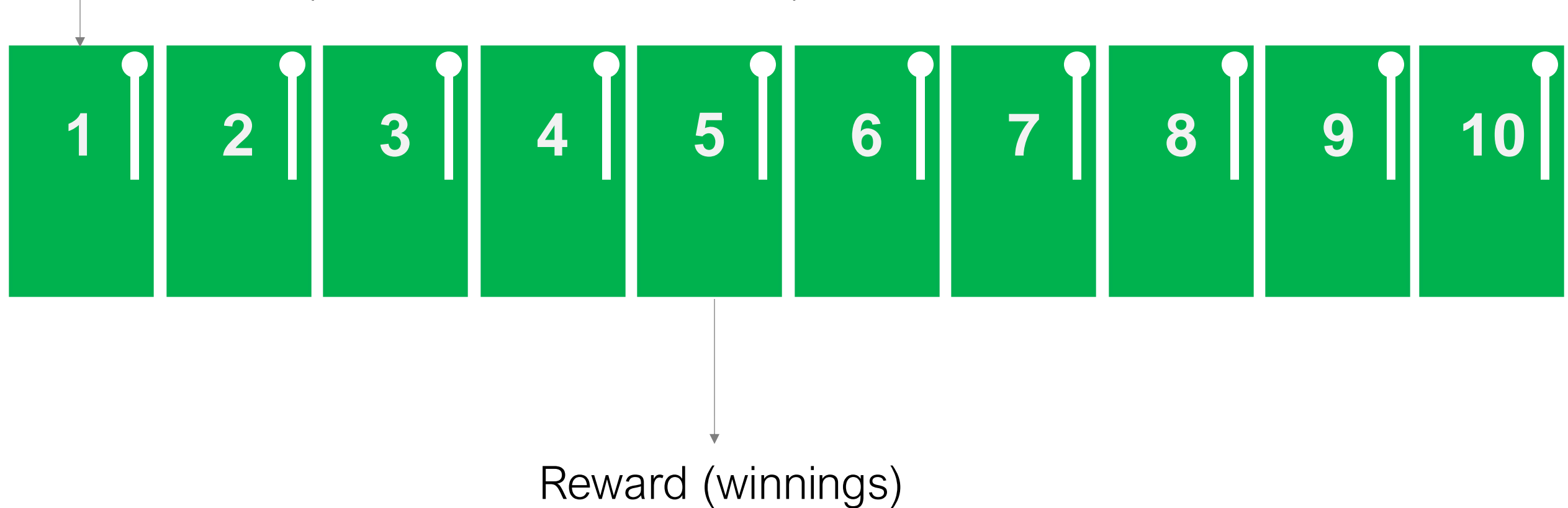
Flipping pancakes: https://youtu.be/W_gxLKSsSIE

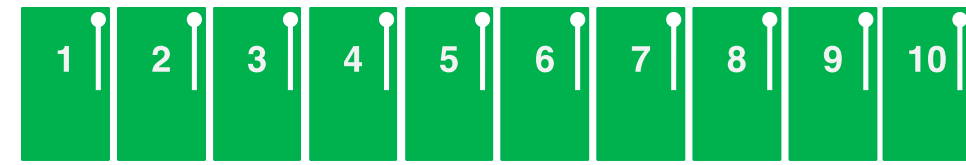**RL is a unifying framework for a wide range of problems**

Multi-armed Bandit

You walk into a casino…

Slot Machine (a.k.a. one-armed bandit)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

Reward (winnings)

Multi-armed bandit problem

Trial/episode: play one machine

Action: pick one machine to play (one action per trial/episode)

Reward: how much you win or lose
- Each machine has an unknown probability of payoff/reward
- The rewards are stochastic (their distributions are unknown)

Action-Value: expected reward for taking each action

State: only 1 "state" in this problem - our environment doesn't change

create a policy

Policy: How do we choose actions to maximize our total rewards?
- If we knew the best machine, we'd always pick it
- This is what we want to learn

Multi-armed bandit

The *true* **action-value** of an action is $q_*(a)$

Our *estimated* **action-value** at the tth play is $q_t(a)$

If action a has been chosen k_a times prior to t:

$$q_t(a) = \frac{r_1 + r_2 + \cdots + r_{k_a}}{k_a}$$

As we take action a more, our action-value estimates improve

Multi-armed bandit policies, $\pi(s)$

Greedy action:

Select $a^* = \arg\max_a q_t(a)$

Problem: if the initial rewards are not representative, this will be suboptimal

ϵ-Greedy methods:

Select a^* with probability $1 - \epsilon$, otherwise, randomly select another option

Problem: in the long run, this will waste reward once the best action is known
Solution: reduce ϵ over time
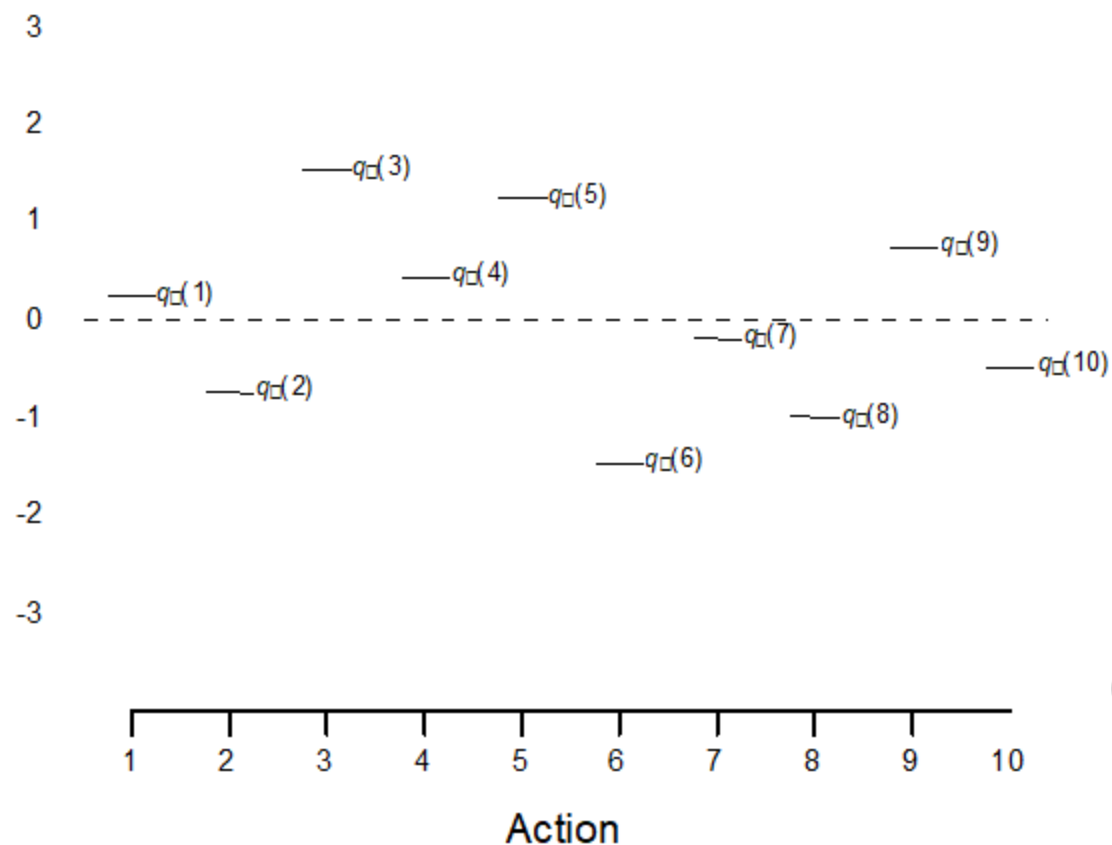
Alternative:

Select the action probabilities based on the expected value

Probability of selecting action $P(a) = \dfrac{\exp(q_t(a))}{\sum_{b=1}^{n} \exp(q_t(b))}$
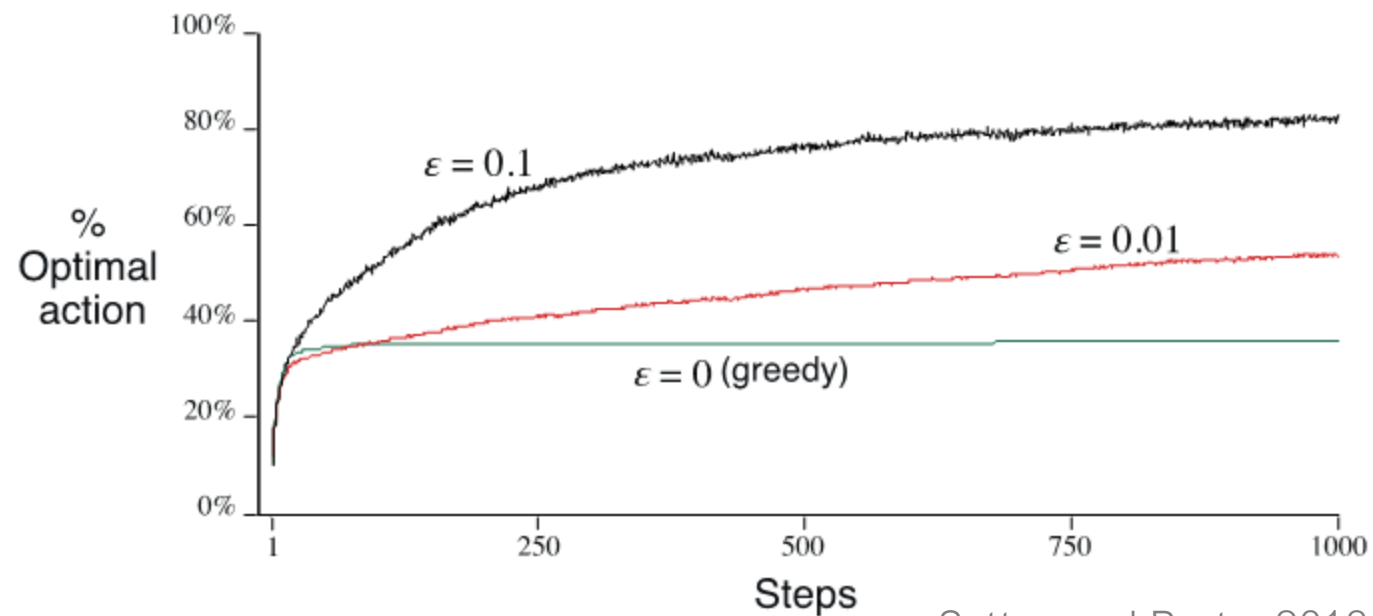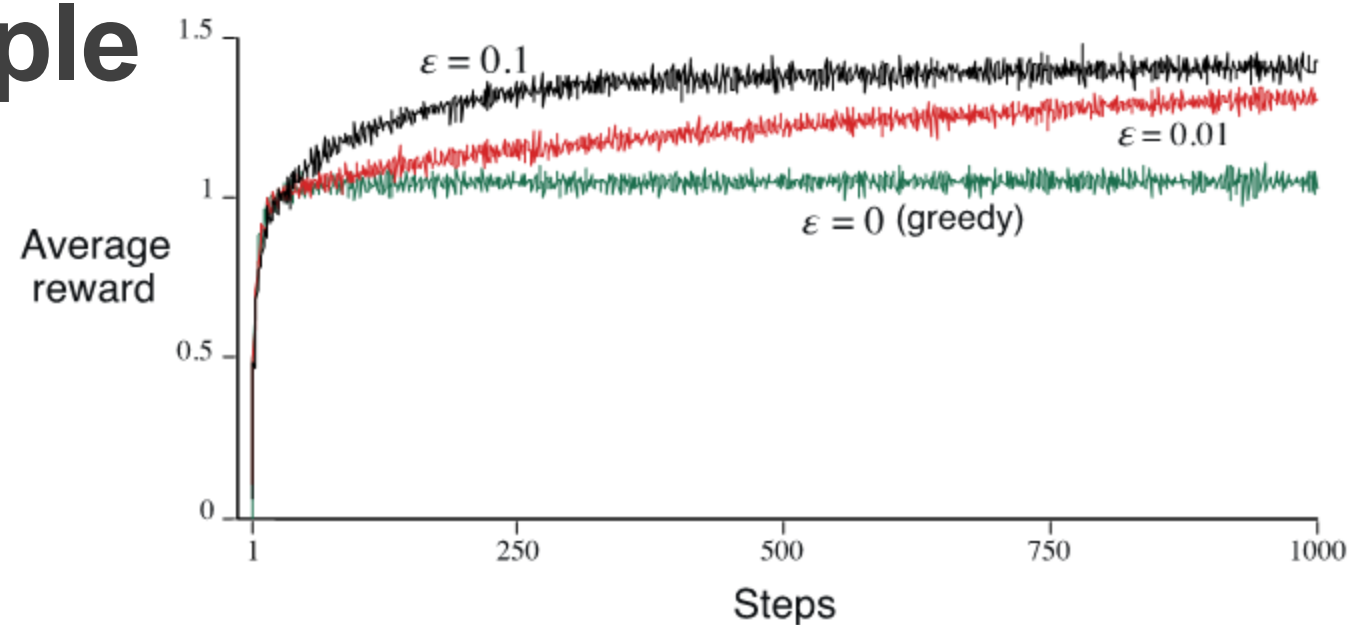
10-Armed Bandit Example

Note: Each distribution has a mean $q_*(a)$ with unit variance

Sutton and Barto, 2018

Reinforcement Learning Roadmap

① Core concepts in reinforcement learning

Actions, Rewards, Value, Environments, and Policies

② Markov decision processes

…and Markov chains and Markov reward processes

③ Dynamic Programming

How do we find optimal policies?
(Bellman equations)

④ Monte Carlo Control

How do we estimate our value functions?
How do we use the value functions to choose actions?
How do we learn optimal policies from experience?
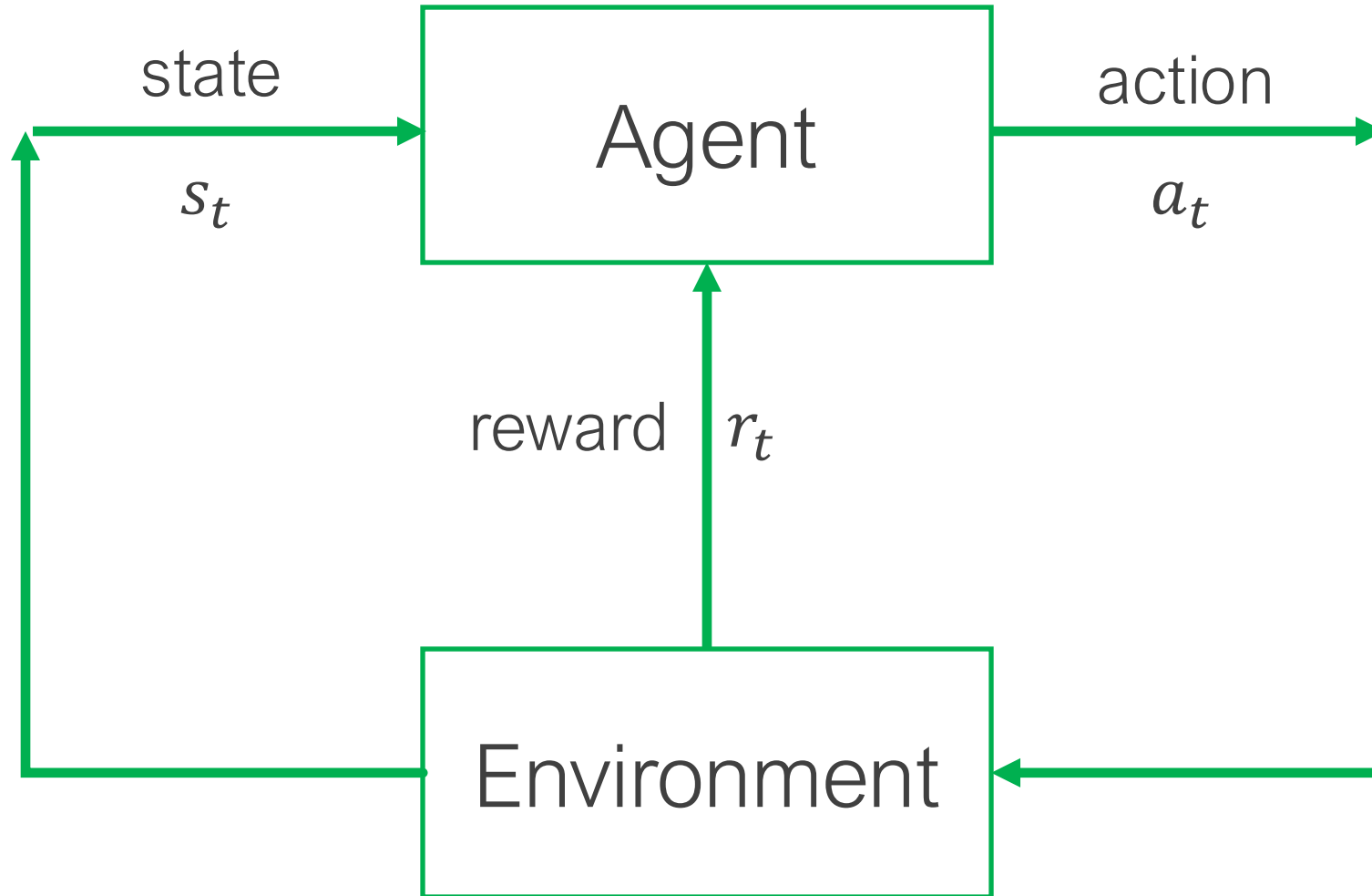
Knowledge of **Environment**

Perfect knowledge
Known Markov
Decision Process

No knowledge
Must learn from
experience

Agent-environment Interaction

state s_t

Agent

action a_t

reward r_t

Environment

Agent at each step t…

Encounters state, s_t
Executes action a_t
Receives scalar reward, r_{t+1}

Environment at each step t…

Receives action a_t
Transitions to state, s_{t+1}
Emits scalar reward, r_{t+1}

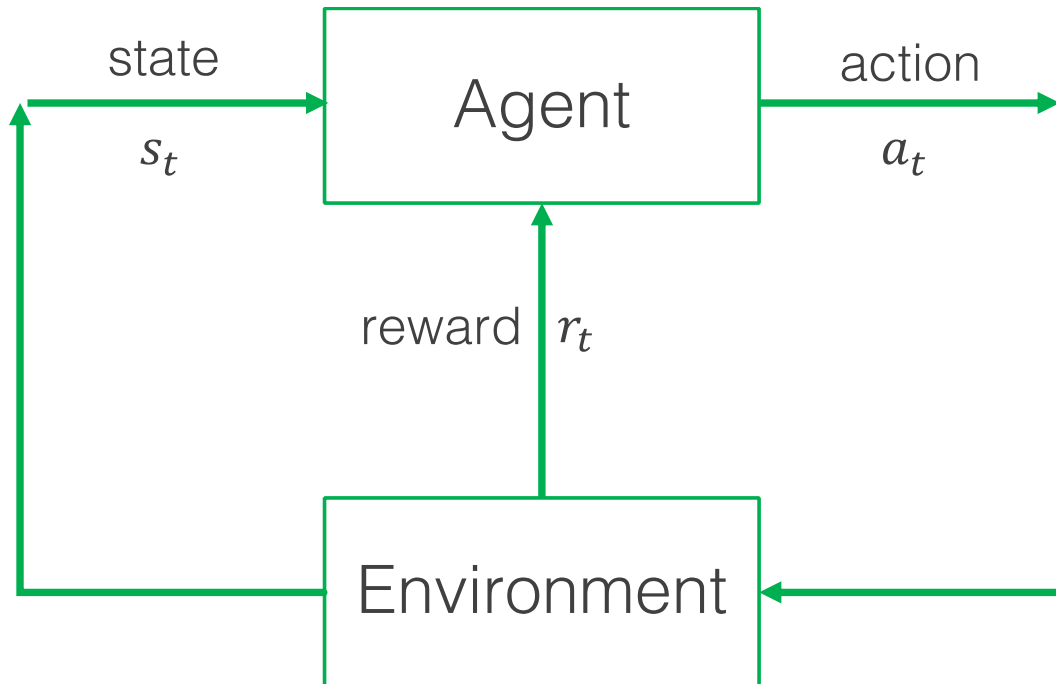**Actions**: choices made by the agent
States: basis on which choices are made
Rewards: define the agent's goals

David Silver, 2015

Reinforcement Learning Components

state
s_t

Agent

action
a_t

reward r_t

Environment

Policy (agent behavior), $\pi(s)$

Reward function (the goal), r_t

Value functions (expected returns),
$v(s)$ State value
$q(s, a)$ Action value

Maze Example: Policy, Value, and Reward
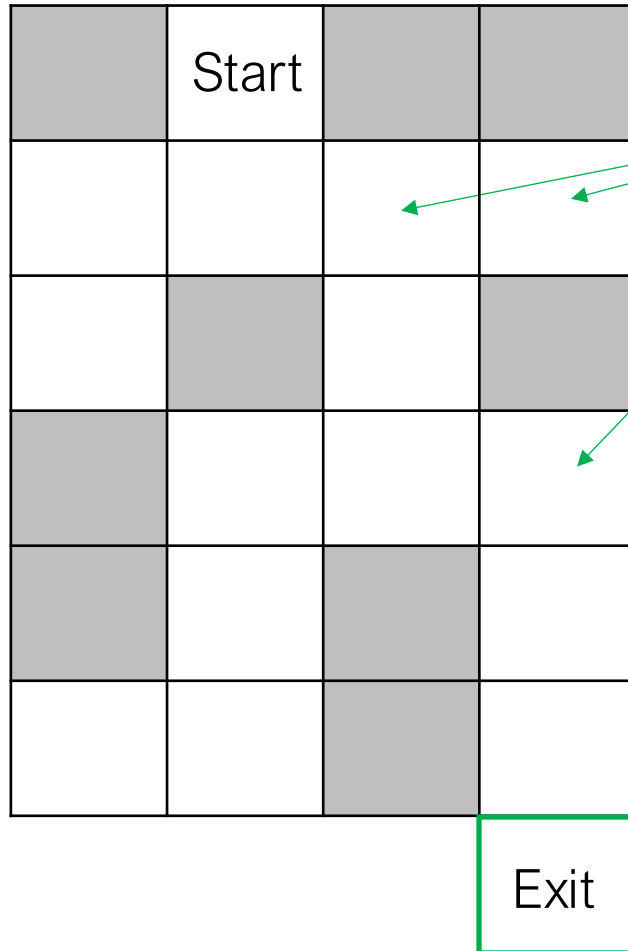
Each location in the maze represents a **state**

The **reward** is -1 for each step the agent is in the maze

Available **actions**: move ↑,↓,←,→ (as long as that path is not blocked)

Policy $\pi(s)$

(which actions to take in each state)

Start

	↓		
→	→	↓	←
↑		↓	
	→	→	↓
	↑		↓
→	↑		↓
		Exit	

Adapted from David Silver, 2015

Policy $\pi(s)$
(which actions to take in each state)

Start

	↓		
→	→	↓	←
↑		↓	
	→	→	↓
	↑		↓
→	↑		↓

Exit

Reward r_t
(rewards are received after actions are taken)

Start

	-1		
-1	-1	-1	-1
-1		-1	
	-1	-1	-1
	-1		-1
-1	-1		-1

Exit

Adapted from David Silver, 2015

Policy $\pi(s)$
(which actions to take in each state)

Start

	↓		
→	→	↓	←
↑		↓	
	→	→	↓
	↑		↓
→	↑		↓

Exit

Reward r_t
(rewards are received after actions are taken)

Start

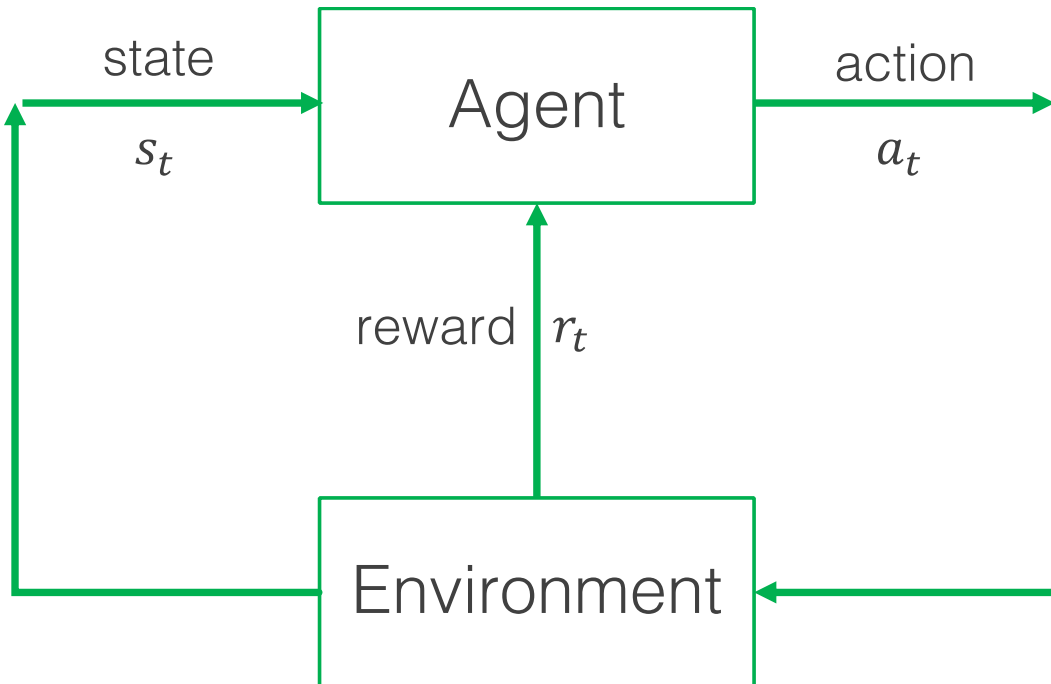|	-1		
-1	-1	-1	-1
-1		-1	
	-1	-1	-1
	-1		-1
-1	-1		-1

Exit

State Value $v_\pi(s)$
(expected cumulative rewards starting from current state **if** we follow the policy)

Start

	-8		
-8	-7	-6	-7
-9		-5	
	-5	-4	-3
	-6		-2
-8	-7		-1

Exit

Policy

Policy, $\pi(s)$
- Selects an action to choose based on the state
- Determines an agent's "behavior"

Deterministic policy:
$$a = \pi(s)$$

Stochastic policy:
$$\pi(a|s) = P(a_t = a|s_t = s)$$

Helps us "explore" the state space

RL tries to learn the "best" policy

state
s_t

Agent

action
a_t

reward r_t

Environment

Goals and rewards

Rewards are the **only way** of communicating RL goals

Ex 1: Robot learning a maze
- 0 until it escapes, then +1 when it does
- -1 until it escapes (encourages it to escape quickly)

Ex 2: Robot collecting empty soda cans
- +1 for each empty soda can
- Negative rewards for bumping into things

Chess: what if we set +1 for capturing a piece?
(it may not win the game and still maximize rewards)

What you want achieved not **how**

Returns / cumulative reward

Episodic tasks (finite number, T, of steps, then reset)
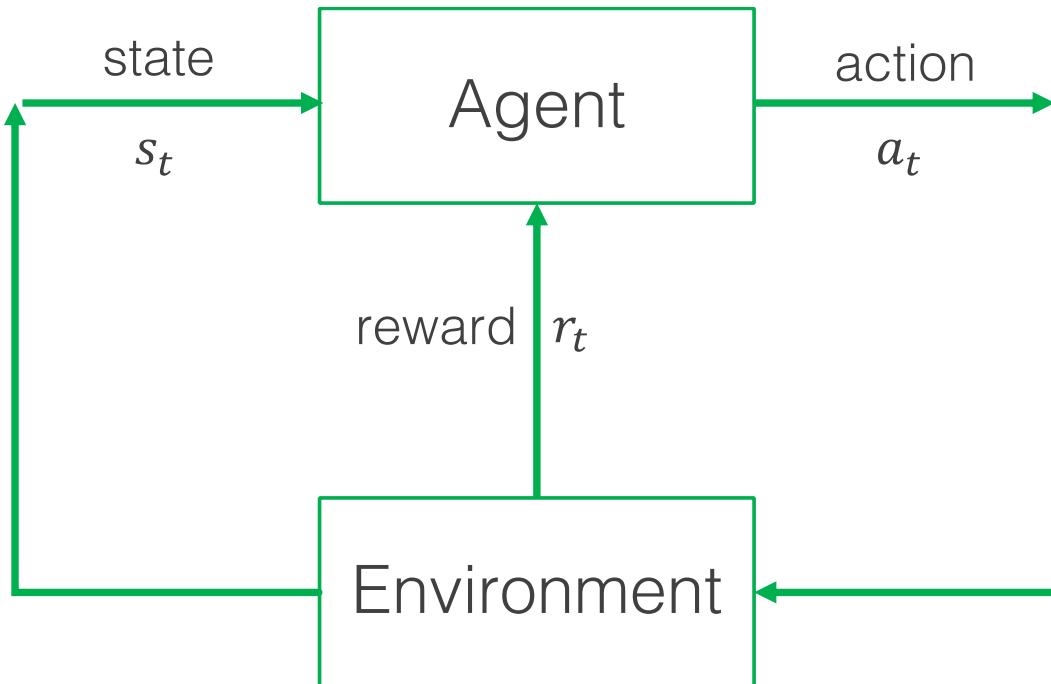
$$G_t = r_{t+1} + r_{t+2} + \cdots + r_T$$

Continuing tasks with discounting $(T \to \infty)$

$$G_t = r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} \ldots = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$$

where $0 \leq \gamma \leq 1$ is the discount rate

This makes the agent care more about immediate rewards

Value functions

State Value function, $v_\pi(s)$
- How "good" is it to be in a state, s_t then follow policy π to choose actions
- Total expected rewards

$$v_\pi(s) = E_\pi[G_t | s_t = s]$$

Action Value function, $q_\pi(s,a)$
- How "good" is it to be in a state, s, take action a, then follow policy π to choose actions
- Total expected rewards

$$q_\pi(s,a) = E_\pi[G_t | s_t = s, a_t = a]$$

Where $\quad G_t = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$

state s_t → Agent → action a_t

reward r_t

Environment

Policy $\pi(s)$
(which actions to take in each state)

Reward r_t
(rewards are received after actions are taken)

State Value $v_\pi(s)$
(expected cumulative rewards starting from current state **if** we follow the policy)

Action Value $q_\pi(s, a)$
(expected cumulative rewards starting from current state **if** we take action a then follow the policy)

Start

	↓		
→	→	↓	←
↑		↓	
	→	→	↓
	↑		↓
→	↑		↓

Exit

Start

	-1		
-1	-1	-1	-1
-1		-1	
	-1	-1	-1
	-1		-1
-1	-1		-1

Exit

Start

	-8		
-8	-7	-6	-7
-9		-5	
	-5	-4	-3
	-6		-2
-8	-7		-1

Exit

↑	-9
→	-7
←	-9

↑	-4
↓	-2

Adapted from David Silver, 2015

Reinforcement Learning Components

**Policy** (determines agent behavior), $\pi(s)$
- Determines action given current state
- Agent's way of behaving at a given time

Reward function (sets the goal), r_t
- Maps state of the environment to a reward that describes the state desirability
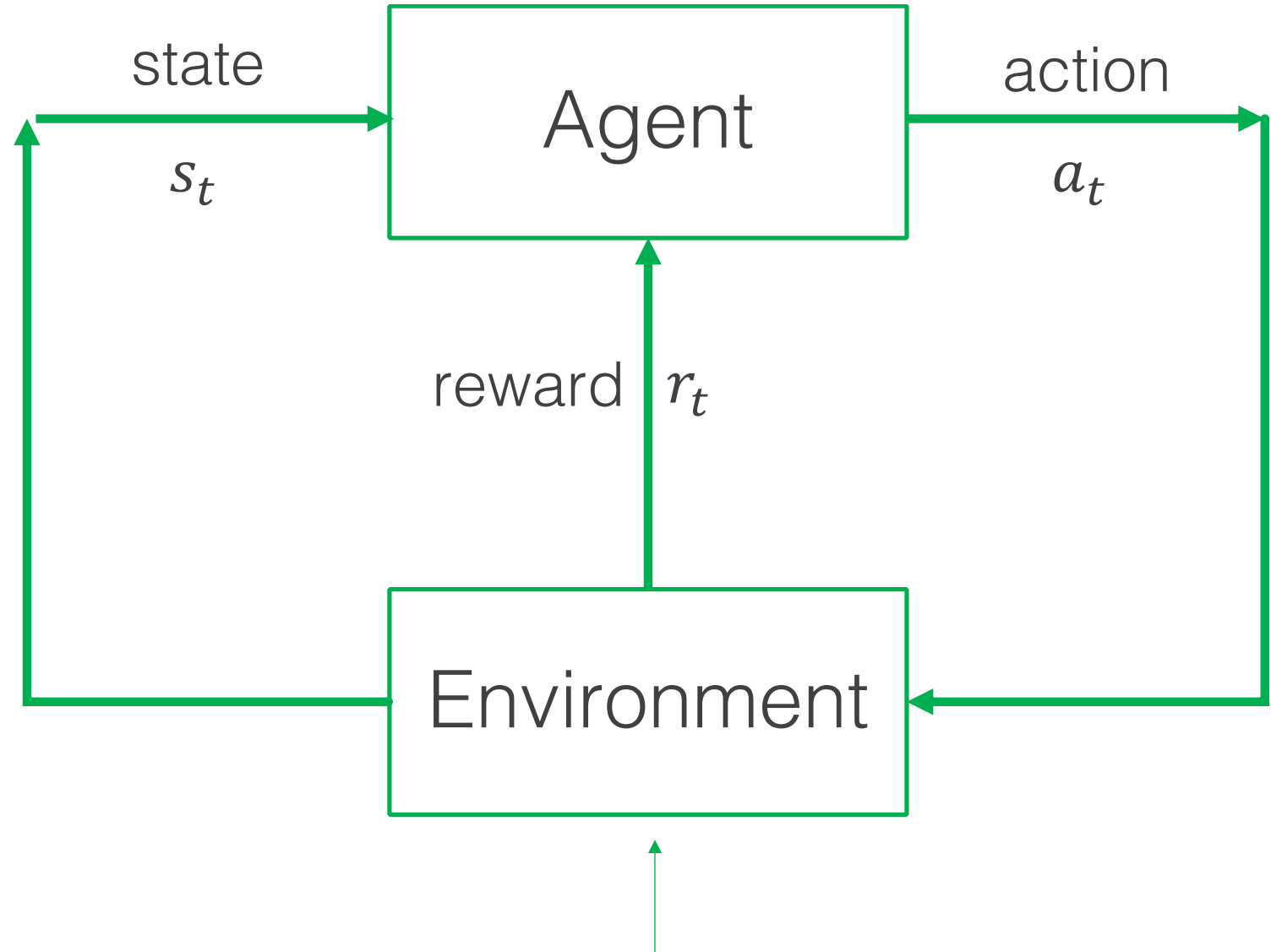- Objective is to **maximize total rewards**

Value (estimates expected returns), $v(s), q(s, a)$
- Expected returns from a state and following a specific policy
- How "good" is each state

state
s_t

Agent

action
a_t

reward r_t

Environment

Reinforcement Learning I

Environment

state

Agent

action

s_t

a_t
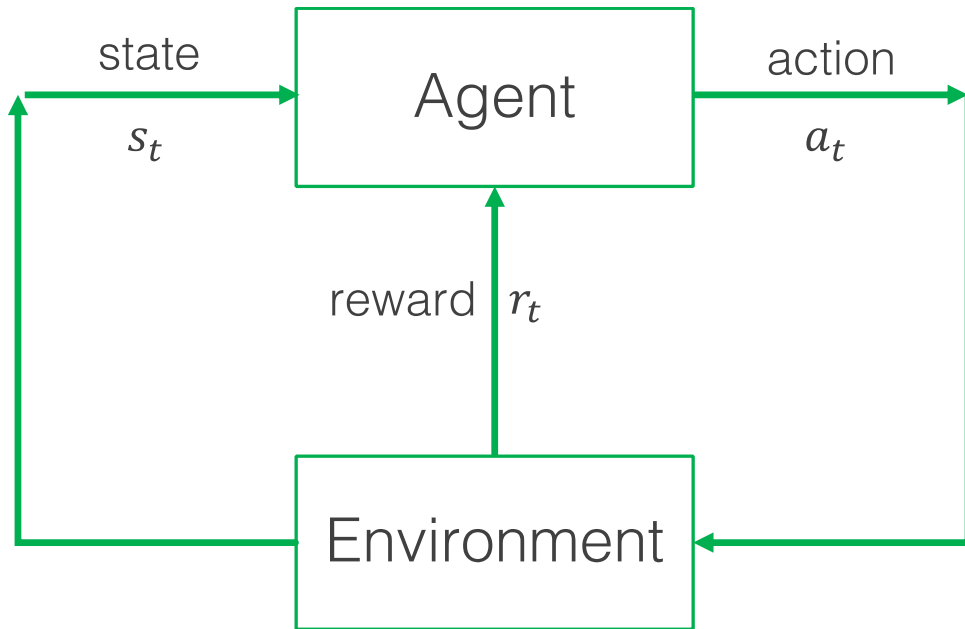
reward r_t

Environment

Markov Decision Process

(assumed formulation for many RL problems)

Goal

Maximize returns (expected rewards)

Find the best policy to guide our actions in an environment
(agent-environment interface is idealized as a Markov Decision Process)

Reinforcement Learning Roadmap

1 Core concepts in reinforcement learning

Actions, Rewards, Value, Environments, and Policies

Knowledge of **Environment**

Perfect knowledge
Known Markov
Decision Process

2 Markov decision processes

…and Markov chains and Markov reward processes

3 Dynamic Programming

How do we find optimal policies?
(Bellman equations)

No knowledge
Must learn from
experience

4 Monte Carlo Control

How do we estimate our value functions?
How do we use the value functions to choose actions?
How do we learn optimal policies from experience?