

Two period model of a non-renewable resource

1. Consider extraction of a non-renewable natural resource. The inverse demand function for the depletable resource is $P = 20 - 2Q$ in both periods 1 and 2 and the marginal cost of supplying it is \$3. The discount rate is 10%. There are 10 units total.
 - (a) Explain what the resource constraint is and then write it in mathematical form
 - (b) What is the per-unit profit for extracting resources in period 1?
 - (c) What is the per-unit profit for extracting resources in period 2? What is the present value of the per-unit profit from the viewpoint of period 1?
 - (d) Describe in words why you must equate the marginal unit's profit in each periods (the optimality condition).
 - (e) What two pieces of information are needed in order to solve for the optimal extraction Q_1^* and Q_2^* ?
 - (f) Solve for the optimal extraction Q_1^* and Q_2^* .
 - (g) Describe using specific numbers why $Q_1 = 3$ and $Q_2 = 4.5$ is not optimal
 - (h) What is the marginal user cost? Interpret this number.
 - (i) Now assume $r = 0$. What is the optimal allocation now? Why did optimal allocation change in the direction that it did?

2. Consider extraction of a non-renewable natural resource. The inverse demand function for the depletable resource is $P = 12 - Q$ in both periods 1 and 2 and the marginal cost of supplying it is \$3. The discount rate is 10%. There are 7.5 units total.
 - (a) Find the equilibrium allocation in each period for resource extraction
 - (b) Describe using the concept of marginal user cost why $Q_1 = 3$ and $Q_2 = 4.5$ is not optimal
 - (c) What is the marginal user cost? Interpret this number.
 - (d) Now assume $r = 0$. What is the optimal allocation now? Why did it change in the direction that it did?

3. Consider extraction of a non-renewable natural resource. The inverse demand function for the depletable resource is $P = 12 - Q$ in both periods 1 and 2 and the marginal cost of supplying it is $2 + Q/2$. The discount rate is 6%. There are 15 units total.
 - (a) Find the equilibrium allocation in each period for resource extraction
 - (b) What is the marginal user cost? Interpret this number.