

# CHEG231 exam 1 sheet

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## mass balances

$$\Delta M = \Delta M_{\text{in}} - \Delta M_{\text{out}} \quad \frac{dM}{dt} = \dot{M}_{\text{in}} - \dot{M}_{\text{out}}$$

## energy balance, difference form

$$\left[ U + m \left( \frac{v^2}{2} + gh \right) \right]_f - \left[ U + m \left( \frac{v^2}{2} + gh \right) \right]_i = Q + W_S + W_{PV} \dots + \sum_{k=1}^K \Delta m_k \left( \hat{U} + P\hat{V} + \frac{v^2}{2} + gh \right)_k$$

## energy balance, differential form

$$\frac{d}{dt} \left\{ U + M \left( \frac{v^2}{2} + mg \right) \right\} = \dot{Q} + \dot{W}_s + \dot{W}_{PV} + \sum_{k=1}^K \dot{m}_k \left( \hat{U} + P\hat{V} + \frac{v^2}{2} + mg \right)$$

## entropy balances

$$S_2 - S_1 = \sum_k \int_{t_1}^{t_2} \dot{m}_k \hat{S}_k dt + \int_{t_1}^{t_2} \frac{\dot{Q}}{T} dt + S_{\text{gen}} \quad \frac{dS}{dt} = \sum_{k=1}^K \dot{m}_k \hat{S}_k + \frac{\dot{Q}}{T} + \dot{S}_{\text{gen}}$$

$$C_V = \left( \frac{\partial \underline{U}}{\partial T} \right)_V$$

$$C_P = \left( \frac{\partial \underline{H}}{\partial T} \right)_P$$

$$\text{For Ideal Gasses: } C_P^* = C_V^* + R \quad \text{and } C_V^* = df/2$$

$$\underline{U}^{IG} = C_V^* T$$

$$\underline{H}^{IG} = C_P^* T$$

For solids and liquids:  $\underline{H} \approx \underline{U}$  and incompressible. Also  $C_P = 3NR = 24.924 \text{ J/mol}\cdot\text{K}$  approx for solids.

## lever rule (properties of one component system w/ two phases)

$$\hat{\theta} = \omega^I \hat{\theta}^I + \omega^{II} \hat{\theta}^{II} = \omega^I \hat{\theta}^I + (1 - \omega^I) \hat{\theta}^{II}$$

## entropy stuff

$$\Delta \underline{S}_{\text{ideal gas}} = C_p^* \ln \left( \frac{T_2}{T_1} \right) - R \ln \left( \frac{P_2}{P_1} \right)$$

$$\Delta \underline{S}_{\text{Liquid}} = C_p^* \ln \left( \frac{T_2}{T_1} \right)$$

Helmholts Energy: difference is work required to bring closed, isothermal, constant volume system from state 1 to state 1

$$A = U - TS$$

Gibbs energy: helpmoltz but for closed, isothermal, isobaric system

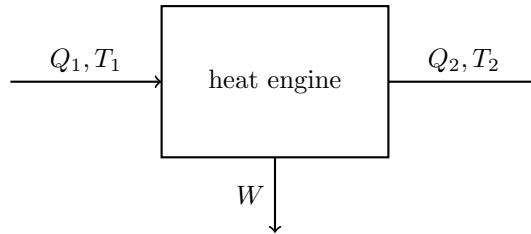
$$G = U + PV - TS = H - TS$$

Gibbs equation

$$d\underline{U} = T d\underline{S} - P d\underline{V}$$

## 1 Carnot Derivation

Consider a closed system of a heat engine



energy balance:

$$\cancel{\frac{dU}{dt}} = \dot{Q} + \dot{W} + \cancel{\sum \dot{m}_k \hat{u}_k}$$

$$0 = Q_1 + Q_2 + W$$

entropy balance:

$$\cancel{\frac{dS}{dt}} = \frac{\dot{Q}_1}{T_1} + \frac{\dot{Q}_2}{T_2} + \cancel{\sum_{k=1}^K \dot{m}_k \hat{s}_k} + \dot{S}_{\text{gen}}$$

$$0 = \frac{\dot{Q}_1}{T_1} + \frac{\dot{Q}_2}{T_2} + \dot{S}_{\text{gen}}$$

integrating, and remembering that reversible processes are more efficient than irreversible processes

$$0 = \frac{Q_1}{T_1} + \frac{Q_2}{T_2}$$

$$\frac{Q_1}{T_1} = \frac{-Q_2}{T_2}$$

$$Q_2 = \frac{-Q_1 T_2}{T_1}$$

and taking this into the energy balance

$$-W = Q_1 + \frac{-Q_1 T_2}{T_1} = Q_1 \left( \frac{T_1 - T_2}{T_1} \right)$$

$$\eta = \frac{-W}{Q_1} = \left( \frac{T_1 - T_2}{T_1} \right)$$