

Homework 1

Kyle Wodehouse

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1 Syllabus Review

- (a) 207 Dupont Hall
- (b) 6 homework assignments
- (c) 17 at very least.
- (d) 'analyze and select an appropriate material for a given application' and 'select an appropriate method to characterize the structure or properties of a material.'

2 Bonding Energy

a.

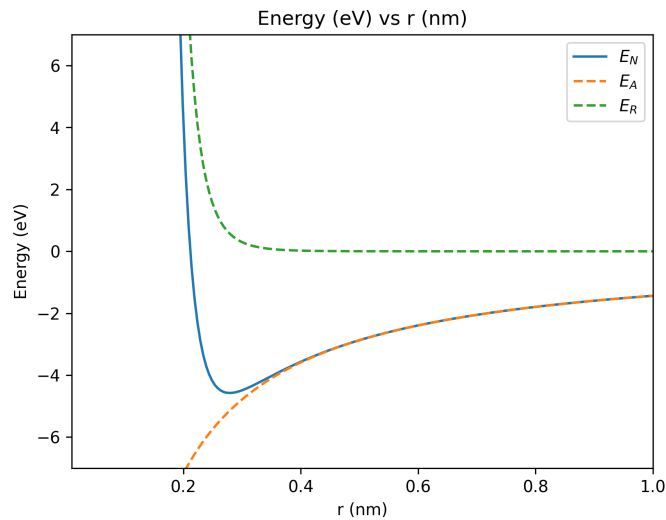


Figure 1: K^+ and Cl^- energy profile

b.

for this one I used some python code to put a vertical line at the distance where energy is minimized—the *equilibrium bond length will be when the energy is at a local minimum*. To be a little more rigorous and get some more digits I also loaded up desmos and graphically found the minimum on there as well.

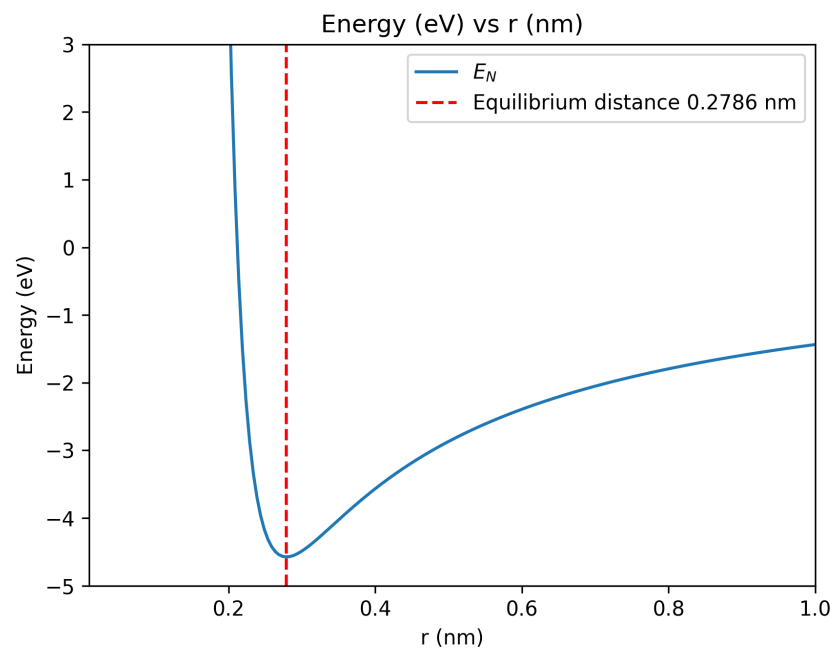


Figure 2: K^+ and Cl^- energy profile with local minimum displayed

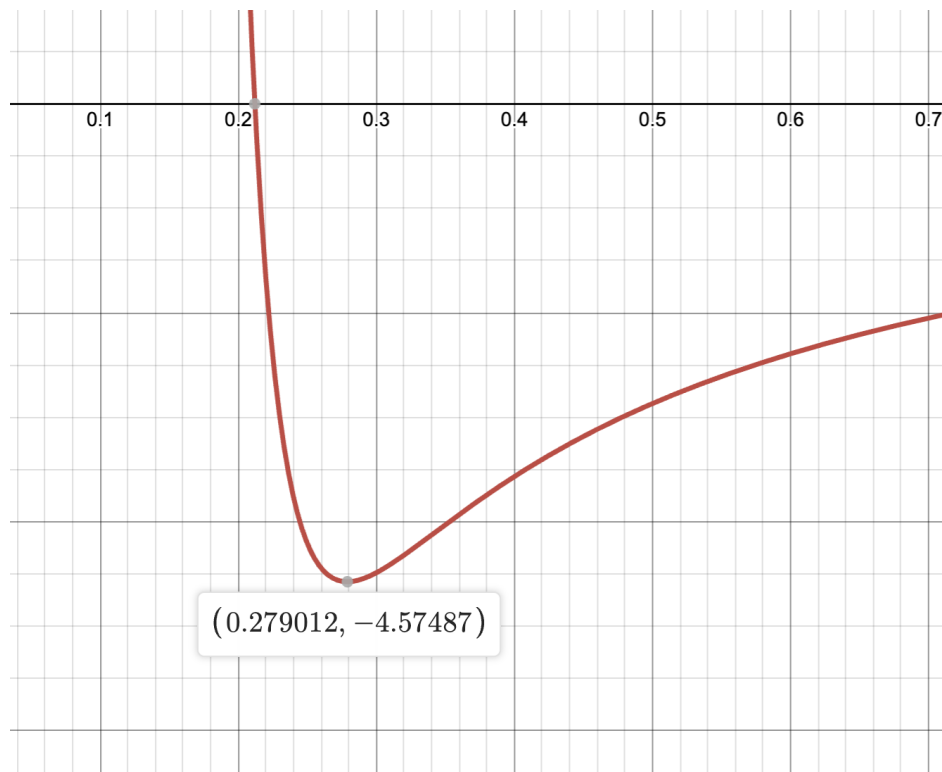


Figure 3: K^+ and Cl^- energy profile on desmos with local minimum displayed

From the desmos graph, the equilibrium spacing and the magnitude of the bonding energy are 0.279 nm

and -4.57 eV respectively.

c.

To mathematically calculate it we can take the derivative, set it equal to zero, and solve for r and then plug that into the original equation to get the energy.

At equilibrium spacing,

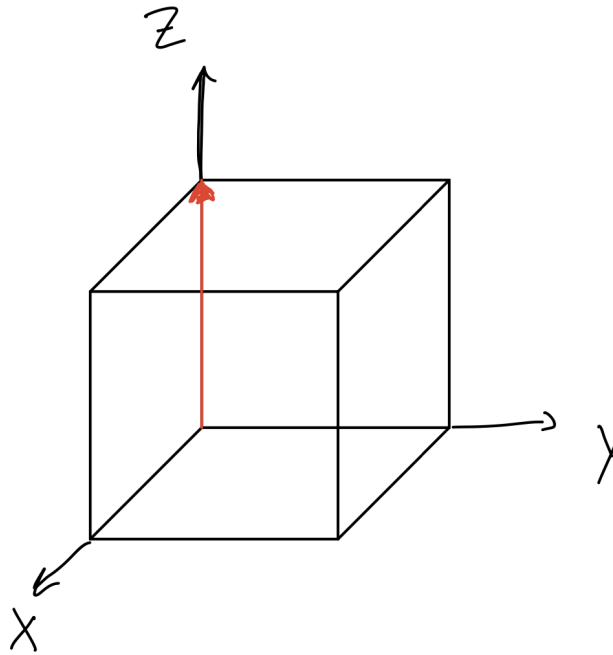
$$\begin{aligned}\frac{dE}{dr} &= 0 \\ \frac{d}{dr} \left(-\frac{A}{r} + \frac{B}{r^9} \right) &= 0 \\ \frac{A}{r^2} - \frac{9B}{r^{10}} &= 0 \\ A &= \frac{9B}{r^8} \\ r^8 &= \frac{9B}{A} \\ r &= \left(\frac{9B}{A} \right)^{1/8} \\ &= \left(\frac{9 \times (5.86 \times 10^{-6})}{1.436} \right)^{1/8} \\ &= 0.279 \text{ nm}\end{aligned}$$

Now we can plug this into the original equation to get the energy at the equilibrium spacing:

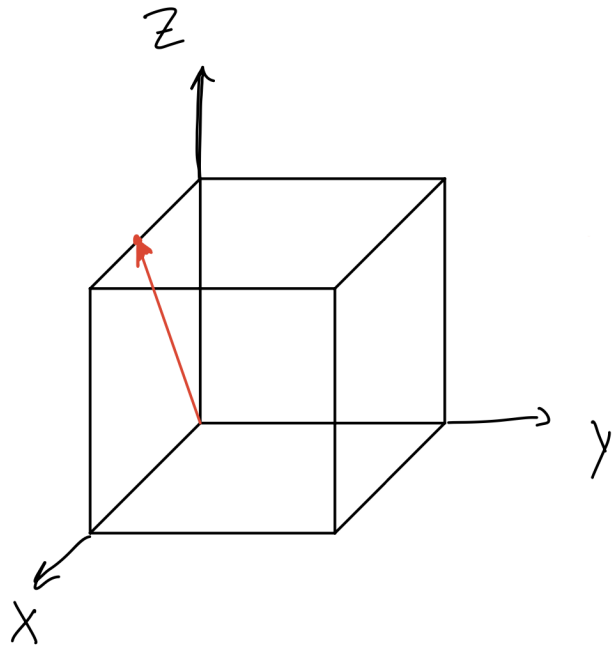
$$\begin{aligned}E &= -\frac{1.436}{0.279} + \frac{5.86 \times 10^{-6}}{(0.279)^9} \\ &= -4.57 \text{ eV}\end{aligned}$$

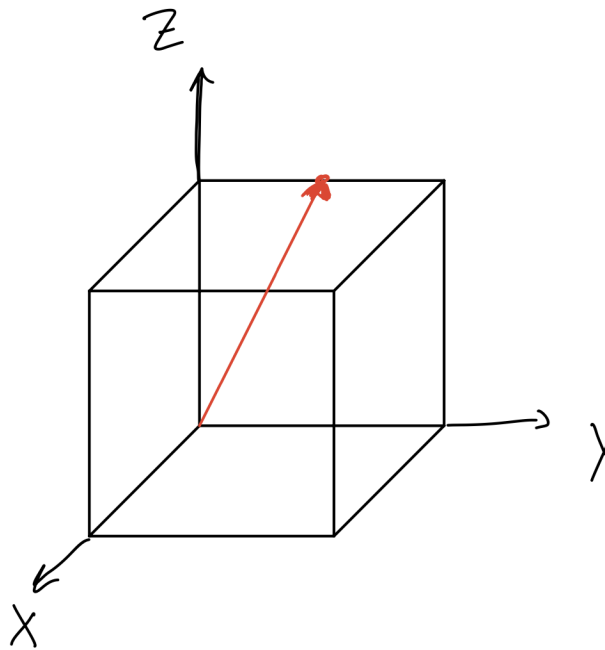
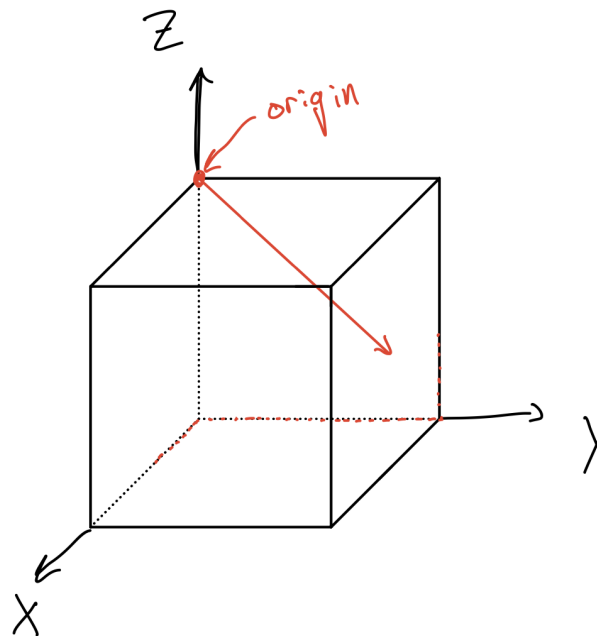
3 Miller Indices: Directions

a. $[001]$



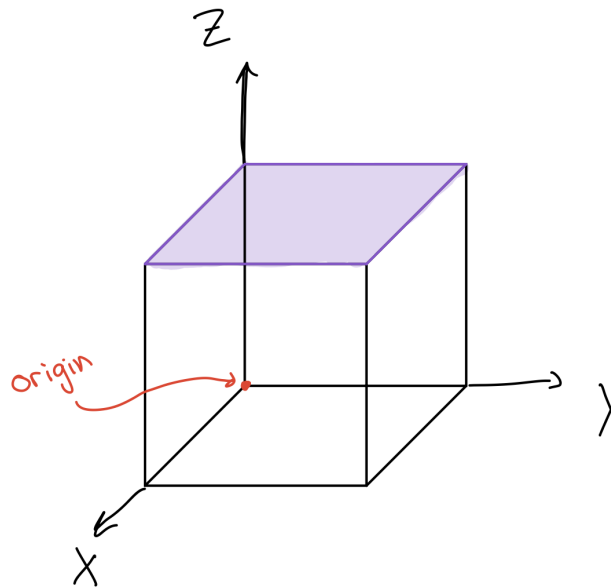
b. $[102]$



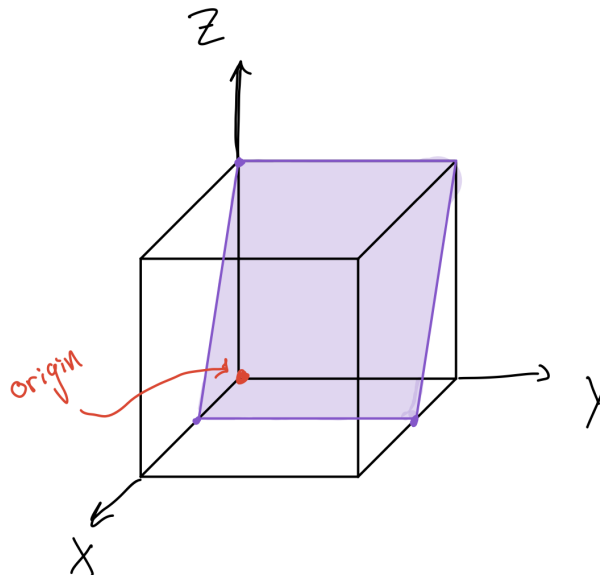
c. $[012]$ d. $[12\bar{1}]$ 

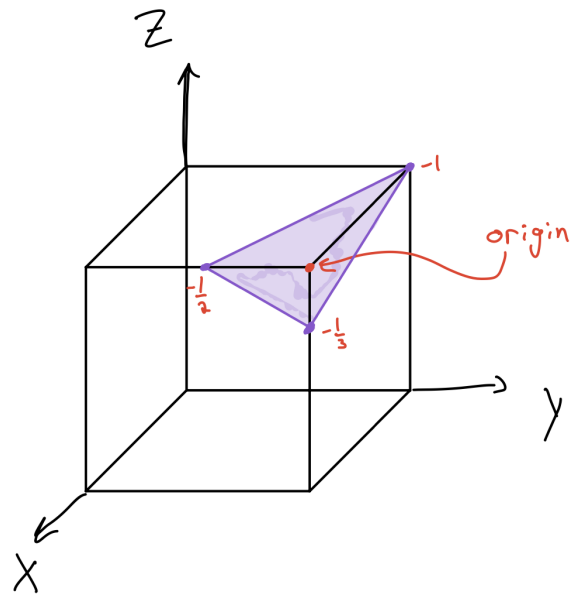
4 Miller Indices: Planes

a. (001)



b. (201)



c. $(\bar{1}\bar{2}\bar{3})$ d. $(1\bar{1}\bar{2})$ 