

# Deformed shell effects in $^{48}\text{Ca}+^{249}\text{Bk}$ quasifission fragments

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**Background:**

**Purpose:**

**Methods:**

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**Conclusions:**

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## I. INTRODUCTION

Quasifission occurs when the collision of two heavy nuclei produces two fragments with similar characteristics to fusion-fission fragments, but without the intermediate formation of a fully equilibrated compound nucleus [1–3]. It is the main mechanism that hinders fusion of heavy nuclei and then the formation of superheavy elements [4–7]. It is then crucial to achieve a deep understanding of quasifission in order to minimize its impact and maximize the formation of compound nuclei for heavy and superheavy nuclei studies.

Quasifission also provides a unique probe to quantum many-body dynamics of out-of-equilibrium nuclear systems. For instance, quasifission studies bring information on mass equilibration time-scales [8–10], on shell effects in the exit channels [11–15], as well as on the nuclear equation of state [16, 17].

In fusion-fission, the exit channel is essentially determined by the properties of the compound nucleus, and does not depend a priori on the specificities of the entrance channel. This is not the case in quasifission which is known to preserve a strong memory of the entrance channel properties. As a result, understanding the interplay between the entrance and exit channels requires a large amount of experimental systematic studies. These include investigations of the role of beam energy [12, 18], fissility of the compound nucleus [19, 20], deformation of the target [12, 21–24], spherical shells of the collision partners [25, 26], and the neutron-to-proton ratio  $N/Z$  of the compound nucleus [27, 28].

On the theory side, quasifission has been studied with various approaches. This includes classical methods such as a transport model [29], the dinuclear system model [30–33], and models based on the Langevin equation [34–38]. Microscopic approaches such as quantum molecular dynamics [39–41] and the time-dependent Hartree-Fock (TDHF) theory

[14, 15, 27, 38, 42–51] have also been used. See [52–55] for recent reviews on TDHF.

An advantage of microscopic calculations is that their only inputs are the parameters of the energy density functional describing the interaction between the nucleons. Since the latter are usually fitted on nuclear structure properties only, such calculations do not require any parameter determined from reaction mechanisms, such as nucleus-nucleus potentials. In addition, TDHF calculations treat both reaction mechanisms and structure properties on the same footing. This is important for reactions with actinide targets which exhibit a strong quadrupole deformation.

Indeed, the outcome of the calculations strongly depend on the orientation of the nuclei. For instance, TDHF calculations of  $^{40}\text{Ca}+^{238}\text{U}$  reaction showed that only collisions with the side of the  $^{238}\text{U}$  could lead to configurations which are compact enough to enable fusion [14]. This is at variance with collisions with the tip of  $^{238}\text{U}$  which seem to always lead to a fast quasi-fission (after  $\sim 5 - 10$  zeptoseconds of contact time) as long as contact between collision partners is achieved. A remarkable observation of this work was the systematic production of lead nuclei ( $Z = 82$ ), known to possess a strong spherical proton shell gap, in tip collisions only, showing a strong influence of orientation dependent shell effects in the production of the fragments. Such influence of shell effects was proposed to explain peaks in fragment mass distributions [11, 12, 14], but experimental confirmation came only recently with the observation of a peak of quasifission fragments at  $Z = 82$  protons from X-ray measurements [15].

Deformed shell effects in the region of  $^{100}\text{Zr}$  have also been invoked to interpret the outcome of TDHF simulations of  $^{40,48}\text{Ca}+^{238}\text{U}, ^{249}\text{Bk}$  collisions [44, 46]. It is then natural to wonder if other shell effects, spherical or deformed, could be driving the dinuclear system out of its compact shape, into quasifission. Potential candidates are shell effects known to influence the outcome of fission reaction. It has recently been proposed that octupole deformed shell effects, in particular with  $Z$  or  $N = 52 - 56$ , are the main driver to asymmetric fission [56, 57]. The fact that  $^{208}\text{Pb}$  can easily acquire an oc-

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tupole deformation (its first excited state is an  $3^-$  octupole vibration) is compatible with this interpretation. Note also that some superheavy nuclei like  $^{294}\text{Og}$  are expected to encounter super asymmetric fission and produce a heavy fragment around  $^{208}\text{Pb}$  [58–61], conforing the idea that quasifission valleys could match fission ones.

In this work we study the  $^{48}\text{Ca}+^{249}\text{Nk}$  reaction at  $E_{cm} = 234$  MeV with the TDHF approach. Previous TDHF studies of quasifission with actinide targets were restricted to one or two orientations of the target to limit computational time. However, to allow possible comparison with experimental data, it is important to simulate a range of orientations in addition to the usual tip and side configurations. We therefore performed systematic simulations, spanning both a range of orientations and a range of angular momenta. This allow us to study correlations between, e.g., mass, angle, kinetic energy, as well as to predict distributions of neutron and proton numbers at the mean-field level. This distributions are used to identify potential shell gaps driving quasifission. The method is described in section II. The results are discussed in section III. We then conclude in section IV.

## II. METHOD

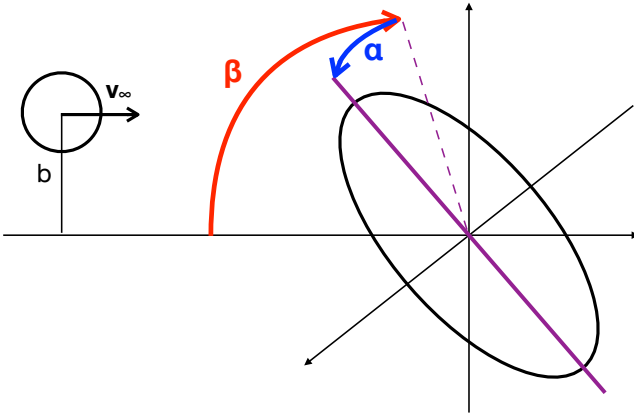


FIG. 1. (Color online) Schematic representation of the initial configuration for an impact parameter  $b$  and a velocity vector  $\mathbf{v}_\infty$  defining the collision plane and the collision axis. The orientation of the target is defined by the angles  $\beta$  (rotation around the axis perpendicular to the reaction plane) and  $\alpha$  (rotation around the collision axis).

Assuming the  $^{249}\text{Bk}$  nucleus to be axially symmetric with no octupole deformation, the cross-section or yield for a specific reaction channel  $\xi$  is proportional to

$$\sigma_\xi \propto \sum_L (2L+1) \int_0^{\pi/2} d\beta \sin\beta \int_0^\pi d\alpha P_L^{(\xi)}(\beta, \alpha). \quad (1)$$

$P_L^{(\xi)}(\beta, \alpha)$  is the probability for the reaction channel  $\xi$  and an orientation of the target defined by the rotation angles  $\beta$  and  $\alpha$  (see Fig. 1). The orientation of the deformation axis is obtained by applying first a rotation of an angle  $\beta$  around the

axis perpendicular to the reaction plane, and then a rotation of an angle  $\alpha$  around the collision axis.

The TDHF calculations are performed for a range of orbital angular momenta  $L_i\hbar$  with  $\{L_i\} = \{0, 10, 20 \dots N_L\}$  and  $N_L = 12$  or 13, depending on the orientation (some orientations lead to quasi-elastic collisions at  $L = 120$ , in which case  $L = 130$  is not computed). The first term is then replaced by

$$\sum_L (2L+1) \rightarrow \sum_{i=1}^{N_L} K_i \quad \text{with} \quad K_i = \sum_{L=L_i-\Delta_i^-}^{L_i+\Delta_i^+} (2L+1),$$

where  $\Delta^+ = 5$ ,  $\Delta_1^- = 0$  and  $\Delta_{i \neq 1} = 1 = 4$ .

The double integral in Eq. 1 is computationally too demanding. The integral over  $\alpha$  is then replaced by a sum over probabilities for  $\alpha = 0$  and  $\pi$ . Equivalently, we can ignore  $\alpha$  and extend the integral over  $\beta$  up to  $\pi$ . We then define the probability

$$\tilde{P}_{L_i}^{(\xi)}(\beta) = \begin{cases} P_{L_i}^{(\xi)}(\beta, 0) & \text{if } \beta \leq \frac{\pi}{2} \\ P_{L_i}^{(\xi)}(\pi - \beta, \pi) & \text{if } \beta > \frac{\pi}{2} \end{cases}.$$

The remaining integral over  $\beta$  is discretised with  $N_\beta = 12$  angles  $\{\beta_n\} = \{0, 15, 30, \dots, 165\}$  deg. We can finally write the approximate cross-section as

$$\sigma_\xi \simeq \sum_{i=1}^{N_L} K_i \sum_{n=1}^{N_\beta} C_n \tilde{P}_{L_i}^{(\xi)}(\beta_n) \quad (2)$$

where we have defined

$$C_n = \begin{cases} 2(1 - \cos \delta) & \text{if } n = 1 \\ \cos(\beta_n - \delta) - \cos(\beta_n + \delta) & \text{if } n > 1 \end{cases}$$

with  $\delta = 7.5$  deg. Note that, because of its semi-classical behaviour, the TDHF theory leads to probabilities  $\tilde{P}_{L_i}^{(\xi)}(\beta_n) = 0$  or 1 for the reaction channel  $\xi$  and for a given orientation and angular momentum.

## III. RESULTS

### A. Quasifission characteristics

The  $^{48}\text{Ca}+^{249}\text{Bk}$  at  $E_{cm} = 234$  MeV has been studied as a function of the orientation  $\beta$  of the target (see Fig. 1) and as a function of orbital angular momentum  $L$ , given in units of  $\hbar$ . Figure 2 shows a typical example of density evolution for

Side collisions ( $\beta \sim 90$  degrees) lead to fusion.

Energy/deformation fast/slow quasifission [64] Fast quasifission [20]

## IV. CONCLUSIONS

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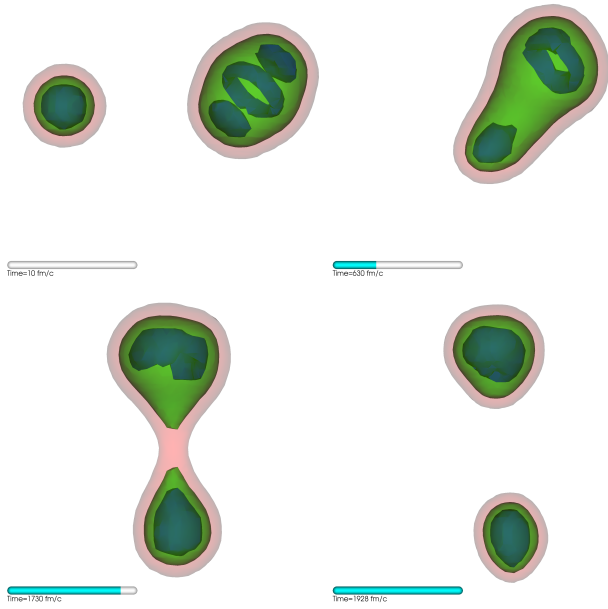


FIG. 2. (Color online) Isodensity surfaces at  $p = XX, YY$  and  $ZZ \text{ fm}^{-3}$  in blue, green and pink, respectively, shown at time  $t = 10$  (a), 630 (b), 1730 (c) and 1928 fm/c (d) for an initial orientation  $\beta = WWW$  degrees and an angular momentum  $Lh = NNh$ . For visualisation purpose, the reaction plane is  $QQ$  degrees off the plane of the page.

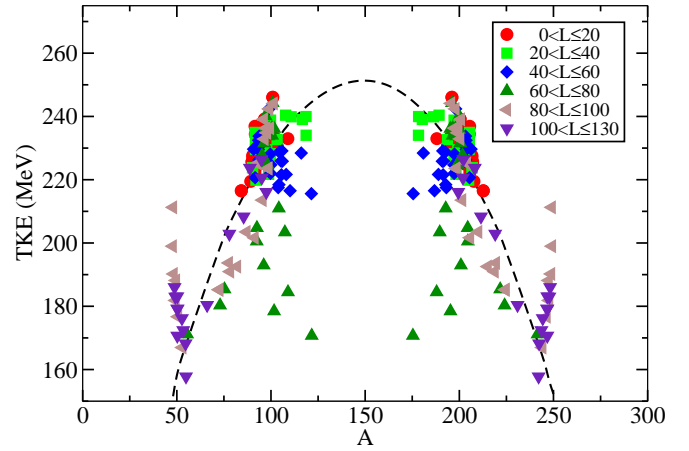


FIG. 3. (Color online) Total kinetic energy of the fragments as a function of their mass ratio. The curve corresponds to the Viola systematics [62, 63].

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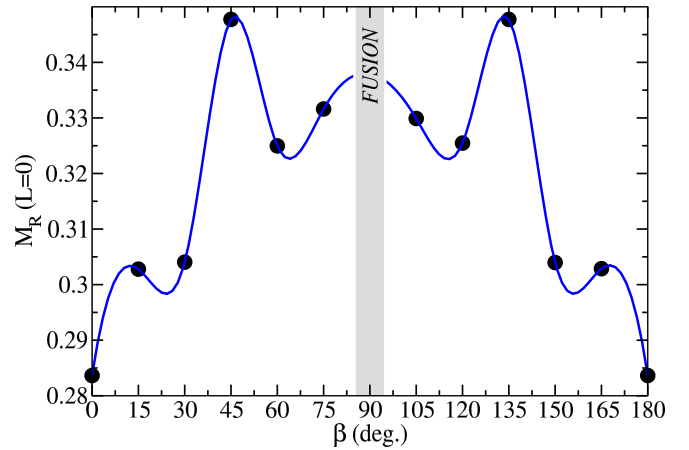


FIG. 4. (Color online) Mass ratio  $M_R$  as a function of orientation angle  $\beta$  for central collisions. Fusion is indicated by the shaded area.

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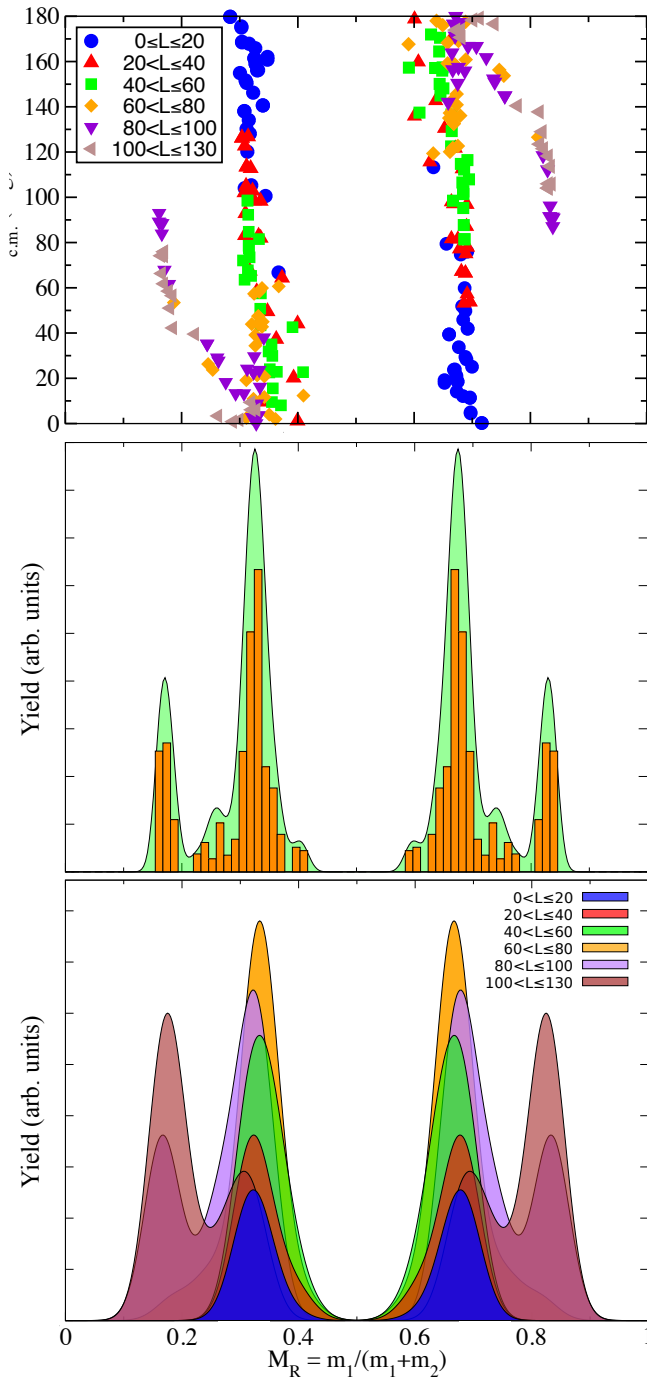


FIG. 5. (Color online). (a) Distribution of scattering angle  $\theta_{cm}$  versus mass ratio  $M_R$  (MAD). The colors correspond to different ranges of angular momenta. (b) Fragment mass yield (histogram). The solid line gives a smooth representation of the histogram using gnuplot k-density function with width  $XX$ . (c) Mass yields obtained for different ranges of angular momenta.

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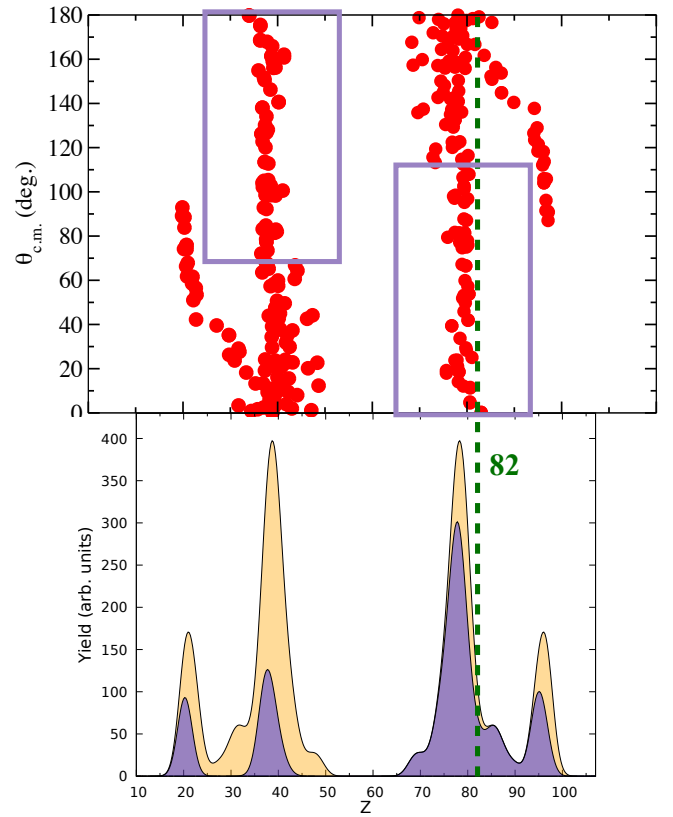


FIG. 6. (Color online). (a) Distribution of scattering angle  $\theta_{cm}$  versus proton number  $Z$  (ZAD). (b) Fragment proton number yield without (black solid line) and with angular cut  $\theta_{cm} > 70$  degrees (dashed line). The vertical lines represent potential proton shell gaps.

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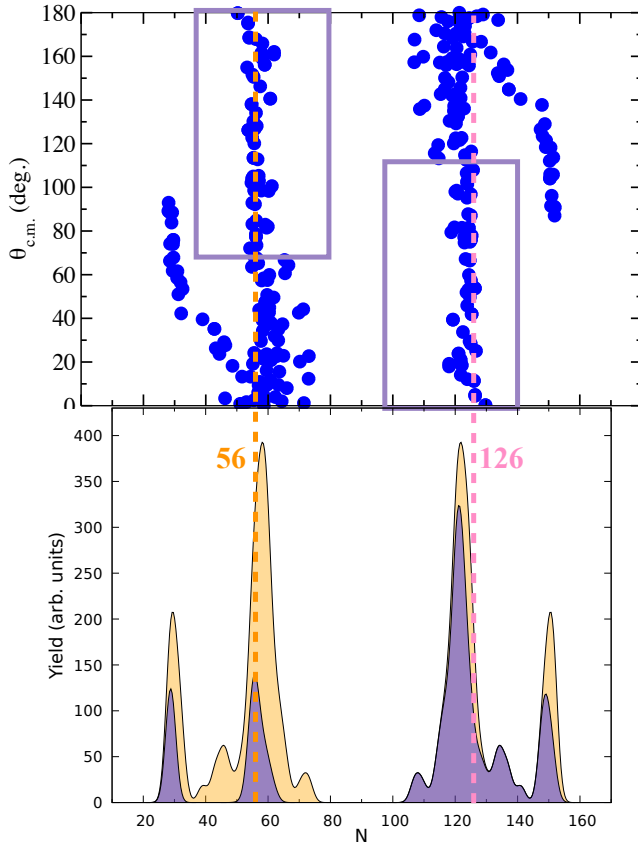


FIG. 7. (Color online). (a) Distribution of scattering angle  $\theta_{cm}$  versus neutron number  $N$  (NAD). (b) Fragment neutron number yield without (black solid line) and with angular cut  $\theta_{cm} > 70$  degrees (dashed line). The vertical lines represent potential neutron shell gaps.

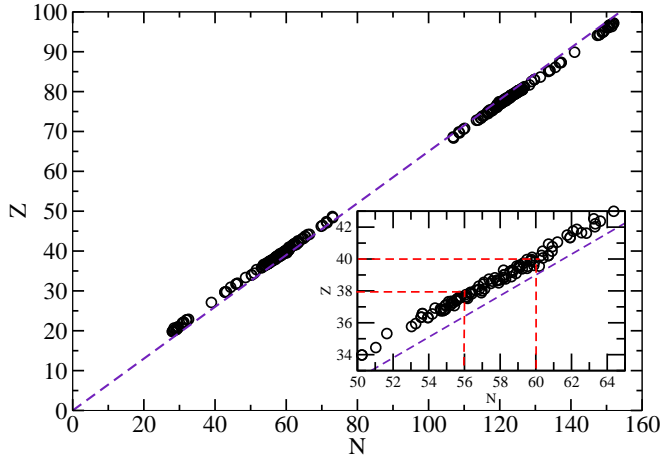


FIG. 8. (Color online). Distribution of proton number  $Z$  versus neutron number  $N$  of the fragments. The dashed line represents the  $N/Z$  ratio of the compound nucleus. The inset is a zoom around the light fragment. Thin dashed lines indicate the positions of  $^{94}\text{Sr}$  ( $Z = 38$ ,  $N = 56$ ) and  $^{100}\text{Zr}$  ( $Z = 40$ ,  $N = 60$ ).

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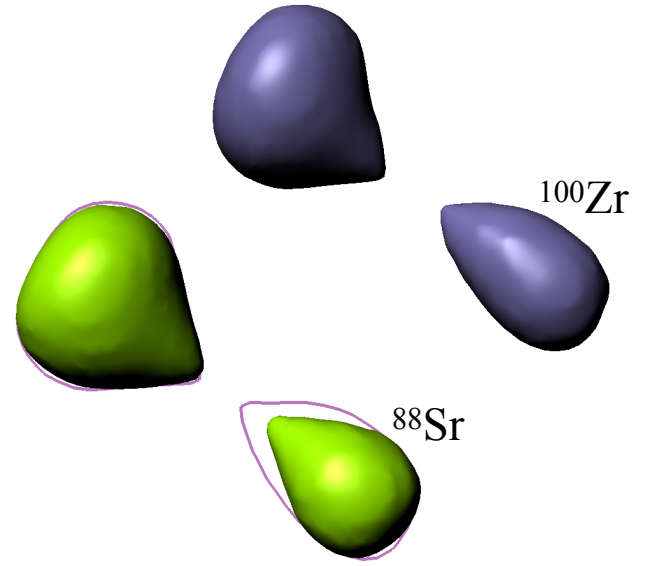


FIG. 9. (Color online). Isodensity surfaces at  $\rho = 0.1 \text{ fm}^{-3}$  for  $L = NN$  and  $\beta = XXX$  degrees (top), and  $L = MM$  and  $\beta = YYY$  degrees (bottom), just after breaking of the neck. The light fragment (right) in the top is a  $^{94}\text{Sr}$  ( $Z = 38$ ,  $N = 56$ ) and a  $^{100}\text{Zr}$  ( $Z = 40$ ,  $N = 60$ ) in the bottom. The contour line in the bottom represents the same density as in the top.

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