

matrix prints position for row/column, vector doesn't.

Note, if you subset a vector from matrix, R automatically drops attribute `dim()`.

e.g. `X[1, c(1:2)]` → vector.

if you want to keep as 1x2 matrix.

`X[1, c(1:2), drop = FALSE]` → matrix.

e.g. `X[X[,1] < 0,]`

select row, produce corresponding columns.

e.g. `X[c(1:2), c(1:2)][2,2]`

order operation.

e.g. `matrix(1:24, 6, 4)[1:2, 1:2]`.

Operations: `*, -, +, /, ^`

element operation.

$$A_{2 \times 2} * B_{2 \times 2} = \begin{bmatrix} a_{11}b_{11} & a_{12}b_{12} \\ a_{21}b_{21} & a_{22}b_{22} \end{bmatrix}$$

$$A_{2 \times 2} + \underbrace{C}_{2 \text{ element vector}} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} + \begin{bmatrix} C_1 & C_1 \\ C_2 & C_2 \end{bmatrix}.$$

$$\text{if } C \text{ is 3 element vector.} \Rightarrow \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} + \begin{bmatrix} C_1 & C_3 \\ C_2 & C_1 \end{bmatrix}.$$

ex. R_{TxN} stock returns
3000 x 1000

$R_F \rightarrow$ 3000 vectors of risk-free rates.

Non-R way

$$R - (R_F - C)_{Tx1 \quad 1 \times N}.$$

R-way

$$R - R_F.$$

Matrix Operations

$$A_{50 \times 5} B_{5 \times 10} = C_{50 \times 10}.$$

$$\underline{A \% * \% B}$$

multiplication of matrix.

Matrix Inversion

$$\text{solve}(A) = A^{-1}$$

Matrix Transpose

$$t(A) \rightarrow \text{transpose}(A')$$

ex. $X_{100 \times 5} \quad Y = X\beta + u.$

$$\beta = (X'X)^{-1}X'Y.$$

$$X'X \leftarrow t(X) \%*\% X.$$

$$X'Y \leftarrow t(X) \%*\% Y.$$

$$\hat{\beta} = (X'X)^{-1}X'Y \leftarrow \text{solve}(XX) \%*\% XY.$$

Faster Way: $XX \leftarrow \text{crossprod}(X)$ \leftarrow upper triangular matrix.
 $XY \leftarrow \text{crossprod}(X, Y)$

3rd type of object: List. \rightarrow collection of elements of possible diff types.

$\text{is(mylist)} \Rightarrow$ "list", "vector".

Accessing the elements

1) `mylist[[1]]`

2) `mylist$name`.

when unique, partial name works too.

3) Subsetting: `mylist[c(1,4)]`.

If you don't know names: use `names(mylist)`.

`names()` works on all objects.

↳ everything is a list!

this is why `res$coef` works!

Data Frame:

\approx matrix Data \rightarrow the k variables could be different.
 $n \times k$.

ex. Income Province Conservative
 ✓ ✓ ✓
 "numerical" "characters" "logical"

If order is the same, `Data$income` is the same as `Data[,1]`.

4th type of object : Functions.

Loops : $X_{100 \times 1}$

$S \leftarrow 0$

① for (i in $1:100$),
 $\{ S \leftarrow S + X[i] \}$.

② $i = 1$

while ($i \leq 100$) {
 $S \leftarrow S + X[i]$
 $i \leftarrow i + 1$ }.

③ $i = 1$

while (TRUE)
 $\{ S \leftarrow S + X[i]$
 $i \leftarrow i + 1$.
 if ($i > 100$)
 break }.

function:

→ write all functions in a single file. (procedure. R).

✓ use source file.

ex.1 mysum ← function(x)
{ n ← length(x)
 for (i in 1:n){
 s ← s + x[i]}
 return(s).
}

ex.2 myplot ← function(f, a, b, np=100,...).
{ x ← seq(a, b, length.out=np).

 y ← f(x, ...). *pass argument.*

 plot(x, y, main="my plot", xlab="x", ylab="y", type="l")
}

myplot(dchisq, 1, 10, df=4)



y = dchisq(x, df=4).