

MIST Pitch REsolving Spectroscopy for Electron Transport: Attitude Determination and Control Systems

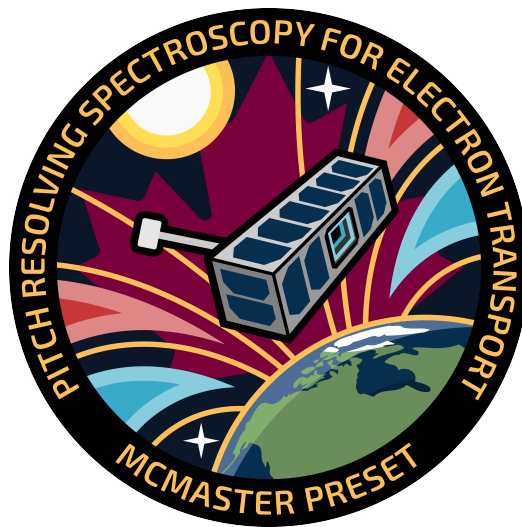
February 26 2024

by

The ADCS Subteam

Lead by Kyle Drury and George Moise

Supervised by Dr. Andrei Hanu



McMaster
University



Abstract

The Attitude Determination and Control Systems (ADCS) used in the McMaster Interdisciplinary Satellite Team's (MIST) latest mission, Pitch REsolving Spectroscopy for Electron Transport (PRESET), is presented. To achieve mission objectives, ADCS features an active magnetorquer-based control system. The onboard magnetometer determines attitude, and actuation is achieved by passing pulse width modulated currents through the three orthogonally-placed torque rods. In this paper, the selected hardware and the various control mods that will be implemented will be reviewed. Furthermore, the control algorithms and the mathematical framework that ungirds these algorithms will be explained in detail.

Contents

1	Introduction	4
2	Quantifying the Disturbance Environment	5
2.1	Gravity Gradient	5
2.2	Solar Pressure	5
2.3	Aerodynamic Drag	5
2.4	Magnetic Torque	5
3	Attitude Determination and Control System	6
3.1	Reference Frames	6
3.1.1	Earth-Centered Inertial (ECI) Frame	6
3.1.2	Earth-Centered Earth-Fixed (ECEF) Frame	6
3.1.3	Orbital (O) Frame	6
3.1.4	Satellite Body (B) Frame	7
3.2	Attitude Representation	7
3.2.1	Direction Cosine Matrix	7
3.2.2	Euler Angles	7
3.2.3	Quaternion Representation	8
3.3	Rotational Kinematics and Dynamics	9
3.3.1	Angular Velocity and Momentum	9
3.3.2	Equations of Motion	10
3.3.3	Kinematic Equations	10
3.4	Attitude Determination	10
3.4.1	Sensors	10
3.4.2	Attitude Determination Technique	10
3.5	Attitude Control Maneuvers	12
3.5.1	Actuation	12
3.5.2	Bdot Detumbling Algorithm	12
3.5.3	Initial Alignment	13
3.5.4	y-Axis Alignment	13
3.5.5	Spin-Up	14
3.5.6	Orbital Plane Alignment	14
3.5.7	Spin-Axis Tilt Correction	15
3.5.8	Spin-Axis Realignment Corrections	15
4	PRESET ADCS	17
4.1	PRESET ADCS Hardware	17
4.2	Custom Magnetorquers	17
4.2.1	Air-Cored Magnetorquer	17
4.2.2	Ferromagnetic-Cored Magnetorquers	18
4.3	PRESET ADCS Algorithms	18
4.3.1	ADCS Modes	18

List of Abbreviations

ADCS	Attitude Determination and Control Systems
CDH	Command and Data Handling
DCM	Direction Cosine Matrix
ECEF	Earth-Centered Earth-Fixed
EKF	Extended Kalman Filter
IGRF	International Geomagnetic Reference Frame
KF	Kalman Filter
MIST	McMaster Interdisciplinary Satellite Team
OBC	On-Board Computer
PRESET.....	Pitch REsolving Spectroscopy for Electron Transport
TQR	Magnetorquer/Torquer

1 Introduction

The latest MIST mission, PRESET, aims to determine the angular and energy spectrums of energy-depositing electrons in the Earth's Van Allen Belts. The Van Allen Belts are regions of the geomagnetic field with high concentrations of charged subatomic particles. These particles enter the magnetosphere at different angles and with different energies and deposit a portion of their energy depending on the angle of their trajectory with respect to the local magnetic field. This energy deposition drives atmospheric processes such as ozone loss, and for this reason, MIST is conducting a precise experiment to determine how much energy is being deposited, and what sorts of particles are making up the bulk of this contribution.

These charged particles are most concentrated at the magnetic poles, and for this reason, PRESET aims to achieve a sun-synchronous polar orbit to collect data. For collecting angular and energy data, PRESET is armed with a collimator comprised of sensitive detectors. To achieve mission objectives, the satellite must achieve a spin rate of 30 deg/s in one of the two spin configurations:

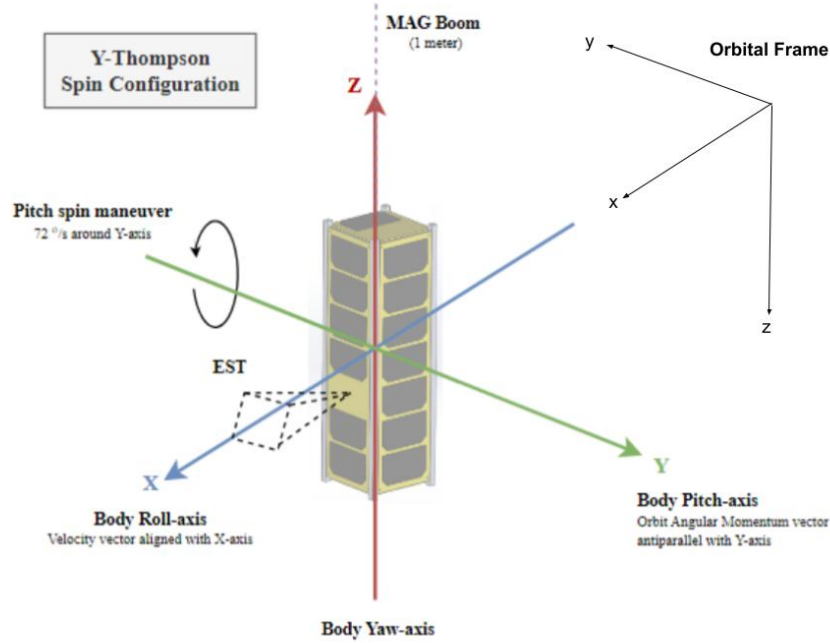


Figure 1: Y-Thompson and Yaw-Orbit Spin Configurations

Spin-stabilization is achieved using magnetic actuators, controlled by a Nanomind On-Board Computer (OBC). The magnetic field is measured using a magnetometer built into the OBC, and angular rates are determined with either the built-in gyroscope or the rotation of the geomagnetic field vector in the satellite frame.

2 Quantifying the Disturbance Environment

To perform actuator-sizing calculations, it is critical to know what sort of disturbance torques are expected. To this end, four main sources of disturbance torques will be considered; gravity gradient, aerodynamic, solar pressure, and magnetic torques [5]. Just to make sure that mission objectives are attainable, a worst-case scenario is imagined for these sizing calculations. In particular, we imagine that the 6kg 3U CubeSat has a uniform density throughout, except on one of the sides, where we imagine the 1.7kg payload takes up an entire U of volume.

2.1 Gravity Gradient

The gravity gradient torque is caused by differential gravitational forces along the body of the satellite and is denoted \mathbf{T}_{gg} . It is given by the following:

$$\vec{T}_{gg} = \frac{3\mu}{r_p^3} |\vec{I}_{max} - \vec{I}_{min}| \sin 2\theta \quad (2.1)$$

where μ is the gravitational parameter $3.986 \times 10^{14} \text{m}^3 \text{s}^{-2}$, r_p is the periapsis radius in meters, θ is the angular deviation from the nadir, and $\mathbf{I}_{\min/\max}$ is the minimum/maximum moment of inertia about either of the principle axes. The gravity gradient torque is found to be on the order of 10^{-7}Nm .

2.2 Solar Pressure

Solar pressure torque is caused by photons that impinge on the satellite's surface and transfer some of their momentum, giving rise to a force that has the potential to turn the satellite. It is denoted as \mathbf{T}_{sp} and given by the following:

$$\vec{T}_{sp} = \frac{\Phi}{c} A_{sp} (1 + q) \cos(i) |\vec{c}_{sp} - \vec{c}_g| \quad (2.2)$$

where Φ is the solar flux (which is $1367 \text{W/m}^2 \pm 3\%$ at the Earth's orbit), \vec{c}_{sp} and \vec{c}_g are the centers of solar pressure and gravity, i is the angle between the normal and the photons, q is the reflectivity of the material (derived from the absorptivity of the solar cells, which over the majority of the satellite surface), A_{sp} is the projected area along the sun vector, and c is the speed of light. \vec{T}_{sp} is found to be on the order of 10^{-11}Nm .

2.3 Aerodynamic Drag

This torque is caused by the air resistance met by the satellite traveling through the high atmosphere. It is denoted \mathbf{T}_{sp} and given by the following:

$$\vec{T}_a = \frac{1}{2} \rho_{atm,p} C_D A_a v_p^2 |\vec{c}_a - \vec{c}_g| \quad (2.3)$$

At a 500km orbit, the atmospheric density ρ_{atm} is $7 \times 10^{-13} \text{kg/m}^3$. The drag coefficient C_D is taken to be a liberal 2.5, and the velocity at the periapsis is approximately 4300 m/s. \mathbf{c}_a is the pressure center, and \mathbf{c}_g is again the center of gravity. The aerodynamic drag torque is found to be on the order of 10^{-9}Nm .

2.4 Magnetic Torque

The magnetic torque is caused by the magnetic component in the satellite and electrical currents traveling through circuit boards and other electrical components. A precise determination of the satellite dipole moment is a complex matter, but we can make some approximations.

$$\vec{T}_m = D_m \frac{\lambda M_m}{r_p^3} \quad (2.4)$$

M_m is the magnetic moment of the Earth, given as $7.96 \times 10^{15} \text{ Tm}^3$. λ is a unitless parameter in [1,2] that depends on the inclination of the satellite orbit. Since PRESET is in a polar orbit, $\lambda = 2$. The periapsis radius is again taken to be 500km above the Earth's surface. According to [?], D_m typically ranges between 0.1 and 20 Am^2 . If we refer to the CubeSpace page for the torque rods, the CR0003 is suitable for 3U cubesats like PRESET, and is capable of a dipole moment of 0.3 Am^2 . For this reason, we will take D_m to be 0.3 Am^2 . Making these substitutions yields a magnetic torque on the order of 10^{-5} Nm . From this, it is clear that the magnetic torque will be the dominant disturbance on the satellite by two orders of magnitude.

3 Attitude Determination and Control Systems

3.1 Reference Frames

3.1.1 Earth-Centered Inertial (ECI) Frame

The ECI frame is of fundamental importance; it provides a constant framework upon which all other frames can be represented. With the origin at the center of the earth, the \hat{z} -axis is pointed toward the magnetic north pole, the \hat{x} -axis is in the direction of the vernal equinox, and the \hat{y} -axis completes the orthogonal triad [8]. the ECI reference frame is referred to by the vector $\mathbf{I} = \{i_x, i_y, i_z\}$.

3.1.2 Earth-Centered Earth-Fixed (ECEF) Frame

The ECEF frame shares the \hat{z} -axis with the ECI frame, except the \hat{x} -axis is pointed in the direction of the Prime Meridian, and the \hat{y} -axis completes the orthogonal triad [8]. The ECEF frame is referred to by the vector $\mathbf{E} = \{\epsilon_x, \epsilon_y, \epsilon_z\}$.

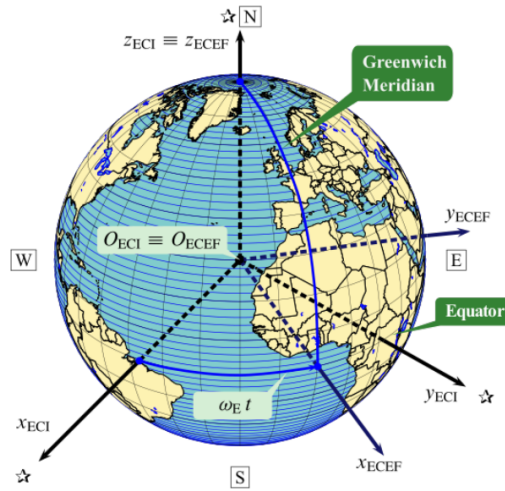


Figure 2: The ECI and ECEF frames [8]

3.1.3 Orbital (O) Frame

The O frame origin is located at the satellite body center of mass, with the \hat{z} -axis pointing along the nadir, the \hat{x} -axis along the satellite velocity vector, and the \hat{y} -axis completes the orthogonal triad. The O frame is referred to by the vector $\mathbf{O} = \{o_x, o_y, o_z\}$.

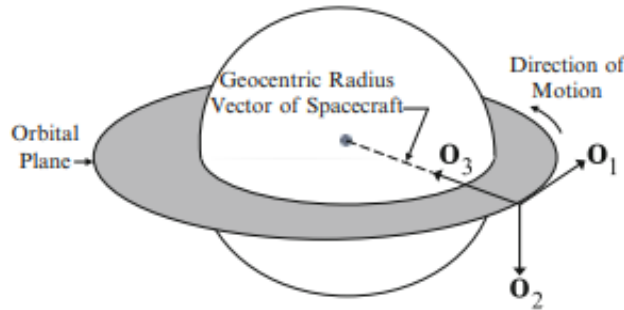


Figure 3: The classical orbital frame [5]

3.1.4 Satellite Body (B) Frame

The SB frame origin is at the satellite center of mass, and the axes are fixed with respect to the principal axes of the satellite body. The B frame is referred to be the vector $B = \{b_x, b_y, b_z\}$. This coordinate system is depicted in Figure 1.

3.2 Attitude Representation

There are three common ways that orientations in 3D space can be described. This section outlines the Direction Cosine Matrix (DCM), the Euler angles representation, and the quaternion representation.

3.2.1 Direction Cosine Matrix

The DCM matrix \mathcal{C} is a rotation that transforms a vector in an initial frame to a target frame by representing the axes of the target frame in terms of the initial frame. The DCM matrix is definitionally invertible, and is given by the following equations:

$$\hat{b}_1 = \mathcal{C}_{11}\hat{a}_1 + \mathcal{C}_{12}\hat{a}_2 + \mathcal{C}_{13}\hat{a}_3 \quad (3.1)$$

$$\hat{b}_2 = \mathcal{C}_{21}\hat{a}_1 + \mathcal{C}_{22}\hat{a}_2 + \mathcal{C}_{23}\hat{a}_3 \quad (3.2)$$

$$\hat{b}_3 = \mathcal{C}_{31}\hat{a}_1 + \mathcal{C}_{32}\hat{a}_2 + \mathcal{C}_{33}\hat{a}_3 \quad (3.3)$$

where \vec{b} is target frame and \vec{a} is the initial frame and \hat{a}, \hat{b} are unit length. From this, it can be seen where the DCM gets its moniker:

$$\mathcal{C}_{ij} = \hat{b}_i \cdot \hat{a}_j = \cos \alpha_{ij} \quad (3.4)$$

The DCM has the property that its inverse is equal to its transpose. Furthermore, a DCM that goes from frame A to B and a DCM from B to C can be combined to give a DCM that goes from A to C.

3.2.2 Euler Angles

Euler's rotation theorem states that any rotation can be described by composing three separate rotations θ, ϕ, ψ about the coordinate axes $\hat{x}, \hat{y}, \hat{z}$.

$$\mathbf{R}_x(\theta) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{bmatrix} \quad (3.5)$$

$$\mathbf{R}_y(\phi) = \begin{bmatrix} \cos \phi & 0 & \sin \phi \\ 0 & 1 & 0 \\ -\sin \phi & 0 & \cos \phi \end{bmatrix} \quad (3.6)$$

$$\mathbf{R}_z(\psi) = \begin{bmatrix} \cos \psi & -\sin \psi & 0 \\ \sin \psi & \cos \psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (3.7)$$

Now any rotation R can be described by $R_x(\theta) \cdot R_y(\phi) \cdot R_z(\psi)$. A limitation of this representation is known as "gimbal lock," which happens when a degree of freedom is lost when a 90° rotation is performed [3].

3.2.3 Quaternion Representation

The quaternion representation is an outgrowth of Euler's theorem that states that any orientation in 3D space can be expressed as a single rotation about the so-called "Euler axis." A quaternion \mathbf{q} consists of a scalar part q_4 and vector part $[q_1, q_2, q_3]$:

$$\mathbf{q} = \begin{bmatrix} \vec{q} \\ q_4 \end{bmatrix} = \begin{bmatrix} q_1 \\ q_2 \\ q_3 \\ q_4 \end{bmatrix} \quad (3.8)$$

The components of \mathbf{q} can be expressed in terms of the Euler axis $\vec{e} = \{e_x, e_y, e_z\}$ and the Euler angle θ :

$$\begin{aligned} q_1 &= \hat{e}_x \sin(\theta/2) \\ q_2 &= \hat{e}_y \sin(\theta/2) \\ q_3 &= \hat{e}_z \sin(\theta/2) \\ q_4 &= \cos(\theta/2) \end{aligned} \quad (3.9)$$

The four quaternion components satisfy

$$\sqrt{q_1^2 + q_2^2 + q_3^2 + q_4^2} = \|\mathbf{q}\| = 1 \quad (3.10)$$

The DCM can be expressed in terms of the attitude quaternion as follows [2]:

$$\mathbf{R}(\mathbf{q}) = \begin{bmatrix} q_1^2 - q_2^2 - q_3^2 + q_4^2 & 2(q_1q_2 + q_3q_4) & 2(q_1q_3 + q_2q_4) \\ 2(q_1q_2 - q_3q_4) & -q_1^2 + q_2^2 - q_3^2 + q_4^2 & 2(q_2q_3 + q_1q_4) \\ 2(q_1q_3 + q_2q_4) & 2(q_2q_3 - q_1q_4) & -q_1^2 - q_2^2 + q_3^2 + q_4^2 \end{bmatrix} = (q_4^2 - \|\mathbf{q}\|^2)\mathbf{I}_3 + 2\mathbf{q}\mathbf{q}^T - 2q_4[\mathbf{q}\times] \quad (3.11)$$

where $[\mathbf{q}\times]$ is the cross product matrix defined as

$$[\mathbf{q}\times] = \begin{bmatrix} 0 & -q_3 & q_2 \\ q_3 & 0 & -q_1 \\ -q_2 & q_1 & 0 \end{bmatrix} \quad (3.12)$$

Conversely, the quaternion components can be represented in terms of the matrix elements of the DCM:

$$\begin{aligned} q_1 &= \frac{1}{4q_4}(\mathcal{C}_{23} - \mathcal{C}_{32}) \\ q_2 &= \frac{1}{4q_4}(\mathcal{C}_{31} - \mathcal{C}_{13}) \\ q_3 &= \frac{1}{4q_4}(\mathcal{C}_{12} - \mathcal{C}_{21}) \\ q_4 &= \pm \frac{1}{2}\sqrt{1 + \mathcal{C}_{11} + \mathcal{C}_{22} + \mathcal{C}_{33}} \end{aligned} \quad (3.13)$$

Another interesting property of the quaternion \mathbf{q}_b^a is that its inverse \mathbf{q}_a^b is also its conjugate $\overline{\mathbf{q}_b^a}$, where the conjugate of \mathbf{q} is given by

$$\mathbf{q} = \begin{bmatrix} -\vec{q} \\ q_4 \end{bmatrix} = \begin{bmatrix} -q_1 \\ -q_2 \\ -q_3 \\ q_4 \end{bmatrix} \quad (3.14)$$

In addition, a rotation matrix acting on a vector can be represented by multiplying the vector on the right side by a quaternion, and the left side by its quaternion conjugate:

$$\begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ 0 \end{bmatrix} = \overline{\mathbf{q}_a^b} \otimes \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ 0 \end{bmatrix} \otimes \mathbf{q}_a^b \quad (3.15)$$

Similar to rotation matrices, $\mathbf{q}_b^c \otimes \mathbf{q}_a^b = \mathbf{q}_a^c$.

3.3 Rotational Kinematics and Dynamics

3.3.1 Angular Velocity and Momentum

In rotational dynamics, we are often interested in the rate at which one frame rotates with respect to another frame. The shorthand ω_a^b is adopted to denote the angular velocity of frame B in frame A. From this, some simple properties of ω can be extrapolated, such as

$$\begin{aligned} \vec{\omega}_a^b &= -\vec{\omega}_b^a \\ \vec{\omega}_a^b + \vec{\omega}_b^c &= \vec{\omega}_a^c \end{aligned} \quad (3.16)$$

The derivative of a vector in a different frame is given by

$$\frac{d\vec{v}_b}{dt} = \frac{d\vec{v}_a}{dt} + \vec{\omega}_a^b \times \vec{v}_a \quad (3.17)$$

If a satellite (or any rigid body) in frame S is spinning at some rate ω_i^s with respect to some inertial frame i, then the angular momentum of the body is

$$\vec{h}_s = \mathbf{J}\omega_i^s \quad (3.18)$$

where $[\mathbf{J}]$ is the standard 3x3 inertia tensor.

3.3.2 Equations of Motion

Under the influence of an external torque, a rigid body in an inertial frame experiences a change in angular momentum:

$$\frac{d\vec{h}_i}{dt} = \vec{\tau}_{ext} \quad (3.19)$$

From (4.2), it follows that

$$\frac{d\vec{h}_a}{dt} + \vec{\omega}_i^a \times \vec{h}_a = \frac{d\vec{h}_i}{dt} = \vec{\tau}_{ext} \quad (3.20)$$

where A is some arbitrary rotating reference frame rotating with respect to inertial frame I. Equations (3.17) through (3.20) can be used to show that

$$\frac{d\omega_i}{dt} = \mathbf{J}^{-1}(\vec{\tau}_{ext} - \vec{\omega}_i \times \mathbf{J}\vec{\omega}_i) \quad (3.21)$$

3.3.3 Kinematic Equations

The kinematic equations are a set of differential equations that can be solved to give the satellite's equation(s) of motion. We shall use the quaternion differential equations of motion that were used in the NEUDOSE analysis [?]:

$$\begin{aligned}\dot{\mathbf{q}} &= \mathbf{q} \otimes [0 \ \omega_x \ \omega_y \ \omega_z] \\ I_x \dot{\omega}_x + (I_y - I_z) \omega_y \omega_z &= T_x \\ I_y \dot{\omega}_y + (I_x - I_z) \omega_x \omega_z &= T_y \\ I_z \dot{\omega}_z + (I_y - I_x) \omega_x \omega_y &= T_z\end{aligned}\tag{3.22}$$

3.4 Attitude Determination

The sensors and computational algorithms used in the PRESET mission will be outlined in this section.

3.4.1 Sensors

Magnetometer: a device that can measure the strength and direction of a local magnetic field.

Gyroscope: an inertial sensor capable of measuring angular acceleration around three orthogonal axes. Data can be integrated with respect to time to determine the angular rate of the device in an inertial frame.

3.4.2 Attitude Determination Technique

To determine the satellite attitude in the ECI frame, the magnetometer tracks the local magnetic field for about twenty minutes. From this data, the orientation of the satellite shall be determined. The PRESET ADCS system focuses on using simple strategies to minimize risks (attitude determination and/or control failure), reduce computing power costs, and ensure maximum robustness. The approach outlined in this section is inspired by [4] relies on the fact that the spin configuration (Y-Thompson, Figure 1) is known.

1. The objective is to fit the magnetometer data using two parameters θ and ϕ to determine the direction of PRESET's axis of rotation (ie. the body \hat{y} -axis) by using the known *International Geomagnetic Reference Frame* data, a model of the geomagnetic field in the ECEF frame. To do this, we derive a generalized rotation matrix to transfer between the ECEF/IGRF frame to the satellite body frame. In other words, we derive a relationship between the field vector in the ECEF frame to the body frame given the radial and azimuthal displacement from the desired attitude.
2. Suppose that the body frame is initially in the correct position; that is, the body \hat{y} axis is aligned with the negative orbital \hat{y} -axis. This is accomplished by rotating the frame about the \hat{x} -axis by π radians.
3. Furthermore, let us now assume that the axis has shifted in the radial direction toward the velocity vector from the negative orbital \hat{y} -axis by θ . This amounts to a rotation about the orbital \hat{z} -axis by θ . Then suppose that this axis is rotated in the azimuthal angle by ϕ . In this case, the axis of rotation would be \hat{e} , the $-\hat{y}$ -axis rotated by $\frac{\pi}{2} + \theta$.
4. If the spin-axis has shifted in the body frame, then there will be a further rotation about \hat{e} by some angle; given the inertia tensor of PRESET, we expect this angle to be 1.3° in the $+\hat{z}$ direction (however, this might not be the case; this would be an added parameter if the non-rotated fit model isn't successful).
5. Finally, we must account for the actual rotation of the satellite at rate ω around the axis we had at the end of step 3. Denote this vector \vec{S} .

Working our way backward through the steps, our 2-parameter expression for the IGRF field in the body frame is given by

$$\begin{aligned}\vec{B}_B &= C_{B,O} \cdot C_{O,ECEF} \cdot \vec{B}_{ECEF}(\varphi, \xi, r) \\ &= [R_{\vec{S}}(\omega t) \cdot R_{\vec{e}}(1.3 \text{ deg}) \cdot R_{\vec{e}}(\phi) \cdot R_{\vec{z}}(\pi/2 + \theta) \cdot R_{\vec{x}}(\pi)] \cdot C_{O,ECEF} \cdot \vec{B}_{ECEF}\end{aligned}\quad (3.23)$$

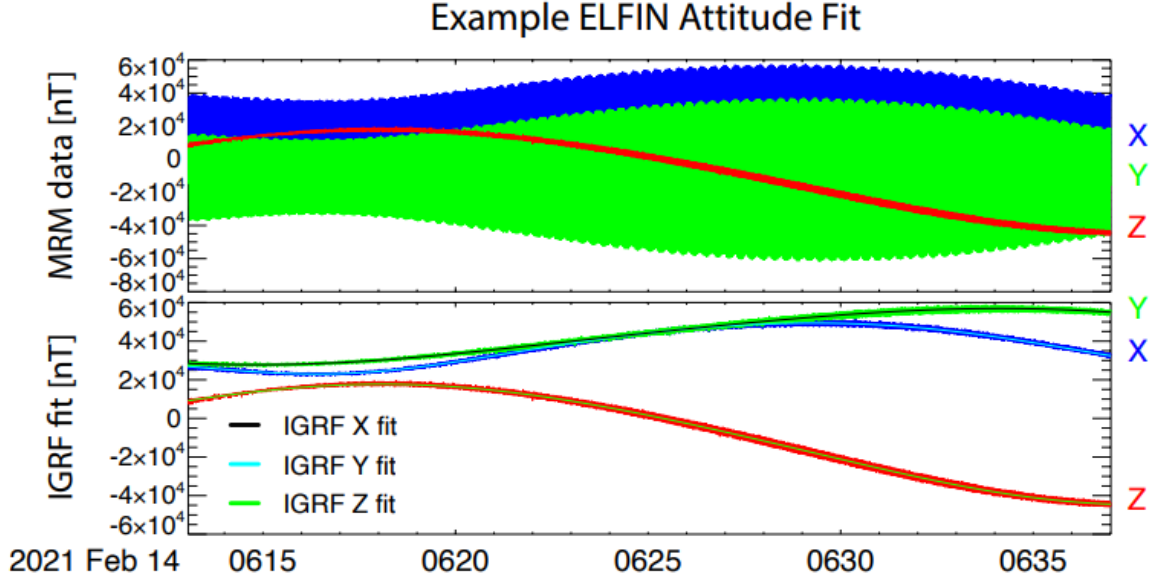


Figure 4: Fitting magnetometer data [4]

The fit is validated by performing more than 100 fits with different initial guesses evenly distributed over a sphere. Fits with the lowest uncertainties tend to line up, giving the operator a good indication of the true orientation of the satellite.

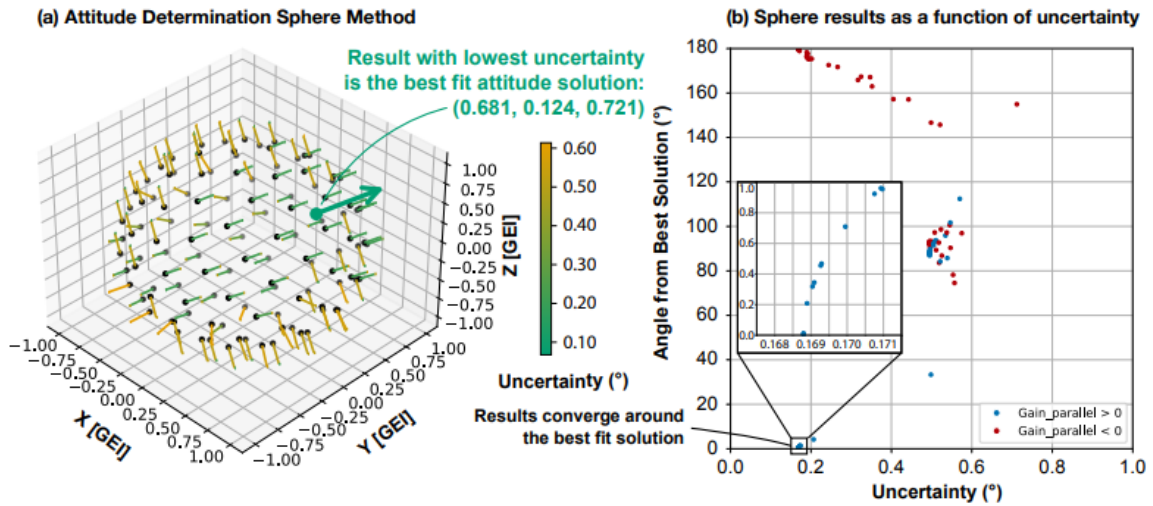


Figure 5: Fit validation using the so-called "sphere method." Note that all the green axes are parallel or antiparallel [4]

3.5 Attitude Control Maneuvers

This section will briefly discuss the actuators used in the PRESET mission and will go into detail about control algorithms.

3.5.1 Actuation

Magnetic Torquers (TQRs): Also known as torquers, torque rods, or magnetorquers, these actuators consist of a conducting wire wound around either an air-cored frame or a ferromagnetic rod. When a potential difference is applied, a magnetic dipole moment that interacts with the local geomagnetic field generates a torque on the satellite. Using three orthogonally placed torquers, 3-axis control can be achieved.

3.5.2 Bdot Detumbling Algorithm

When the satellite deploys, it must be detumbled into a stationary orientation using the Bdot control algorithm. The idea behind this algorithm is to produce a magnetic dipole moment using the onboard TQRs to generate a torque that opposes the natural rotation of the satellite. The Bdot control law is stated as [7]:

$$\vec{\mu}_{Bdot} = -K_b \vec{B} \quad (3.24)$$

where K_b is a gain constant that accounts for the torque rod specifications and the satellite properties. The control torque that results from this dipole moment is calculated from the standard cross-product with the geomagnetic field vector.

To derive K_b , consider the geomagnetic field, which varies between 25,000 nT and 65,000 nT. We also note the maximum rate we expect to be spinning at upon deployment ω_{max} (this will be provided when a launch provider is determined), and the maximum dipole moment produced by the actuators μ_{max} . If the satellite is spinning perpendicular to the geomagnetic field, then along a given axis, $B_i = B \cos \omega_{max} t$, so $\vec{B}_i = -B \omega_{max} \sin \omega_{max} t$. In this case,

$$\text{Max}[\vec{B}_i] = B_{max} \omega_{max} \quad K_b = \frac{\mu_{max}}{B_{max} \omega_{max}} \quad (3.25)$$

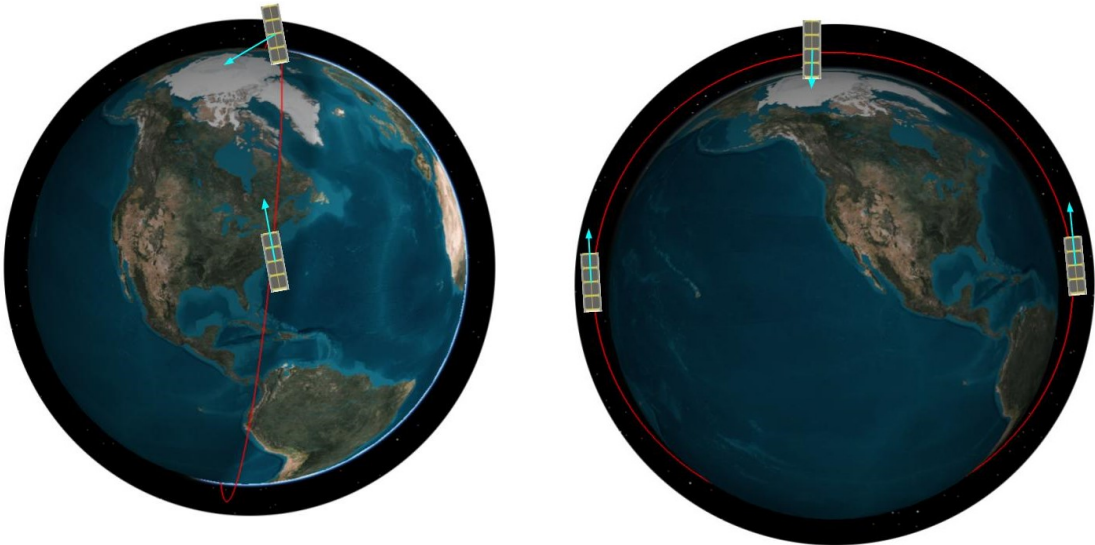


Figure 6: PRESET in polar orbit with field vector at poles and equator

3.5.3 Initial Alignment

All maneuvering will be done near the equator or poles, as these are the regions that will allow us to align the satellite such that it can be spun-up.

Initial alignment shall be achieved by magnetizing PRESET's z-TQR near the equator so it will be align with the magnetic field in the equatorial region. This ensures that we will be able to properly PRESET's \hat{y} -axis with the equator at the poles. This is because the attitude in the ECI frame will be the same throughout the orbit.

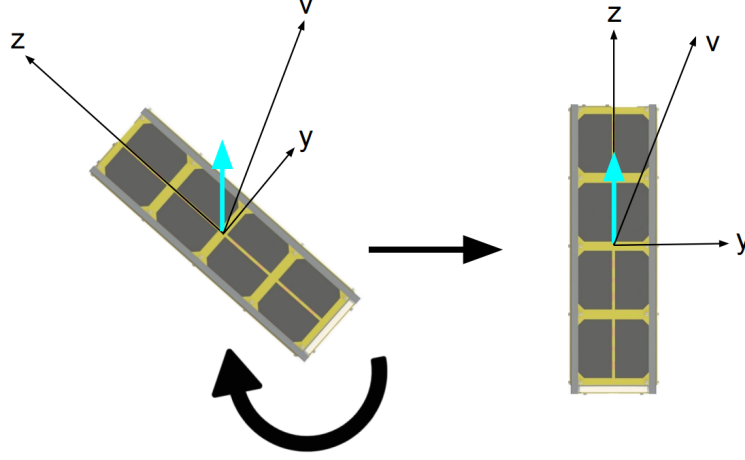


Figure 7: Aligning the \hat{z} -axis at the equator to prepare for y-Axis alignment at the poles

3.5.4 y-Axis Alignment

When the \hat{z} -axis is in line with the field at the equator, when PRESET gets to the polar regions, it's \hat{x} -axis should be in parallel with the equator, and the field should be contained in the body yz plane. This geometry allows us to ensure that any tilt about the \hat{x} -axis can be corrected by either magnetizing the y-TQR, z-TQR, or both, depending on the instantaneous attitude.

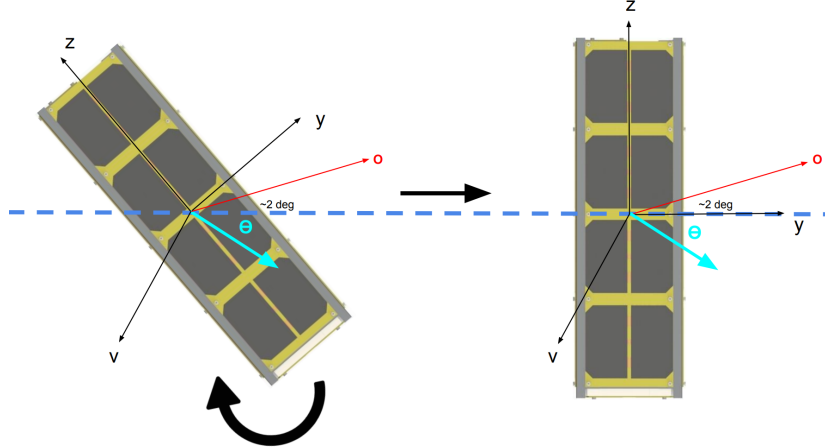


Figure 8: y-Axis Alignment at the poles. Torque can be generated using the z or y torquers, or by using both of them to attain an orientation given by θ .

3.5.5 Spin-Up

Once \hat{y} -axis alignment has been achieved, the desired spin-axis will be perpendicular to the magnetic field over the entire orbit, except close to the poles. From here, spin-up can be achieved by pulsing the

z-TQRs or magnetizing the y-TQRs, depending on the rate of rotation and instantaneous attitude of the satellite. Spin-up will proceed until a rotation rate of 25 deg/s is achieved.

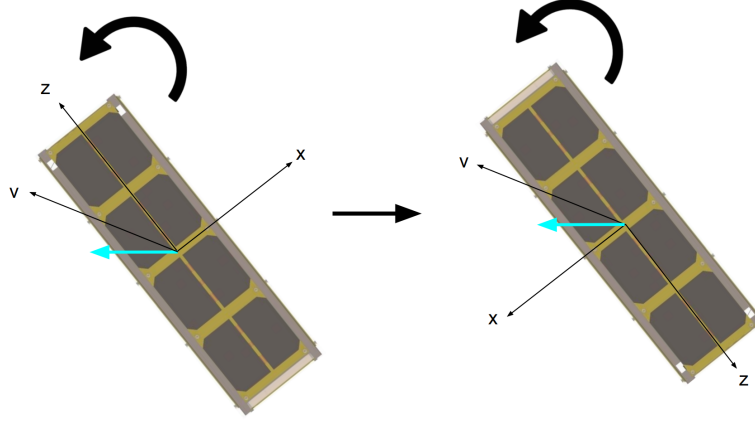


Figure 9: Spin-Up by pulsing the z-TQR at the frequency of rotation. Spin-up can be initiated by magnetizing the y-TQR to avoid using too much power.

3.5.6 Orbital Plane Alignment

Once the nominal rotation rate is achieved, PRESET needs to be shifted into the proper Y-Thompson spin configuration. This can be done near the equators by magnetizing the y-TQR, causing PRESET to rotate about the nadir until it's spin-plane is in the orbital plane. For more precision, the y- and z-TQRs can be pulsed in concert at the exact angle the velocity vector makes with the orbital plane (similar to the strategy employed at the poles in \hat{y} -axis alignment).

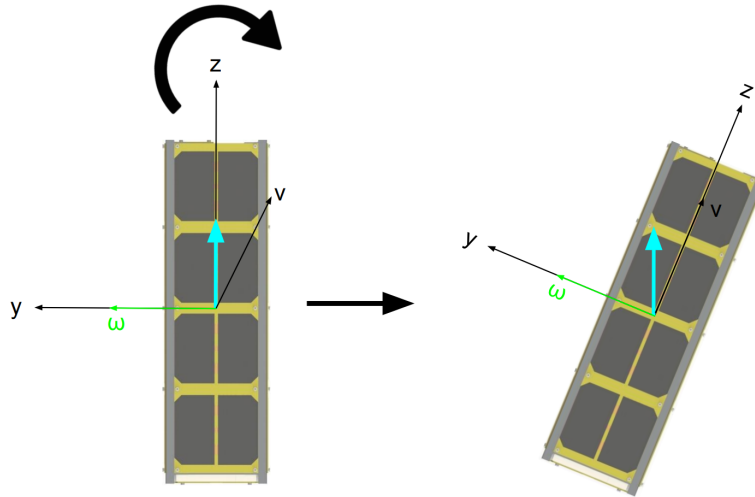


Figure 10: Align the spin plane with the orbital plane by either magnetizing the y-TQR, pulsing the z-TQR, or pulsing both the y- and z-TQRs together.

3.5.7 Spin-Axis Tilt Correction

When the spin-axis tilts toward the positive \hat{z} -axis, as we expect it to given the PRESET inertia tensor, this deviation needs to be corrected. We expect the tilt to be about 1.3° . This error can be corrected in fashion very similar to the orbital plane alignment, except instead of simply magnetizing the y-TQR, the y- or z-TQRs *must* be pulsed at the precise moments the satellite yz plane is in-line

with the field vector. Each magnetization/pulse will provide PRESET a small kick that will bring it back into Y-Thompson.

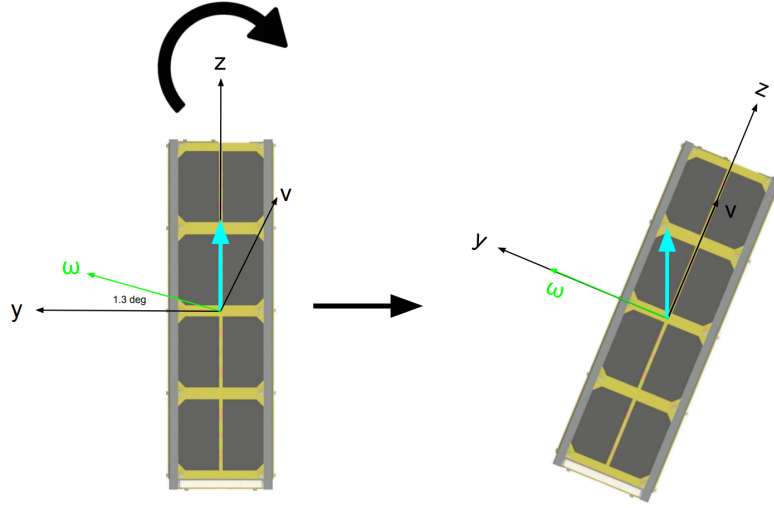


Figure 11: Correct the spin-axis tilt by pulsing either the y- or z-TQRS, or both at the same time with an angle of 1.3° .

3.5.8 Spin-Axis Realignment Corrections

If the entire spin-axis becomes misaligned (ie. angular momentum of PRESET in the inertial frame has changed due to disturbances), then previously discussed maneuvers can be used to correct this. In particular, if...

- PRESET becomes tilted about the orbital x-axis, this can be corrected with a y-axis alignment maneuver at the poles
- PRESET becomes tilted about orbital z-axis, this can be corrected using an orbital plane alignment maneuver at the equator
- PRESET angular rate becomes too fast/slow, rate corrections performed by reversing the orbital alignment maneuver, then spinning up/down

4 PRESET ADCS

4.1 PRESET ADCS Hardware

The PRESET ADCS is controlled via the AVR32 Microcontroller within the ADCS-dedicated onboard computer (OBC) by GomSpace. The OBC is provided with 3.3V by the BUS that can be used to move pulse-width-modulated current through the torque rods. The Nanomind also has a built-in gyroscope, magnetometer, and H-Bridge. The ADCS OBC is connected to the main PC104 board for communications with other subsystems in the satellite.

4.2 Custom Magnetorquers

PRESET ADCS features two ferromagnetic-cored torquers placed within the frame of a third air-cored TQR to minimize its size. PRESET opted to manufacture a system in-house so that specifications could better-fit requirements.

The criteria for optimizing the TQRs are as follows:

1. Ensure that the maximum dipole moments of each torquer are as equal as possible
2. Minimize the time constant t_c of each torquer to ensure maximum efficiency (efficiency is hindered when t_c is greater than the update frequency)
3. Minimize the difference between the electrical resistance of each torquer and the optimal resistance given by V_{bus}, I_{max} .

4.2.1 Air-Cored Magnetorquer

The magnetic moment of a solenoid is given as

$$\vec{\mu} = NI\vec{A} \quad (4.1)$$

with

$$I = \frac{V_{Bus}}{R} = \frac{V_{Bus}}{\rho l_w} \quad l_w = 2N(l + w) \quad A = lw \quad (4.2)$$

where L_w is the length of wire used, ρ is the resistance of the wire used in Ω/m , N is the number of turns in the solenoid, and l, w are the length and width of the air-cored frame. From (4.1) and (4.2) it follows that

$$\mu = \frac{V_{Bus}lw}{2\rho(l + w)} \quad (4.3)$$

Therefore, the magnetic moment generated by the air-cored is solely dependent on the wire used and the frame geometry.

The time constant of a solenoid is given as

$$t_c = \frac{L}{R} \quad \text{with} \quad L = \frac{\mu_0 N^2 A}{h} \quad (4.4)$$

where h is the height of the air-cored frame. It follows from this that

$$t_c = \frac{\mu_0 Nlw}{2h\rho(l + w)} \quad (4.5)$$

4.2.2 Ferromagnetic-Cored Magnetorquers

Ferromagnetic materials are non-linear, so the calculation of their dipole moment is non-trivial. The magnetic moment at saturation of a ferromagnetic torque rod was developed in [1]:

$$\mu = \left(\frac{rV_{bus}}{2\rho} \right) \left(1 + \frac{\mu_r - 1}{1 + (\mu_r - 1)N_d} \right) \quad (4.6)$$

where μ_r is the relative permeability of the core material, r is the core radius, ρ is the resistance per unit length, and N_d is the demagnetization factor derived in [6]:

$$N_d = \frac{4 \left[\ln \left(\frac{l_{core}}{r} \right) - 1 \right]}{\left(\frac{l_{core}}{r} \right)^2 - 4 \ln \left(\frac{l_{core}}{r} \right)} \quad (4.7)$$

where l_{core} is the length of the core, and r is as defined above. Experimental tests will have to be run to determine the characteristic hysteresis loop.

4.3 PRESET ADCS Algorithms

4.3.1 ADCS Modes

The PRESET ADCS is divided into four primary modes (Figure 8):

1. **Standby Mode:** Nothing happens. The system is powered on and awaits commands from the CDH command scheduler or the ground station. In Standby Mode, the satellite state can be obtained.
2. **Detumble Mode:** Initiated shortly after deployment, or at the discretion of the ground station.
3. **Maneuver Mode:** Using data collected in Standby, the satellite can maneuver to correct angular rate and/or attitude errors.
4. **Monitoring Mode:** Designed for periods spent in the polar regions where science is being done; this mode measures the satellite state rapidly to detect if the satellite's attitude or rate is outside allowable limits. If an error is detected, the satellite is sent to Standby.

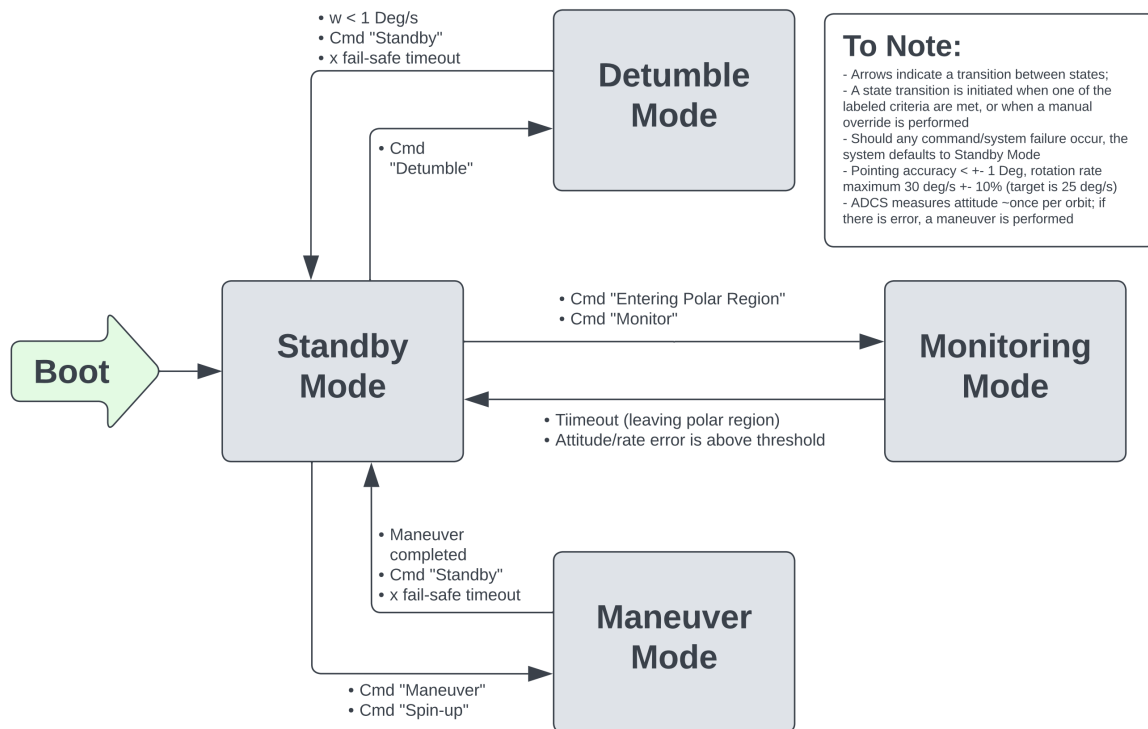


Figure 12: PRESET ADCS State Diagram (PRE-ACS-002-LD-P1)

References

- [1] The hysteresis loop and magnetic properties, Accessed on 2024-02-13. Web.
- [2] Computer Sciences Corporation. Attitude Systems Operation. *Spacecraft Attitude Determination and Control*. Reidel, 1978. Accessed on 15th March 2024 via National Library of Australia.
- [3] James Diebel. Representing attitude: Euler angles, unit quaternions, and rotation vectors. *Matrix*, 58, 01 2006.
- [4] Tsai et al. Remote sensing of electron precipitation mechanisms enabled by elfin mission operations and adcs. *Journal of Geophysical Research: Space Physics*, 118(5):2791–2804, 2013.
- [5] David F. Everett and Jeffrey J. Puschell. *Space Mission Engineering: The New SMAD*. Microcosm Press, 2011.
- [6] Mohamad Fakhari Mehrjardi and Mehran Mirshams. Design and manufacturing of a research magnetic torquer rod. In *Fourth International Conference on Experimental Mechanics*, 2009.
- [7] A. C. Stickler and K. T. Alfrend. Elementary magnetic attitude control system. *Journal of Spacecraft and Rockets*, 12(4):282–287, 1975.
- [8] M. Vos. Delfi-n3xt’s attitude determination and control subsystem: Implementation and verification of the hardware and software. Master’s thesis, Delft University of Technology, Delft, Netherlands, May 2013.