Kyle M'Graw

$$\hat{F}_n(x) = \frac{1}{n} \sum_{i=1}^{n} H(x-x_i)$$
 $\hat{F}_n(y) = \frac{1}{n} \sum_{i=1}^{n} H(y-x_i)$ 

$$\mathbb{E}[\hat{F}_{n}(x),\hat{F}_{n}(y)] = \mathbb{E}\left[\inf_{x \in \mathcal{X}_{n}} \hat{S}_{n} + (x-x_{n}) \hat{S}_{n} + (y-x_{n}) \right]$$

If i=j they are independent so we get F(x).F(y)

If i=j we get whichever of x or y is smaller

because the heavisite function is O for values larger

$$E[\hat{F}_{n}(x).\hat{F}_{n}(y)] = \begin{cases} \frac{1}{n^{2}}(n(n-1)F(x)F(y) + nF(y)) & x > y \\ \frac{1}{n^{2}}(n(n-1)F(x)F(y) + nF(x)) & x \leq y \end{cases}$$

$$C_{00}(\hat{F}_{n}(x), \hat{F}_{n}(y)) = \begin{cases} \frac{1}{N^{2}}(n(n-1)F(x)F(y) + nF(y)) - F(x)F(y) & x > y \\ \frac{1}{N^{2}}(n(n-1)F(x)F(y) + nF(x)) - F(x)F(y) & x \leq y \end{cases}$$

$$= \begin{cases} \frac{n-1}{N}F(x)F(y) + \frac{1}{N}F(y) - F(x)F(y) & x > y \\ \frac{n-1}{N}F(x)F(y) + \frac{1}{N}F(x) - F(x)F(y) & x \leq y \end{cases}$$

$$= \underbrace{\begin{cases} \frac{F(Y) - F(X)F(Y)}{N} & X > Y \\ \frac{F(X) - F(X)F(Y)}{N} & X \geq Y \end{cases}}_{R}$$

2. 
$$k_{F} = \frac{\int (x - m_{F})^{3} dF(x)}{(\int (x - m_{F})^{3} dF(x)^{3} dF(x)} \times F(x) \rightarrow \hat{F}_{n}(x) \qquad \hat{\mu}_{n} \rightarrow X_{n}$$

$$= \frac{\int (x - \overline{X}_{F})^{3} d\hat{F}_{n}(x)}{(\int (x - \overline{X}_{F})^{3} d\hat{F}_{n}(x))} \times n$$

$$=\frac{\frac{1}{n}\frac{2}{2}(x;-\overline{x}_{n})^{2}}{(\frac{1}{n}\frac{2}{2}(x;-\overline{x}_{n})^{2})^{2}}$$

$$\frac{1}{n}\frac{2}{n}(x;-\overline{x}_{n})^{2}$$

$$\frac{1}{n}\frac{2}{n}(x;-\overline{x}_{n})^{2}$$

$$= \frac{1}{2} \frac{\sum_{i=1}^{n} (x_i - \overline{X}_n)^3}{\sum_{i=1}^{n} (x_i - \overline{X}_n)^3}$$

$$\frac{\partial}{\partial x} = \min_{x \in X} \frac{1}{2} \frac{1}{2} \frac{1}{2} H(x - X; ) = 1 \frac{1}{2}$$

$$= \min_{x \in X} \frac{1}{2} \frac{1}{2} \frac{1}{2} H(x - X; ) = 1 \frac{1}{2}$$

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$$B[\hat{\theta}_{n}] = E[\hat{\theta}_{n}] - 0 = E[e^{X_{n}}] - e^{X_{n}}$$

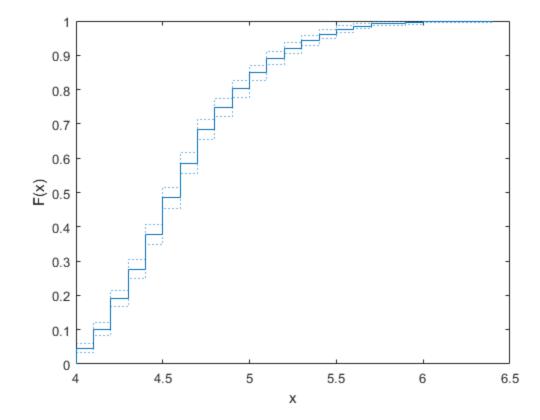
$$E[e^{X_{n}}] = E[e^{\frac{1}{2}X_{n}}] = E[e^{\frac{1}{2}X_{n}}] = E[e^{\frac{1}{2}X_{n}}] - e^{X_{n}}$$

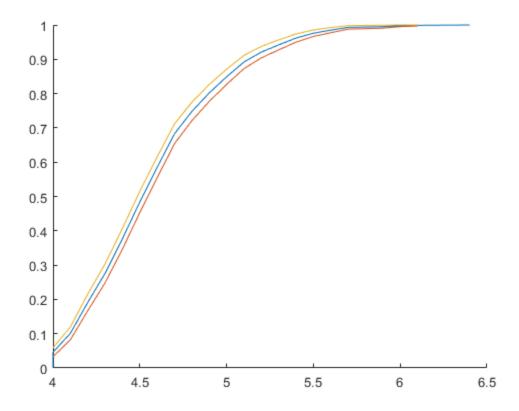
$$= e^{\frac{1}{2}X_{n}} + \frac{1}{2X_{n}} = e^{X_{n}} + \frac{1}{2X_$$

$$=\frac{e^{\frac{n}{2}}}{n}+\frac{e^{\frac{n}{8}}}{n^2}+O\left(\frac{1}{n^3}\right)$$

```
A = importdata("fiji.txt");
mags = A(:,5);
n = length(mags);
a = 1 - 0.95;
figure
ecdf(mags,'Alpha',a,'Bounds','on')

[f,x,flo,fup] = ecdf(mags,'Alpha',a);
figure
hold on
plot(x,f)
plot(x,flo)
plot(x,fup)
hold off
```





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```
mu = 5;
n = 100;
theta = exp(mu);
data = randn([n 1])+mu;
total = 0;
for i=1:n
    dataS = cat(1, data(1:i-1), data(i+1:n));
    total = total+exp(mean(dataS));
end
thetaJ = total/n;
thetaH = exp(mean(data));
bias = (n-1)*(thetaJ-thetaH);
realBias = exp(mu+(1/(2*n))) - theta;
disp([bias realBias])
% (b) The jackknife bias is close to the real bias of 0.7439
% Jackknife bias was 0.8624 in the last run
r = 10^4;
totalN = 0;
totalJ = 0;
for i=1:r
    data = randn([n 1])+mu;
    total = 0;
    for j=1:n
        dataS = cat(1, data(1:j-1), data(j+1:n));
        total = total + exp(mean(dataS));
    end
    thetaB = total/n;
    thetaN = exp(mean(data));
    thetaJ = n*thetaN - (n-1)*thetaB;
    totalN = totalN + thetaN;
    totalJ = totalJ + thetaJ;
end
B1 = totalN/r - theta;
B2 = totalJ/r - theta;
disp([B1 B2])
% (c) B1 is close to what we see for the bias but B2 is consistently
lower
% than B1 and the bias.
% In the last run B1 was 0.7376 and B2 was -0.0090
    0.8316
              0.7439
    0.8349
              0.0883
```

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