Kyle Mc Graw

1.
$$I(R) = \int_{CR} \frac{z + \log(z)}{z^3 + 1} dz \qquad + \frac{\text{continuous}}{z^2 - 1}$$

$$C_R! |z| = R - \frac{\pi}{2} \leq A_{19}(z) \leq \frac{\pi}{2} \qquad \text{for any } R$$

$$\left| \frac{1}{2 + \log(2)} \right| = \frac{12 + \log(2)!}{12^3 + 1!} = \frac{12 + \log(2)!}{|2^3 + 1|} = \frac{1}{|R^3 - 1|}$$

$$= \frac{|Z + \log |z| + |A_{1}g(z)|}{|R^{3} - 1|} = \frac{|Z + \log R + |A_{1}g(z)|}{|R^{3} - 1|}$$

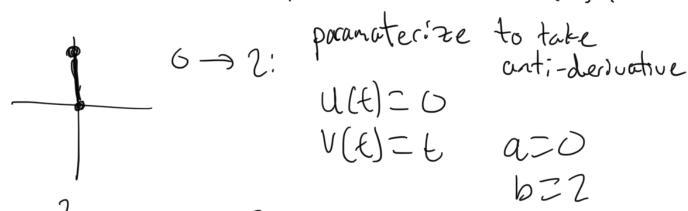
2. a)
$$\int_{C} \frac{(oS) \frac{1}{2}}{(2-i)(2-i)} d2$$

$$\int_{C} \frac{(oS) \frac{1}{2}}{(2-i)(2-i)} d2 = \int_{C} \frac{(oS) \frac{1}{2}}{(2-i)} d2 = \int_{C} \frac{(oS) \frac{1}{2}}{$$

Nou, ve can use Cauchy Integral Formula

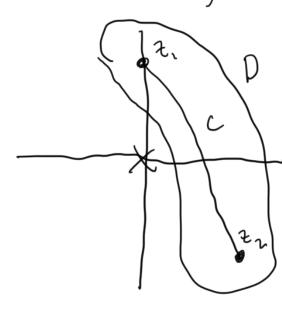
$$=\frac{2\pi i}{1-i}+0=\frac{2\pi i}{1-i}$$

b)
$$\int_{C} \overline{z} dz$$
 $\overline{z} = 0$ $\overline{z} = 2$:
 $\int_{C} f(z) dz = \int_{u}^{b} f(z(z)) z'(z) dz$
 $\int_{C} dz = \int_{u}^{b} (u(z) - v(z)) (u'(z) + iv'(z)) dz = i \int_{u}^{b} u(z) dz + \int_{u}^{b} v(z) dz$
 $\int_{C} \overline{z} dz = \int_{u}^{b} (u(z) - v(z)) (u'(z) + iv'(z)) dz = i \int_{u}^{b} u(z) dz + \int_{u}^{b} v(z) dz$



$$= \int_{0}^{2} dt + \int_{0}^{L} t dt$$

$$= \int_{0}^{2} t dt = \frac{z^{2}}{2} \Big|_{0}^{2} = 2$$



7 continuous in D D does not contain O

 $\int_{C}^{-\frac{1}{2}} \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right) \right) - \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right)$

$$= \frac{3}{2} \left(e^{\frac{1}{3} \log \pi} \left((\omega) \left(-\frac{1}{4} \pi \right) + i \sin \left(-\frac{1}{4} \pi \right) \right) - e^{\alpha} \left(\cos \left(\frac{1}{3} \pi \right) + i \sin \left(\frac{1}{3} \pi \right) \right) \right)$$

$$= \frac{3}{2} \left(\frac{2}{3} \left(\frac{\pi}{2} - \frac{1}{4} i \right) - \left(\frac{1}{4} + \frac{\pi}{2} i \right) \right)$$

$$= \frac{3}{2} \left(\frac{2}{3} \frac{3}{3} - 1 - \frac{3}{2} \frac{2^{3} + i \pi}{2} \right)$$

$$= \frac{3}{2} \left(\frac{2^{3} (3) - 1}{2} - \frac{3}{2} \frac{2^{3} + i \pi}{2} \right)$$

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$$= \frac{1}{4} \left(\frac{2^{3} (3) - 1}{2} - \frac{3}{2} \frac{2^{3} + i \pi}{2} \right)$$

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$$= \frac{1}{4} \left(\frac{3} (3) - \frac{3}{4} - \frac{3}{4} -$$

$$=\frac{1}{1+i}\left(\frac{e^{-2\pi}+e^{\pi}}{e^{-1}}\right)$$

$$=\frac{1}{2}\left(\frac{e^{-2\pi}+e^{\pi}}{e^{-1}}\right)-\frac{1}{2}\left(\frac{e^{-2\pi}+e^{\pi}}{e^{-1}}\right);$$

$$\approx 0.0225-0.0225;$$

Y.
$$I = \int_{0}^{\infty} \frac{(x^{2}+1)(x^{2}+4)^{2}}{(x^{2}+1)(x^{2}+4)^{2}} dx$$

$$X = \frac{1}{1} - \frac{1}{1} \cdot \frac{1}{1} - \frac{1}{1} \cdot \frac{1}{1}$$

$$\int_{C} \frac{2^{6} - 8}{(12^{2} + 1)[2^{2} + 1]^{2}} dx = \int_{C} \frac{x^{6} - 8}{(12^{2} + 1)[2^{2} + 1]^{2}} dx + \int_{C} \frac{2^{6} - 8}{(12^{2} + 1)[2^{2} + 1]^{2}} dx$$

$$\int_{C} \frac{2^{6} - 8}{(12^{2} + 1)[2^{2} + 1]^{2}} dz = \int_{C} \frac{2^{6} - 8}{(12 + i)(2 - i)[2 + 2i)[2 - 2i]^{2}} dz$$

$$= \int_{C_{1}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} + \int_{C_{2}} \frac{2^{6}-8}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}(2+1i)^{2}} \frac{dz}{(2+i)^{2}} \frac{dz}{(2+i)^{$$

$$T = 0 - \lim_{R \to \infty} \int_{C_R} \frac{2^6 - 8}{(12^2 + 11)[2^2 + 11]^2} dz$$

$$\left| \left((2^{2} + 1)(2^{2} + 4) \right)^{2} \right| = \left| (2^{2} + 1)(2^{2} + 4) \right|^{2} \ge \left| \left(12^{2} - 1 \right)(12^{2} - 4) \right|^{2}$$

$$= \left| \left(R^{2} - 1 \right) \left(R^{2} - 4 \right) \right|^{2} = \left(\left(R^{2} - 1 \right) \left(R^{2} - 4 \right) \right)^{2}$$

L2 TR+R = 12+1)R

$$\left|\int_{CR} \frac{2^{6} - 8}{(12^{2} + 1)[2^{2} + 4)]^{2}} dZ\right| \leq \frac{R^{6} - 8}{(12^{6} + 1)(R^{2} + 4)} \cdot (\pi + 1)R \approx \frac{R^{2}}{R^{8}} \rightarrow 0$$

$$CR = \frac{2^{6} - 8}{(12^{2} + 1)[2^{2} + 4)]^{2}} dZ$$

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$$CR = \frac{R^{6} - 8}{(12^{2} + 1)[2^{2} + 4)[2^{2} + 4]} dZ$$

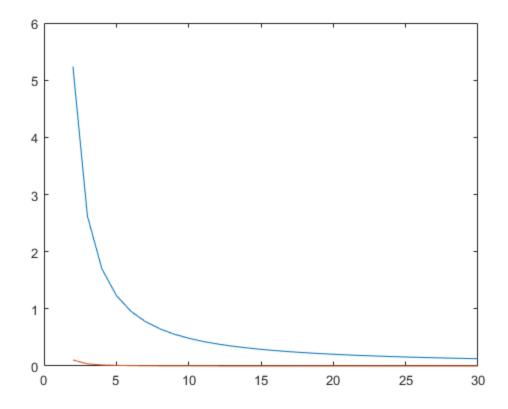
$$CR = \frac{R^{6} - 8}{(12^{2} + 1)[2^{2} + 4]} dZ$$

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$$T=0-0=0$$

```
R=2:30;
fun = @(z) (z+log(z))./(z.^3.+1);
par = @(t) fun(R.*cos(t)+R.*1i.*sin(t));
b = abs(integral(par,-pi/2,pi/2,'ArrayValued',true));
a = R.*pi.*(R+abs(log(R))+pi)./abs(R.^3-1);
plot(R,a,R,b)
```



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