$$I = \int_0^\infty \frac{x^3 \sin(2x)}{(x^2+1)^2} dx$$

$$\int_{\mathcal{Z}} \frac{z^{3} e^{2iz}}{(z^{2}+1)^{2}} dz$$

$$(z+i)(z-i))^{2}$$

$$\int_{C} f(z)e^{i2z} dz = \int_{R} f(x)e^{i2x} dx + \int_{C_{R}} f(z)e^{i2z} dz$$

$$\left|\frac{z^{3}}{(z^{2}+1)^{2}}\right| \leq \frac{|z|^{3}}{|z^{2}+1|^{2}} \leq \frac{R^{3}}{(|z|^{2}+1)^{2}} \leq \frac{R^{3}}{(|z|^{2}+1)^{2}}$$

$$\int_{L} \frac{z^{3}e^{2i\pi}}{(z^{2}+1)^{n}} d\tau = 2\pi i \lim_{z \to i} \frac{d}{dz} \left(|z-i|^{2} \frac{z^{3}e^{2i\pi}}{(z^{2}+1)^{2}}\right)$$

$$=2\pi i \lim_{z \to i} \left(\frac{3z^{2}e^{2iz}}{(z+i)^{2}} + \frac{z^{3}2ie^{2iz}}{(z+i)^{2}} + \frac{-2z^{3}e^{2iz}}{(z+i)^{3}} \right)$$

$$=2\pi i \left(\frac{-3e^{2}}{-4} + \frac{2e^{2}}{-4} + \frac{2ie^{2}}{-8i} \right)$$

$$= 2\pi \cdot \left(\frac{-3e^{2}}{-4} + \frac{2e^{2}}{-4} + \frac{2ie^{2}}{-8i}\right)$$

$$\begin{array}{l}
= 2\pi i \left(\frac{1}{4} e^{2x} - \frac{1}{2} e^{2x} - \frac{1}{4} e^{-x} \right) \\
= 0 \\
0 = \int_{-R}^{R} \frac{x^{3} \sin(2x)}{(x^{3} + 1)^{2}} dx + 0 \\
0 = 2 \int_{0}^{R} \frac{x^{3} \sin(2x)}{(x^{3} + 1)^{2}} dx + 0 \\
\int_{0}^{\infty} \frac{x^{3} \sin(2x)}{(x^{3} + 1)^{2}} dx = 0 \\
\int_{0}^{\infty} \frac{x^{3} \sin(2x)}{(x^{3} + 1)^{2}} dx = \int_{0}^{\infty} \frac{x^{3}$$

$$= 2\pi i \left(\frac{-1}{(i-1)(i+1)2i}\right)$$

$$= 2\pi i \left(\frac{-1}{-4i}\right) = \frac{\pi}{2}$$

$$\int_{C_{\xi_{i-1}}}^{2^{i}} dz = -\pi i \lim_{z \to 1} \frac{z^{i}}{(z-1)(z+1)(z-1)}$$

$$= -\pi i \left(\frac{1}{-2(i+1)(i-1)}\right)$$

$$= -\pi i \left(\frac{1}{-2(i+1)(i-1)}\right)$$

$$= -\pi i \left(\frac{1}{2(i+1)(i-1)}\right)$$

$$= -\pi i \left(\frac{1$$

$$= \int_{0}^{\infty} \frac{r^{\frac{1}{4}} - \frac{1}{e^{\frac{1}{4}}(r^{\frac{1}{4}})} e^{\frac{1}{4}(r^{\frac{1}{4}}-1)} e^{\frac{1}{4}(r^$$

5. a)
$$y'' + 2y' + 5y = 0$$
 $y(6) = 6$ $y'(0) = 4$ $y \neq 0$

$$d_{11} = -\frac{2 \pm \sqrt{4-20}}{2} = -1 \pm 2i$$

μ= -1 λ=2 γ(t)=(, e ωs(2t) + (, e sin(2t)) γ'(t)=-(,e+ωs(2t)-2(,e+sin(2t)-6e+sm(2t)+2c,e+ωs(2t))

```
응 {
f=@(x) (x.^3).*sin(2*x)./((x.^2+1).^2);
I=integral(f,0,Inf);
disp(I)
응 }
tspan1 = [1 0.2];
tspan2 = [1 2];
f=@(t,y) -2/t*y+t-1+1/t;
y0 = 1/3;
[t1,y1] = ode45(f,tspan1,y0);
[t2,y2] = ode45(f,tspan2,y0);
t = [t1 \ t2];
y = [y1 \ y2];
yExact=@(t) 1/4.*t.^2-1/3.*t+1/2-1/12.*t.^-2;
figure
p1 = plot(t, yExact(t), 'r-o');
hold on;
p2 = plot(t,y,'b-x');
hold off;
legend([p1(1);p2],'Exact','Numerical');
figure
p2 = semilogy(t,abs(yExact(t)-y));
Warning: Ignoring extra legend entries.
```





